Digging into Depth of Knowledge

ROBERT KAPLINSKY





CCSS.MATH.CONTENT.4.MD.A.3 nmand of Apply the area and perimeter formulas for harder or rectangles in real world and mathematical problems. meet the equal intensity, u of each grade: conceptua skills and fluency, and application.

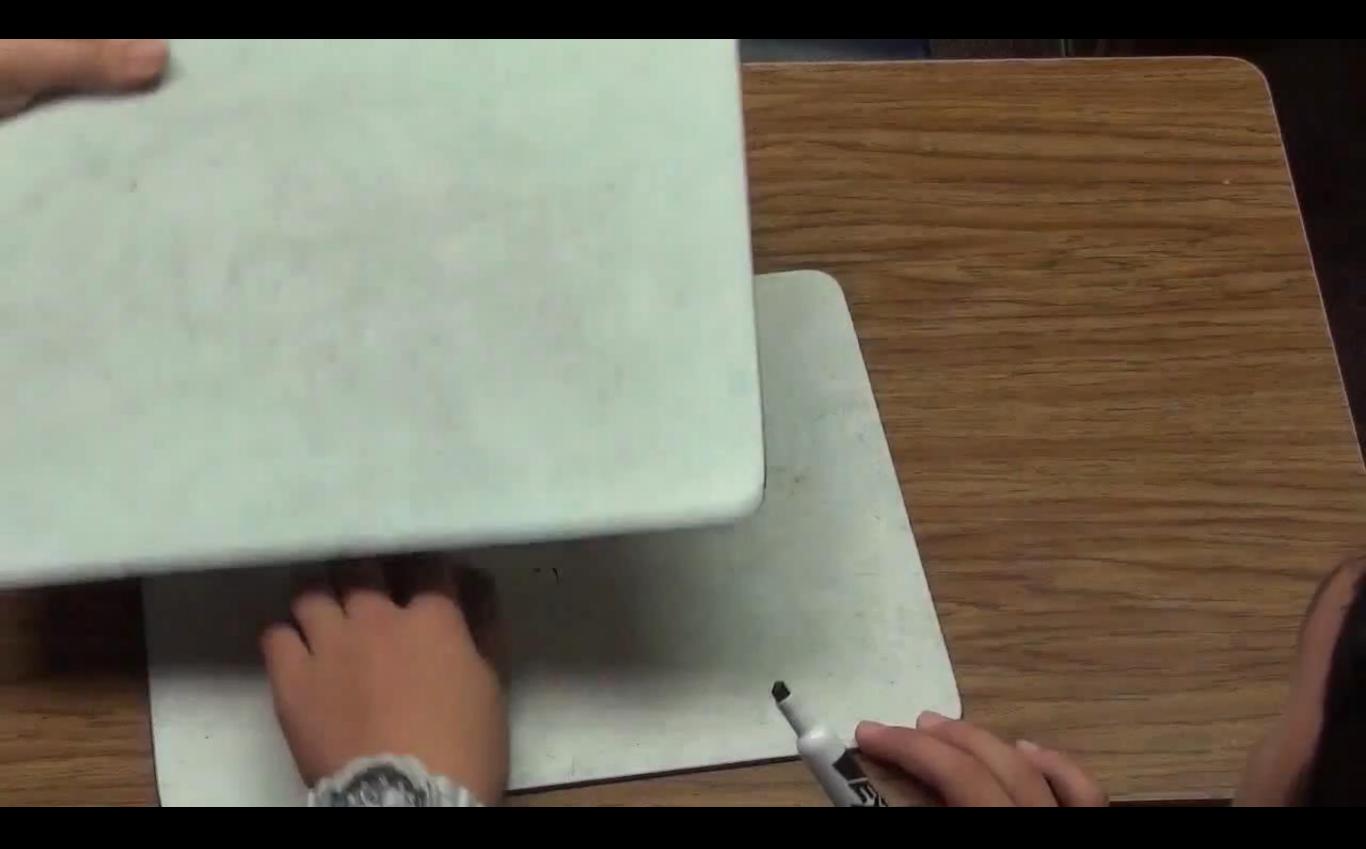
Source: http://www.corestandards.org/other-resources/key-shifts-in-mathematics/

What is the perimeter of a rectangle that measures 8 units by 4 units?





