

Paramount USD
Robert Kaplinsky
May 17, 2014









DOUBLE-DOUBLE[®] *Double Meat & Double Cheese* **2⁶⁵**

CHEESEBURGER **1⁷⁵**

HAMBURGER **1⁵⁰**

FRENCH FRIES **1⁰⁵**

SHAKES *Chocolate
Strawberry
Vanilla* **1⁵⁵**

<u>SM</u>	<u>MED</u>	<u>LG</u>	<u>X-LG</u>
99	1¹⁰	1²⁹	1⁴⁹
COKE <i>Classic or Diet</i>			
SEVEN-UP			
ROOT BEER			
DR PEPPER			
LEMONADE			
ICED TEA			

MILK	70
COFFEE	70



OPEN 10:30 a.m. to 1:00 a.m.
.....**Fri. and Sat. until 1:30 a.m.**

2004-10-31

8:21 PM

YOUR GUEST NUMBER IS
98

IN-N-OUT BURGER LAS VEGAS EASTERN
2004-10-31

165 1 5 98

8:21 PM

Cashier: SAM

GUEST #: 98

Counter-Eat In

Db Db	2.65
98 Meat Pty XChz	88.20
Counter-Eat In	90.85
TAX 7.50%	6.81
Amount Due	97.66
CASH TENDER	\$97.66
Change	\$.00

2004-10-31

Cashier: SAM

GUEST #: 98

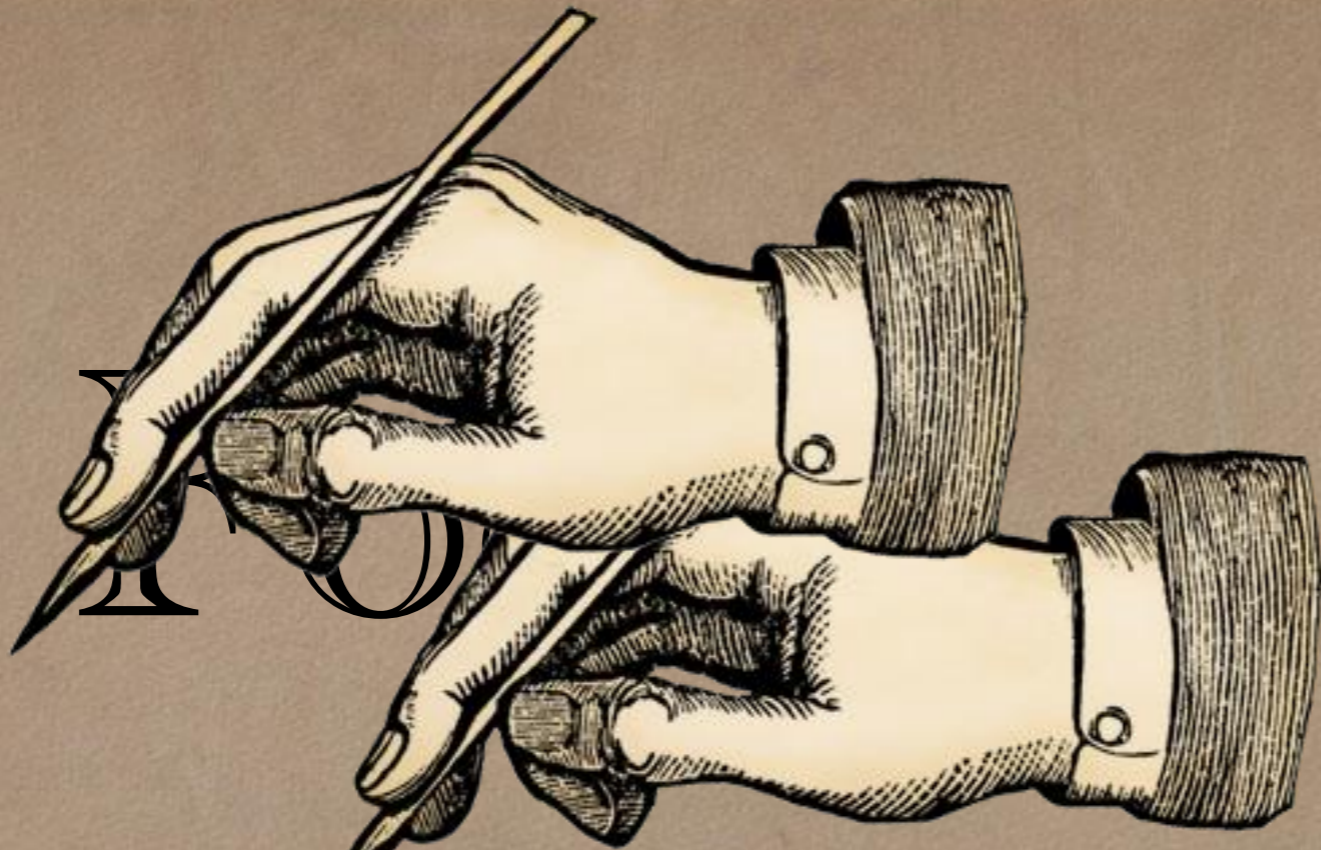
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2004-10-31

8:21 PM

	Serving Size (g)	Calories
Hamburger w/Onion	243	390
Cheeseburger w/Onion	268	480
Double-Double w/Onion	330	670



•

Coherence

•



•

Rigor

Layers	Cost
1	\$1.75
2	\$2.65
3	\$3.55
4	\$4.45
.	.
.	.
20	\$18.85
.	.
.	.
100	\$90.85
.	.
.	.
N	$\$1.75 + (N-1)*\0.90

bun + produce + meat + cheese + meat + cheese = \$2.65

bun + produce + meat + cheese = \$1.75

meat + cheese = \$0.90

The Reality

- Students needed guidance to figure out a layer's cost
- Not every class is ready to go straight to 100×100
- Common wrong answers included:
 - \$175.00 ($\1.75×100 cheeseburgers)
 - \$132.50 ($\2.65×50 Double-Doubles)
- Students had equations that had more than X patties
- Students were surprised to see three different equations:
 - Starting with a Double-Double
 - Starting with a cheeseburger
 - Starting with produce and bun only

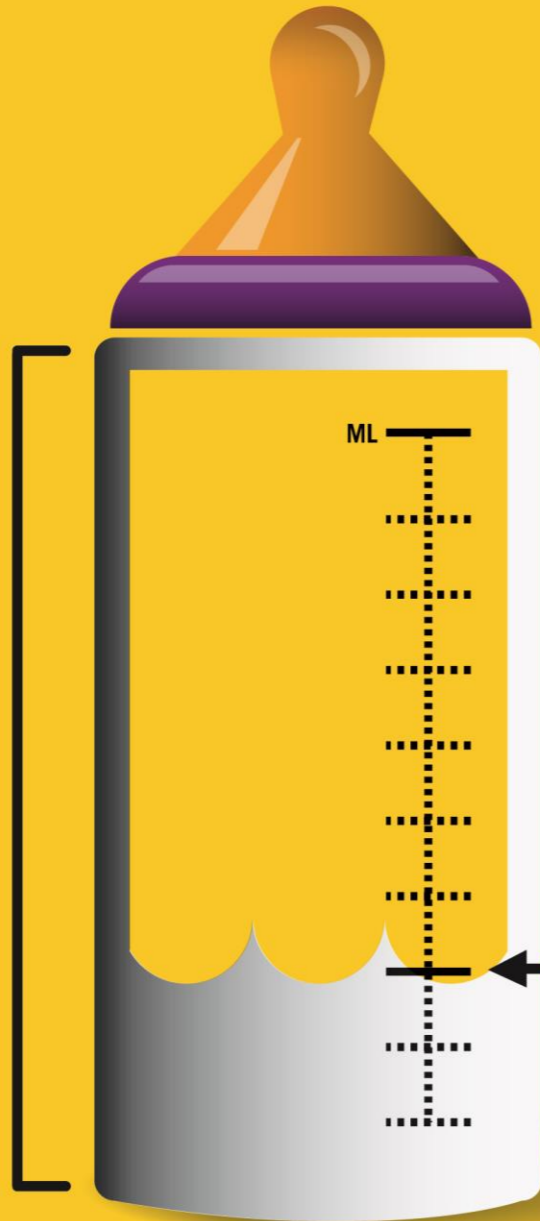
STUDENT WORK

What problem are you trying to figure out?	
<p>How much does a 100x100 burger cost?</p> <p style="text-align: right;">Regular (one patty) \$1.25</p> <p style="text-align: center;">\$132.50</p>	
What do you already know from the problem?	What do you need to know to solve the problem?
<ul style="list-style-type: none"> • there's 100 beef patties • costs 2.50 	<ul style="list-style-type: none"> • How much does a regular cheeseburger cost. 25.1 - <p style="text-align: center;">OP.</p> <p style="text-align: center;">OP. OP.</p>
What is your conclusion?	
<p>To get the answer, I first figured out what the price of a regular & double-double cheeseburgers are. From there I subtracted the price of the produce & buns, then multiplied by 100. That gave me the answer, which I once again had to add the price of the buns & produce.</p> <p style="text-align: center;"> $22.8 + 00.1 - xOP_0 = P$ $128.0 + xOP_0 = P$ </p>	

CHOOSE CAR SEAT:
BY AGE & SIZE



THE NUMBER
OF PEOPLE
**WHO
THINK**
THEY HAVE
THEIR CHILD IN
THE RIGHT
SEAT.



THE ONES
**WHO
ACTUALLY
DO.**

KNOW FOR SURE
IF YOUR CHILD IS IN THE RIGHT CAR SEAT.



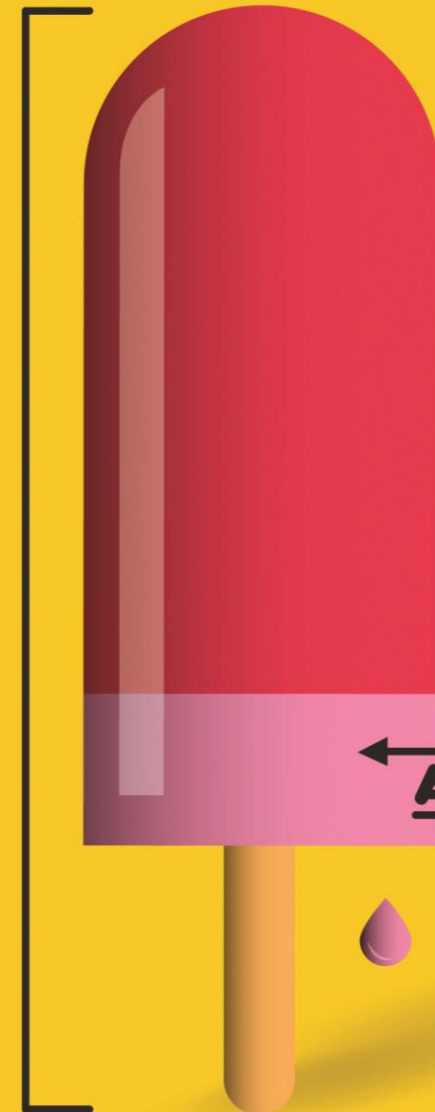
VISIT SAFERCAR.GOV/THERIGHTSEAT



CHOOSE CAR SEAT:
BY AGE & SIZE



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VISIT SAFERCAR.GOV/THERIGHTSEAT



Math Question

- Solve the problem on your own. Do not work or share your answer with anyone else.
- You will have 30 seconds to complete it.
- Write your answer down on a paper.
- Pay attention to the emotions you feel while solving the problem and write those emotions down as well.

