

# How Old Is The Shepherd?

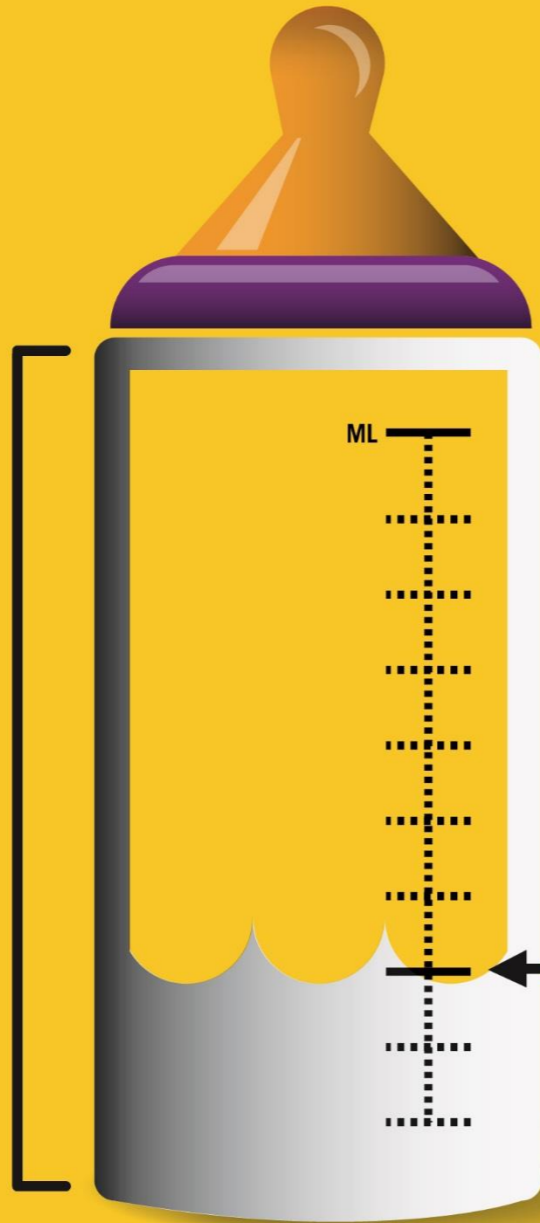
ROBERT KAPLINSKY

 @robertkaplinsky

CHOOSE CAR SEAT:  
BY AGE & SIZE



THE NUMBER  
OF PEOPLE  
**WHO  
THINK**  
THEY HAVE  
THEIR CHILD IN  
THE RIGHT  
SEAT.



THE ONES  
**WHO  
ACTUALLY  
DO.**

**KNOW FOR SURE**  
IF YOUR CHILD IS IN THE RIGHT CAR SEAT.



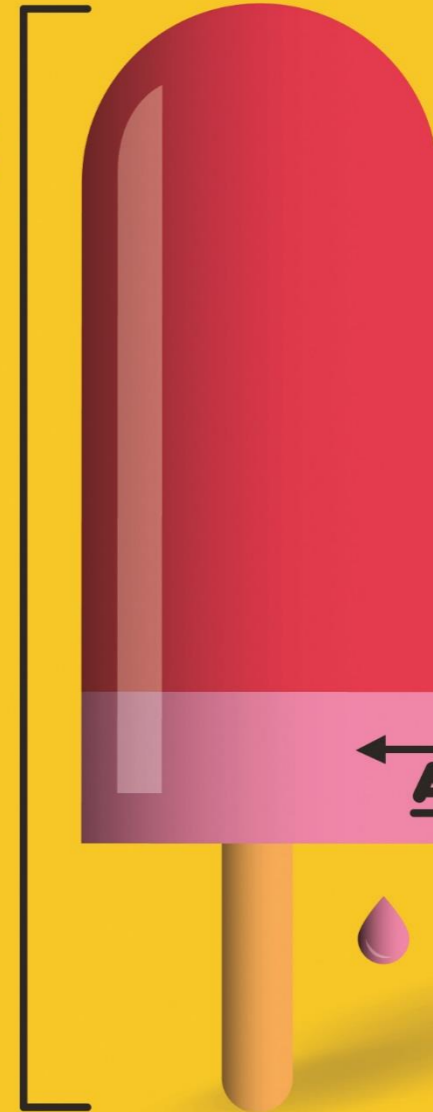
VISIT [SAFERCAR.GOV/THERIGHTSEAT](http://SAFERCAR.GOV/THERIGHTSEAT)



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# Math Question

- Solve the problem on your own. Do not work or share your answer with anyone else.
- You will have 30 seconds to complete it.
- Write your answer down on a paper.

There are 125  
sheep and 5 dogs  
in a flock. How old  
is the shepherd?





# Of the 32 students I interviewed...

- 75% of them gave me numerical responses
- 2 students calculated the answer to be 130 ( $125 + 5$ )
- 2 students calculated the answer to be 120 ( $125 - 5$ )
- 12 students calculated the answer to be 25 ( $125 \div 5$ )
- 0 students calculated the answer to be 625 ( $125 \times 5$ )
- 4 students stated that they guessed their answer (90, 5, 42, and 50)
- 4 students tried to divide 125 by 5 but could not correctly implement the procedure

# Takeaways

- Making sense of mathematics
- Intellectual autonomy
  - Intellectual autonomy is about being able to think for yourself and not being dependent on others for the direction and control of one's thinking.

# What Does the NHTSA Say?

## Key Statistics and Consumer Insights:

- Motor vehicle crashes are the leading cause of death for children age 1 through 12 years old.<sup>1</sup>

According to a NHTSA study, 3 out of 4 kids are not as secure in the car as they should be because their car seats are not being used correctly.

be reduced by about half if the correct child safety seats were always used.

