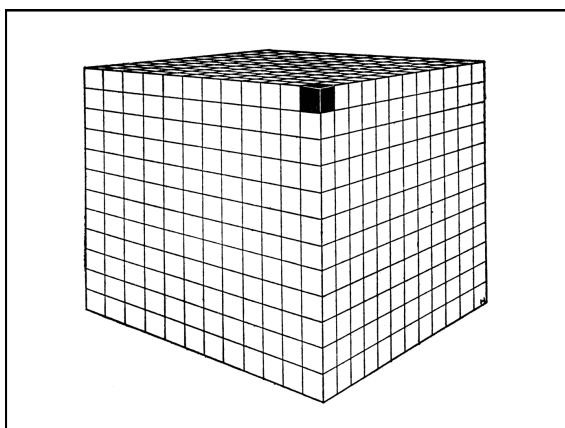
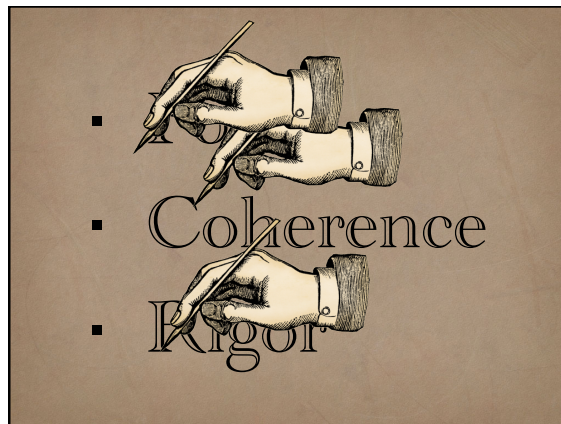


Content Standards

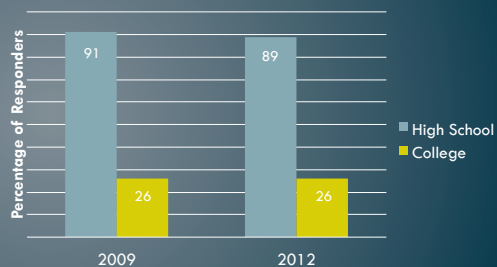
- 6.G.2 - Find the volume of a right rectangular prism with fractional edge lengths
- 7.G.6 - Solve real-world and mathematical problems involving area, volume and surface area



WHY DO WE NEED THE COMMON CORE STANDARDS?

- What is the purpose of K-12 Ed?
 - College readiness
 - ACT National Curriculum Survey
 - Surveyed 9,937 educators.

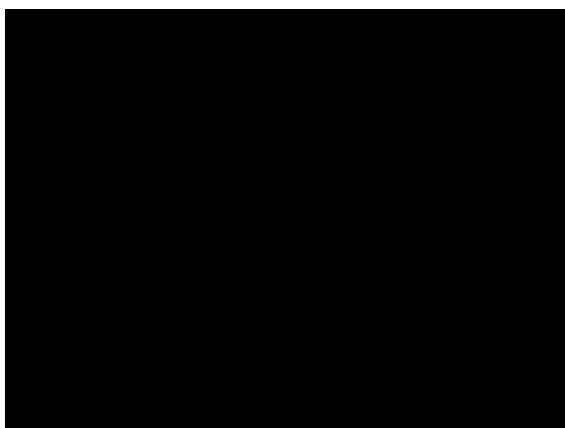
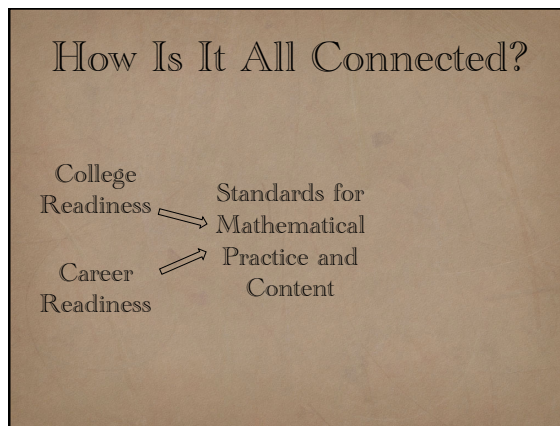
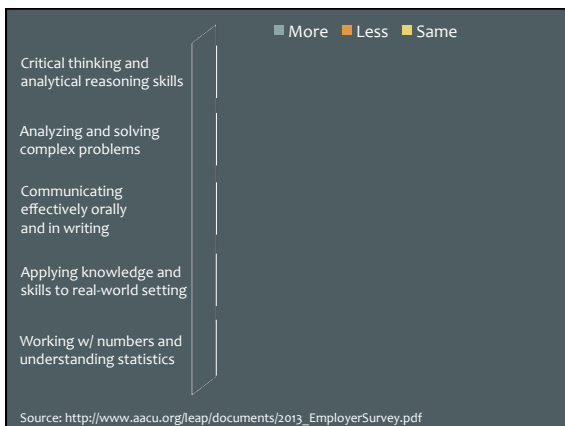
“Well” or “Very Well” Prepared for College



