Webster Groves School District NOVEMBER 6, 2014









DOUBLE-DOUBLE Double Meat & 265 CHEESEBURGER 175 HAMBURGER **1**50 **FRENCH FRIES** ICED TEA 155 SHAKES Chocolate Strawberry 70 COFFEE



OPEN 10:30 a.m. to 1:00 a.m. Fri. and Sat. until 1:30 a.m.

www.FriedmanArchives.com

2004-10-31	
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Cashier: SAM GUEST #: 98	
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GUEST

2.65 88.20 90.85 6.81 97.66 \$97.66 \$.00

In

8:21 PM

	Serving Size (g)	Calories
Hamburger w/Onion	243	390
Cheeseburger w/Onion	268	480
Double-Double w/Onion	330	670



Layers	Cost
1	\$1.75
2	\$2.65
3	\$3.55
4	\$4.45
•	•
•	•
20	\$18.85
•	•
•	
100	\$90.85
•	•
•	•
Ν	\$1.75 + (N-1)*\$0.90

bun + produce + meat + cheese + meat + cheese = \$2.65

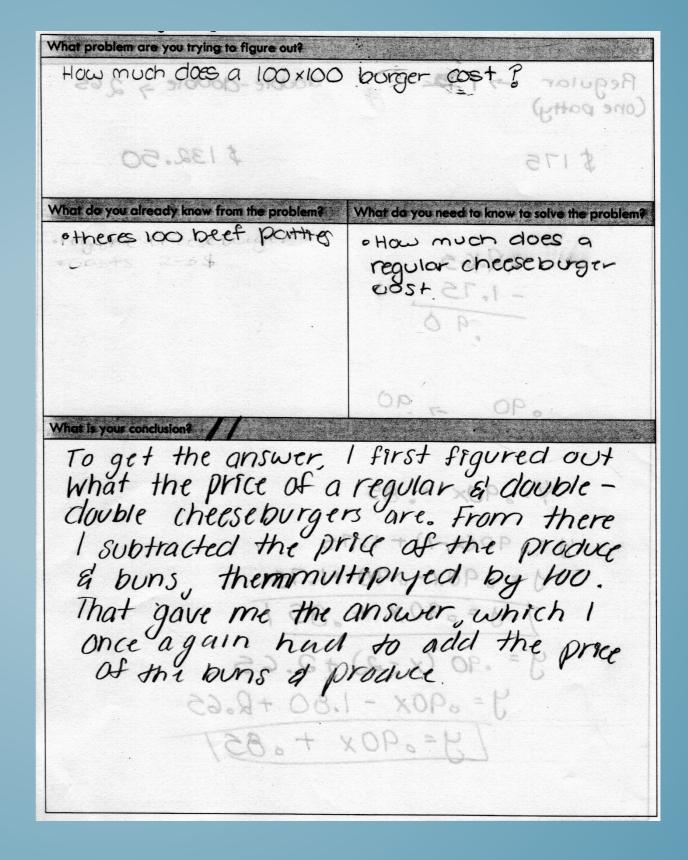
bun + produce + meat + cheese = \$1.75

meat + cheese = \$0.90

The Reality

- Students needed guidance to figure out a layer's cost
- Not every class is ready to go straight to 100x100
- Common wrong answers included:
 - \$175.00 (\$1.75 x 100 cheeseburgers)
 - \$132.50 (\$2.65 x 50 Double-Doubles)
- Students had equations that had more than X patties
- Students were surprised to see three different equations:
 - Starting with a Double-Double
 - Starting with a cheeseburger
 - Starting with produce and bun only

STUDENT WORK





Math Question

- Solve the problem on your own. Do not work or share your answer with anyone else.
- You will have 30 seconds to complete it.
- Write your answer down on a paper.

There are 125 sheep and 5 dogs in a flock. How old is the shepherd?

Of the 32 students I interviewed...

- 75% of them gave me numerical responses
- 2 students calculated the answer to be 130(125 + 5)
- 2 students calculated the answer to be 120(125-5)
- 12 students calculated the answer to be 25 (125 \div 5)
- O students calculated the answer to be 625 (125 x 5)
- 4 students stated that they guessed their answer (90, 5, 42, and 50)
- 4 students tried to divide 125 by 5 but could not correctly implement the procedure

Takeaways

- Making sense of mathematics
- Intellectual autonomy
 - Intellectual autonomy is about being able to think for yourself and not being dependent on others for the direction and control of one's thinking.

What Does the NHTSA Say?

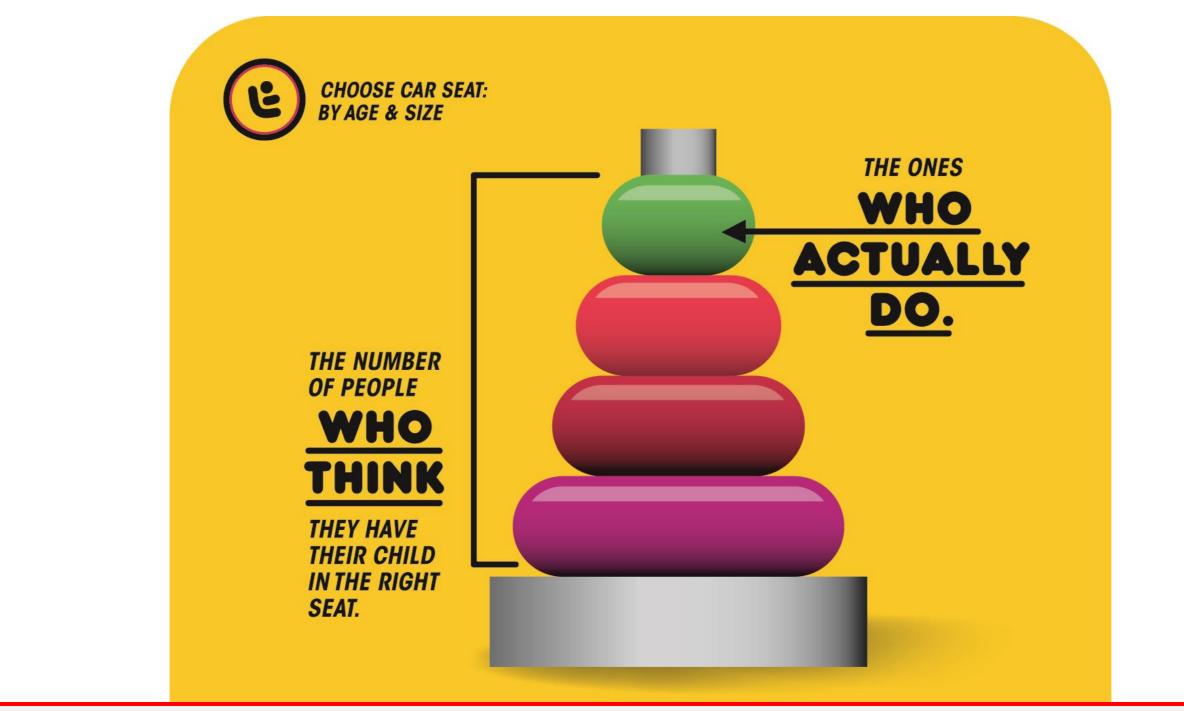
Key Statistics and Consumer Insights:

• Motor vehicle crashes are the leading cause of death for children age 1 through 12 years old.¹

According to a NHTSA study, 3 out of 4 kids are not as secure in the car as they should be because their car seats are not being used correctly.

be reduced by about hair if the correct child safety seats were always used.