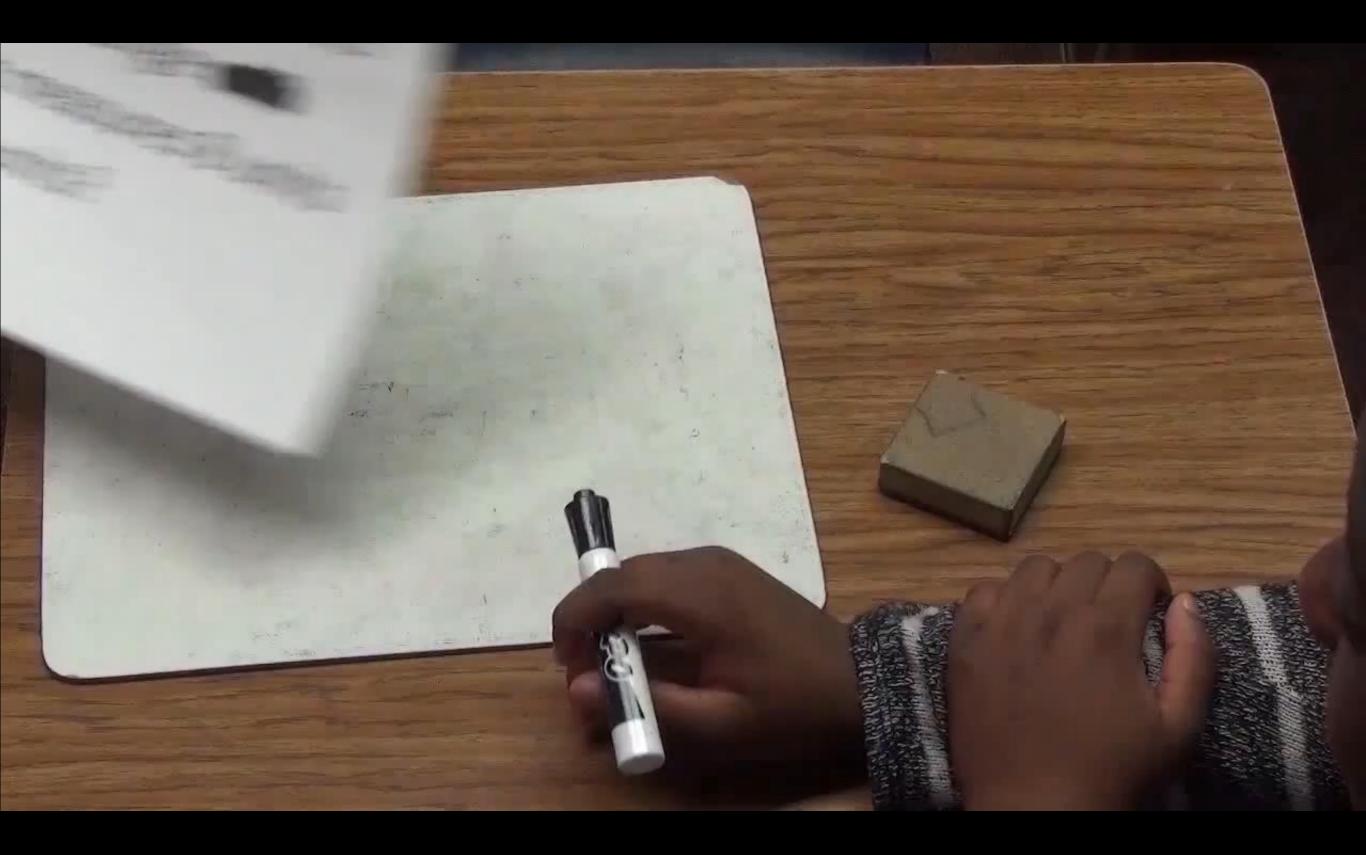
List the dimensions of a rectangle with a perimeter of 24 units.