There are 125
sheep and 5 dogs
in a flock. How old
is the shepherd?

Of the 32 students I interviewed...

- 75% of them gave me numerical responses
- 2 students calculated the answer to be 130 ($125 + 5$)
- 2 students calculated the answer to be 120 ($125 - 5$)
- 12 students calculated the answer to be 25 ($125 \div 5$)
- 0 students calculated the answer to be 625 (125×5)
- 4 students stated that they guessed their answer (90, 5, 42, and 50)
- 4 students tried to divide 125 by 5 but could not correctly implement the procedure

Takeaways

- Making sense of mathematics
- Intellectual autonomy
 - Intellectual autonomy is about being able to think for yourself and not being dependent on others for the direction and control of one's thinking.

What Does the NHTSA Say?

Key Statistics and Consumer Insights:

- Motor vehicle crashes are the leading cause of death for children age 1 through 12 years old.¹

According to a NHTSA study, 3 out of 4 kids are not as secure in the car as they should be because their car seats are not being used correctly.

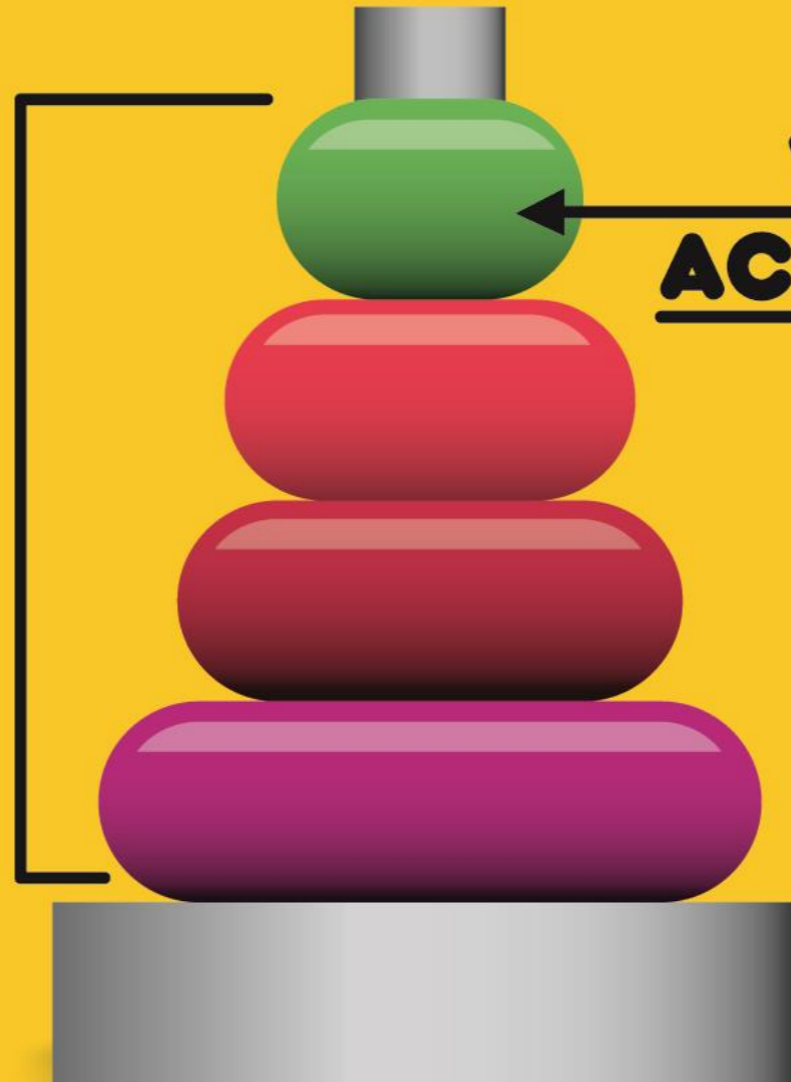
be reduced by about half if the correct child safety seats were always used.

¹ Source: Based on the latest mortality data currently available from the CDC's National Center for Health Statistics.



CHOOSE CAR SEAT:
BY AGE & SIZE

THE NUMBER
OF PEOPLE
**WHO
THINK**
THEY HAVE
THEIR CHILD
IN THE RIGHT
SEAT.



THE ONES
**WHO
ACTUALLY
DO.**

- “because they have their child in the right seat”
- “because their car seats are not being used correctly”

IF YOUR CHILD IS IN THE RIGHT CAR SEAT.



VISIT SAFERCAR.GOV/THERIGHTSEAT



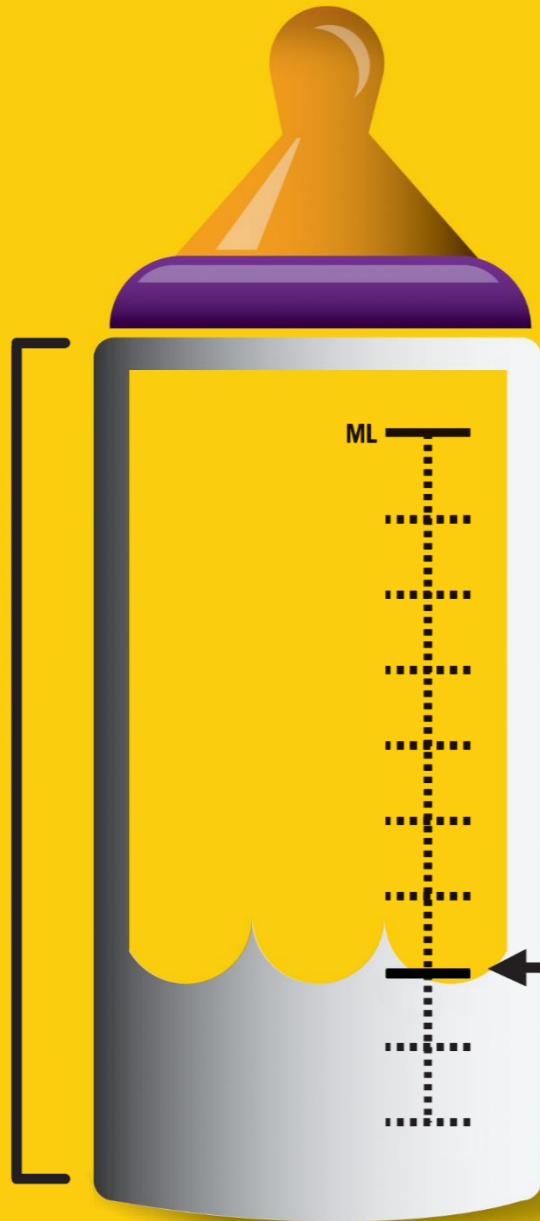
CHOOSE CAR SEAT:
BY AGE & SIZE



THE NUMBER
OF PEOPLE

**WHO
THINK**

THEIR CAR
SEATS ARE
BEING USED
CORRECTLY.



THE ONES
**WHO
ACTUALLY
DO.**

KNOW FOR SURE
IF YOUR CHILD IS IN THE RIGHT CAR SEAT.



VISIT SAFERCAR.GOV/THERIGHTSEAT



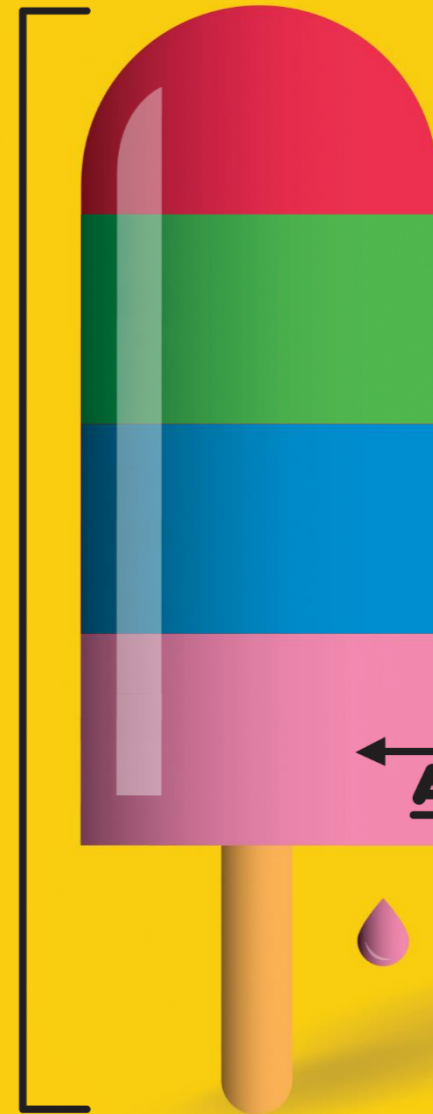
CHOOSE CAR SEAT:
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THE NUMBER
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THE ONES
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KNOW FOR SURE
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VISIT SAFERCAR.GOV/THERIGHTSEAT





LIVE

FOX
NEWS

Junction



PGR
PROCURADURÍA
GENERAL DE
LA REPÚBLICA

**SUBPROCURADURIA
DE INVESTIGACIÓN ESPECIALIZADA
EN DELINCUENCIA ORGANIZADA**

PGR
PROCURADURÍA
GENERAL DE
LA REPÚBLICA





FOX



...oyol

WHAT ISN'T MATHEMATICAL MODELING?