¹ Source: Based on the latest mortality data currently available from the CDC's National Center for Health Statistics.



- "because they have their child in the right seat"
- "because their car seats are not being used correctly"

IF YOUR CHILD IS IN THE RIGHT CAR SEAT.

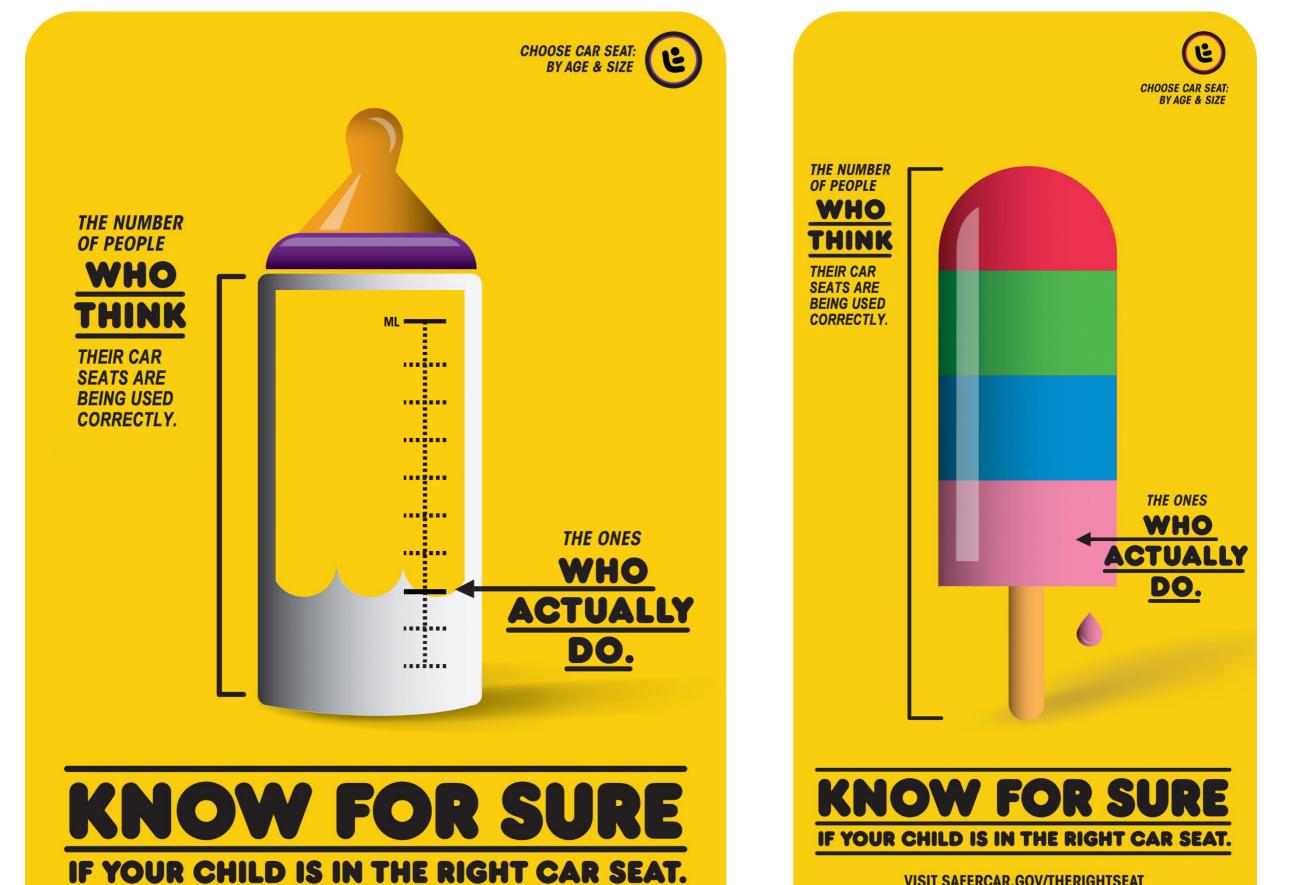


VISIT SAFERCAR.GOV/THERIGHTSEAT



Child Car

Safety



VISIT SAFERCAR.GOV/THERIGHTSEAT





Ad

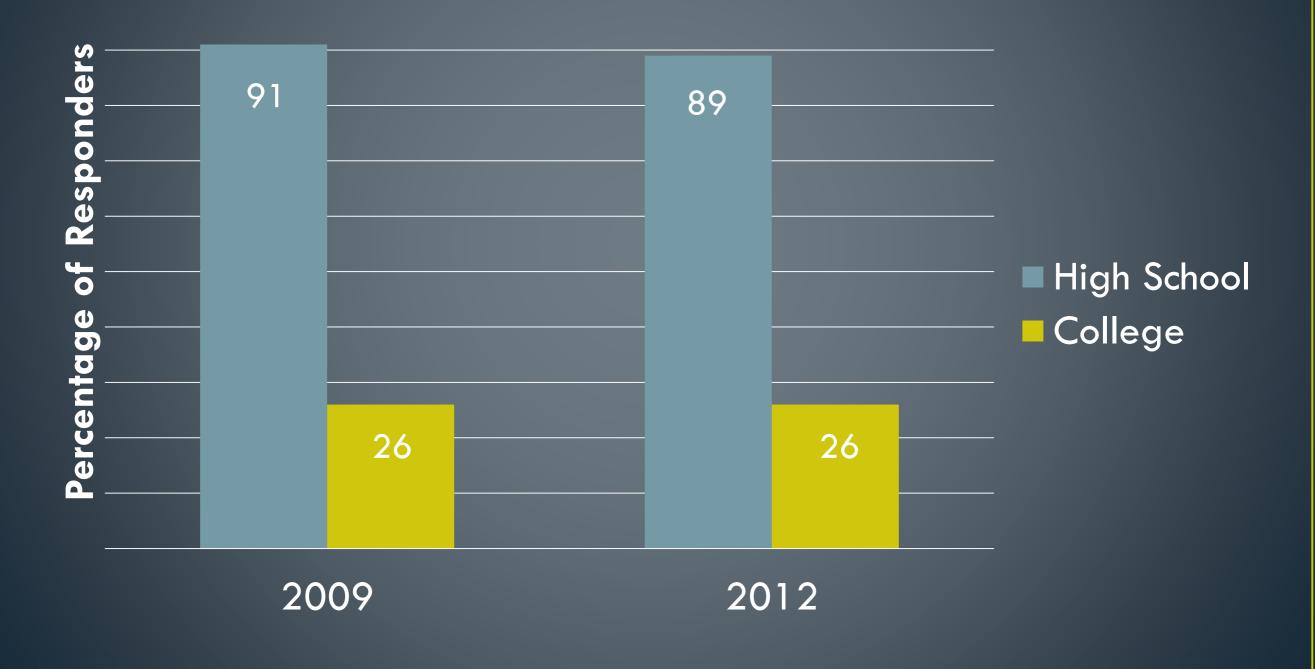


WHAT IS THE PURPOSE OF A K-12 EDUCATION?

 College readiness

 ACT National Curriculum Survey
 Survey
 Surveyed 9,937 educators

"Well" or "Very Well" Prepared for College



Source: http://www.act.org/research/policymakers/pdf/NCS-PolicySummary2012.pdf

WHAT IS THE PURPOSE OF A K-12 EDUCATION?