Components of Rigor Procedural Skill and Fluency

Conceptual Understanding





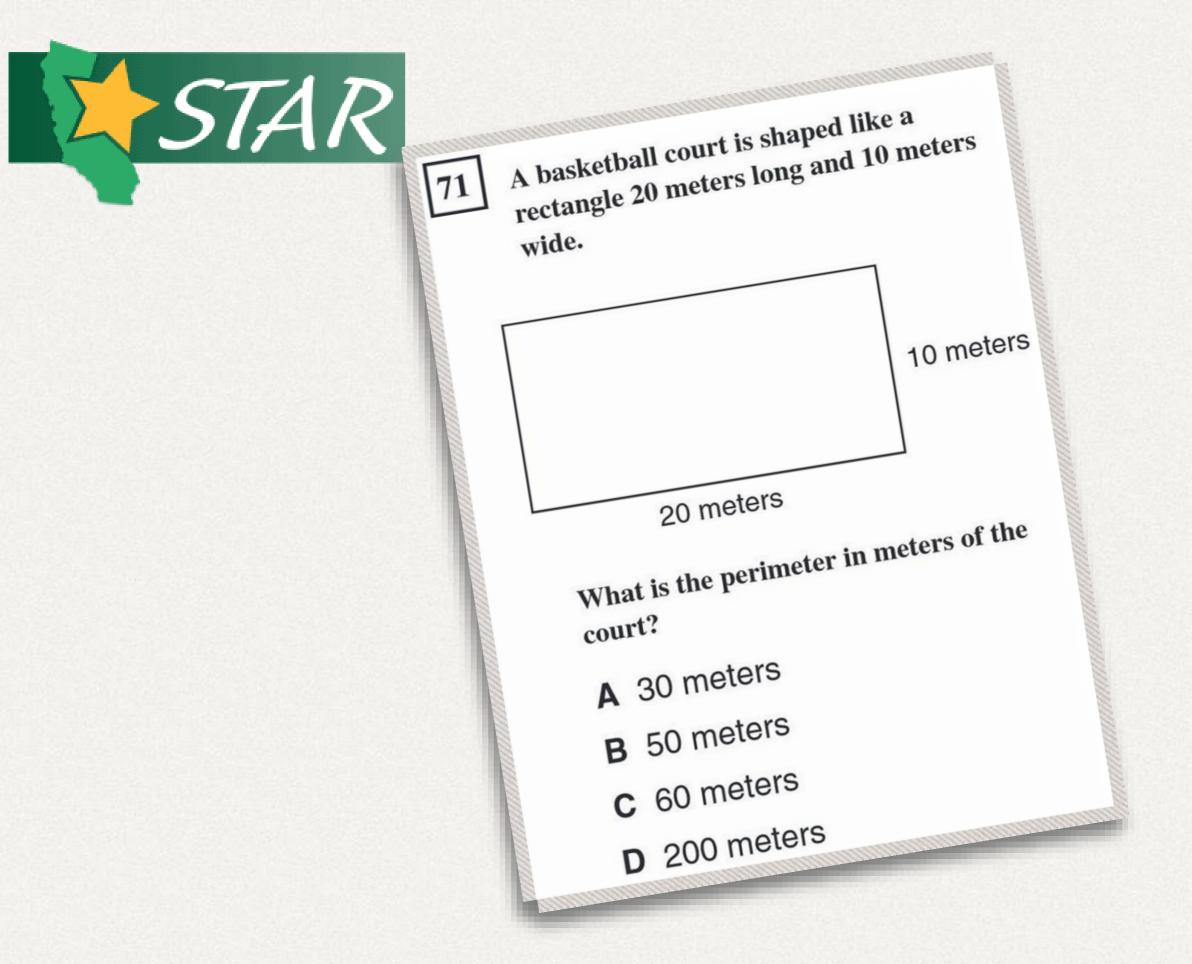




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Components of Rigor Procedural Skill and Fluency

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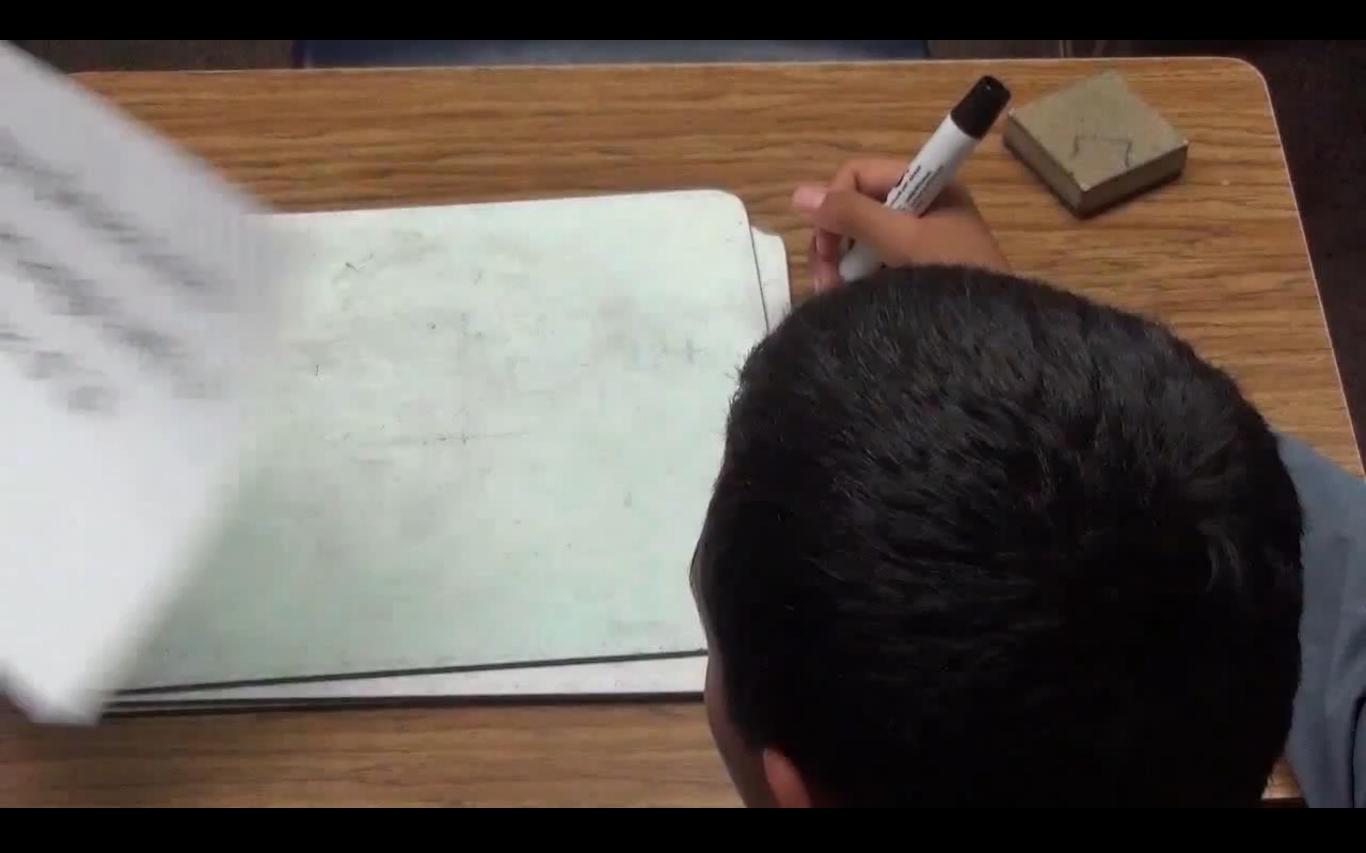


Source: http://www.cde.ca.gov/ta/tg/sr/documents/cstrtqmath3.pdf

What is the perimeter of a rectangle **Mathematics** that measures 8 units by 4 units?











Of all the rectangles with a perimeter of 24 units, which one has the most area?