- *It is not modeling in the sense of, “I do; now you do.”*
- *It is not modeling in the sense of using manipulatives to represent mathematical concepts.*
- *It is not modeling in the sense of a “model” being just a graph, equation, or function.*
- *It is not just starting with a real world situation and solving a math problem.*
- *It is not beginning with the mathematics and then moving to the real world.*

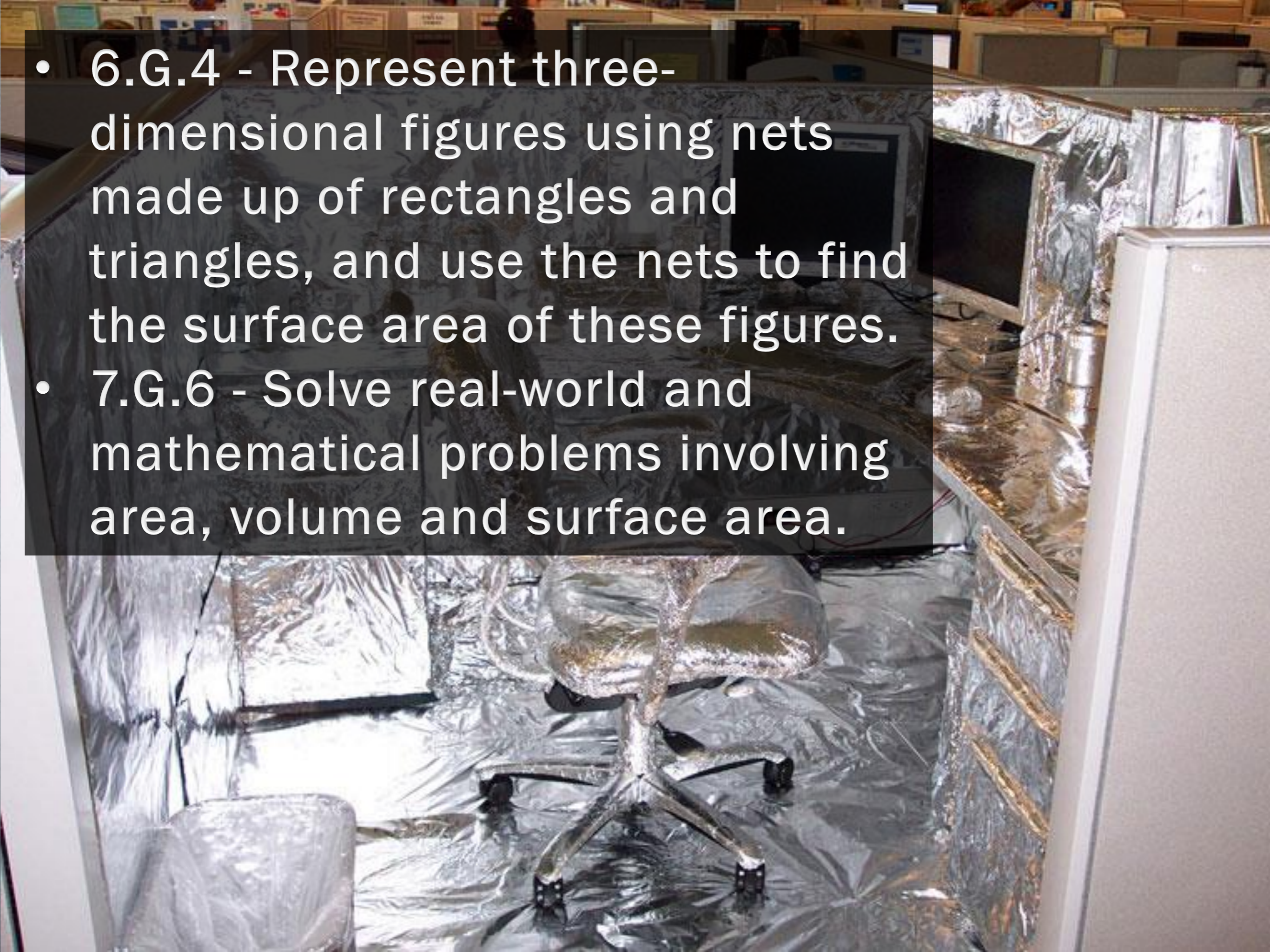
PROBLEM- BASED LEARNING FAQ

- *How often do teachers do problem-based learning?*
- *How long do problem based lessons take?*
- *Do teachers use problem-based lessons to introduce a topic or after you've already taught it?*
- *How is problem-based learning assessed?*
- *How much time does it take to create a problem-based lesson?*

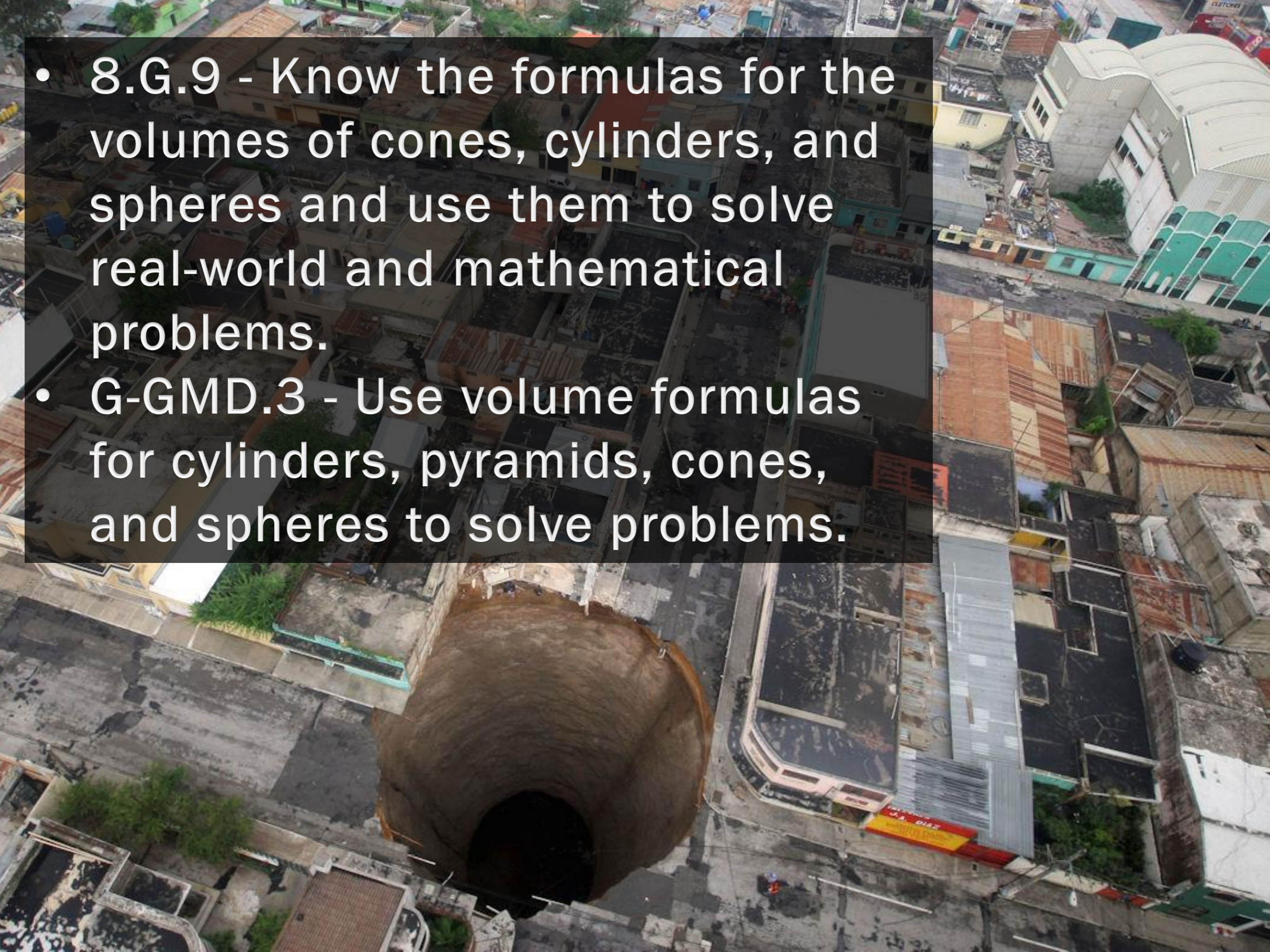
The Four C's

- o Communication
- o Curiosity

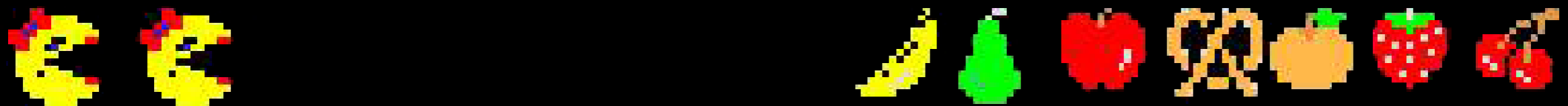
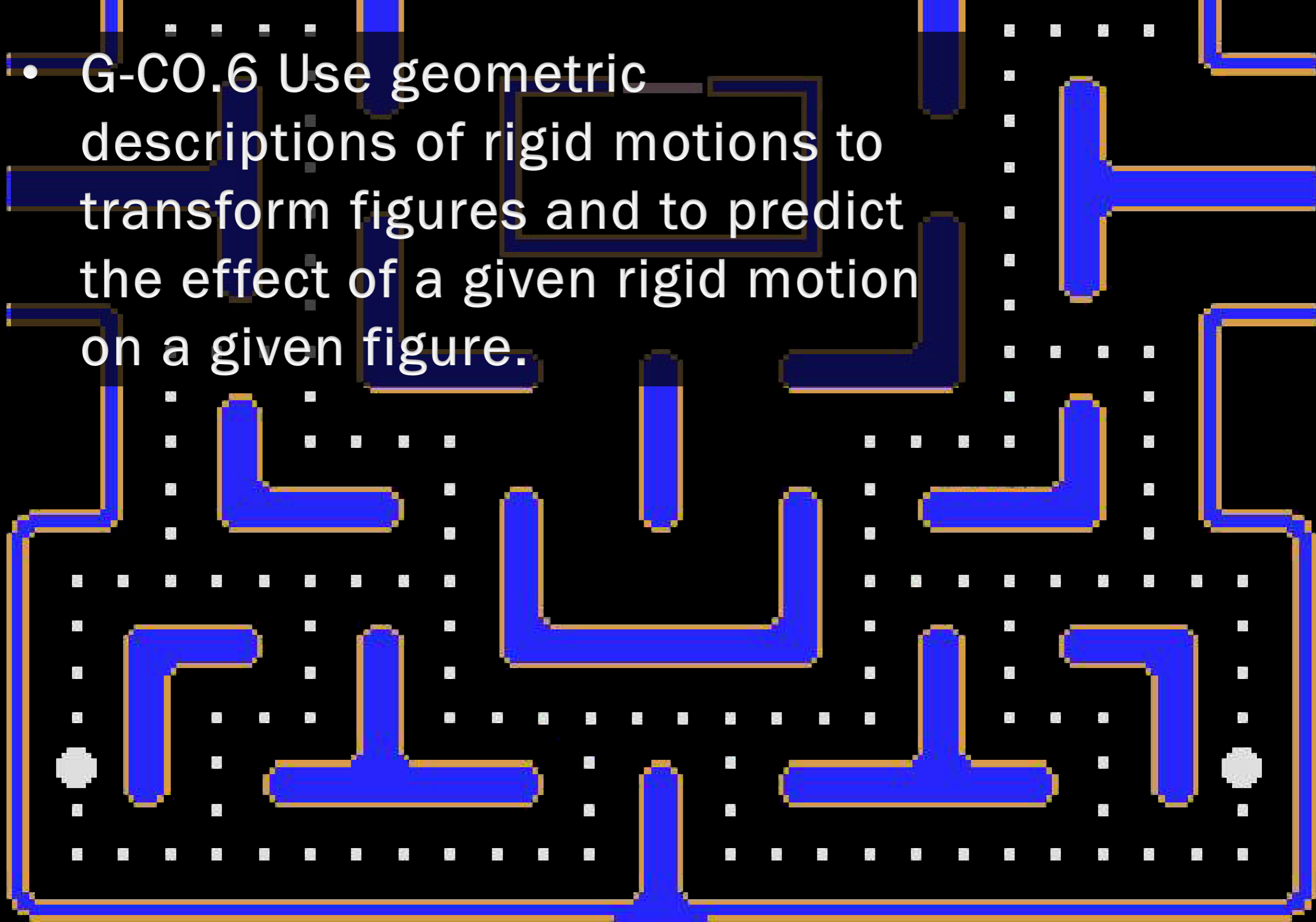
- 6.G.4 - Represent three-dimensional figures using nets made up of rectangles and triangles, and use the nets to find the surface area of these figures.
- 7.G.6 - Solve real-world and mathematical problems involving area, volume and surface area.