 College readiness
 Career readiness

 Association of American Colleges and Universities survey
 Surveyed over 300

- Surveyed over 300 employers with at least 25 employees and many new hires Critical thinking and analytical reasoning skills

Analyzing and solving complex problems

Communicating effectively orally and in writing

Applying knowledge and skills to real-world setting

Working w/ numbers and understanding statistics

More Less Same

Source: http://www.aacu.org/leap/documents/2013_EmployerSurvey.pdf

Working Lunch Question

Make the smallest difference using the numbers 1 through 9 no more than one time each.

 2	 2
A second second	- No. 1
	2 •
	-
	-
 Sec. 2	 - 1 - 1





SUBPROCURADURIA DE INVESTIGACIÓN ESPECIALIZADA EN DELINCUENCIA ORGANIZADA

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PROCUREQUELA

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WHAT ISN'T MATHEMATICAL MODELING?

- It is not modeling in the sense of, "I do; now you do."
- It is not modeling in the sense of using manipulatives to represent mathematical concepts.
- It is not modeling in the sense of a "model" being just a graph, equation, or function.
- It is not just starting with a real world situation and solving a math problem.
- It is not beginning with the mathematics and then moving to the real world.

Source: http://www.cde.ca.gov/ci/ma/cf/documents/aug2013apxdmathmodel.pdf

PROBLEM-BASED LEARNING FAQ

- How often do teachers do problem-based learning?
- How long do problem based lessons take?
- Do teachers use problem-based lessons to introduce a topic or after you've already taught it?
- How is problem-based learning assessed?
- How much time does it take to create a problem-based lesson?

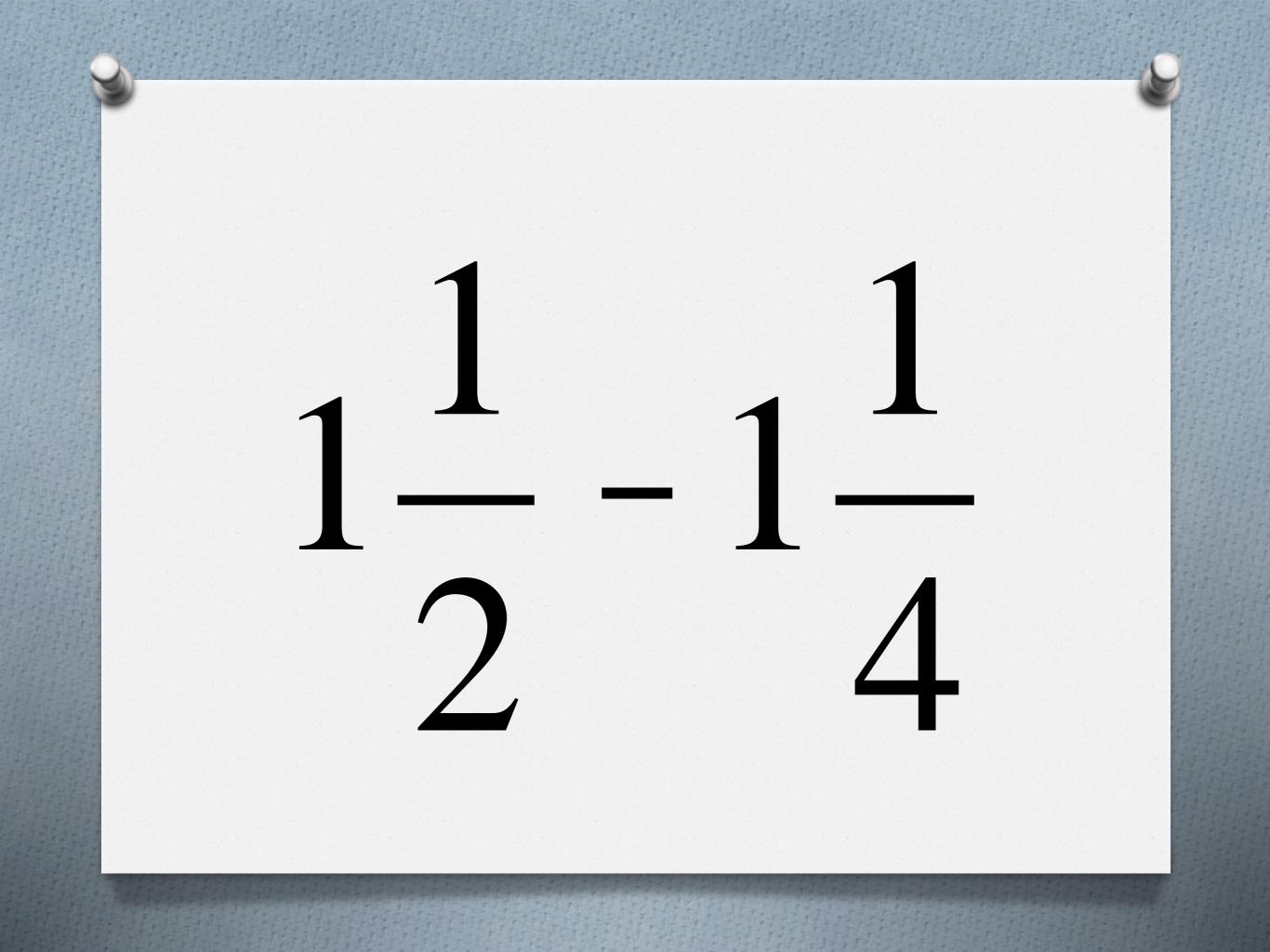
WHAT DOES IT LOOK LIKE...

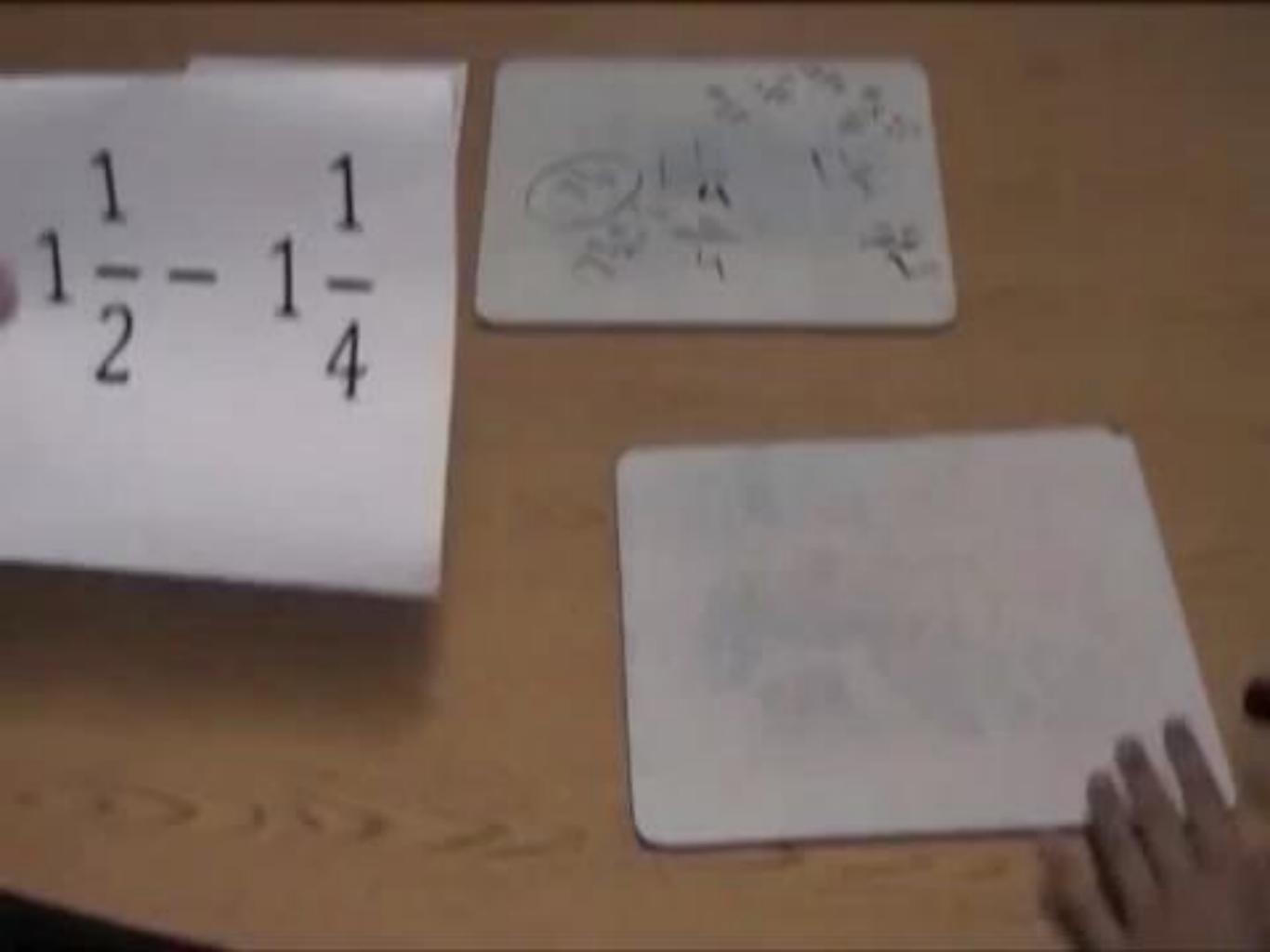
- when students have procedural skill but not conceptual understanding or the ability to apply mathematics?
- when students <u>can</u> work with numbers but <u>cannot</u>:
 - critically think
 - applying knowledge and skills to real-world settings
 - analyze and solve complex problems

