# Wentzville School District

**ROBERT KAPLINSKY** 



Goals Engaging problem solving Real world problem-based learning Higher depth of knowledge problems Better implementation Improve our ability to ask questions Practice preparing to implement a lesson Figure out how to deal with uncomfortable situations









### DOUBLE-DOUBLE Double Meat & 265 CHEESEBURGER 175 HAMBURGER **1**50 **FRENCH FRIES** ICED TEA 155 SHAKES Chocolate Strawberry 70 COFFEE



OPEN 10:30 a.m. to 1:00 a.m. Fri. and Sat. until 1:30 a.m.

www.FriedmanArchives.com

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Cashier: SAM

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GUEST

2.65 88.20 90.85 6.81 97.66 \$97.66 \$.00

In

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	Serving Size (g)	Calories
Hamburger w/Onion	243	390
Cheeseburger w/Onion	268	480
Double-Double w/Onion	330	670



Layers	Cost
1	\$1.75
2	\$2.65
3	\$3.55
4	\$4.45
•	•
•	•
20	\$18.85
•	•
•	
100	\$90.85
•	•
•	•
Ν	\$1.75 + (N-1)*\$0.90

bun + produce + meat + cheese + meat + cheese = \$2.65

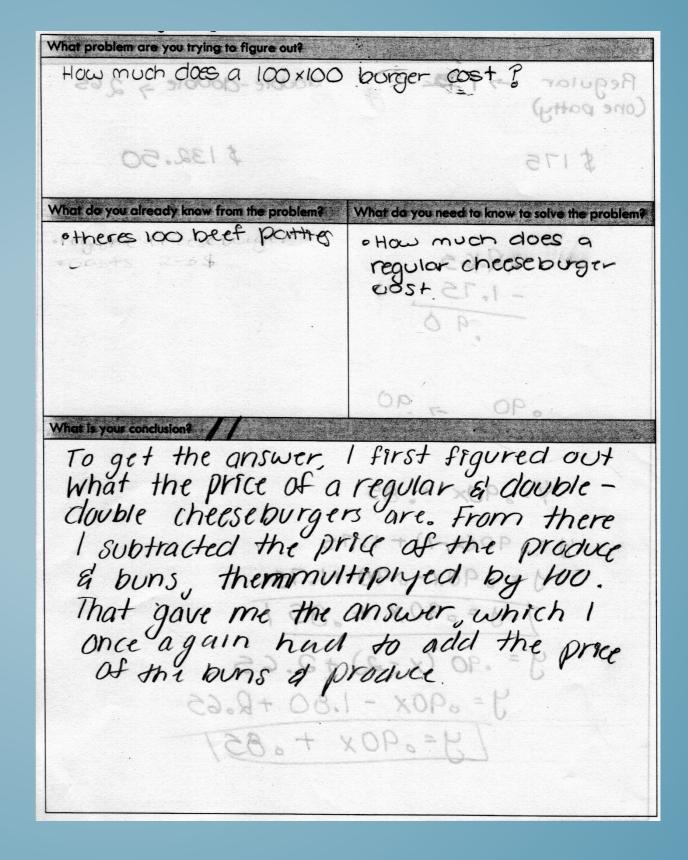
bun + produce + meat + cheese = \$1.75

meat + cheese = \$0.90

# The Reality

- Students needed guidance to figure out a layer's cost
- Not every class is ready to go straight to 100x100
- Common wrong answers included:
  - \$175.00 (\$1.75 x 100 cheeseburgers)
  - \$132.50 (\$2.65 x 50 Double-Doubles)
- Students had equations that had more than X patties
- Students were surprised to see three different equations:
  - Starting with a Double-Double
  - Starting with a cheeseburger
  - Starting with produce and bun only

### STUDENT WORK



The only difference between a double double and a choeseburger is one patty and one slice of cheese. So you subtract the prices of the two to find the price of only one patty & cheese. You then use that number (.90) & subtract it from the price of all the extra stuff. Maltiply by 100

What is your conclusion?