Source: <http://www.act.org/research/policymakers/pdf/NCS-PolicySummary2012.pdf>

WHY DO WE NEED THE COMMON CORE STANDARDS?

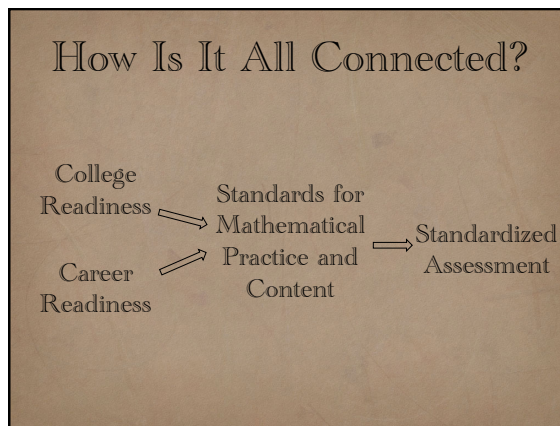
- What is the purpose of K-12 Ed?
 - College readiness
 - Career readiness
 - Association of American Colleges and Universities survey
 - Survey over 300 employers with at least 25 employees and many new hires.

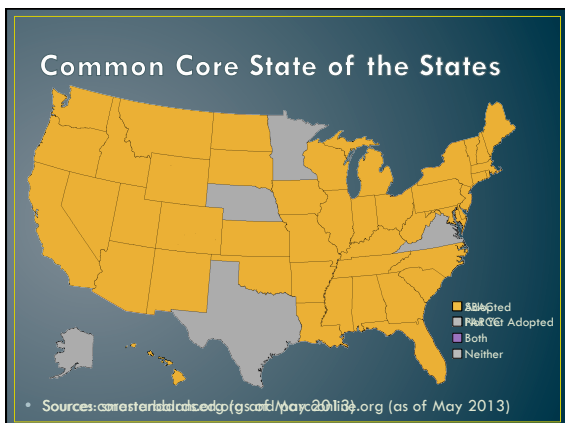


Content Standards

- 8.F.4 - Construct a function to model a linear relationship between two quantities.

- ### Standards for Mathematical Practice
1. Make sense of problems and persevere in solving them.
 2. Reason abstractly and quantitatively.
 3. Construct viable arguments and critique the reasoning of others.
 4. Model with mathematics.
 5. Use appropriate tools strategically.
 6. Attend to precision.
 7. Look for and make use of structure.
 8. Look for and express regularity in repeated reasoning.





SMARTER BALANCED ASSESSMENT

- Students in grades 3 through 8 and grade 11 will be assessed.
- Computer adaptive
- Both electronic and human scoring.
- Interim assessments
- Practice tests just released on May 29th.