How far apart are the exits on this freeway: Jct 90 and Jefferson Blvd?









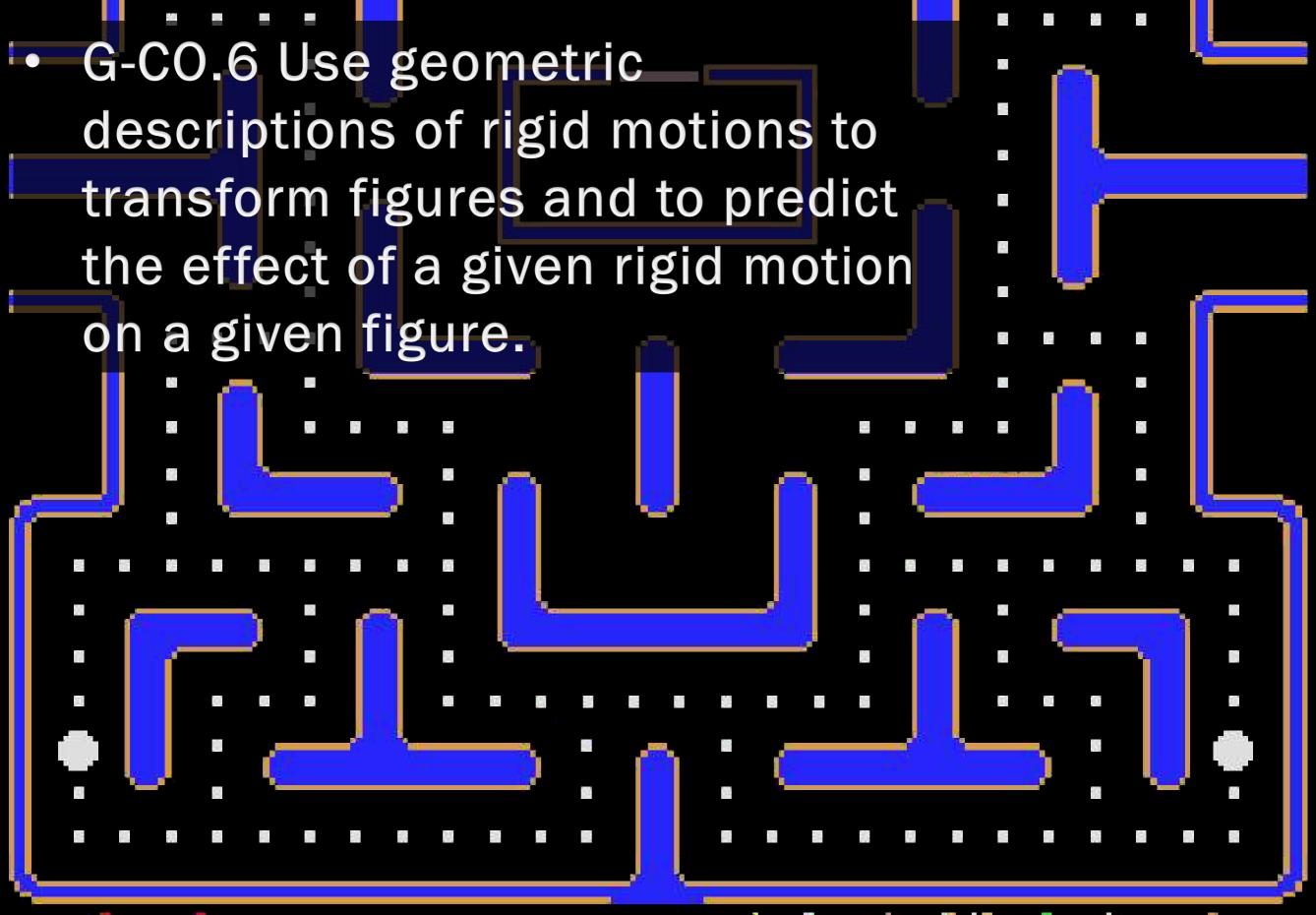


The Four C's

CommunicationCuriosity

6.G.4 - Represent threedimensional figures using nets made up of rectangles and triangles, and use the nets to find the surface area of these figures. 7.G.6 - Solve real-world and mathematical problems involving area, volume and surface area.

8.G.9 - Know the formulas for the volumes of cones, cylinders, and spheres and use them to solve real-world and mathematical problems. G-GMD.3 - Use volume formulas for cylinders, pyramids, cones, and spheres to solve problems.



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A-CED.1 - Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions. F-IF.7a - Graph linear and quadratic functions and show intercepts, maxima, and minima.

6.RP.2 - Understand the concept of a unit rate

Product

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The Four C's

Communication
Curiosity
Critical Thinking

Problem Solving Framework

Inspired by Geoff Krall's resources at emergentmath.com

ame:	Period: Date:
What problem are you trying to figure out?	What guesses do you have?
What do you already know from the problem?	What do you need to know to solve the problem?
What should we title this lesson?	
What is your conclusion? How did you reach that	conclusion?

The Four C's

- Communication
- Curiosity
- Critical Thinking
- Content Knowledge

Questioning Scenarios

- The activity begins with teachers in groups of three taking the roles of teacher, student, or observer.
- The individuals playing the role of teacher and student each receive a slip of paper describing their scenario.
- The individual playing the role of observer waits to record all of the teacher's questions to the student.
- Once the activity begins, the teacher will talk to the student in the context of the scenario they read about on the slips of paper.

What did you get for the area of the circle with a radius of 2 units?



Great. Do you have any questions?