00:00:00:00 Of all the rectangles with a perimeter of 24 units, which one has the mast area?

Components of Rigor Procedural Skill and Fluency

Conceptual Understanding

Defining the Problem

Students appear to demonstrate "deep, authentic command of mathematical concepts" when given commonly used problems. However with more challenging problems, the same students seem to no longer demonstrate that command.

Addressing the Problem

- First, we must have a clear understanding about why these problems are different from one another.
- Next, we need to practice using these problems so that we understand how students may react to them.
- Last, we need a source that can provide us with a variety of free problems.

DOK Distinguishing Between Depth of Knowledge Levels in Mathematics

Topic	Adding Whole Numbers	Money	Fractions on a Number Line	Area and Perimeter	Subtracting Mixed Numbers
CCSS	• 1.NBT.4	• 2.MD.8	 3.NF.2 	 3.MD.8 	• 5.NF.1
Standard(s)	• 2.NBT.5			• 4.MD.3	
DOK 1 Example	Find the sum. $44 + 27 =$	If you have 2 dimes and 3 pennies, how many cents do you have	Which point is located at $\frac{7}{12}$ below? L M N O ++++++++++++++++++++++++++++++++++++	Find the perimeter of a rectangle that measures 4 units by 8 units.	Find the difference. $5\frac{1}{2} - 4\frac{2}{3} =$
DOK 2 Example	Fill in the boxes below using the whole numbers 1 through 9, no more than one time each, so that you make a true equation. + 53 =	Make 47¢ in three different ways with either quarters, dimes, nickels, or pennies.	Label the point where $\frac{3}{4}$ belongs on the number line below. Be as precise as possible.	List the measurements of three different rectangles that each has a perimeter of 20 units.	Create three different mixed numbers that will make the equation true by using the whole numbers 1 through 9, no more than one time each,. You may reuse the same whole numbers for each of the three mixed numbers. $5\frac{4}{5} - \boxed{\frac{1}{5}} = 3\frac{1}{20}$
DOK 3 Example	Make the largest sum by filling in the boxes below using the whole numbers 1 through 9, no more than one time each.	Make 47¢ using exactly 5 coins with either quarters, dimes, nickels, or pennies.	Create 5 fractions using the whole numbers 0 through 9, no more than one time each, as numerators and denominators and correctly place them all on a number line.	What is the greatest area you can make with a rectangle that has a perimeter of 24 units?	Make the smallest difference by filling in the boxes below using the whole numbers 1 through 9, no more than one time each.

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More free DOK 2 & 3 problems available at openmiddle.com | © 2015 Robert Kaplinsky, robertkaplinsky.com

DOK Distinguishing Between Depth of Knowledge Levels in Mathematics

Topic	Surface Area and	Probability	Transformations	Factoring	Quadratics in Vertex
	Volume			Quadratics	Form
CCSS	• 6.G.4	• 7.SP.5	• 8.G.1	 A-SSE.3a 	• F-IF.7a
Standard(s)	• 7.G.6	• 7.SP.7	• G-CO.5		
DOK 1	Find the surface	What is the probability of	Rotate the image below 90°	Find the factors:	Find the roots and
Example	area of a	rolling a sum of 5 using	counterclockwise and reflect it		maximum of the
	rectangular prism	two 6-sided dice?	across a	$2x^2 + 7x + 3$	quadratic equation
	that measures 3		horizontal		below.
	units by 4 units by		line.		
	5 units.		B		$y=3(x-4)^2-3$
DOK 2	List the	What value(s) have a	List three sequences of	Fill in the blank	Create three
Example	measurements of	1/12 probability of being	transformations that take pre-	with integers so	equations for
	three different	rolled as the sum of two	image	that the quadratic	quadratics in vertex
	rectangular prisms	6-sided dice?	ABCD to	expression is	form that have roots
	that each has a		image	factorable.	at 3 and 5 but have
	surface area of 20		A'B'C'D'.	2	different maximum
	square units.		Pre-Image Image	$x^2 + x + 4$	and/or minimum
DOK 3	What is the	Fill in the blanks to	What is the fewest number of	Fill the blank by	values. Create a quadratic
Example	greatest volume	complete this sentence	transformations needed to take	finding the largest	equation with the
Lxample	you can make with	using the whole numbers	pre-image ABCD to image A'B'C'D'?	and smallest	largest maximum
	a rectangular	1 through 9, no more	pre image Abeb to image Abeb i	integers that will	value using the
	prism that has a	than one time each.	B	make the quadratic	whole numbers 1
	surface area of 20			expression	through 9, no more
	square units?	Rolling a sum of on	\geq \sim	factorable.	than one time each.
		twosided dice is the			
		same probability as rolling	∼в ∨	$2x^2 + 3x + $	$y = -[(x-[)^2 + [])^2$
		a sum of on two	ن Pre-Image Image		Andre
		sided dice.			

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DOK Level Differences

Level 1: Recall & Reproduction

- Often a trivial application of facts.
- Requires little to no cognitive effort beyond remembering the right formula.
- Usually only one answer.

Level 2: Skills & Concepts

- Usually requires more than one step to solve.
- Often multiple answers.

Level 3: Strategic Thinking

- Usually requires critical thinking about the best way to approach a problem.
- May be multiple answers or a single optimal answer.
- Often challenging enough to make your head hurt.