SMARTER BALANCED PROBLEM TYPES

- Selected-response items
 - Prompt students to select one or more responses from a set of options.

Source: <http://sampleitems.smarterbalanced.org/itempreview/sbac/>

Look at each expression. Is it equivalent to $\frac{x+3y}{2}$
 Select Yes or No for expressions A – D.

A. $4x + 3y$

Score Result

Your response earned 1 points of a possible 1

All credit answer	Your answer
The student correctly classified each expression.	<input checked="" type="checkbox"/>

Ok

D. $\frac{2}{3} \left(\frac{5x}{6} + \frac{9y}{4} - \frac{x}{12} \right)$ Yes No

For each linear equation in the table, select whether the equation has no solution, one solution, or infinitely many solutions.

Score Result

Your response earned 0 points of a possible 1

All credit answer	Your answer
The student correctly identified the number of solutions for each equation.	<input checked="" type="checkbox"/>

Ok

$-12(x + 2) = -14x + 2$	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
-------------------------	-------------------------------------	--------------------------	--------------------------

SMARTER BALANCED PROBLEM TYPES

- Selected-response items
- Technology-enhanced items
 - Use technology to collect evidence through a non-traditional response type, such as editing text or drawing an object.

Source: <http://sampleitems.smarterbalanced.org/itempreview/sbac/>

The point on the number line shows the location of $-3\frac{1}{2}$

Score Result


Your response earned 2 points of a possible 2

All credit answer	Your answer
The student correctly identified the location of $-3\frac{1}{2}$ plus (-5) .	✓
The student correctly identified the location of $-3\frac{1}{2} - 3\frac{1}{2}$.	✓
The student correctly identified the location of $-3\frac{1}{2}$ plus $3\frac{1}{2}$.	✓
The student correctly identified the location of $-3\frac{1}{2} - (-5)$.	✓

Ok

$-3\frac{1}{2} + 3\frac{1}{2}$ $-3\frac{1}{2} + (-5)$

Two water tanks are shown. Tank A is a rectangular prism and Tank B is a cylinder. The tanks are not drawn to scale.



Score Result

Your response earned 1 points of a

All credit answer	Your answer
The student used the relationship between the volumes to calculate the radius of the base of the cylinder.	✓

Ok

Drag one number into the box to show the approximate radius of the base of Tank B.

0 1 2 3 4 5 6 7 8 9

SMARTER BALANCED PROBLEM TYPES

- Selected-response items
- Technology-enhanced items
- Constructed-response items
 - Students produce a text and/or numerical response in order to collect evidence about their knowledge or understanding.

Source: <http://sampleitems.smarterbalanced.org/itempreview/sbac/>

For full credit (2 points):

- Student reaches the correct conclusion.

AND

- Student provides sufficient reasoning to support this conclusion.

For partial credit (1 point):

- Student reaches the correct conclusion but does not provide sufficient reasoning to support this conclusion.

OR

- Student does not reach the correct conclusion but provides reasoning to support this conclusion that contains a minor conceptual or computation error.

For full credit (2 points):

- Student reaches the correct conclusion.

AND

- Student provides sufficient reasoning to support this conclusion.

For partial credit (1 point):

- Student reaches the correct conclusion but does not provide sufficient reasoning to support this conclusion.

OR

- Student does not reach the correct conclusion but provides reasoning to support this conclusion that contains a minor conceptual or computation error.

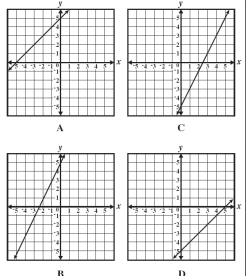
SMARTER BALANCED PROBLEM TYPES

- Selected-response items
- Technology-enhanced items
- Constructed-response items
- Performance tasks
 - Measure a student's ability to integrate knowledge and skills across multiple standards.