What did you get for the area of the circle with a radius of 2 units?

4 pi

Great. How did you get your answer?

The radius is 2 so I plugged it into 2 pi r and got 4 pi.

Depth of Knowledge • What?

Depth of Knowledge Examples

<u>Perimeter</u>

- DOK 1 What is the perimeter of a rectangle with that measures 8 units by 4 units?
- DOK 2 List the dimensions of a rectangle with a perimeter of 24 units.
- DOK 3 Of all the rectangles with a perimeter of 24 units, which one has the most area?

<u>Surface Area</u>

- DOK 1 What is the surface area of a rectangular prism that measures 8 units by 4 units by 3 units?
- DOK 2 List the dimensions of a rectangular prism with a surface area of 20 square units.
- DOK 3 Of all the rectangular prisms with a surface area of 20 square units, which one has the most volume?

Depth of Knowledge • What? • Hows • Why?

Depth of Knowledge – Level One

What is the circle's circumference? $\pi \approx 3.14$

10 units

 $C = \pi \cdot 20$ $C \approx 3.14 \cdot 20$ $C \approx 62.8 \text{ units}$ area? π ≈ 3.14

10 units

What is the circle's

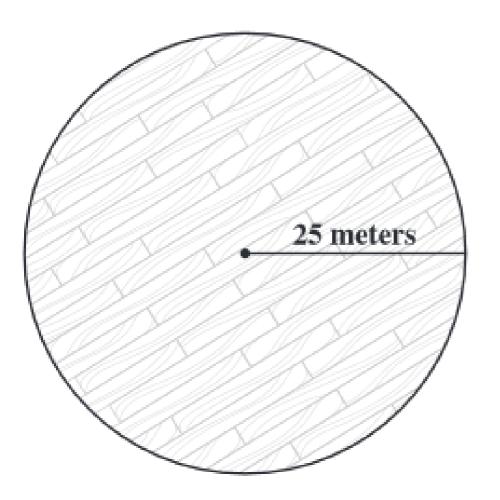
 $A = \pi \cdot 10^{2}$ $A \approx 3.14 \cdot 100$ $A \approx 314 \text{ units}^{2}$

 $C = \pi d$ or $C = 2\pi r$

 $A = \pi r^2$



This circular stage has a radius of 25 meters.

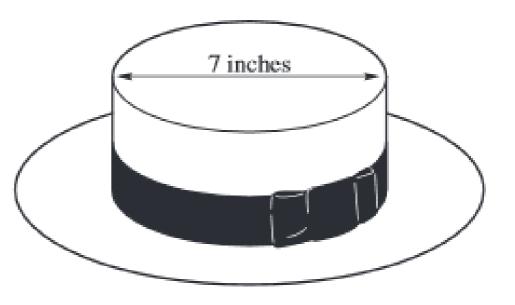


Which equation could be used to find the area of the stage in square meters?

- A $A = 25\pi$
- $\mathbf{B} = A = 50\pi$
- $C \quad A = \pi \cdot 25^2$
- $\mathbf{D} \quad A = \pi \bullet 50^2$



The top part of this hat is shaped like a cylinder with a diameter of 7 inches.

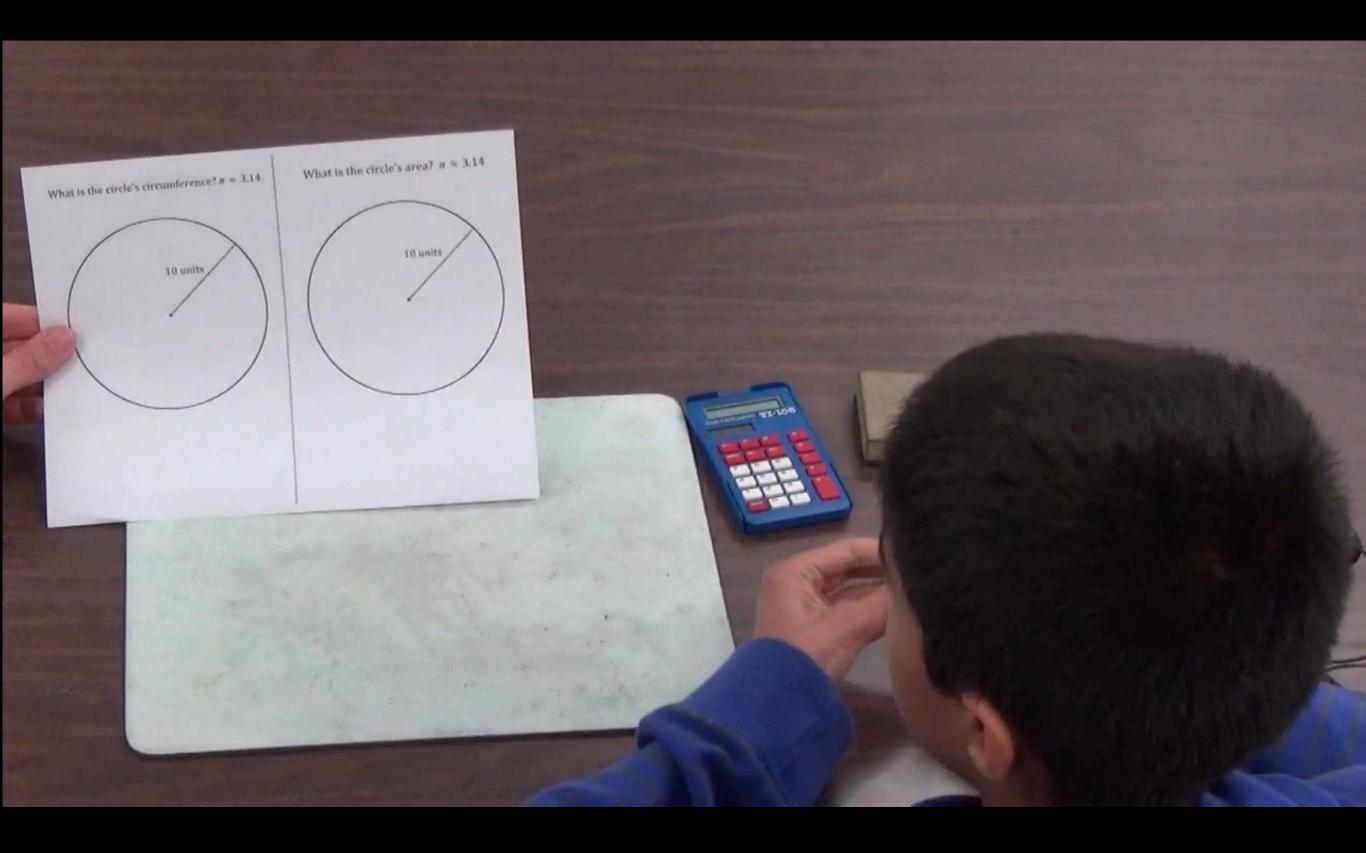


Which measure is *closest* to the length of the band that goes around the outside of the hat?