Level 4: Extended Thinking

In mathematics these are generally represented by performance tasks or problem-based lessons.

Probability What is the probability of rolling a sum of 5 using two 6sided dice?

Probability What value(s) have a $\frac{1}{12}$ probability of being rolled as the sum of two 6-sided dice?

Author: Daniel Luevanos

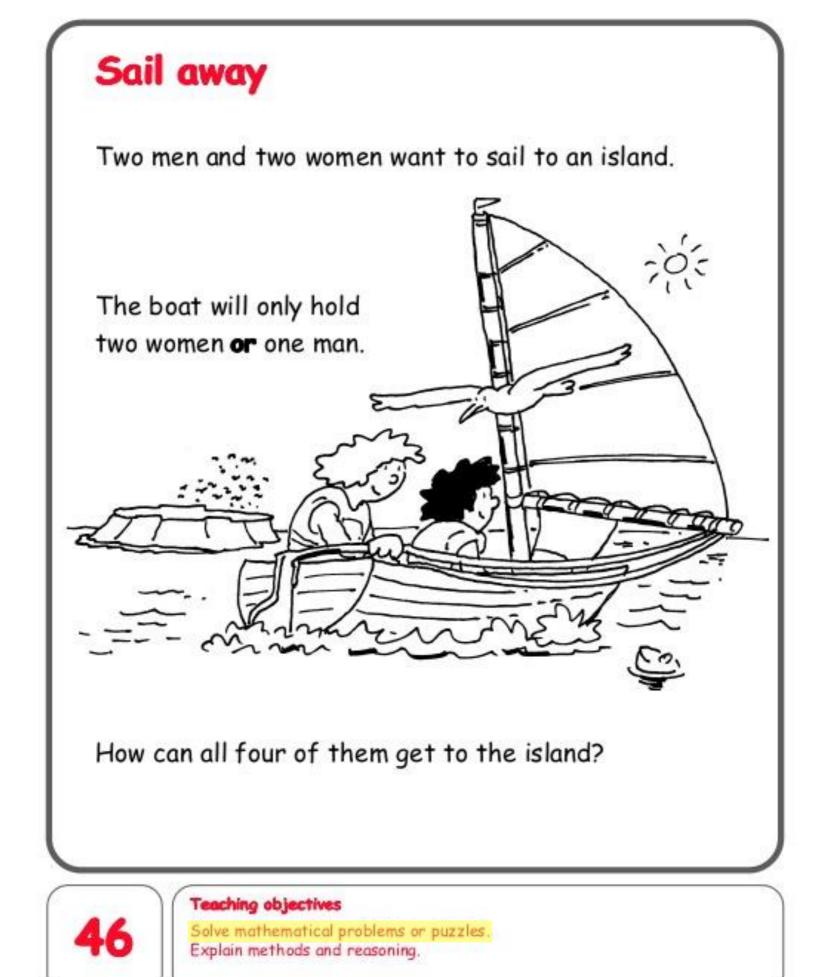
Probability

Fill in the blanks to complete this sentence using the whole numbers 1 through 9, no more than one time each.

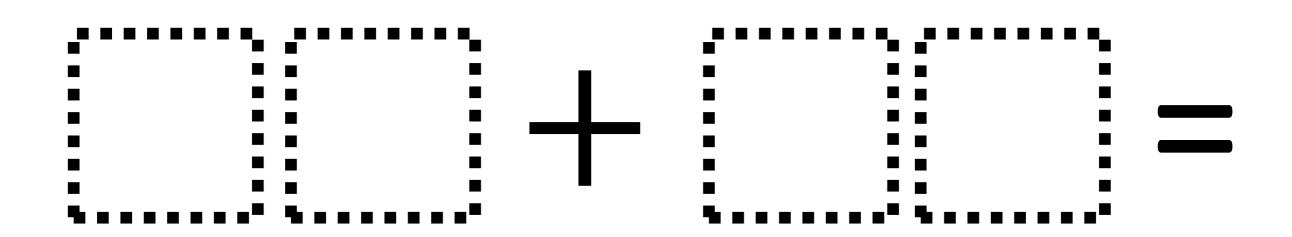
Rolling a sum of _____ on two _____-sided dice is the same probability as rolling a sum of _____ on two _____-sided dice.

Authors: Audrey Mendivil, Daniel Luevanos, and Robert Kaplinsky





Make the largest sum by filling in the boxes below using the whole numbers 1 through 9, no more than one time each.