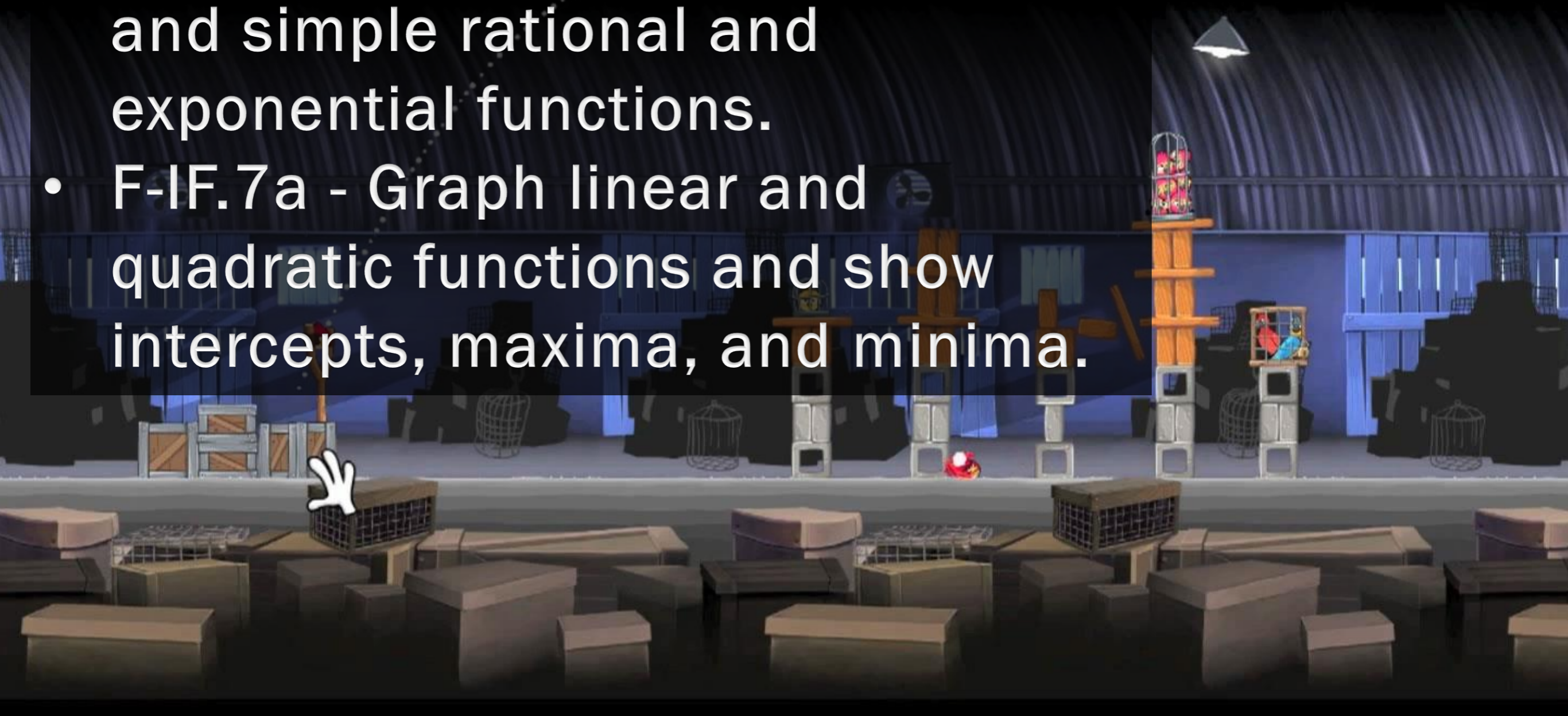
- 8.G.9 - Know the formulas for the volumes of cones, cylinders, and spheres and use them to solve real-world and mathematical problems.
- G-GMD.3 - Use volume formulas for cylinders, pyramids, cones, and spheres to solve problems.



- G-CO.6 Use geometric descriptions of rigid motions to transform figures and to predict the effect of a given rigid motion on a given figure.



- A-CED.1 - Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions.
- F-IF.7a - Graph linear and quadratic functions and show intercepts, maxima, and minima.



- 6.RP.2 - Understand the concept of a unit rate



The Four C's

- o Communication
- o Curiosity
- o Critical Thinking

Problem Solving Framework

- ▶ Inspired by Geoff Krall's resources at emergentmath.com

Name: _____ Period: _____ Date: _____

What problem are you trying to figure out?

What do you already know from the problem?

What do you need to know to solve the problem?

What is your conclusion?

The Four C's

- o Communication
- o Curiosity
- o Critical Thinking
- o Content Knowledge

***WHAT
DOES IT
LOOK
LIKE...***

- when students have procedural skill but not conceptual understanding or the ability to apply mathematics?
- when students struggle to process mathematics at a higher depth of knowledge?

How far apart are the exits on this freeway: Jct 90 and Jefferson Blvd?





$$1\frac{1}{2} - 1\frac{1}{4}$$

$$1\frac{1}{2} - 1\frac{1}{4}$$

$1\frac{1}{2} - 1\frac{1}{4}$

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$\frac{2}{4} - \frac{1}{4}$

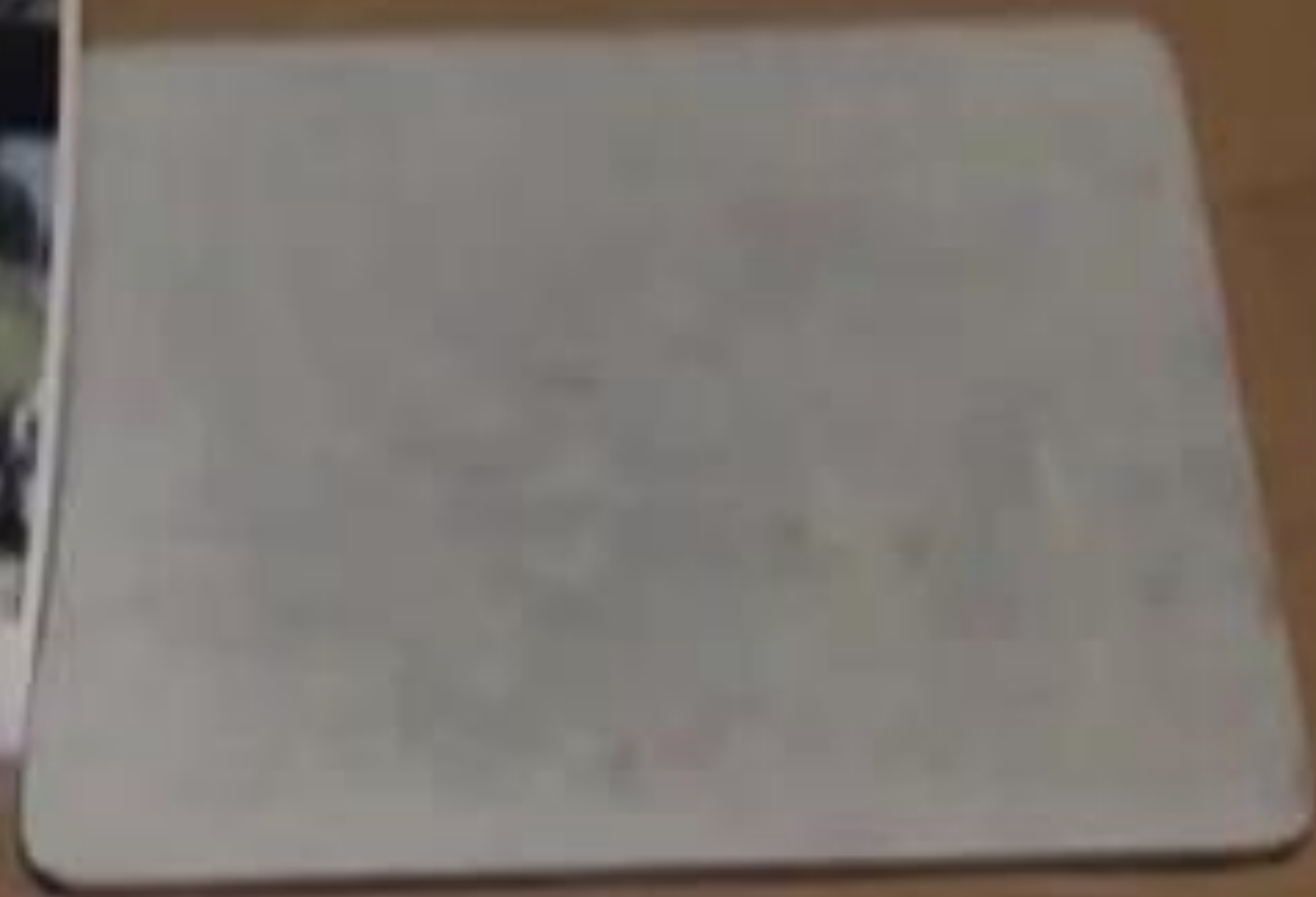
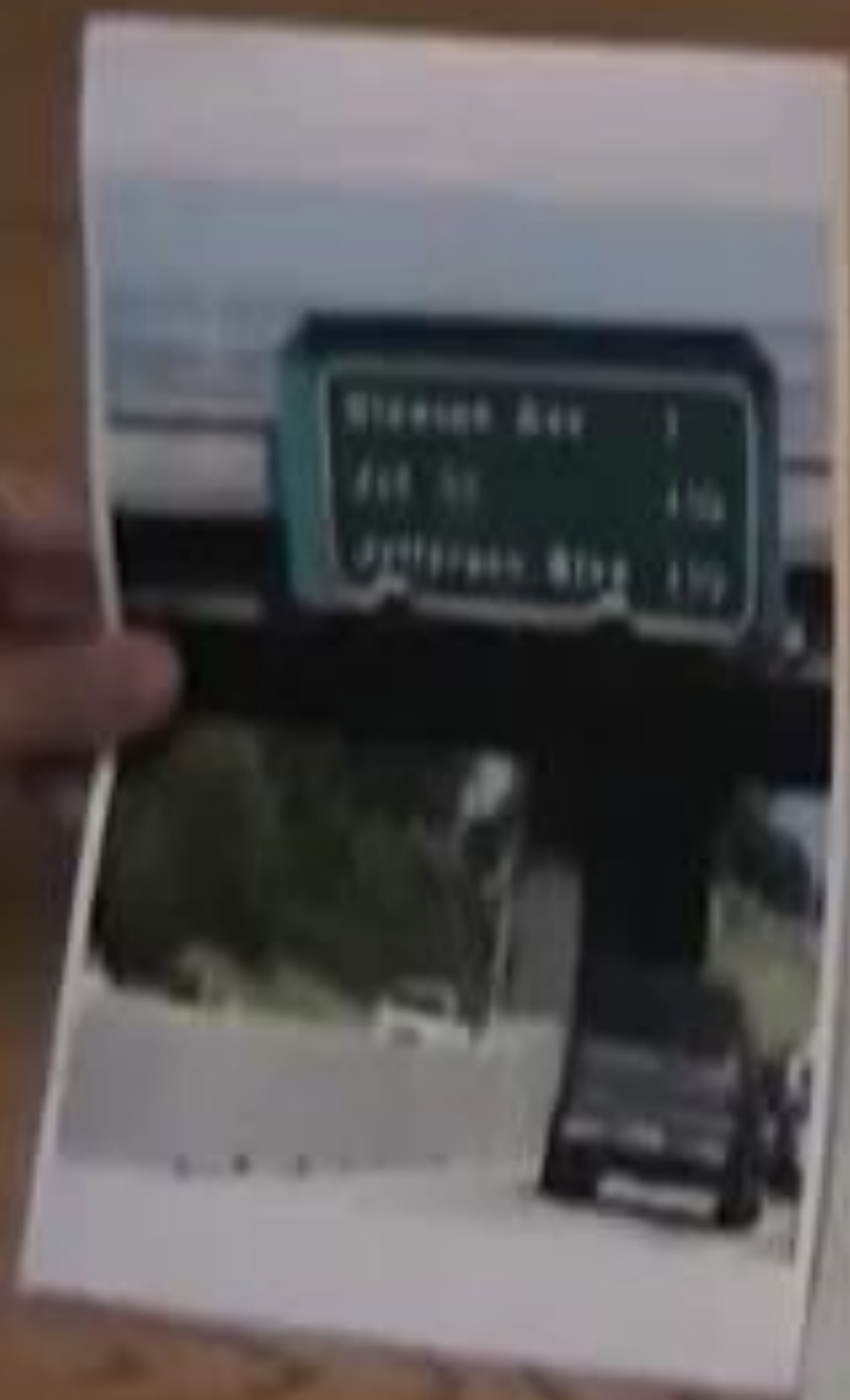
$\frac{1}{4}$