- A 10.1 inches
- B 11.0 inches
- C 22.0 inches
- D 38.5 inches

CSM00268

Source: 6th Grade CST Released Test Questions - http://www.cde.ca.gov/ta/tg/sr/documents/cstrtqmath6.pdf



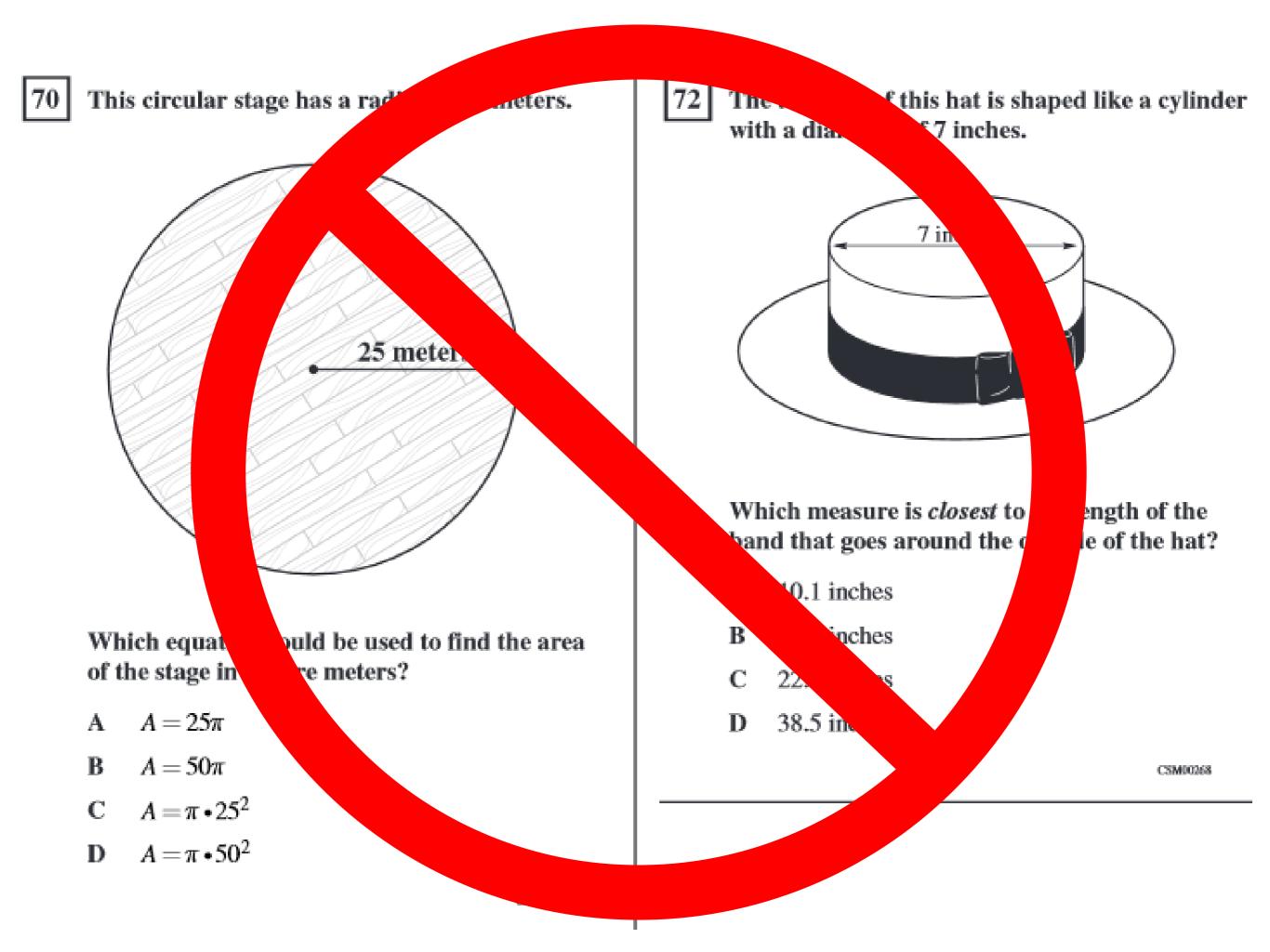
Student Data Facts

- 396 seventh grade students were assessed
- 68.26% correctly answered the circumference question
- 78.59% correctly answered the area question



Mathematics Preliminary Summative Assessment Blueprint Target Sampling Mathematics Grade 7—Table 6b

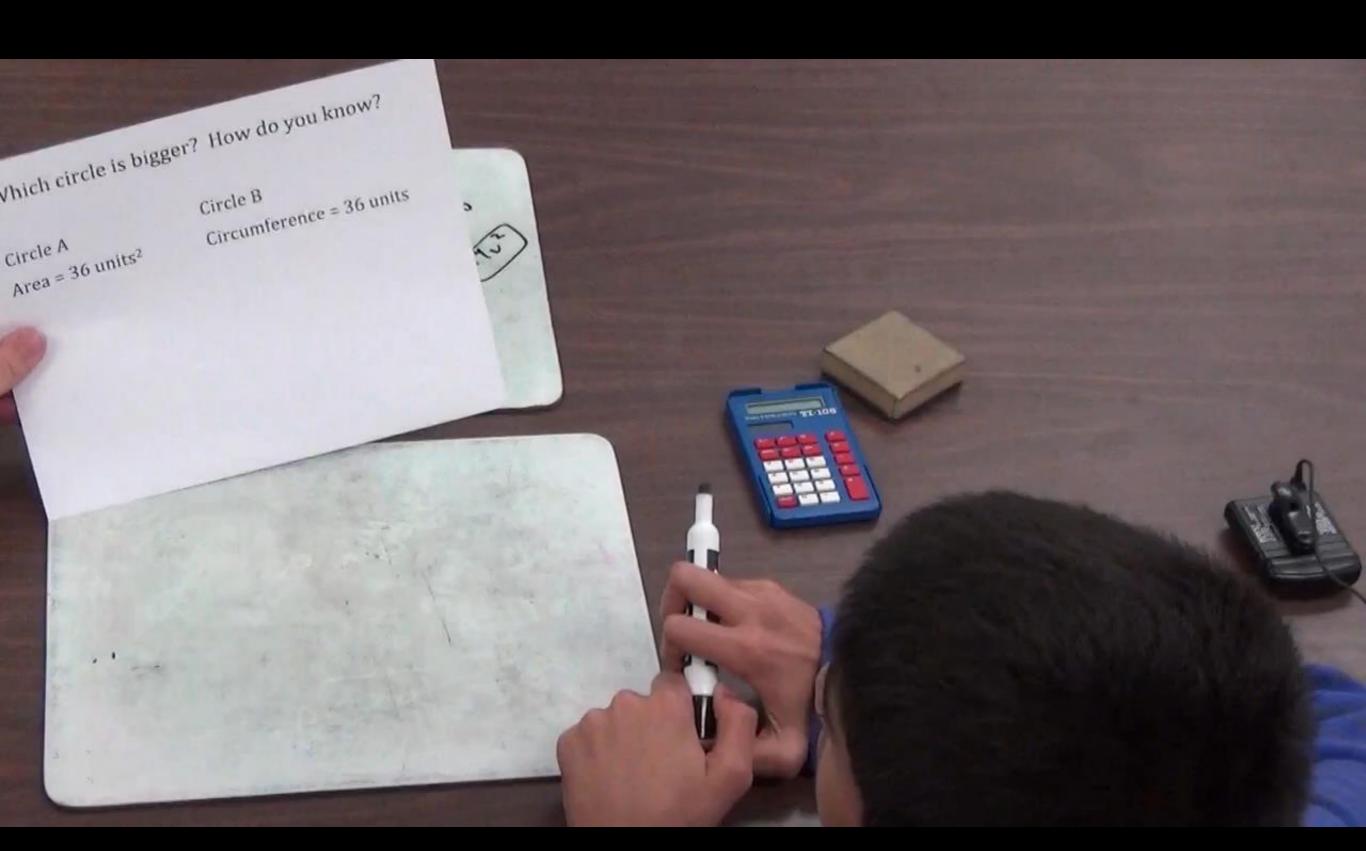
Claim	Content Category	Assessment Targets	DOK		# Scored sks		n # Items m Type	Min/Max Number
	Category			CAT	PT/ECR	SR	CR	of Items
		A. Analyze proportional relationships and use them to solve real-world and mathematical problems.	1,2	p(9)=1.0				
E. Draw, construct, and describe geometrical figures and describe the relationship between them.						2	,3	
		F. Solve real-life and mathematical problems involving angle measure, area, surface area, and volume.						,2
Cunnarti		problems involving angle measure, area, surface area, and volume.	1,2					
	Supporting Cluster	G. Use random sampling to draw inferences about a population.	1,2		0	2	1	5/8
		 H. Draw informal comparative inferences about two populations. 	1,2	p(2)=1.0				
		 Investigate chance processes and develop, use, and evaluate probability models. 	1,2					