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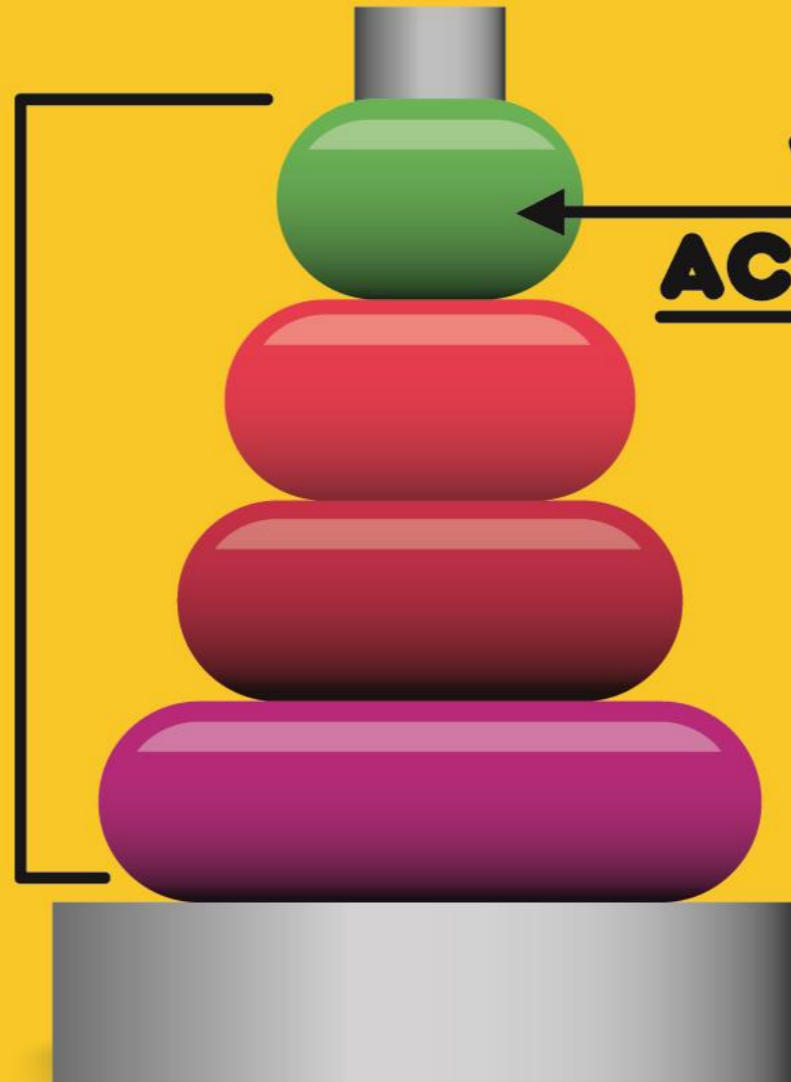
<sup>1</sup> Source: Based on the latest mortality data currently available from the CDC's National Center for Health Statistics.





CHOOSE CAR SEAT:  
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- “because they have their child in the right seat”
- “because their car seats are not being used correctly”

**IF YOUR CHILD IS IN THE RIGHT CAR SEAT.**



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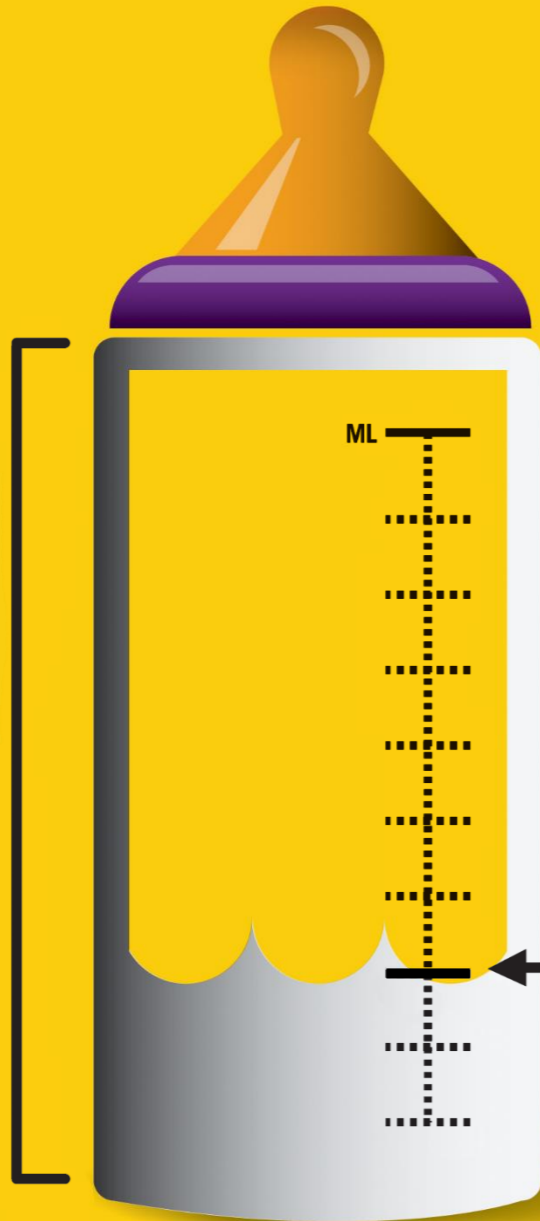
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THE NUMBER  
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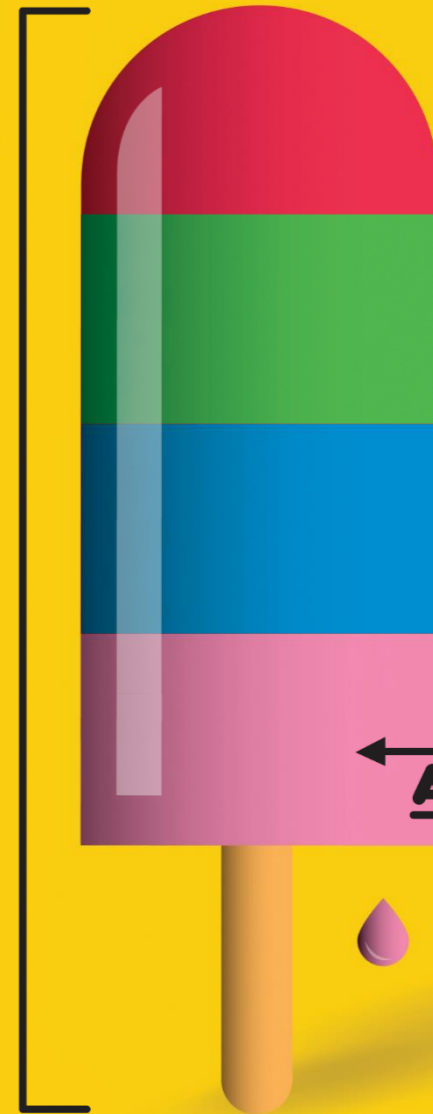
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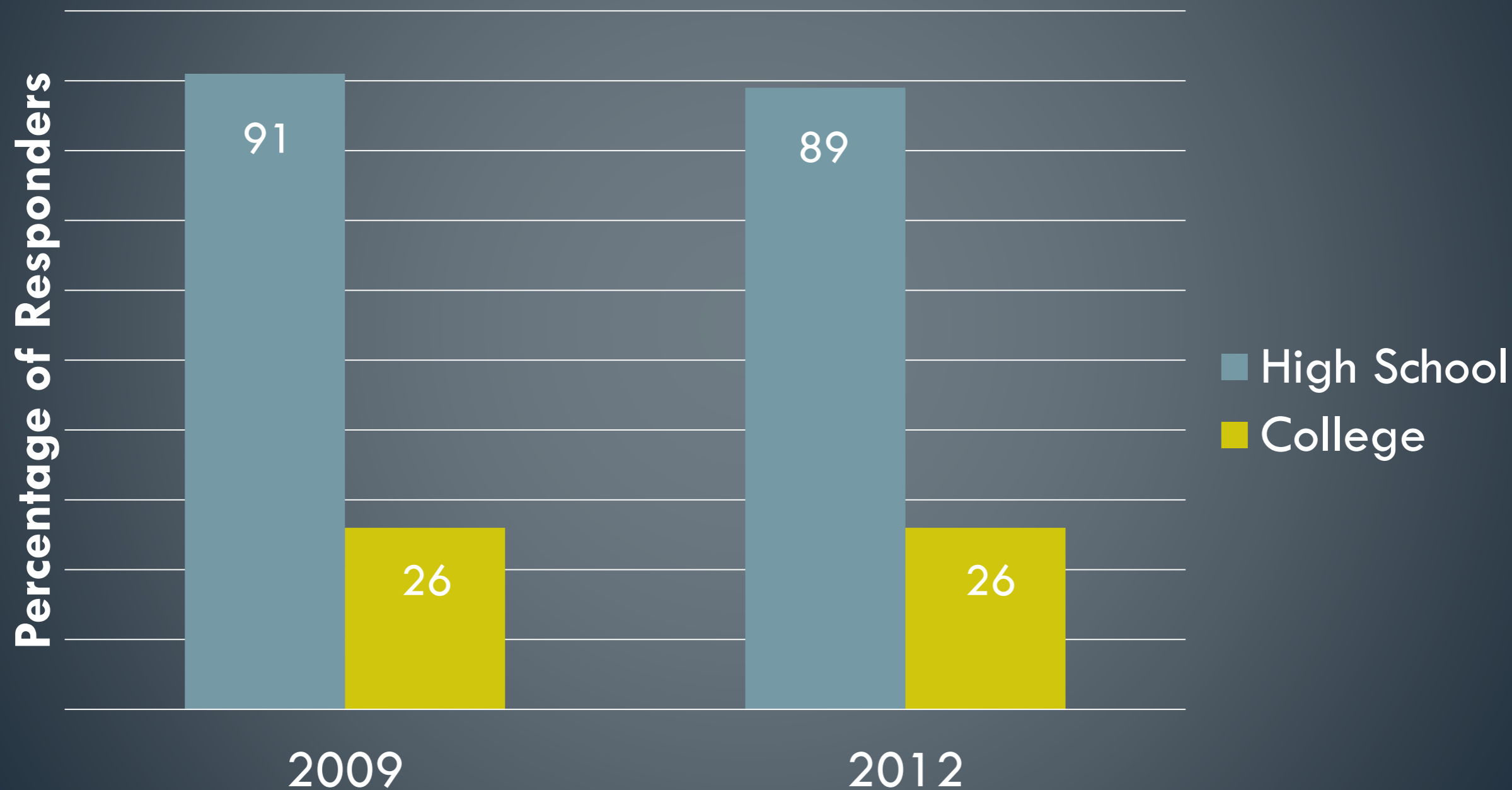
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***WHAT IS THE  
PURPOSE OF  
A K-12  
EDUCATION?***