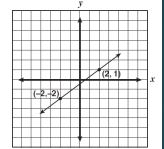
Source: <http://sampleitems.smarterbalanced.org/itempreview/sbac/>

Common Core vs. California Standards

51 Which best represents the graph of $y = 2x - 5$?



52 What is the slope of this line?

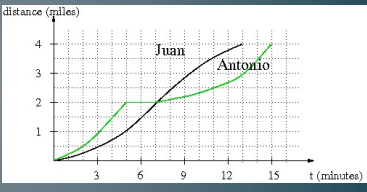


A $\frac{1}{2}$
 B $\frac{3}{4}$
 C 1
 D $\frac{4}{3}$

Source: <http://www.cde.ca.gov/To/tg/sr/documents/cstrtqmath7.pdf>

Common Core vs. California Standards

- Antonio and Juan are in a 4-mile bike race. The graph below shows the distance of each racer (in miles) as a function of time (in minutes).



- Who wins the race? How do you know?
- Imagine you were watching the race and had to announce it over the radio, write a little story describing the race.

Source: <http://www.illustrativemathematics.org/standards/k8>



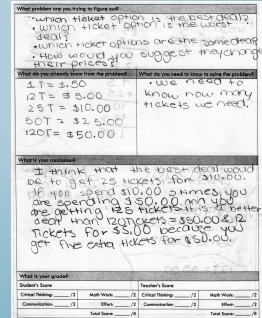
Content Standards

- 6.RP.2 – Understand the concept of a unit
- 6.RP.3 – Use ratio and rate reasoning to solve real-world and mathematical problems.

The Reality

- What does “best” mean?
 - 120 tickets for \$50 is “best” because you get the most tickets
 - 1 ticket for \$0.50 is “best” because you spend the least amount of money
- “What do you need to know to solve the problem?”
 - How many tickets will we use?
 - How long will we be staying there?
 - How many people are we going with?
 - How many tickets do the rides cost?
- Once they started working, they had no idea what to do.
 - They didn’t realize that they could buy multiple sets of tickets.

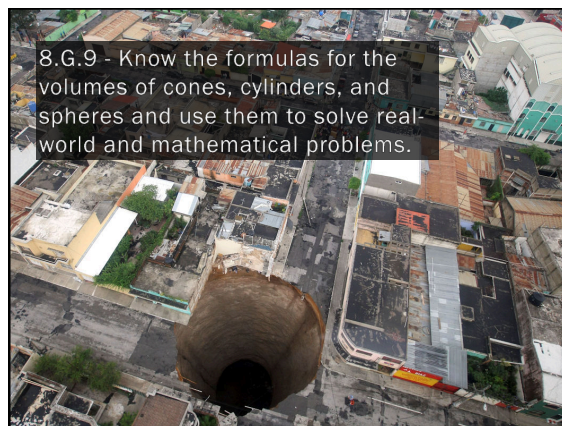
STUDENT WORK SAMPLES



The Four C's

- o Communication
- o Curiosity

8.G.9 - Know the formulas for the volumes of cones, cylinders, and spheres and use them to solve real-world and mathematical problems.



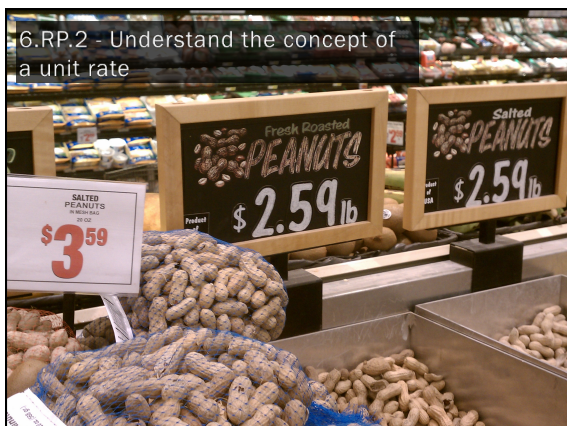
7.RP.2 - Recognize and represent proportional relationships between quantities.