$1\frac{1}{2} - 1\frac{1}{4}$

$1\frac{2}{4} - 1\frac{1}{4}$

$\frac{2}{4} - \frac{1}{4}$

$\frac{1}{4}$



Questioning Scenarios

- The activity begins with teachers in groups of three taking the roles of teacher, student, or observer.
- The individuals playing the role of teacher and student each receive a slip of paper describing their scenario.
- The individual playing the role of observer waits to record all of the teacher's questions to the student.
- Once the activity begins, the teacher will talk to the student in the context of the scenario they read about on the slips of paper.

What did you get for the area of the circle with a radius of 2 units?

4 pi

Great. Do you have any questions?

No

What did you get for the area of the circle with a radius of 2 units?

4 pi

Great. How did you get your answer?

The radius is 2 so I plugged it into $2\pi r$ and got 4 pi.

Depth of Knowledge

- What?

Depth of Knowledge Examples

Perimeter

- DOK 1 – What is the perimeter of a rectangle with that measures 8 units by 4 units?
- DOK 2 – List the dimensions of a rectangle with a perimeter of 24 units.
- DOK 3 – Of all the rectangles with a perimeter of 24 units, which one has the most area?

Surface Area

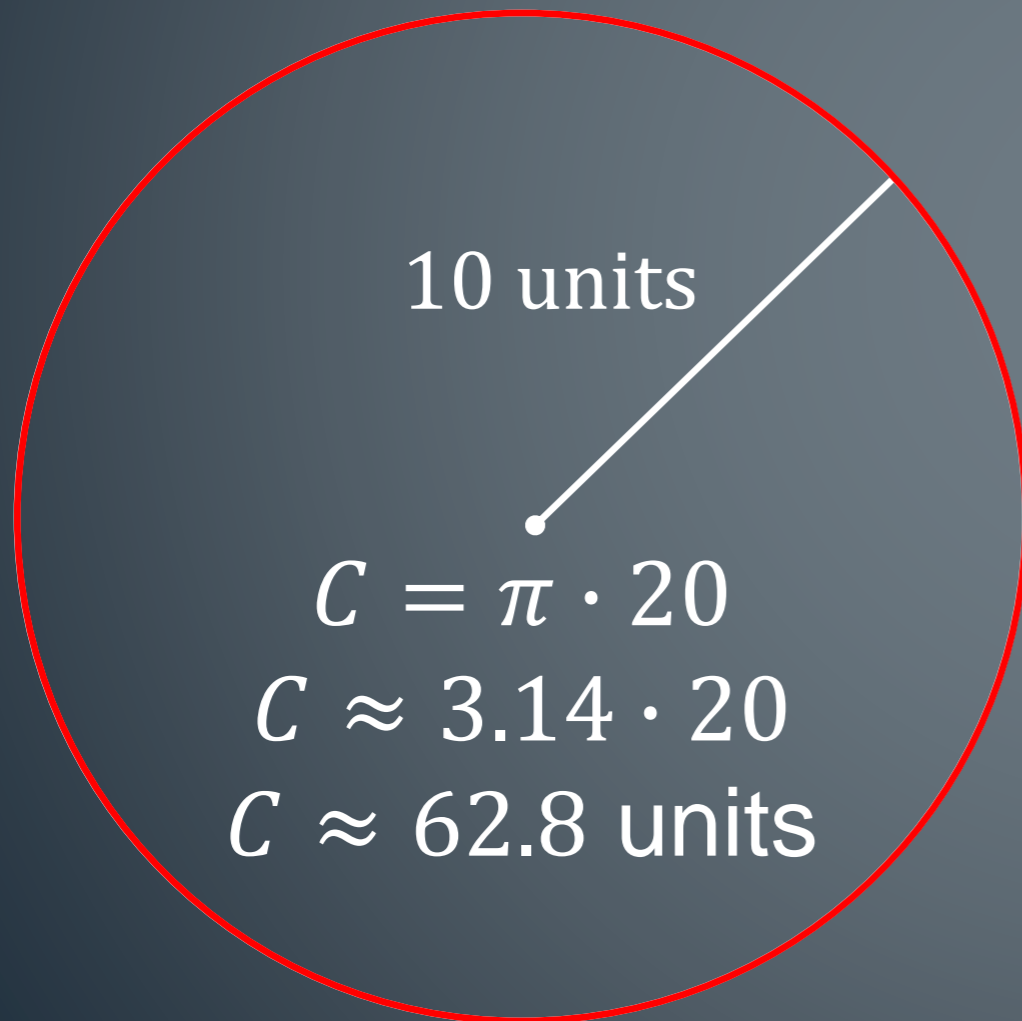
- DOK 1 – What is the surface area of a rectangular prism that measures 8 units by 4 units by 3 units?
- DOK 2 – List the dimensions of a rectangular prism with a surface area of 20 square units.
- DOK 3 – Of all the rectangular prisms with a surface area of 20 square units, which one has the most volume?

Depth of Knowledge

- What?
- How?
- Why?