- College readiness
  - ACT National Curriculum Survey
  - Surveyed 9,937 educators

# “Well” or “Very Well” Prepared for College





# ***WHAT IS THE PURPOSE OF A K-12 EDUCATION?***

- College readiness
- Career readiness
  - Association of American Colleges and Universities survey
  - Surveyed over 300 employers with at least 25 employees and many new hires



■ More ■ Less ■ Same

Critical thinking and analytical reasoning skills

Analyzing and solving complex problems

Communicating effectively orally and in writing

Applying knowledge and skills to real-world setting

Working w/ numbers and understanding statistics



# COMMON CORE

## STATE STANDARDS INITIATIVE

CCSS.MATH.CONTENT.4.MD.A.3

Apply the area and perimeter formulas for rectangles in real world and mathematical problems.

meet the  
equal intensity, the  
of each grade: conceptual  
skills and fluency, and application.

What is the perimeter  
of a rectangle that  
measures 8 units by 4  
units?



# Components of Rigor

Procedural Skill and Fluency

Conceptual Understanding



List the dimensions of  
a rectangle with a  
perimeter of 24 units.



# Components of Rigor

Procedural Skill and Fluency

Conceptual Understanding

***WHY?***







# Components of Rigor

Procedural Skill and Fluency

Conceptual Understanding

List the  
of a rectangle with a  
perimeter of 24  
units.



# Components of Rigor

Procedural Skill and Fluency

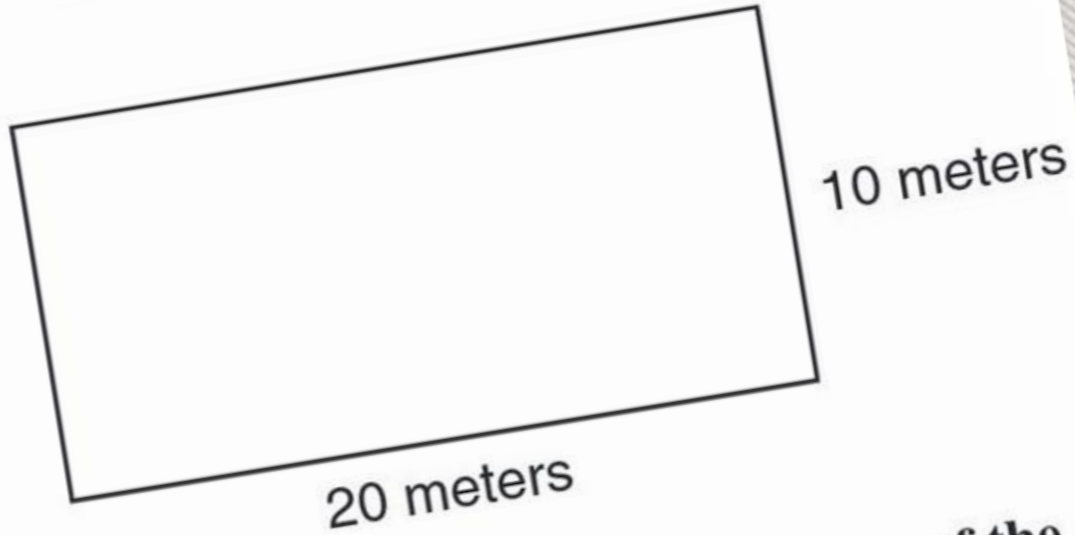
Conceptual Understanding





71

A basketball court is shaped like a rectangle 20 meters long and 10 meters wide.