#### 2.40 A MAL ION I DUM a 200 meete 70 # = X 229 ct the IN E (I+x) OR What is your conclusion? A 100×100 at In-h-out cost \$90.85. To solve that, you start by subtracting the price of a cheese burger from a double double. The answer (.90) is the price of a patty and cheese slice.

You multiply (.90) by one less patty than what you want. (x-1), and you add the price of a cheese burger (1.75). You end up with the eq. [y=,90 (x-1)+1.75.]. For the 100×100, you plug in 100 to the (x) and you end up with \$90.85.  $\begin{aligned} y &= .90(100-1) + 1.75 \\ y &= .90(100-1) + 1.75 \\ y &= .90.85 \end{aligned}$ 

### What is your conclusion?

Figure the price difference from the Double-Double with a cheese burger. Then find out the prize for the produce and cheese-beef. get total into \$ 90.85



# Math Question

- Solve the problem on your own. Do not work or share your answer with anyone else.
- You will have 30 seconds to complete it.
- Write your answer down on a paper.

There are 125 sheep and 5 dogs in a flock. How old is the shepherd?

## Of the 32 students I interviewed...

- 75% of them gave me numerical responses
- 2 students calculated the answer to be 130(125 + 5)
- 2 students calculated the answer to be 120(125-5)
- 12 students calculated the answer to be 25 (125  $\div$  5)
- O students calculated the answer to be 625 (125 x 5)
- 4 students stated that they guessed their answer (90, 5, 42, and 50)
- 4 students tried to divide 125 by 5 but could not correctly implement the procedure

# Takeaways

- Making sense of mathematics
- Intellectual autonomy
  - Intellectual autonomy is about being able to think for yourself and not being dependent on others for the direction and control of one's thinking.

# What Does the NHTSA Say?

#### Key Statistics and Consumer Insights:

• Motor vehicle crashes are the leading cause of death for children age 1 through 12 years old.<sup>1</sup>

According to a NHTSA study, 3 out of 4 kids are not as secure in the car as they should be because their car seats are not being used correctly.

be reduced by about hair if the correct child safety seats were always used.

<sup>&</sup>lt;sup>1</sup> Source: Based on the latest mortality data currently available from the CDC's National Center for Health Statistics.



- "because they have their child in the right seat"
- "because their car seats are not being used correctly"