6.G.4 - Represent three-dimensional figures using nets made up of rectangles and triangles, and use the nets to find the surface area of these figures.



6.RP.2 - Understand the concept of a unit rate



The Four C's

- o Communication
- o Curiosity
- o Critical Thinking
- o Content Knowledge

Questioning Scenarios

- The activity begins with teachers in groups of three taking the roles of teacher, student, or observer.
- The individuals playing the role of teacher and student each receive a slip of paper describing their scenario.
- The individual playing the role of observer waits to record all of the teacher's questions to the student.
- Once the activity begins, the teacher will talk to the student in the context of the scenario they read about on the slips of paper.

What did you get for the area of the circle with a radius of 2 units?

4 pi

Great. Do you have any questions?

No

What did you get for the area of the circle with a radius of 2 units?

4 pi

Great. How did you get your answer?

The radius is 2 so I plugged it into $2\pi r$ and got 4π .

BREAKING DOWN THE CONTENT STANDARDS

- Domain and Conceptual Categories

Domain and Conceptual Categories

K	1	2	3	4	5	6	7	8	HS
Counting & Cardinality									
Number and Operations in Base Ten					Ratios and Proportional Relationships		Number and Quantity		
Number and Operations - Fractions				The Number System					
Operations and Algebraic Thinking					Expressions and Equations		Algebra		
							Functions	Functions	
Geometry									Geometry
Measurement and Data					Statistics and Probability		Statistics & Probability		

Source: <http://www.doe.in.gov/achievement/curriculum/resources-implementing-indianas-common-core-standards>

BREAKING DOWN THE CONTENT STANDARDS

- Domain and Conceptual Categories
- Reading the Content Standards

Domain

The Number System 8.NS

Know that there are numbers that are not rational, and approximate them by rational numbers.

1. Know that numbers that are not rational are called irrational. Understand informally that every number has a decimal expansion; for rational numbers show that the decimal expansion repeats eventually, and convert a decimal expansion which repeats eventually into a rational number.
2. Use rational approximations of irrational numbers to compare the size of irrational numbers, locate them approximately on a number line diagram, and estimate the value of expressions (e.g., n^2). For example, by truncating the decimal expansion of $\sqrt{2}$, show that $\sqrt{2}$ is between 1 and 2, then between 1.4 and 1.5, and explain how to continue on to get better approximations.

Cluster

Standards

BREAKING DOWN THE CONTENT STANDARDS

- Domain and Conceptual Categories
- Reading the Content Standards
 - Fifteen percent
 - Identifying CA additions

Domain

Creating Equations A-CED

Create equations that describe numbers or relationships (linear, quadratic, and exponential (integer inputs only); for A-CED.3 linear only).

1. Create equations and inequalities in one variable (including ones with absolute value) and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions. (CA)
2. Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales. (M)
3. Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or non-viable options in a modeling context. For example, represent inequalities describing nutritional and cost constraints on combinations of different foods. (M)
4. Rearrange formulas to highlight a quantity of interest, using the same reasoning as in solving equations. For example, rearrange Ohm's law $V = IR$ to highlight resistance R . (M)

Cluster


Modeling Standards

Standards

CA Additions

BREAKING DOWN THE CONTENT STANDARDS

- Domain and Conceptual Categories
- Reading the Content Standards
 - Fifteen percent
 - Identifying CA additions
- Understanding the standards



Illustrative Mathematics

HOME

ILLUSTRATIONS

K-8 STANDARDS

HIGH SCHOOL STANDARDS

PRACTICE STANDARDS

FRACTIONS PROGRESSION

FREQUENTLY ASKED QUESTIONS

COMMUNITY


ABOUT US

TERMS OF USE

K-8 Standards

High School Standards

Practice Standards



Illustrative Mathematics provides guidance to states, assessment consortia, testing companies, and curriculum developers by illustrating the range and types of mathematical work that students experience in a faithful implementation of the Common Core State Standards, and by publishing other tools that support implementation of the standards.