What is the perimeter in meters of the court?

- A 30 meters
- B 50 meters
- C 60 meters
- D 200 meters

What is the perimeter  
of a rectangle ~~with~~  
that measures 8 units  
by 4 units?

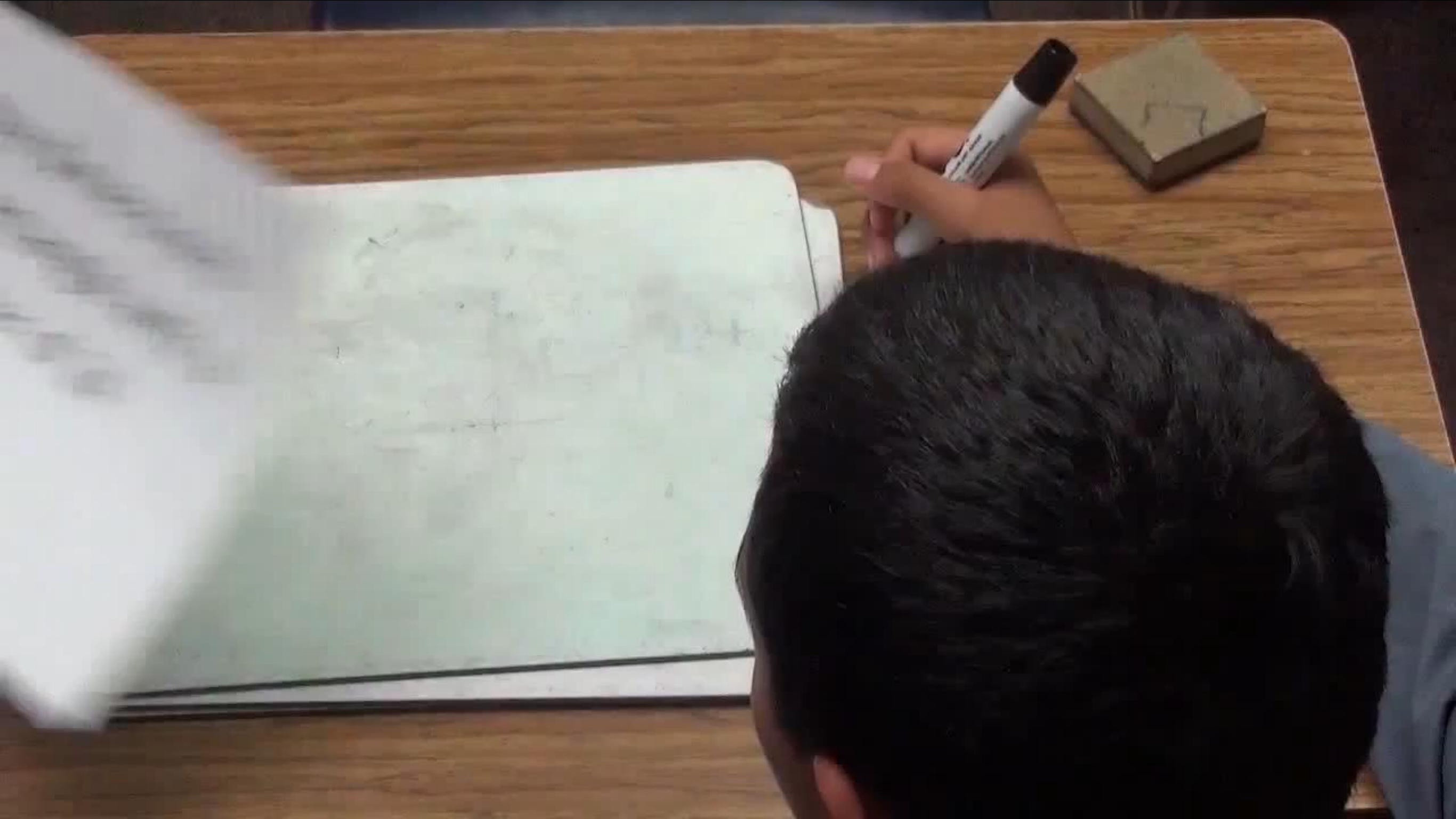




# Components of Rigor

Procedural Skill and Fluency

Conceptual Understanding



# Components of Rigor

Procedural Skill and Fluency

Conceptual Understanding

Of all the rectangles with a perimeter of 24 units, which one has the most area?



Of all the rectangles  
with a perimeter of  
24 units, which one  
has the most area?

00:00:00:00

# Components of Rigor

Procedural Skill and Fluency

Conceptual Understanding

# Defining the Problem



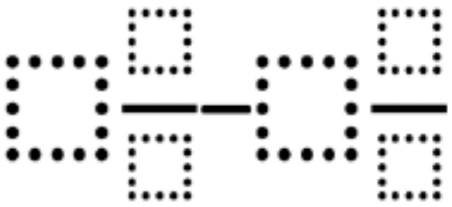
- ▶ Students appear to demonstrate “deep, authentic command of mathematical concepts” when given commonly used problems.
- ▶ However with more challenging problems, the same students seem to no longer demonstrate that command.


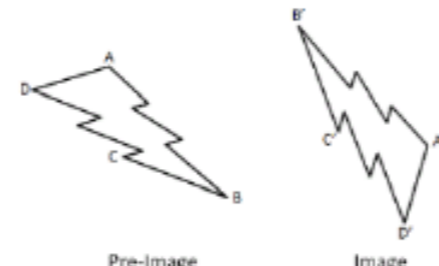
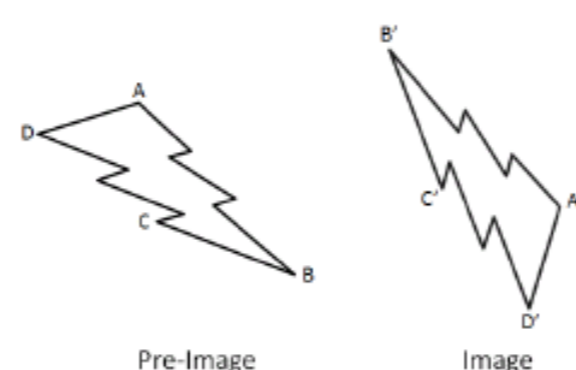
# Addressing the Problem

- ▶ First, we must have a clear understanding about why these problems are different from one another.
- ▶ Next, we need to practice using these problems so that we understand how students may react to them.
- ▶ Last, we need a source that can provide us with a variety of free problems.