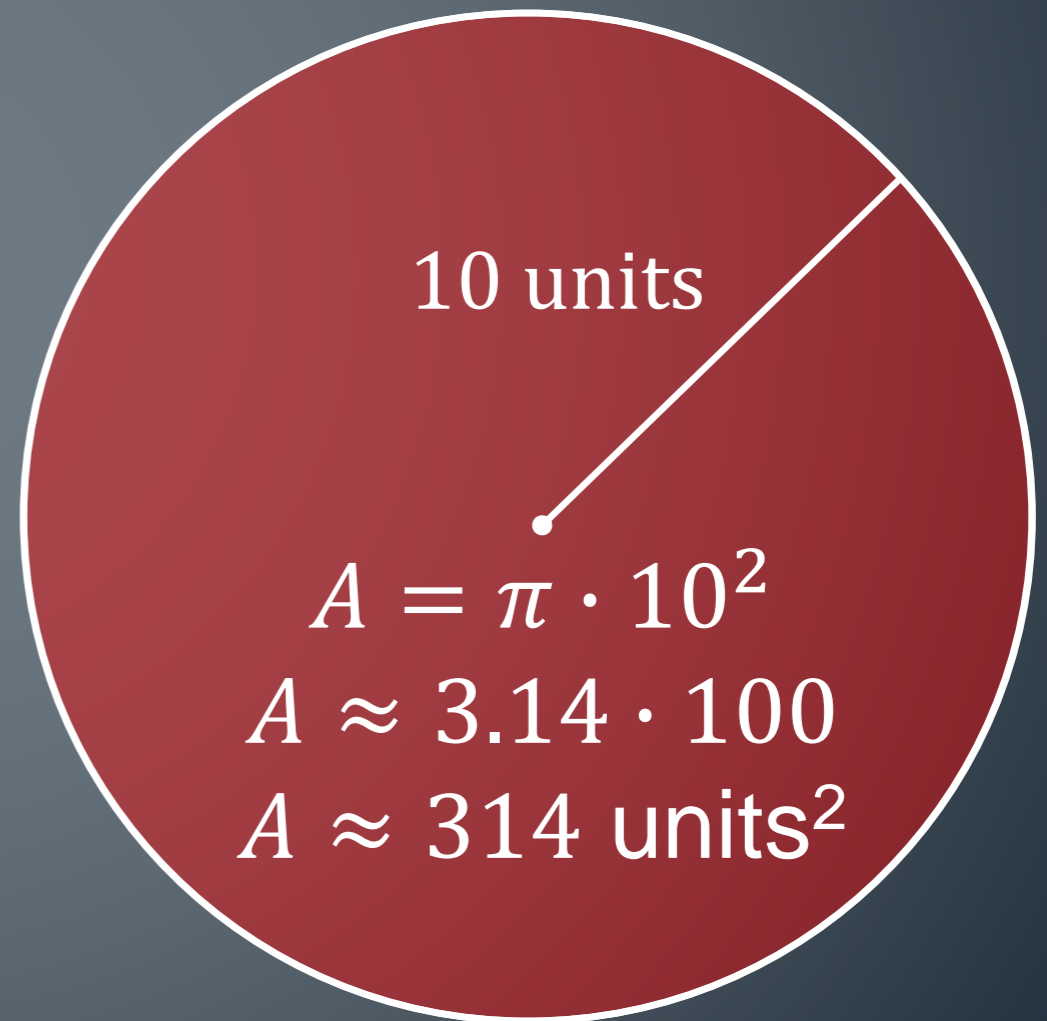
Depth of Knowledge – Level One

What is the circle's circumference? $\pi \approx 3.14$



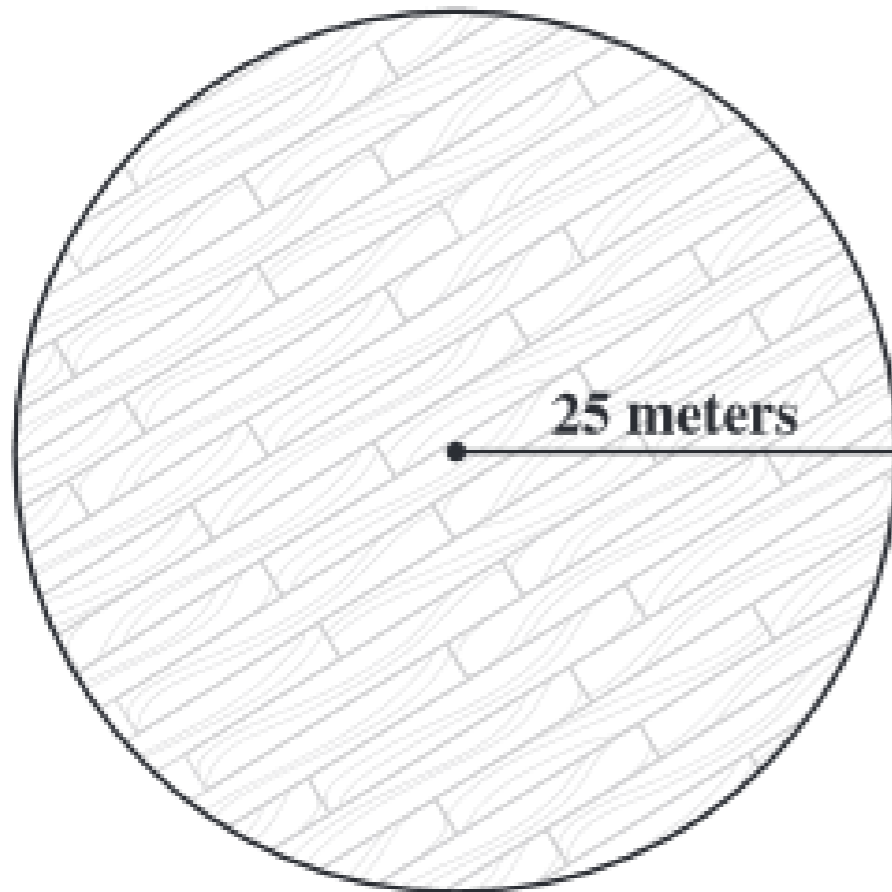
$$C = \pi d \text{ or } C = 2\pi r$$

What is the circle's area? $\pi \approx 3.14$



$$A = \pi r^2$$

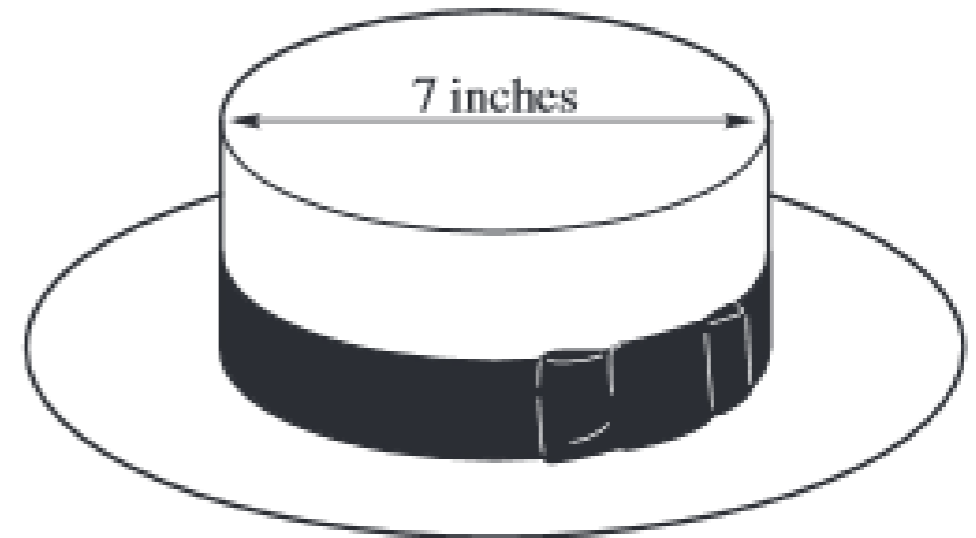
70 This circular stage has a radius of 25 meters.



Which equation could be used to find the area of the stage in square meters?

- A $A = 25\pi$
- B $A = 50\pi$
- C $A = \pi \cdot 25^2$
- D $A = \pi \cdot 50^2$

72 The top part of this hat is shaped like a cylinder with a diameter of 7 inches.



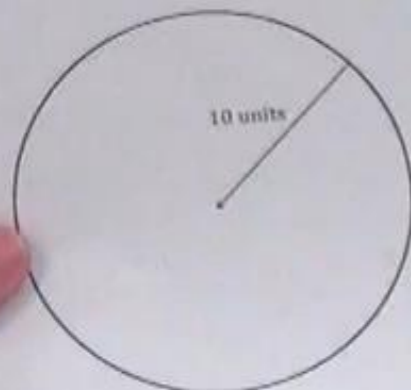
Which measure is *closest* to the length of the band that goes around the outside of the hat?

- A 10.1 inches
- B 11.0 inches
- C 22.0 inches
- D 38.5 inches

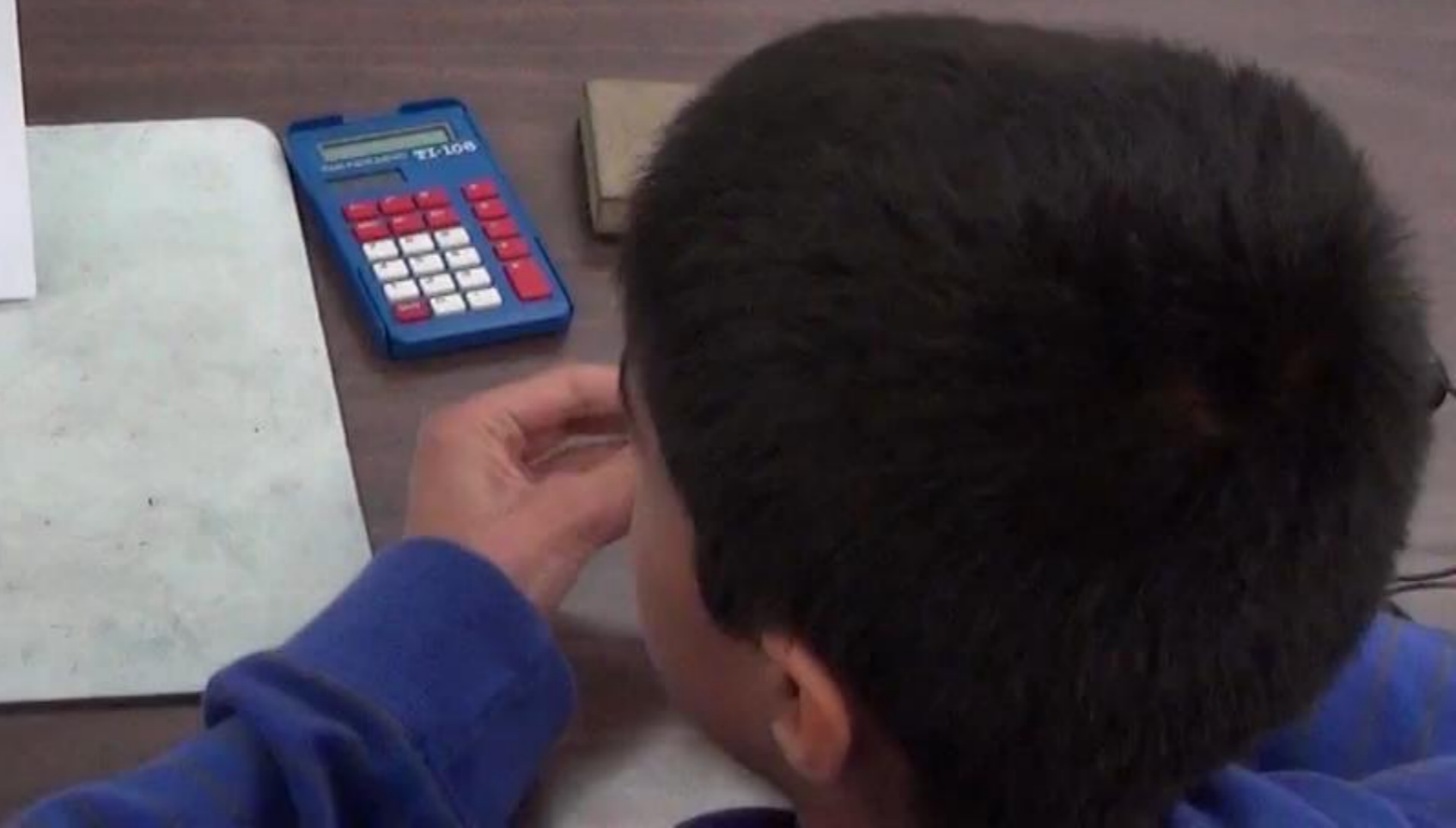
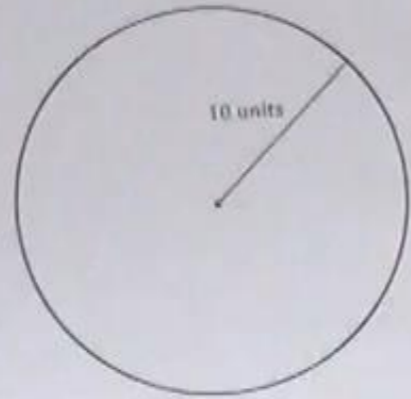
CSM00268