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K	1	2	3	4	5	6	7	8
Geometry								
Measurement and Data				Statistics and Probability				
Number and Operations in Base Ten				The Number System				
Operations and Algebraic Thinking				Expressions and Equations				
Counting and Cardinality		Number and Operations—Fractions			Ratios and Proportional Relationships		Functions	

Show only illustrated standards (?)

Reveal standards automatically (?)

The screenshot shows the Illustrative Mathematics website interface. At the top, there is a navigation bar with numbered tabs from 1 to 8. Below this is a grid of subject areas: Geometry, Statistics and Probability, Number and Operations in Base Ten, The Number System, Operations and Algebraic Thinking, Expressions and Equations, Counting and Cardinality, Number and Operations--Fractions (highlighted in yellow), Ratios and Proportional Relationships, and Functions. Below the grid, there are options to 'Show only illustrated standards (?)' and 'Reveal standards automatically (?)'. The main content area is titled 'Number and Operations--Fractions' and 'Grade 3', with a sub-section '3 NF' and a 'View all' link. Underneath, it says 'A. Develop understanding of fractions as numbers.' followed by two numbered points: '1. Understand a fraction 1/b as the quantity formed by 1 part when a whole is partitioned into b equal parts...' and '2. Understand a fraction as a number on the number line...'.

Content Standards Review

- Read your course standards
 - Introduction
 - Overview
 - Course differences
- Reference standards on illustrativemathematics.org
- Review standards for one or more grade levels above and below

The screenshot shows the Robert Kaplinsky website. At the top left is the logo 'Robert KAPLINSKY Glenrock Consulting'. Below the logo is a large image of a hand pointing towards a building with the text 'How Many Sheets Do You Need To Break Out Of Prison?' and 'Operations with rational numbers'. Below the image is a 'Why Choose Us?' section with a 'Math content expert' badge and a short bio. To the right is a 'Lessons' section with three lesson thumbnails: 'How Can We Water All Of The Grass?', 'How Much Money Is That?', and 'How Much Money Is That?'.