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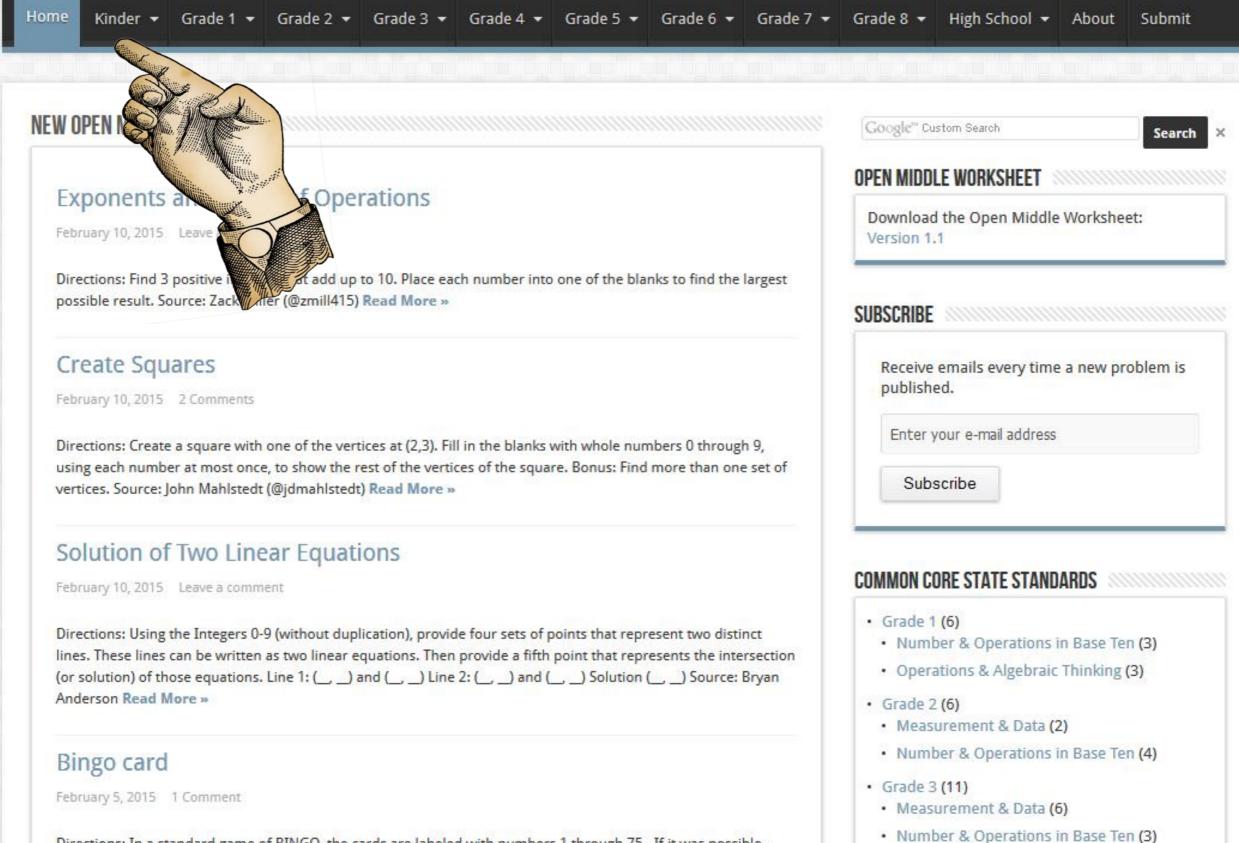
@fawnpnguyen @robertkaplinsky @openmiddle I agree OMP allow for multiple approaches and/or solutions where BT seemed closed most of the time 1:44 PM - 4 May 2015



DOK FAQ

- What DOK level should I start students off with?
- How do teachers fit these problems into their pacing?
- How do I help prevent students from giving up after trying the problem once or twice?
- Where can I find other DOK 2 and DOK 3 problems?
- How can I share DOK 2 and DOK 3 problems I've made?