# DOK | Distinguishing Between Depth of Knowledge Levels in Mathematics

Topic	Adding Whole Numbers	Money	Fractions on a Number Line	Area and Perimeter	Subtracting Mixed Numbers
CCSS Standard(s)	<ul style="list-style-type: none"> <li>1.NBT.4</li> <li>2.NBT.5</li> </ul>	<ul style="list-style-type: none"> <li>2.MD.8</li> </ul>	<ul style="list-style-type: none"> <li>3.NF.2</li> </ul>	<ul style="list-style-type: none"> <li>3.MD.8</li> <li>4.MD.3</li> </ul>	<ul style="list-style-type: none"> <li>5.NF.1</li> </ul>
DOK 1 Example	<p>Find the sum.</p> $44 + 27 =$	<p>If you have 2 dimes and 3 pennies, how many cents do you have</p>	<p>Which point is located at <math>\frac{7}{12}</math> below?</p> 	<p>Find the perimeter of a rectangle that measures 4 units by 8 units.</p>	<p>Find the difference.</p> $5\frac{1}{2} - 4\frac{2}{3} =$
DOK 2 Example	<p>Fill in the boxes below using the whole numbers 1 through 9, no more than one time each, so that you make a true equation.</p> $\square\square + 53 = \square\square$	<p>Make 47¢ in three different ways with either quarters, dimes, nickels, or pennies.</p>	<p>Label the point where <math>\frac{3}{4}</math> belongs on the number line below. Be as precise as possible.</p> 	<p>List the measurements of three different rectangles that each has a perimeter of 20 units.</p>	<p>Create three different mixed numbers that will make the equation true by using the whole numbers 1 through 9, no more than one time each. You may reuse the same whole numbers for each of the three mixed numbers.</p> $5\frac{4}{5} - \square\frac{\square}{\square} = 3\frac{1}{20}$
DOK 3 Example	<p>Make the largest sum by filling in the boxes below using the whole numbers 1 through 9, no more than one time each.</p> $\square\square + \square\square =$	<p>Make 47¢ using exactly 5 coins with either quarters, dimes, nickels, or pennies.</p>	<p>Create 5 fractions using the whole numbers 0 through 9, no more than one time each, as numerators and denominators and correctly place them all on a number line.</p>	<p>What is the greatest area you can make with a rectangle that has a perimeter of 24 units?</p>	<p>Make the smallest difference by filling in the boxes below using the whole numbers 1 through 9, no more than one time each.</p> 

Topic	Surface Area and Volume	Probability	Transformations	Factoring Quadratics	Quadratics in Vertex Form
CCSS Standard(s)	<ul style="list-style-type: none"> <li>6.G.4</li> <li>7.G.6</li> </ul>	<ul style="list-style-type: none"> <li>7.SP.5</li> <li>7.SP.7</li> </ul>	<ul style="list-style-type: none"> <li>8.G.1</li> <li>G-CO.5</li> </ul>	<ul style="list-style-type: none"> <li>A-SSE.3a</li> </ul>	<ul style="list-style-type: none"> <li>F-IF.7a</li> </ul>
DOK 1 Example	Find the surface area of a rectangular prism that measures 3 units by 4 units by 5 units.	What is the probability of rolling a sum of 5 using two 6-sided dice?	Rotate the image below 90° counterclockwise and reflect it across a horizontal line. 	Find the factors: $2x^2 + 7x + 3$	Find the roots and maximum of the quadratic equation below. $y = 3(x - 4)^2 - 3$
DOK 2 Example	List the measurements of three different rectangular prisms that each has a surface area of 20 square units.	What value(s) have a 1/12 probability of being rolled as the sum of two 6-sided dice?	List three sequences of transformations that take pre-image ABCD to image A'B'C'D'. 	Fill in the blank with integers so that the quadratic expression is factorable. $x^2 + \_\_x + 4$	Create three equations for quadratics in vertex form that have roots at 3 and 5 but have different maximum and/or minimum values.
DOK 3 Example	What is the greatest volume you can make with a rectangular prism that has a surface area of 20 square units?	Fill in the blanks to complete this sentence using the whole numbers 1 through 9, no more than one time each.  Rolling a sum of $\_\_$ on two $\_\_$ -sided dice is the same probability as rolling a sum of $\_\_$ on two $\_\_$ -sided dice.	What is the fewest number of transformations needed to take pre-image ABCD to image A'B'C'D'? 	Fill the blank by finding the largest and smallest integers that will make the quadratic expression factorable. $2x^2 + 3x + \_\_$	Create a quadratic equation with the largest maximum value using the whole numbers 1 through 9, no more than one time each. $y = -\square(x - \square)^2 + \square$



# DOK Level Differences



## ▶ **Level 1: Recall & Reproduction**

- ▶ Often a trivial application of facts.
- ▶ Requires little to no cognitive effort beyond remembering the right formula.
- ▶ Usually only one answer.

## ▶ **Level 2: Skills & Concepts**

- ▶ Usually requires more than one step to solve.
- ▶ Often multiple answers.

## ▶ **Level 3: Strategic Thinking**

- ▶ Usually requires critical thinking about the best way to approach a problem.
- ▶ May be multiple answers or a single optimal answer.
- ▶ Often challenging enough to make your head hurt.

## ▶ **Level 4: Extended Thinking**

- ▶ In mathematics these are generally represented by performance tasks or problem-based lessons.