Depth of Knowledge – Level Two Which circle is bigger? How do you know? Circle A Circle B Area = 36 units^2 Circumference = 36 units^2 $A = \pi \cdot r^2$ $C = \pi \cdot 2 \cdot r$ $A \approx 3.14 \cdot 5.73^2$ $36 \approx 6.28 \cdot r$ $A \approx 3.14 \cdot 32.83$ 36 $\overline{6.28} \approx r$ $A \approx 103.15 \text{ units}^2$ 5.73 units $\approx r$

SBAC Constructed Response Rubric

- For full credit (2 points):
 - Student reaches the correct conclusion.
 - AND
 - Student provides sufficient reasoning to support this conclusion.
- For partial credit (1 point):
 - Student reaches the correct conclusion but does not provide sufficient reasoning to support this conclusion.
 OR
 - Student does not reach the correct conclusion but provides reasoning to support this conclusion that contains a minor conceptual or computation error.



Video Facts

- Of the ten students interviewed:
 - Ten correctly answered both of the DOK 1 questions.
 - One earned two points on the DOK 2 question.
 - Six earned one point on the DOK 2 question.
 - Three earned zero points on the DOK 2 question.

Student Data Facts

- Of the 396 seventh grade students who were assessed, 12.12% earned two points on the DOK 2 question.
- 97.92% of the students who correctly answered the DOK 2 question also correctly answered both of the two DOK 1 questions.
- 10.61% of the students who correctly answered both of the two DOK 1 questions also correctly answered the DOK 2 question.

More Student Data Facts

- 28.28% of the students earned only one point.
- All of them earned one point by choosing Circle B and providing insufficient reasoning.
- 59.59% of the students earned no points.

Implementing Higher DOK Problems

- Attempt #1: DOK 3 Subtracting Mixed Numbers
 - Lesson learned

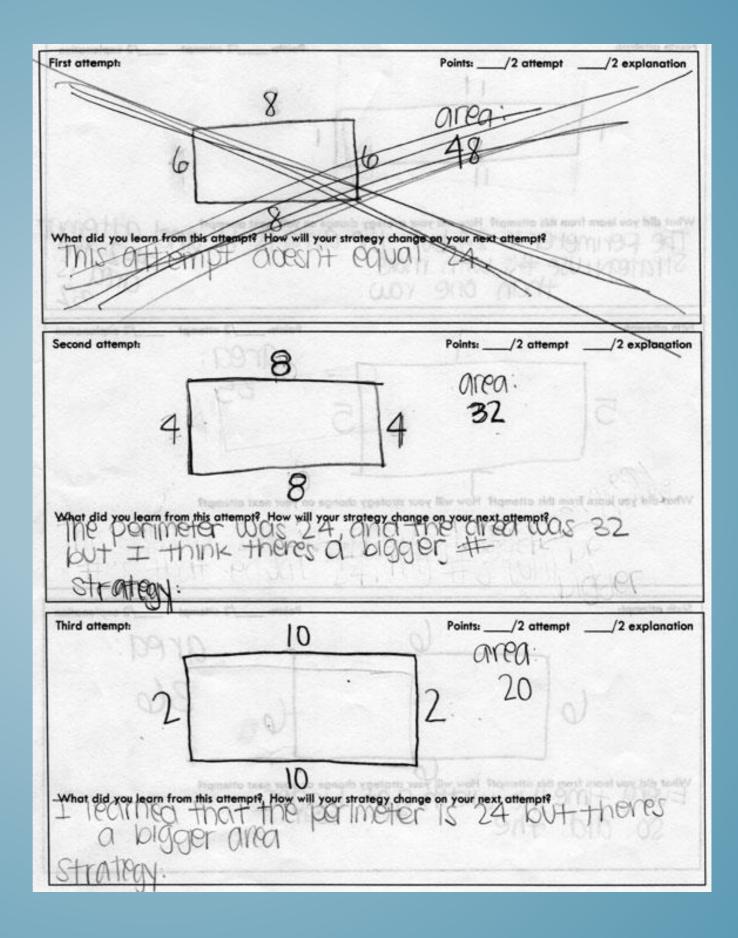
ORDER OF OPERATIONS

RECTANGLES: MAXIMIZING AREA

Directions: What is the greatest area you can make on a rectangle with a perimeter of 24 units?

- $\underbrace{\vdots \div \vdots (\vdots \div \vdots)}_{}$
 - Attempt #3: DOK 3 Area and Perimeter
 - Lessons learned:
 - Most of the 8th graders struggled even with this problem.
 - Would have been wiser to start with a DOK 1, then a DOK 2, and then this DOK 3 problem.

STUDENT WORK





Open Middle Problems

- Open middle problems require a higher depth of knowledge than most problems that assess procedural and conceptual understanding.
- They often have a "closed beginning" meaning that they all start with the same initial problem
- They often have a "closed end" meaning that they all end with the same answer
- They have an "open middle" meaning that there are multiple ways to approach and ultimately solve the problem

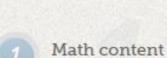
www.openmiddle.com

Problem-Based Lesson Resources

- Problem-based lesson search engine: <u>http://robertkaplinsky.com/prbl-search-engine/</u>
- My lessons: http://www.robertkaplinsky.com/lessons
- Dan Meyer: <u>http://threeacts.mrmeyer.com</u>
- Andrew Stadel: <u>http://tinyurl.com/mrstadel</u>
- Geoff Krall: <u>http://tinyurl.com/PrBLmaps</u>
- Dan Meyer's TED talk: <u>http://tinyurl.com/meyer-TED</u>



Why Choose Us?



expert

Robert graduated from University of California, Los Angeles (UCLA) with a Bachelors of Science in Mathematics. He has taught mathematics to students at the elementary, middle, and high school levels. As

Lessons









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How Much Is One Third Of A Cup Of Butter?



How Do Skytypers Write Messages?