Open Middle Challenging math problems worth solving

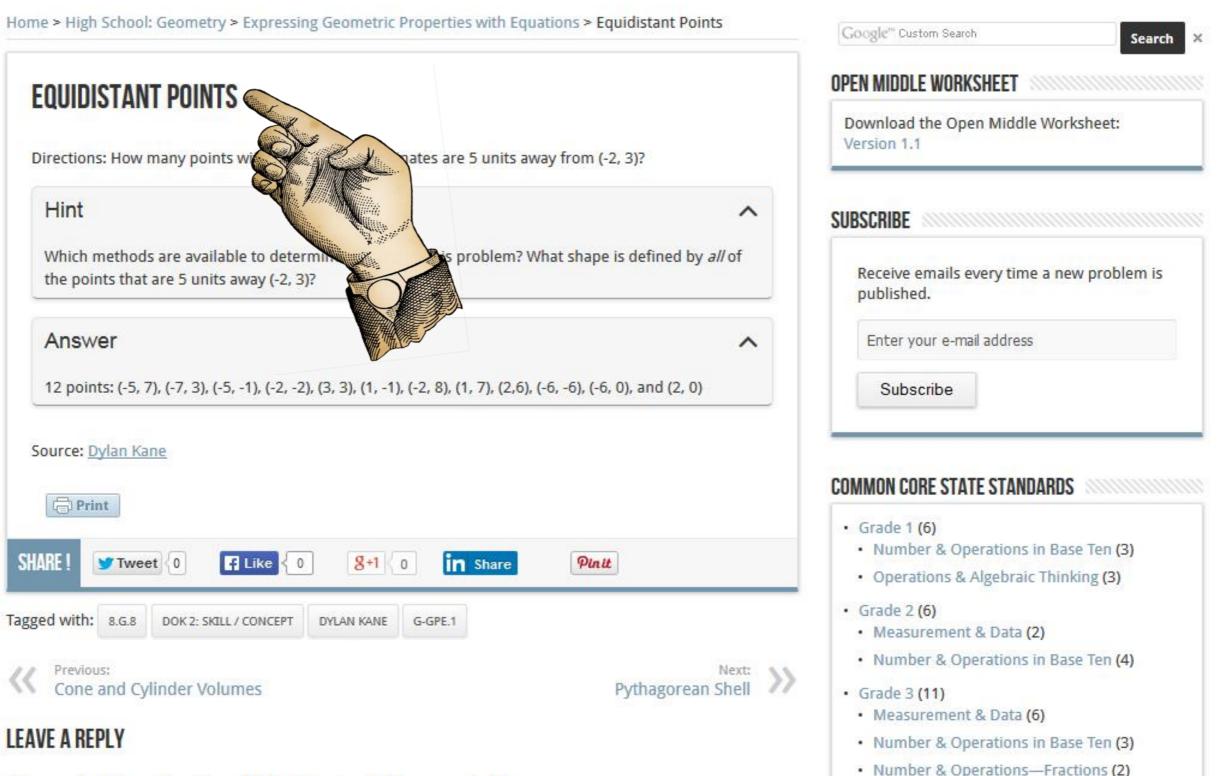


Number & Operations—Fractions (2)

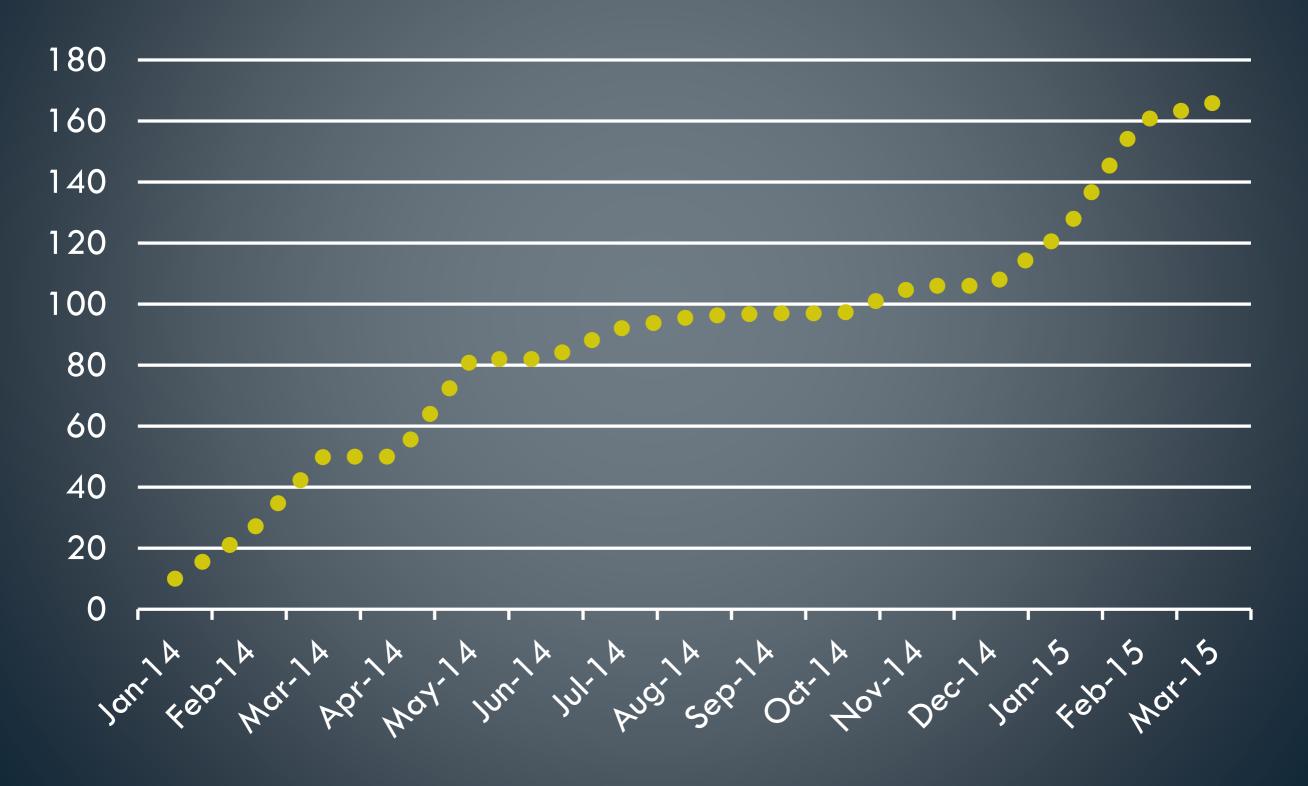
Directions: In a standard game of BINGO, the cards are labeled with numbers 1 through 75. If it was possible, which card would you choose: a card with all of the same number or a standard bingo card? Source: Nanette