### IF YOUR CHILD IS IN THE RIGHT CAR SEAT.

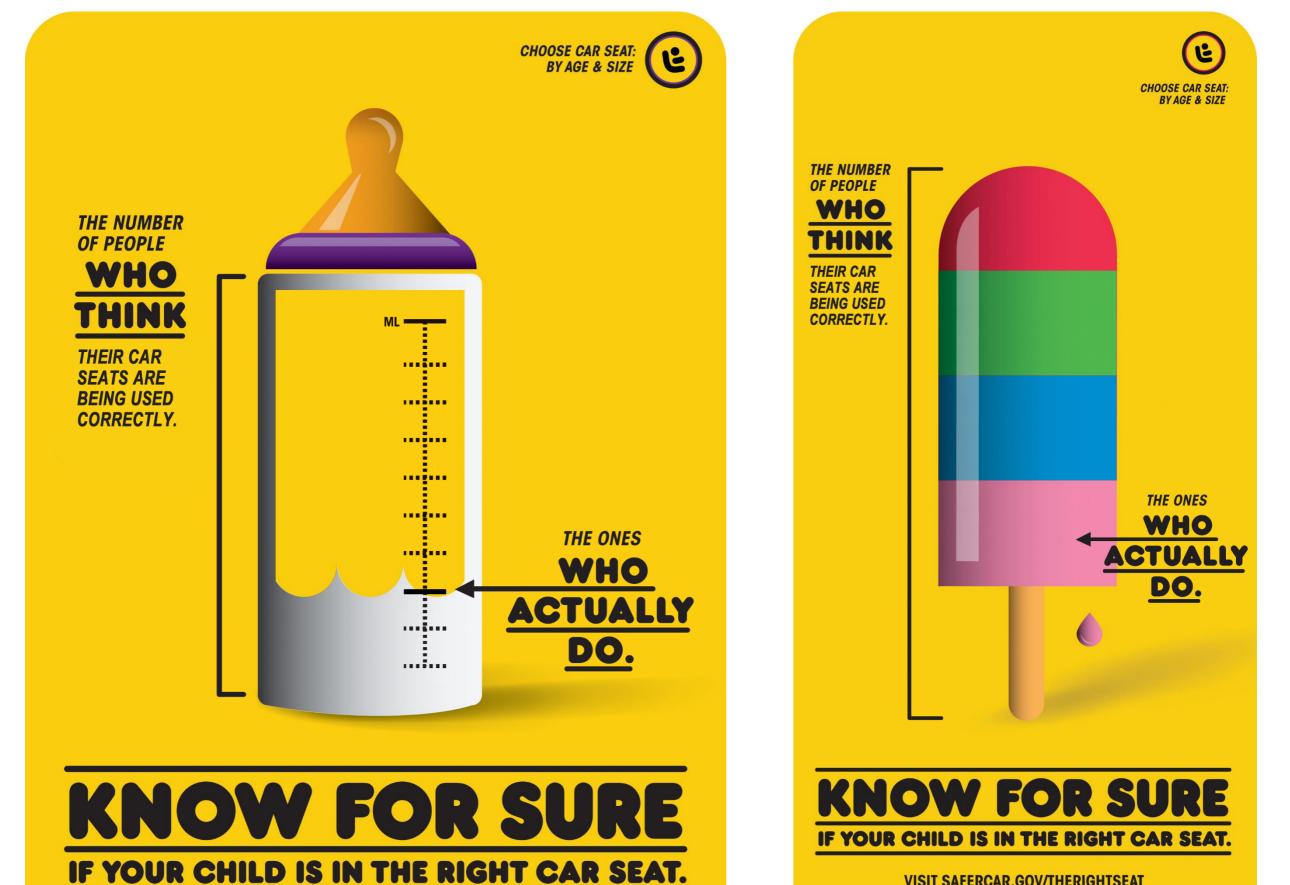


VISIT SAFERCAR.GOV/THERIGHTSEAT



**Child Car** 

Safety



**VISIT SAFERCAR.GOV/THERIGHTSEAT** 





Ad

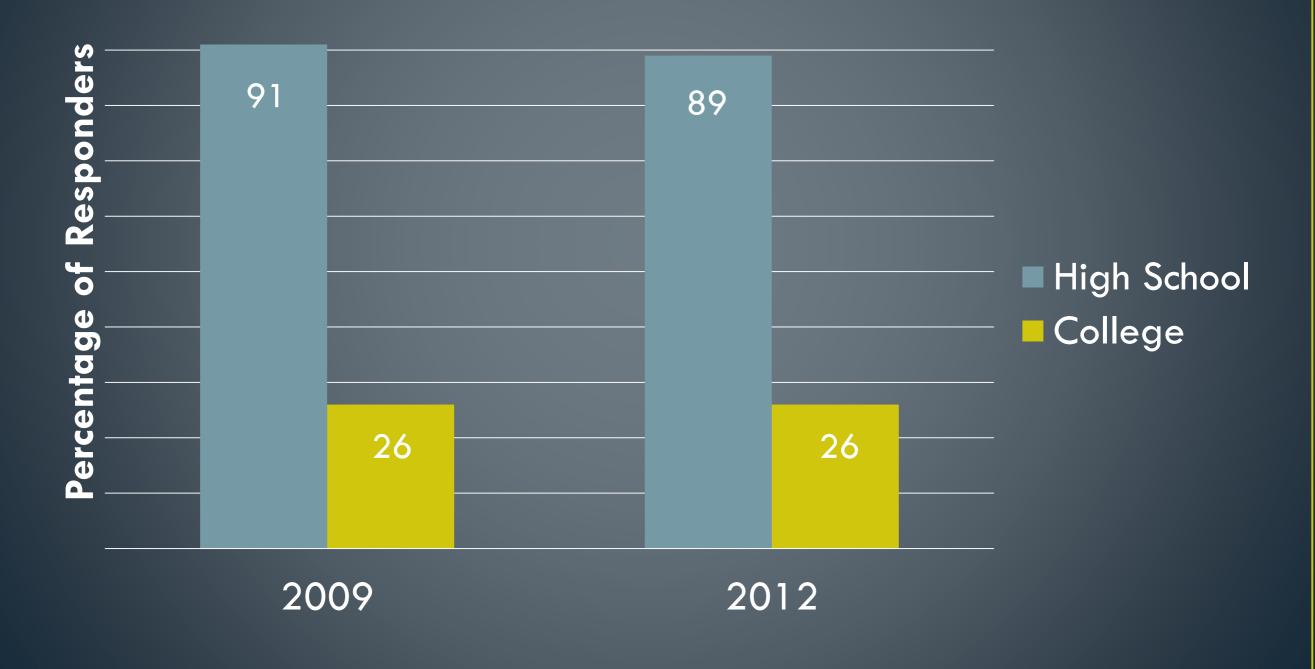


WHAT IS THE PURPOSE OF A K-12 EDUCATION?

 College readiness

 ACT National Curriculum Survey
 Survey
 Surveyed 9,937 educators

### "Well" or "Very Well" Prepared for College



Source: http://www.act.org/research/policymakers/pdf/NCS-PolicySummary2012.pdf

WHAT IS THE PURPOSE OF A K-12 EDUCATION?

 College readiness
 Career readiness

 Association of American Colleges and Universities survey
 Surveyed over 300

- Surveyed over 300 employers with at least 25 employees and many new hires Critical thinking and analytical reasoning skills

Analyzing and solving complex problems

Communicating effectively orally and in writing

Applying knowledge and skills to real-world setting

Working w/ numbers and understanding statistics

#### More Less Same

Source: http://www.aacu.org/leap/documents/2013\_EmployerSurvey.pdf





### SUBPROCURADURIA DE INVESTIGACIÓN ESPECIALIZADA EN DELINCUENCIA ORGANIZADA

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#### WHAT ISN'T MATHEMATICAL MODELING?

- It is not modeling in the sense of, "I do; now you do."
- It is not modeling in the sense of using manipulatives to represent mathematical concepts.
- It is not modeling in the sense of a "model" being just a graph, equation, or function.
- It is not just starting with a real world situation and solving a math problem.
- It is not beginning with the mathematics and then moving to the real world.

Source: http://www.cde.ca.gov/ci/ma/cf/documents/aug2013apxdmathmodel.pdf

PROBLEM-BASED LEARNING FAQ

- How long do problem based lessons take?
- How often do teachers do problem-based learning?
- Do teachers use problem-based lessons to introduce a topic or after you've already taught it?
- How is problem-based learning assessed?
- How much time does it take to create a problem-based lesson?