Robert Kaplinsky's Problem-Based Lessons ☆ 🖿

File Edit View Insert Format Data Tools Help All changes saved in Drive

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	A	В	С	D	Е	F	
1	Task Name	Concept / Skill	Standard 1	Standard 2	Standard 3	Standard 4	Sta
2	How Can We Water All Of The Grass?	Circles, Pythagorean Theorem, trigonometric ratios	7.G.4	8.G.7	G-SRT.8	G-MG.1	G-I
	How Much Money IS That?!	Volume of rectangular prism	5.MD.3	5.MD.4	5.MD.5	5.MD.5b	5.N
	How Much Money Should Dr. Evil Demand?	Exponential Growth	N-RN.2	A-SSE.1	A-SSE.3c	A-SSE.4	A-F
	How Tall Is Mini-Me?	Scale and Dividing Decimals	5.NF.5	5.NF.5a	5.NF.5b	6.NS.3	
	How Did They Make Ms. Pac-Man?	Transformations (Rotations, Reflections, and Translations)	8.G.1	8.G.2	8.G.3	8.G.4	G-5
	Which Ticket Option Is The Best Deal?	Unit Rates and Ratios	6.RP.2	6.RP.3	6.RP.3a	6.RP.3b	
	How Far Apart Are The Freeway Exits?	Fractions on a Number Line and Subtracting Fractions	3.NF.2	3.NF.2b	4.NF.2	4.NF.3a	4.N
	Do We Have Enough Paint?	Area	3.MD.5	3.MD.6	3.MD.7		
	How Many Stars Are There In The Universe?	Scientific Notation	8.EE.3	8.EE.4			
11	What Rides Can You Go On?	Inequalities and Measurement	2.MD.1	6.NS.7a	6.NS.7b		
	Do You Have Enough Money?	Money	2.MD.8				
13	Which Bed Bath & Beyond Coupon Should You Use?	Percent Discount	7.RP.3				
14	Is Gas Cheaper With Cash Or Credit Card?	Percent Discount	7.RP.3				
15	Where's The Nearest Toys R Us?	Pythagorean Theorem (Distance in coordinate system)	8.G.8	G-SRT.8	G-GPE.7		
16	How Sharp Is The iPhone 5's Retina Display?	Pythagorean Theorem (Length of a side)	8.G.7	G-SRT.8	G-GPE.7		
17	When Should She Take Her Medicine?	Operations with Time Intervals	4.MD.2				
18	How Big Are Sunspots?	Converting Units, Proportions, and Scientific Notation	5.MD.1	7.RP.2	7.G.4	8.EE.4	G-I
19	What Michael's Coupon Should I Use?	Percent Discount	7.RP.3	A-CED.3			
20	Is It Cheaper To Pay Monthly or Annually?	Decimal Operations and/or Systems of Equations	5.NBT.7	8.EE.8c	A-CED.3	A-REI.11	F-E
21	How Big Is The 2010 Guatemalan Sinkhole?	Volume of Cylinder	5.MD.3	5.MD.4	5.MD.5	8.G.9	G-(
22	How Can You Win Every Prize At Chuck E. Cheese's?	Decomposing Numbers and/or Systems of Equations	2.NBT.7	3.NBT.2	3.NBT.3	8.EE.8c	A-C
23	How Many Royal Flushes Will You Get?	Probability	7.SP.5	7.SP.6	7.SP.7	S-MD.5	S-N
24	How Much Does The Paint On A Space Shuttle Weigh?	Surface Area	6.G.4	7.G.6	8.G.7	G-MG.1	G-I
25	How Did Motel 6 Go From \$6 to \$66?	Percent Increase and Compound Interest	7.RP.3	A-SSE.1b	F-BF.1	F-IF.8b	F-L
26	How Much Does The Aluminum Foil Prank Cost?	Surface Area and Unit Rates	6.G.4	6.RP.2	6.RP.3	7.G.6	
27	How Many Laps Is A 5k Race?	Perimeter	4.MD.3				
28	Which Toilet Uses Less Water?	Systems of Equations/Inequalities	8.EE.8c	A-CED.3	A-REI.11	F-BF.1	
29	How Did Someone Get A \$103,000 Speeding Ticket In Finland?	Linear Equations	A-CED.2	F-BF.1	F-IF.4	F-IF.6	
30	Which Pizza Is A Better Deal?	Area or Circle, Square, and Unit Rates	3.MD.5	3.MD.6	3.MD.7	4.MD.3	6.F
31	How Big Is The World's Largest Deliverable Pizza?	Area of Square	3.MD.5	3.MD.6	3.MD.7	4.NBT.3	4.N
32	How Many Sheets Do You Need To Break Out Of Prison?	Integer Operations	5.NBT.6				
33	Do Hybrid Cars Pay For Themselves?	Systems of Equations or Rates	6.RP.2	6.RP.3	8.EE.8c	A-CED.3	F-E
34	How Many Hot Dogs Did They Eat?!	Linear and Quadratic Functions	8.F.3	8.F.4	F-BF.1	F-BF.2	F-II
35	How Much Purple Ribbon Will You Need?	Perimeter & Circumference	3.MD.8	4.MD.3	7.G.4		
36	Are We There Yet?	Adding Times	3.MD.1	4.MD.2			
37	Which Chinese Food Coupon Should I Use?	Percent Discount	7.RP.3				
38	How Big Is The Vehicle That Uses Those Tires?	Ratio and Proportions	7.RP.2				
39	Where Would The Angry Birds Have Landed?	Create Equation From Quadratic Graph	A-CED.1	F-BF.1	F-IF.4	F-IF.7a	F-L
40	How Many Movies Can You See In One Day?	Adding Times	3.MD.1	4.MD.2			
41	Which Carrots Should You Buy?	Unit Rates	6.RP.1	6.RP.2	6.RP.3		
42	How Fast Can You Throw A Baseball?	Converting Units and Unit Rates	5.MD.1	6.RP.2			

Go	ogle	
 Google Search	I'm Feeling Lucky	

Problem-Based Lesson Search Engine

This search engine searches all of the sites below to quickly help you find a problem-based lesson (also called 3-Act Task, mathematical modeling, or application problem):

Submit

The links below are the pages that are being searched by the search engine:

- 101 Questions
- Andrew Stadel
- Dan Meyer
- Dane Ehlert
- Emergent Math's Problem Based Curriculum Maps
- Estimation180
- Geoff Krall

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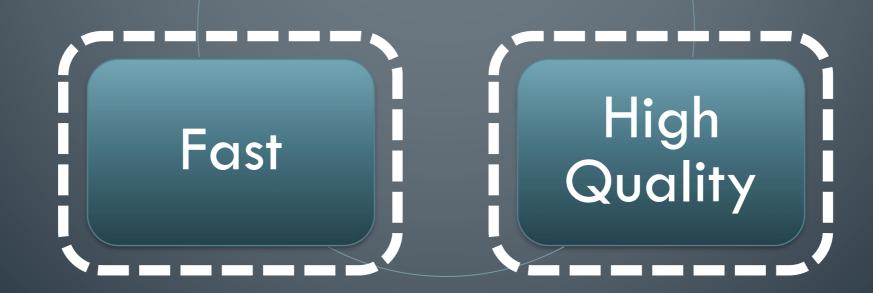
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Construction



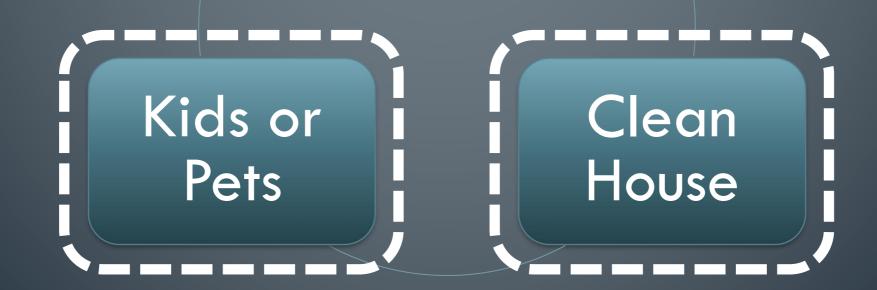












Problem-Based Learning