# ***DOK***

# ***FAQ***

- *What DOK level should I start students off with?*
- *How do teachers fit these problems into their pacing?*
- *How do I help prevent students from giving up after trying the problem once or twice?*
- *Where can I find other DOK 2 and DOK 3 problems?*
- *How can I share DOK 2 and DOK 3 problems I've made?*





## NEW OPEN MIDDLE

### Exponents and Order of Operations

February 10, 2015 Leave a comment

Directions: Find 3 positive integers that add up to 10. Place each number into one of the blanks to find the largest possible result. Source: Zack Miller (@zmill415) [Read More »](#)

### Create Squares

February 10, 2015 2 Comments

Directions: Create a square with one of the vertices at (2,3). Fill in the blanks with whole numbers 0 through 9, using each number at most once, to show the rest of the vertices of the square. Bonus: Find more than one set of vertices. Source: John Mahlstedt (@jdmahlstedt) [Read More »](#)

### Solution of Two Linear Equations

February 10, 2015 Leave a comment

Directions: Using the Integers 0-9 (without duplication), provide four sets of points that represent two distinct lines. These lines can be written as two linear equations. Then provide a fifth point that represents the intersection (or solution) of those equations. Line 1: (  ,  ) and (  ,  ) Line 2: (  ,  ) and (  ,  ) Solution (  ,  ) Source: Bryan Anderson [Read More »](#)

### Bingo card

February 5, 2015 1 Comment

Directions: In a standard game of BINGO, the cards are labeled with numbers 1 through 75. If it was possible, which card would you choose: a card with all of the same number or a standard bingo card? Source: Nanette

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## OPEN MIDDLE WORKSHEET

Download the Open Middle Worksheet:  
Version 1.1

## SUBSCRIBE

Receive emails every time a new problem is published.

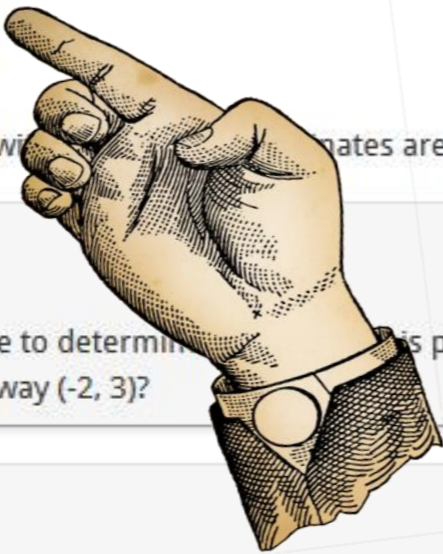
## COMMON CORE STATE STANDARDS

- Grade 1 (6)
  - Number & Operations in Base Ten (3)
  - Operations & Algebraic Thinking (3)
- Grade 2 (6)
  - Measurement & Data (2)
  - Number & Operations in Base Ten (4)
- Grade 3 (11)
  - Measurement & Data (6)
  - Number & Operations in Base Ten (3)
  - Number & Operations—Fractions (2)



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## EQUIDISTANT POINTS



Directions: How many points with integer coordinates are 5 units away from  $(-2, 3)$ ?

### Hint

Which methods are available to determine the answer to this problem? What shape is defined by *all* of the points that are 5 units away  $(-2, 3)$ ?

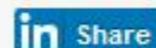
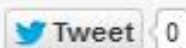
### Answer

12 points:  $(-5, 7)$ ,  $(-7, 3)$ ,  $(-5, -1)$ ,  $(-2, -2)$ ,  $(3, 3)$ ,  $(1, -1)$ ,  $(-2, 8)$ ,  $(1, 7)$ ,  $(2, 6)$ ,  $(-6, -6)$ ,  $(-6, 0)$ , and  $(2, 0)$

Source: [Dylan Kane](#)



SHARE !



Tagged with: [8.G.8](#) [DOK 2: SKILL / CONCEPT](#) [DYLAN KANE](#) [G-GPE.1](#)

Previous: [Cone and Cylinder Volumes](#)

Next: [Pythagorean Shell](#)