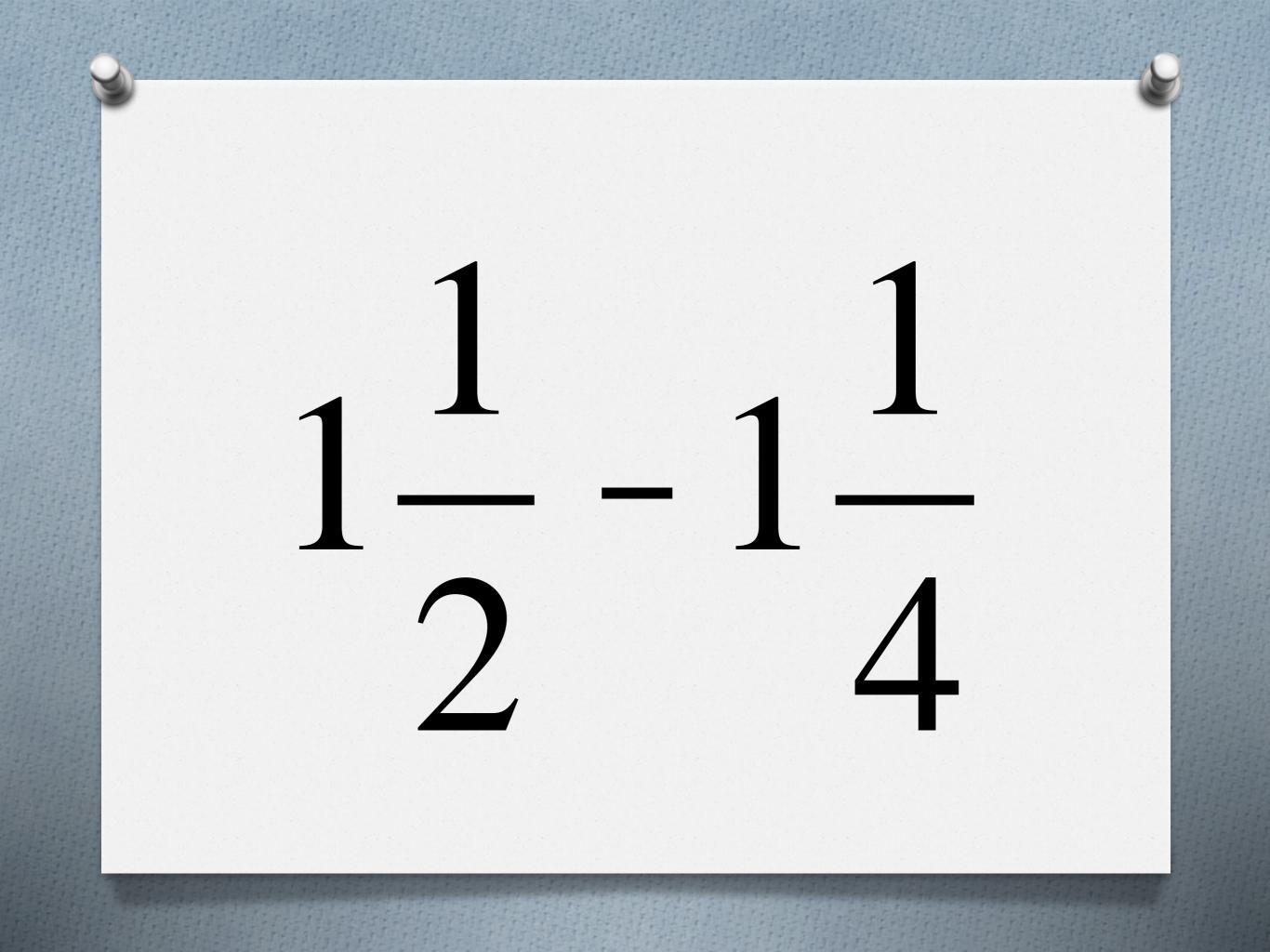
#### WHAT DOES IT LOOK LIKE...