CSM00269

What is the circle's circumference? $\pi \approx 3.14$



What is the circle's area? $\pi \approx 3.14$

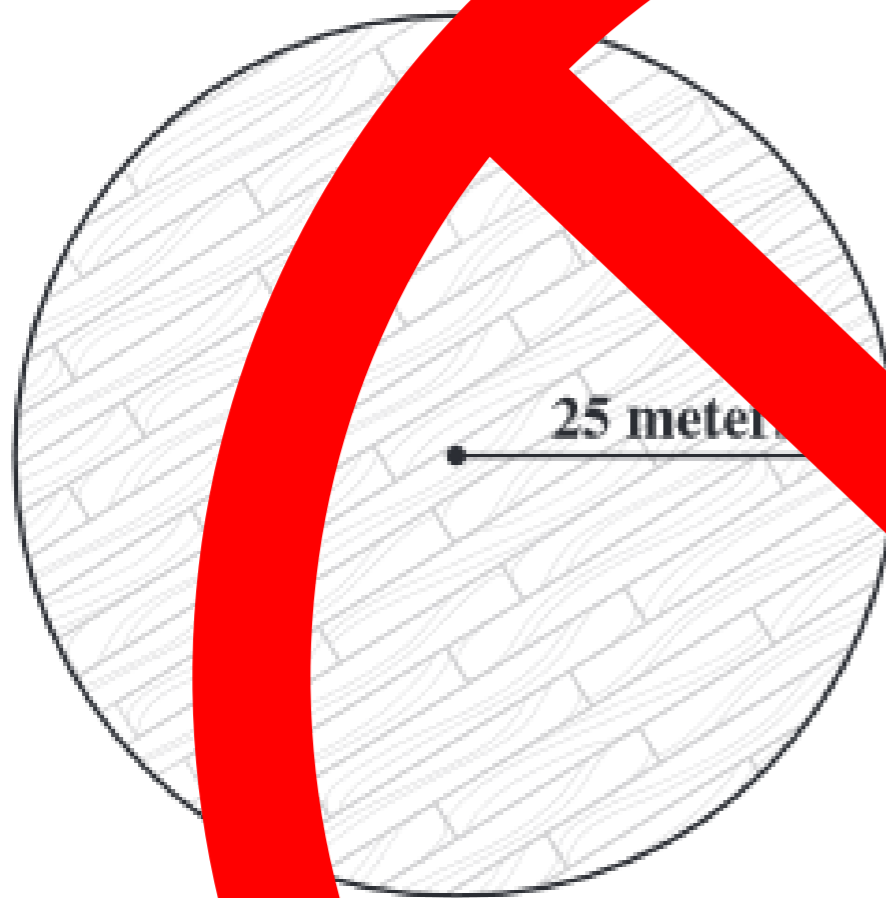


Student Data Facts

- 396 seventh grade students were assessed
- 68.26% correctly answered the circumference question
- 78.59% correctly answered the area question

Claim	Content Category	Assessment Targets	DOK	Minimum # Scored Tasks		Minimum # Items per Item Type		Min/Max Number of Items
				CAT	PT/ECR	SR	CR	
		A. Analyze proportional relationships and use them to solve real-world and mathematical problems.	1,2					
				p(9)=1.0				
Supporting	Supporting Cluster	E. Draw, construct, and describe geometrical figures and describe the relationship between them.						2,3
		F. Solve real-life and mathematical problems involving angle measure, area, surface area, and volume.						1,2
		problems involving angle measure, area, surface area, and volume.	1,2					
		G. Use random sampling to draw inferences about a population.	1,2		0	2	1	5/8
		H. Draw informal comparative inferences about two populations.	1,2					
		I. Investigate chance processes and develop, use, and evaluate probability models.	1,2					
				p(2)=1.0				

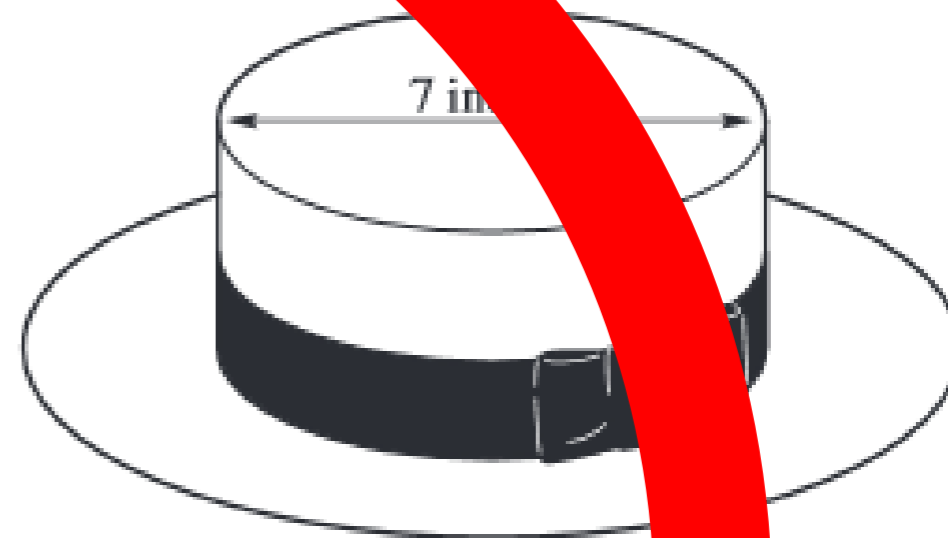
70 This circular stage has a radius of 25 meters.



Which equation could be used to find the area of the stage in square meters?

- A $A = 25\pi$
- B $A = 50\pi$
- C $A = \pi \cdot 25^2$
- D $A = \pi \cdot 50^2$

72 The crown of this hat is shaped like a cylinder with a diameter of 7 inches.



Which measure is *closest* to the length of the band that goes around the circumference of the hat?

- A 10.1 inches
- B 22.8 inches
- C 22.8 inches
- D 38.5 inches

Depth of Knowledge – Level Two

Which circle is bigger? How do you know?

Circle A

$$\text{Area} = 36 \text{ units}^2$$

$$C = \pi \cdot 2 \cdot r$$

$$36 \approx 6.28 \cdot r$$

$$\frac{36}{6.28} \approx r$$

$$5.73 \text{ units} \approx r$$

Circle B

$$\text{Circumference} = 36 \text{ units}$$

$$A = \pi \cdot r^2$$

$$A \approx 3.14 \cdot 5.73^2$$

$$A \approx 3.14 \cdot 32.83$$

$$A \approx 103.15 \text{ units}^2$$

SBAC Constructed Response Rubric

- For full credit (2 points):
 - Student reaches the correct conclusion.

AND

 - Student provides sufficient reasoning to support this conclusion.
- For partial credit (1 point):
 - Student reaches the correct conclusion but does not provide sufficient reasoning to support this conclusion.

OR

 - Student does not reach the correct conclusion but provides reasoning to support this conclusion that contains a minor conceptual or computation error.

Which circle is bigger? How do you know?

Circle A
Area = 36 units²

Circle B
Circumference = 36 units

36



Video Facts

- Of the ten students interviewed:
 - Ten correctly answered both of the DOK 1 questions.
 - One earned two points on the DOK 2 question.
 - Six earned one point on the DOK 2 question.
 - Three earned zero points on the DOK 2 question.

Student Data Facts

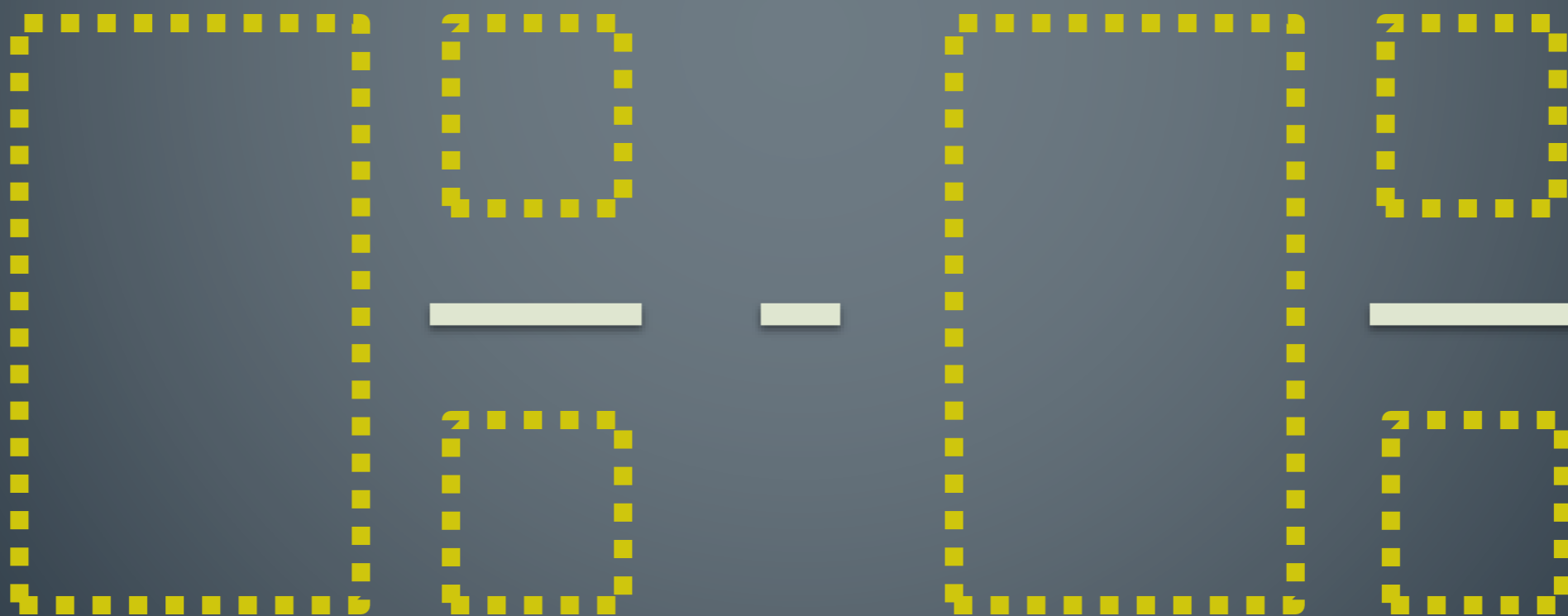
- Of the 396 seventh grade students who were assessed, 12.12% earned two points on the DOK 2 question.
- 97.92% of the students who correctly answered the DOK 2 question also correctly answered both of the two DOK 1 questions.
- 10.61% of the students who correctly answered both of the two DOK 1 questions also correctly answered the DOK 2 question.

More Student Data Facts

- 28.28% of the students earned only one point.
- All of them earned one point by choosing Circle B and providing insufficient reasoning.
- 59.59% of the students earned no points.

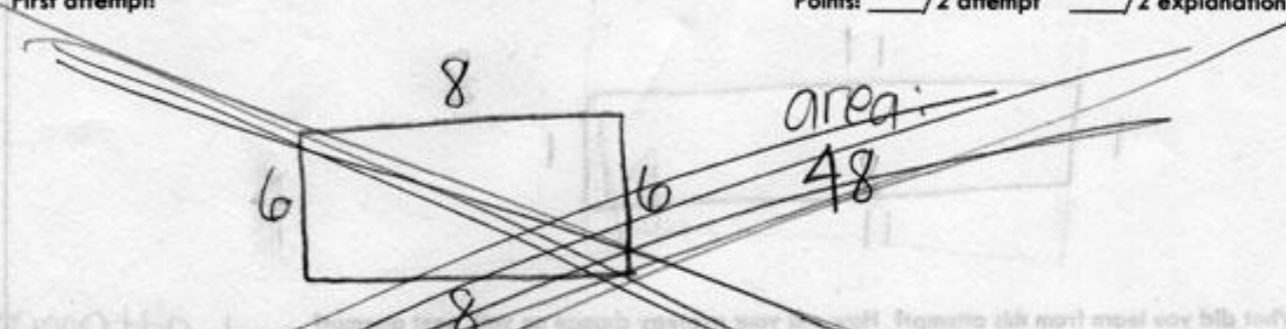
Assessing Deeper Understanding

Make the smallest difference using the numbers 1 through 9 no more than one time each.