## LEAVE A REPLY

## OPEN MIDDLE WORKSHEET

Download the Open Middle Worksheet:  
Version 1.1

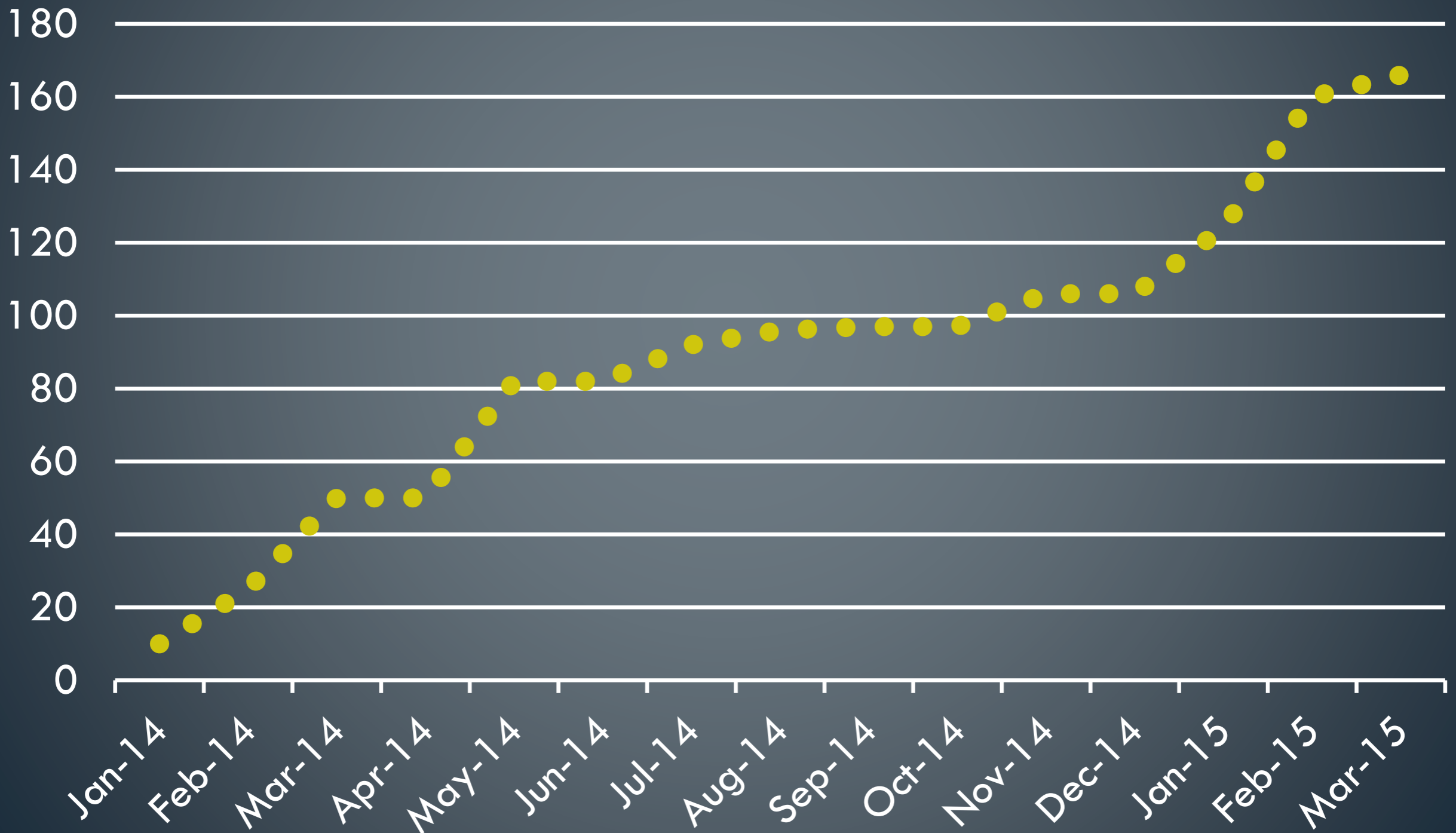
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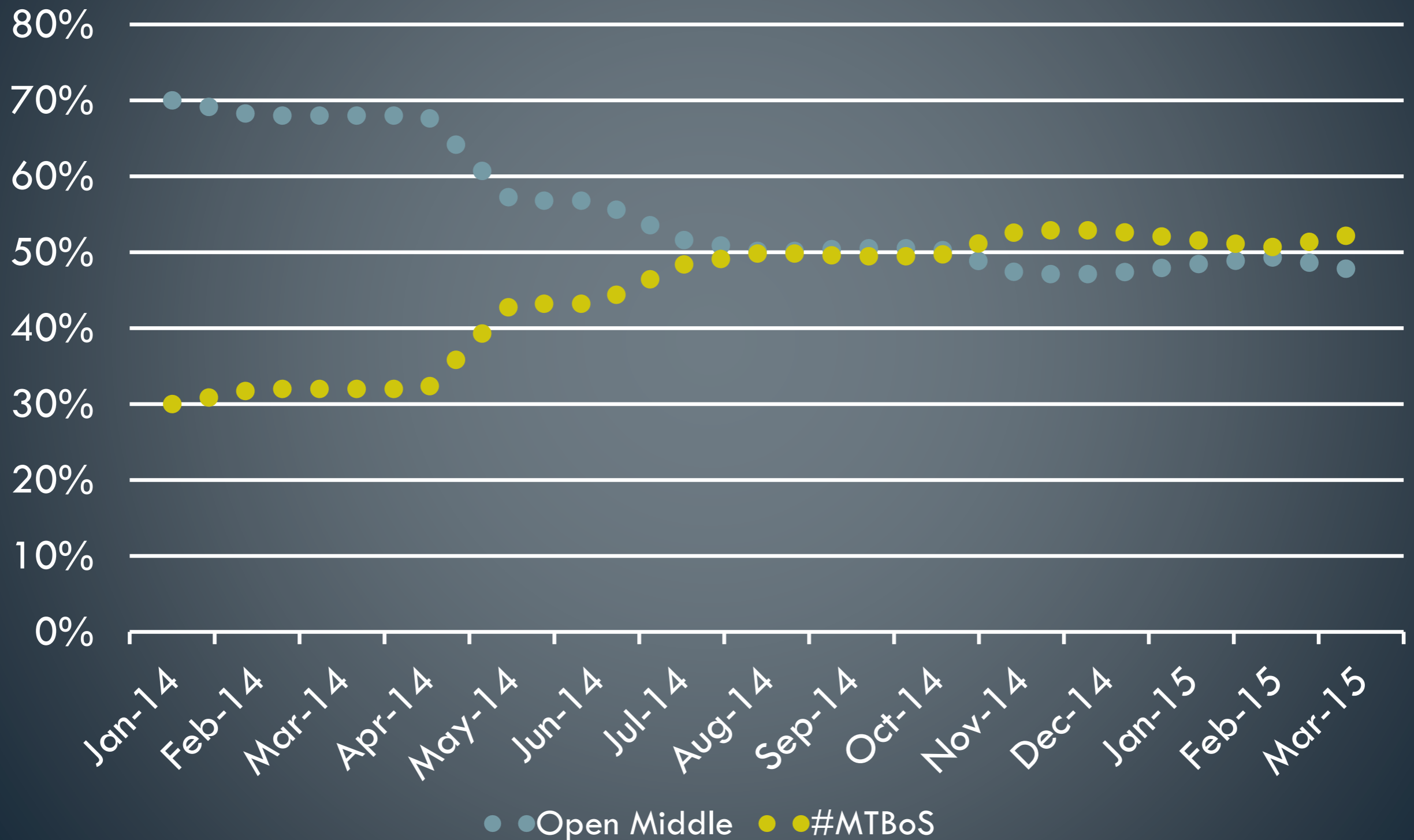
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  - Number & Operations—Fractions (2)