Robert Kaplinsky's Problem-Based Lessons

Task Name	Concept / Skill	Standard 1	Standard 2	Standard 3	Standard 4	Standard 5
How Can We Water All Of The Grass?	Circles, Pythagorean Theorem, trigonometric ratios	7.G.4	8.G.7	G-SRT.8	G-MG.1	G-SP.4
How Much Money Is That?	Volume of rectangular prism	4.MD.3	4.MD.4	4.MD.5	4.MD.6	4.MD.7
How Much Money Should I Sell To Buy A Car?	Exponential Growth	N-RN.2	A-SEF.1	A-SEF.2	A-SEF.3	A-SEF.4
How Can We Water All Of The Grass?	Scale and Similar Figures	5.MF.5	5.MF.6	5.MF.7	5.MF.8	5.MF.9
How Can We Water All Of The Grass?	Transformations (Rotations, Reflections, and Translations)	8.G.1	8.G.2	8.G.3	8.G.4	8.G.5
How Can We Water All Of The Grass?	Unit Rates and Ratios	6.RP.2	6.RP.3	6.RP.4	6.RP.5	6.RP.6
How Can We Water All Of The Grass?	Fractions on a Number Line and Subtracting Fractions	3.NF.2	3.NF.3	4.NF.2	4.NF.3	4.NF.4
How Can We Water All Of The Grass?	Area	3.MD.8	3.MD.9	3.MD.10		
How Can We Water All Of The Grass?	Scientific Notation	5.EE.3	5.EE.4			
How Can We Water All Of The Grass?	Measurement and Measurement	2.MD.8	2.MD.9	3.MD.7		
How Can We Water All Of The Grass?	Money	7.MD.3				
How Can We Water All Of The Grass?	Percent Discount	7.RP.3				
How Can We Water All Of The Grass?	Pythagorean Theorem (Distance in coordinate system)	8.G.4	G-SRT.8	G-SP.7		
How Can We Water All Of The Grass?	Pythagorean Theorem (Length of a side)	8.G.7	G-SRT.8	G-SP.7		
How Can We Water All Of The Grass?	Operations with the Integers	4.MD.2				
How Can We Water All Of The Grass?	Converting Units, Proportions, and Scientific Notation	4.MD.1	7.PP.2	7.G.4	8.EE.4	9
How Can We Water All Of The Grass?	Percent Discount	7.RP.3	A-CEO.3			
How Can We Water All Of The Grass?	One-Step Operations and/or Systems of Equations	6.NBT.7	8.EE.6	A-CEO.3	A-REI.11	F
How Can We Water All Of The Grass?	Volume of Cylinder	5.MD.3	5.MD.4	5.MD.5	8.G.9	8
How Can We Water All Of The Grass?	Determining Numbers and/or Systems of Equations	2.NBT.7	3.NBT.2	3.NBT.3	8.EE.6	A
How Can We Water All Of The Grass?	Probability	7.SP.5	7.SP.6	7.SP.7	5.MD.5	8
How Can We Water All Of The Grass?	Surface Area	6.G.4	7.G.5	8.G.7	G-MG.1	G
How Can We Water All Of The Grass?	Percent Increase and Compound Interest	7.RP.3	A-SEF.15	F-IF.1	F-IF.8	F
How Can We Water All Of The Grass?	Surface Area and Unit Rates	6.G.4	8.RP.2	8.RP.3	7.G.4	
How Can We Water All Of The Grass?	Perimeter	4.MD.3				
How Can We Water All Of The Grass?	Systems of Equations/Inequalities	8.EE.6	A-CEO.3	A-REI.11	F-IF.1	F
How Can We Water All Of The Grass?	Linear Equations	A-CEO.2	F-IF.1	F-IF.4	F-IF.8	
How Can We Water All Of The Grass?	Area of Circle, Square, and Unit Rates	3.MD.5	3.MD.6	3.MD.7	4.MD.3	4
How Can We Water All Of The Grass?	Area of Square	7.MF.6				
How Can We Water All Of The Grass?	Systems of Equations or Rates	6.RP.2	6.RP.3	8.EE.6	A-CEO.3	F
How Can We Water All Of The Grass?	Integer Operations	6.EF.1	8.F.4	F-SE.1	F-SE.2	F
How Can We Water All Of The Grass?	Linear and Quadratic Functions	3.MD.8	4.MD.3	7.G.4		
How Can We Water All Of The Grass?	Perimeter & Circumference	3.MD.8	4.MD.3	7.G.4		
How Can We Water All Of The Grass?	Adding Time	3.MD.1				
How Can We Water All Of The Grass?	Percent Discount	7.RP.3				
How Can We Water All Of The Grass?	Ratios and Proportions	7.RP.2				
How Can We Water All Of The Grass?	Create Equation from Quadratic Graph	A-CEO.1	F-IF.1	F-IF.4	F-IF.7a	F
How Can We Water All Of The Grass?	Linear and Quadratic Graph	3.MD.1	A-MO.2			
How Can We Water All Of The Grass?	Adding Time	3.MD.1				
How Can We Water All Of The Grass?	Unit Rates	6.RP.1	6.RP.2	6.RP.3		
How Can We Water All Of The Grass?	Converting Units and Unit Rates	5.MD.1	5.RP.2			

NEXT STEPS

- Standards for Mathematical Practice
 - Talking and writing about mathematics
- Rigor
 - Application
 - Conceptual understanding
 - Procedural skill and fluency

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