Open Middle Challenging math problems worth solving

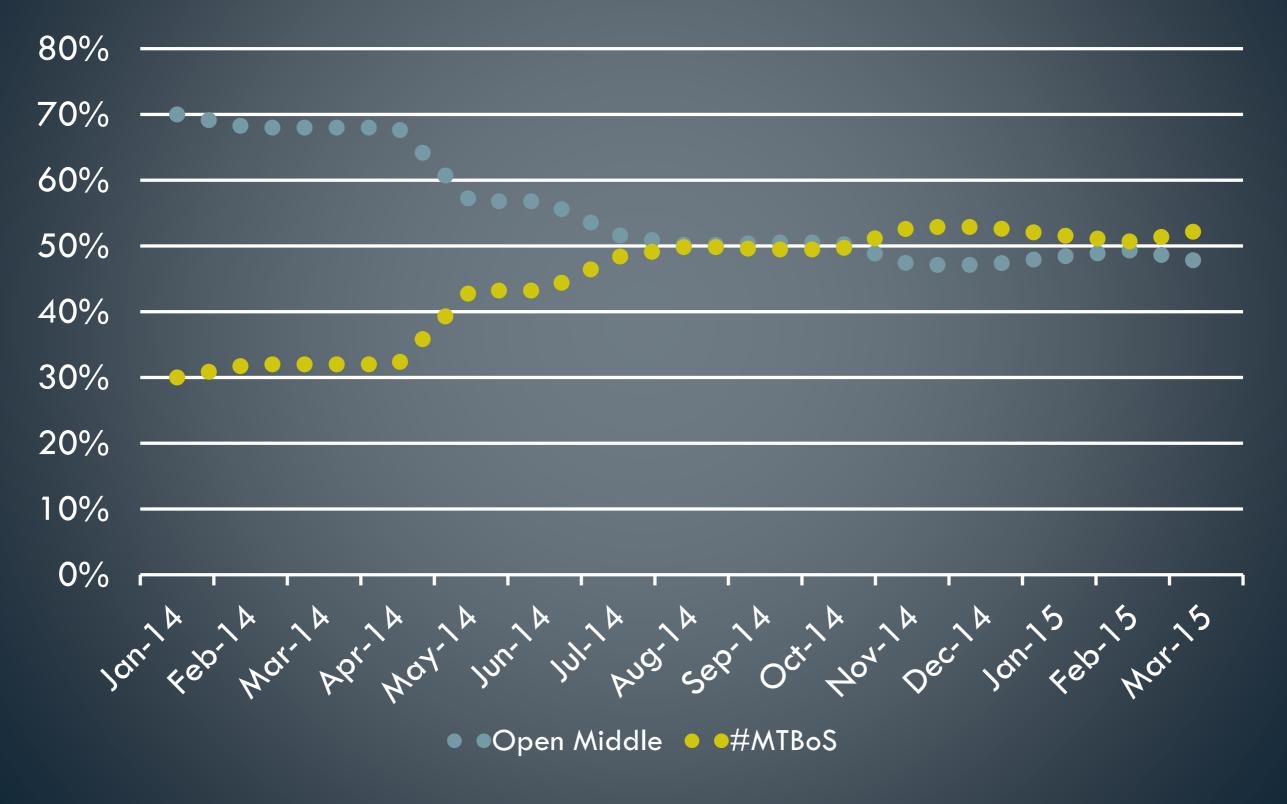
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Total Open Middle Problems



Open Middle Author Percentages



Problems by DOK Level

DOK 2

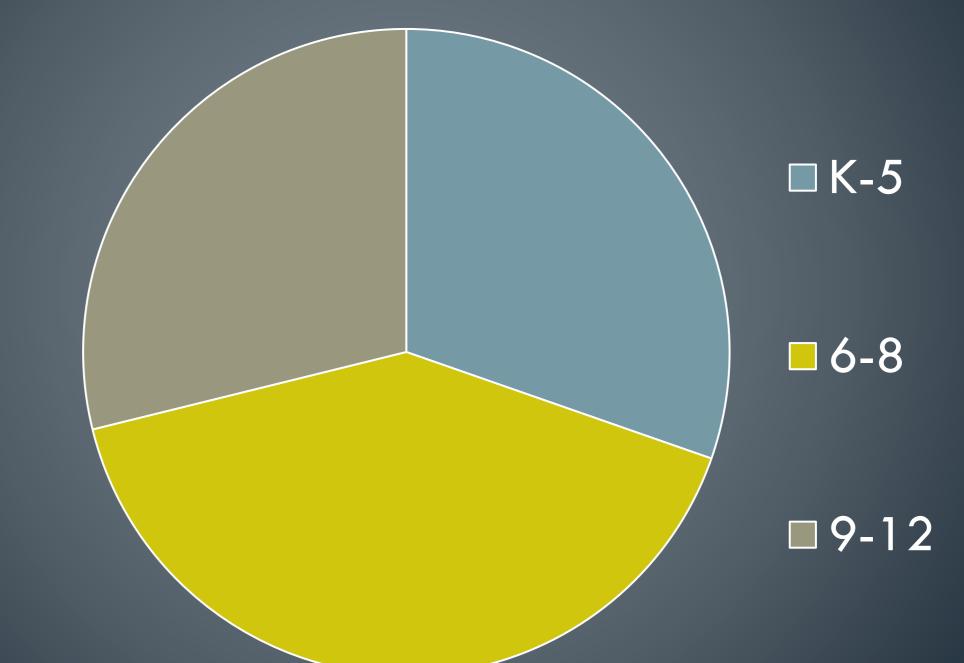
DOK 1

DOK 3

□ DOK 4

Note: Data as of March 2015

Problems by Grade Band



Note: Data as of March 2015



Rigor refers to deep, authentic command of mathematical concepts, not making math harder or introducing topics at earlier grades. To help students meet the standards, educators will need to pursue, with equal intensity, three aspects of rigor in the major work of each grade: conceptual understanding, procedural skills and fluency, and application.

Source: http://www.corestandards.org/other-resources/key-shifts-in-mathematics/

Call to Action

- Commit to one of these choices:
 - Implement a single DOK 2 or DOK 3 problem from openmiddle.com in your classes within the week.
 - Put a DOK 2 question from openmiddle.com on your next assessment.