# Total Open Middle Problems

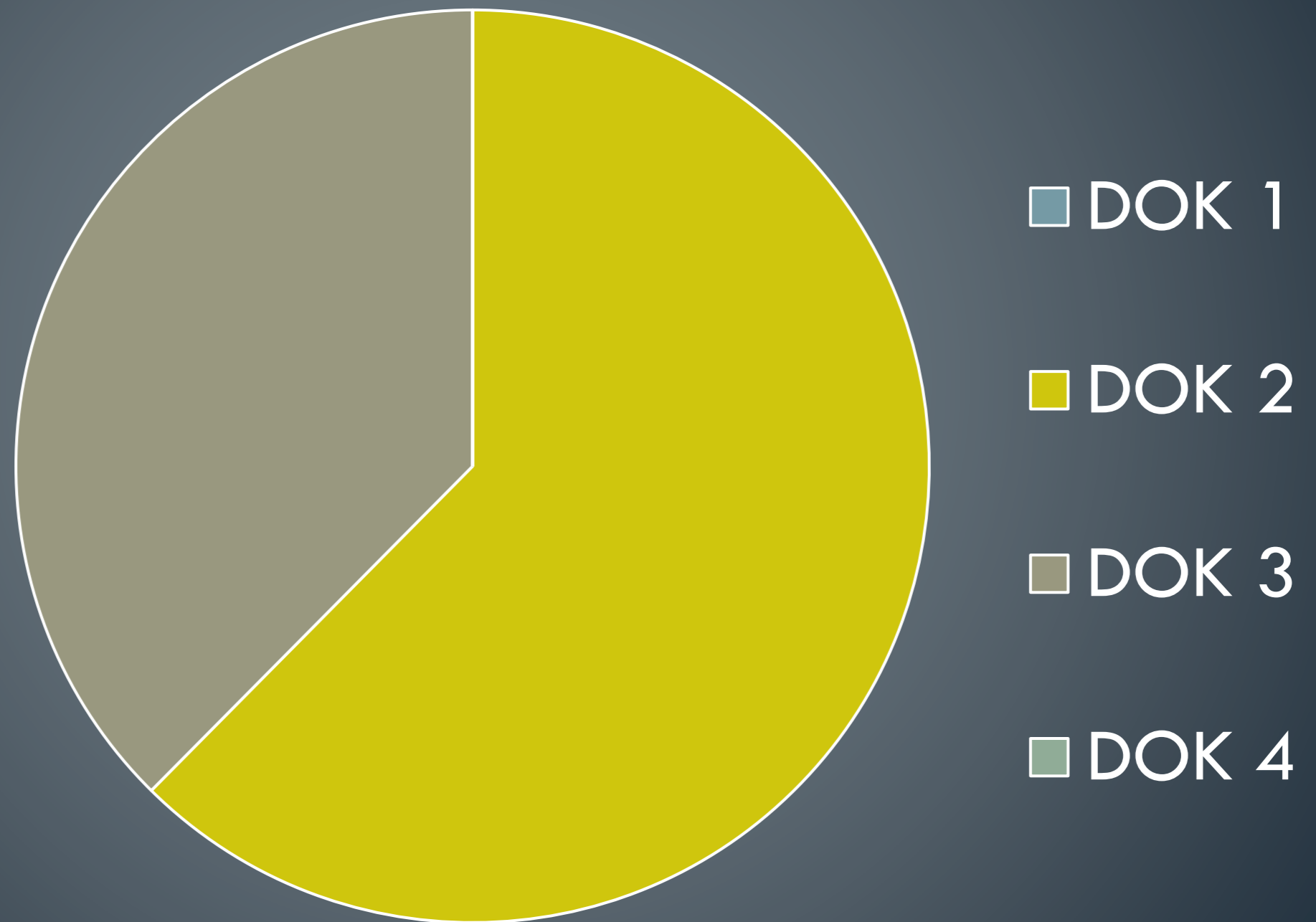


# Open Middle Author Percentages



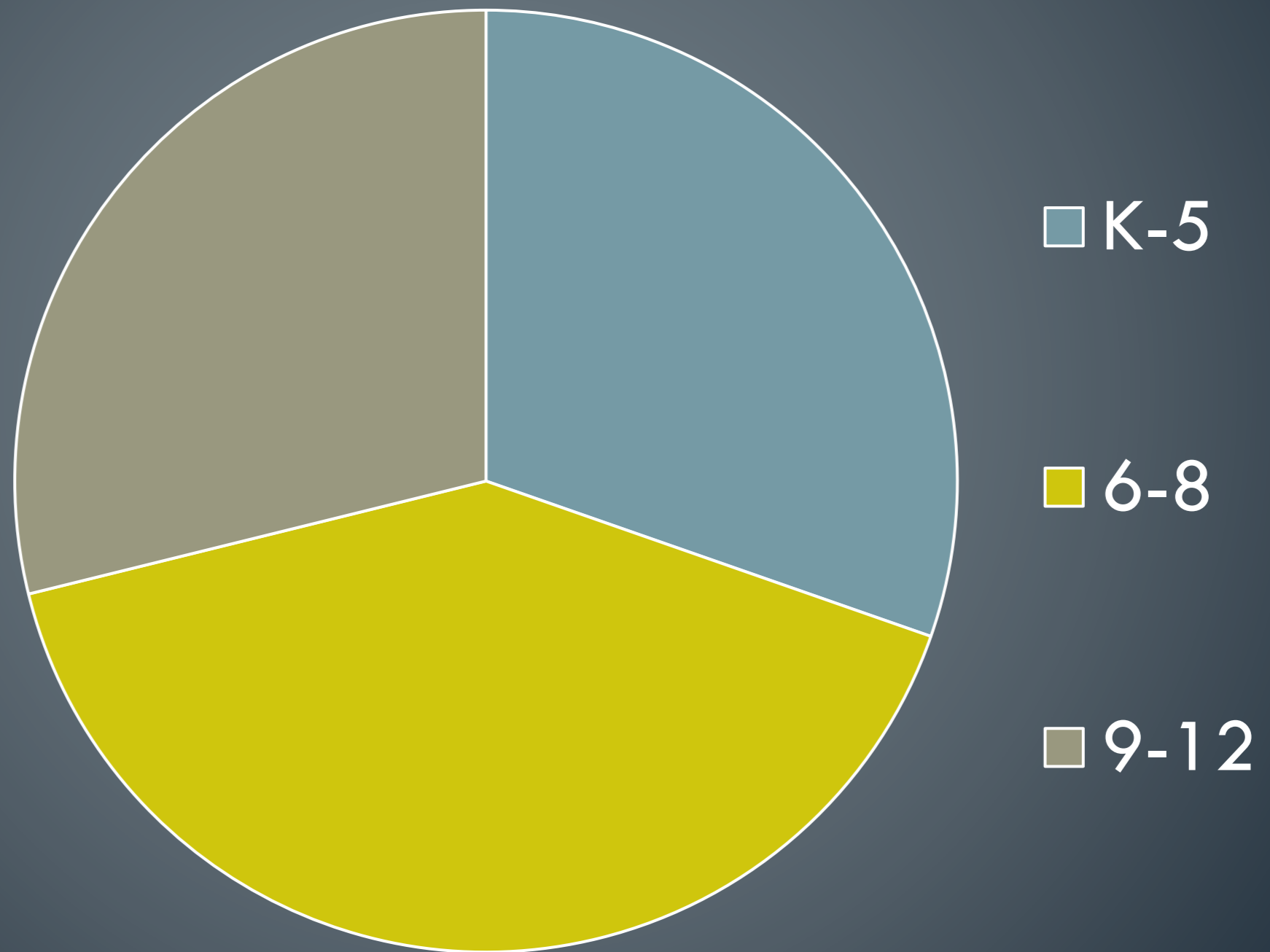


# Problems by DOK Level



Note: Data as of March 2015

# Problems by Grade Band



Note: Data as of March 2015



# COMMON CORE

STATE STANDARDS INITIATIVE

Rigor refers to deep, authentic command of mathematical concepts, not making math harder or introducing topics at earlier grades. To help students meet the standards, educators will need to pursue, with equal intensity, three aspects of rigor in the major work of each grade: conceptual understanding, procedural skills and fluency, and application.



# Call to Action

- ▶ Commit to one of these choices:
  - ▶ Implement a single DOK 2 or DOK 3 problem from [openmiddle.com](https://openmiddle.com) in your classes within the week.
  - ▶ Put a DOK 2 question from [openmiddle.com](https://openmiddle.com) on your next assessment.



# Contact

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