STUDENT WORK

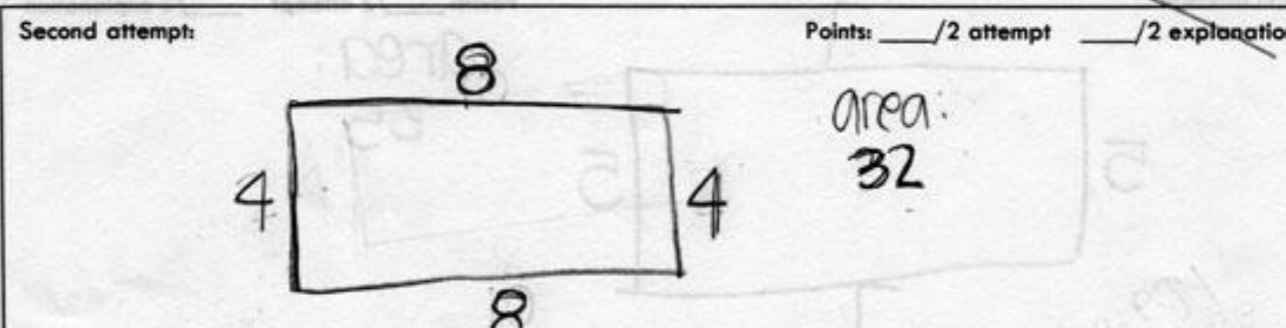
First attempt: Points: ___/2 attempt ___/2 explanation



area: 48

What did you learn from this attempt? How will your strategy change on your next attempt?
This attempt doesn't equal 24.

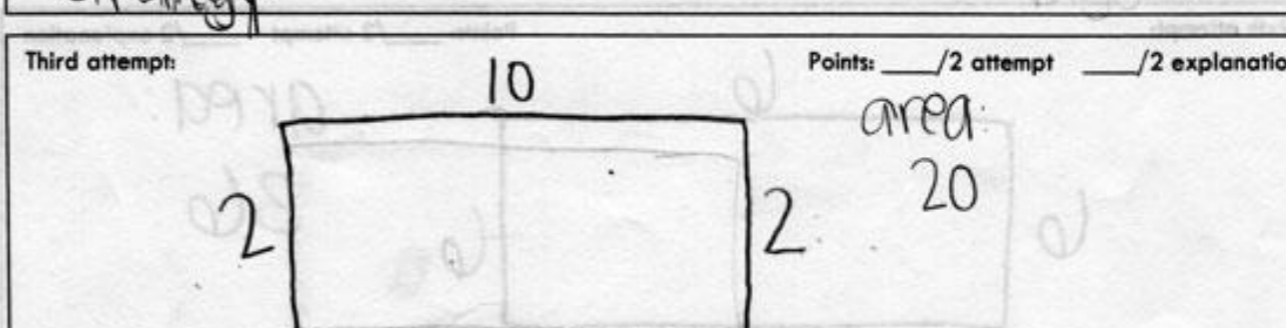
Second attempt: Points: ___/2 attempt ___/2 explanation



area: 32

What did you learn from this attempt? How will your strategy change on your next attempt?
The perimeter was 24, and the area was 32 but I think there's a bigger #
Strategy:

Third attempt: Points: ___/2 attempt ___/2 explanation



area: 20

What did you learn from this attempt? How will your strategy change on your next attempt?
I learned that the perimeter is 24 but there's a bigger area
Strategy:



Open Middle Problems

- Open middle problems require a higher depth of knowledge than most problems that assess procedural and conceptual understanding.
- They often have a “closed beginning” meaning that they all start with the same initial problem
- They often have a “closed end” meaning that they all end with the same answer
- They have an “open middle” meaning that there are multiple ways to approach and ultimately solve the problem

www.openmiddle.com

Problem-Based Lesson Resources

- My lessons: <http://www.robertkaplinsky.com/lessons>
- Dan Meyer: <http://threeacts.mrmeyer.com>
- Andrew Stadel: <http://tinyurl.com/mrstadel>
- Geoff Krall: <http://tinyurl.com/PrBLmaps>
- Nathan Kraft: <http://tinyurl.com/mrkraft>
- Dan Meyer's TED talk: <http://tinyurl.com/meyer-TED>



How Many Sheets Do You Need To Break Out Of Prison?

Operations with rational numbers



Why Choose Us?

1

Math content expert

Robert graduated from University of California, Los Angeles (UCLA) with a Bachelors of Science in Mathematics. He has taught mathematics to students at the elementary, middle, and high school levels. As an instructor for UCLA, he also taught math

Lessons





How Much Is One Third Of A Cup Of Butter?



How Do Skytypers Write Messages?



Robert Kaplinsky's Problem-Based Lessons



	A	B	C	D	E	F	
1	Task Name	Concept / Skill	Standard 1	Standard 2	Standard 3	Standard 4	Sta
2	How Can We Water All Of The Grass?	Circles, Pythagorean Theorem, trigonometric ratios	7.G.4	8.G.7	G-SRT.8	G-MG.1	G-M
3	How Much Money IS That?!	Volume of rectangular prism	5.MD.3	5.MD.4	5.MD.5	5.MD.5b	5.M
4	How Much Money Should Dr. Evil Demand?	Exponential Growth	N-RN.2	A-SSE.1	A-SSE.3c	A-SSE.4	A-R
5	How Tall Is Mini-Me?	Scale and Dividing Decimals	5.NF.5	5.NF.5a	5.NF.5b	6.NS.3	
6	How Did They Make Ms. Pac-Man?	Transformations (Rotations, Reflections, and Translations)	8.G.1	8.G.2	8.G.3	8.G.4	G-S
7	Which Ticket Option Is The Best Deal?	Unit Rates and Ratios	6.RP.2	6.RP.3	6.RP.3a	6.RP.3b	
8	How Far Apart Are The Freeway Exits?	Fractions on a Number Line and Subtracting Fractions	3.NF.2	3.NF.2b	4.NF.2	4.NF.3a	4.N
9	Do We Have Enough Paint?	Area	3.MD.5	3.MD.6	3.MD.7		
10	How Many Stars Are There In The Universe?	Scientific Notation	8.EE.3	8.EE.4			
11	What Rides Can You Go On?	Inequalities and Measurement	2.MD.1	6.NS.7a	6.NS.7b		
12	Do You Have Enough Money?	Money	2.MD.8				
13	Which Bed Bath & Beyond Coupon Should You Use?	Percent Discount	7.RP.3				
14	Is Gas Cheaper With Cash Or Credit Card?	Percent Discount	7.RP.3				
15	Where's The Nearest Toys R Us?	Pythagorean Theorem (Distance in coordinate system)	8.G.8	G-SRT.8	G-GPE.7		
16	How Sharp Is The iPhone 5's Retina Display?	Pythagorean Theorem (Length of a side)	8.G.7	G-SRT.8	G-GPE.7		
17	When Should She Take Her Medicine?	Operations with Time Intervals	4.MD.2				
18	How Big Are Sunspots?	Converting Units, Proportions, and Scientific Notation	5.MD.1	7.RP.2	7.G.4	8.EE.4	G-M
19	What Michael's Coupon Should I Use?	Percent Discount	7.RP.3	A-CED.3			
20	Is It Cheaper To Pay Monthly or Annually?	Decimal Operations and/or Systems of Equations	5.NBT.7	8.EE.8c	A-CED.3	A-REI.11	F-E
21	How Big Is The 2010 Guatemalan Sinkhole?	Volume of Cylinder	5.MD.3	5.MD.4	5.MD.5	8.G.9	G-C
22	How Can You Win Every Prize At Chuck E. Cheese's?	Decomposing Numbers and/or Systems of Equations	2.NBT.7	3.NBT.2	3.NBT.3	8.EE.8c	A-C
23	How Many Royal Flushes Will You Get?	Probability	7.SP.5	7.SP.6	7.SP.7	S-MD.5	S-M
24	How Much Does The Paint On A Space Shuttle Weigh?	Surface Area	6.G.4	7.G.6	8.G.7	G-MG.1	G-M
25	How Did Motel 6 Go From \$6 to \$66?	Percent Increase and Compound Interest	7.RP.3	A-SSE.1b	F-BF.1	F-IF.8b	F-L
26	How Much Does The Aluminum Foil Prank Cost?	Surface Area and Unit Rates	6.G.4	6.RP.2	6.RP.3	7.G.6	
27	How Many Laps Is A 5k Race?	Perimeter	4.MD.3				
28	Which Toilet Uses Less Water?	Systems of Equations/Inequalities	8.EE.8c	A-CED.3	A-REI.11	F-BF.1	
29	How Did Someone Get A \$103,000 Speeding Ticket In Finland?	Linear Equations	A-CED.2	F-BF.1	F-IF.4	F-IF.6	
30	Which Pizza Is A Better Deal?	Area or Circle, Square, and Unit Rates	3.MD.5	3.MD.6	3.MD.7	4.MD.3	6.R
31	How Big Is The World's Largest Deliverable Pizza?	Area of Square	3.MD.5	3.MD.6	3.MD.7	4.NBT.3	4.M
32	How Many Sheets Do You Need To Break Out Of Prison?	Integer Operations	5.NBT.6				
33	Do Hybrid Cars Pay For Themselves?	Systems of Equations or Rates	6.RP.2	6.RP.3	8.EE.8c	A-CED.3	F-E
34	How Many Hot Dogs Did They Eat?!	Linear and Quadratic Functions	8.F.3	8.F.4	F-BF.1	F-BF.2	F-IF
35	How Much Purple Ribbon Will You Need?	Perimeter & Circumference	3.MD.8	4.MD.3	7.G.4		
36	Are We There Yet?	Adding Times	3.MD.1	4.MD.2			
37	Which Chinese Food Coupon Should I Use?	Percent Discount	7.RP.3				
38	How Big Is The Vehicle That Uses Those Tires?	Ratio and Proportions	7.RP.2				
39	Where Would The Angry Birds Have Landed?	Create Equation From Quadratic Graph	A-CED.1	F-BF.1	F-IF.4	F-IF.7a	F-L
40	How Many Movies Can You See In One Day?	Adding Times	3.MD.1	4.MD.2			
41	Which Carrots Should You Buy?	Unit Rates	6.RP.1	6.RP.2	6.RP.3		
42	How Fast Can You Throw A Baseball?	Converting Units and Unit Rates	5.MD.1	6.RP.2			

Contact

Robert Kaplinsky



robert@robertkaplinsky.com



robertkaplinsky.com/pusd/



[@robertkaplinsky](https://twitter.com/robertkaplinsky)