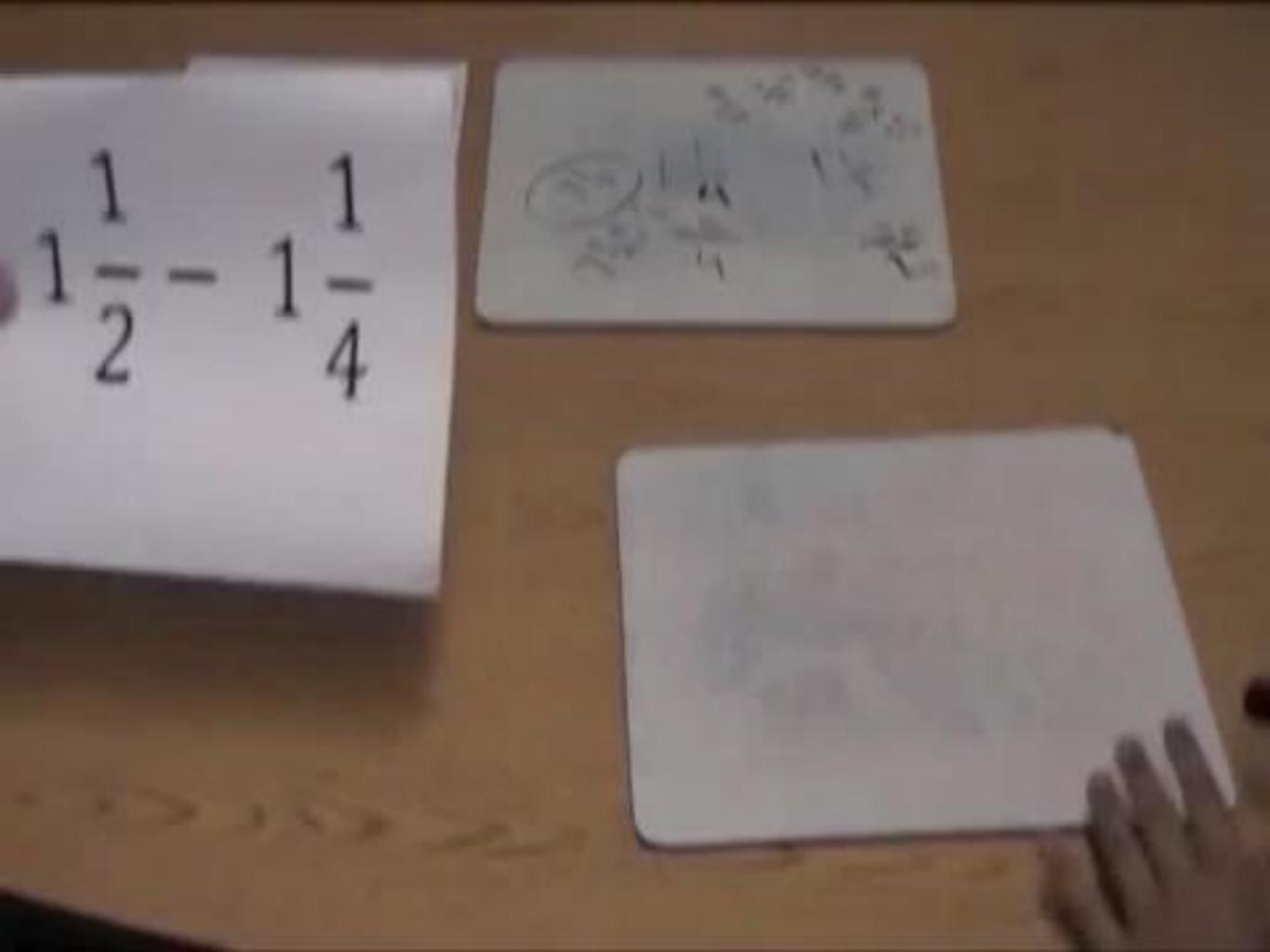
- when students have procedural skill but not conceptual understanding or the ability to apply mathematics?
- when students <u>can</u> work with numbers but <u>cannot</u>:
  - critically think
  - applying knowledge and skills to real-world settings
  - analyze and solve complex problems

How far apart are the exits on this freeway: Jct 90 and Jefferson Blvd?









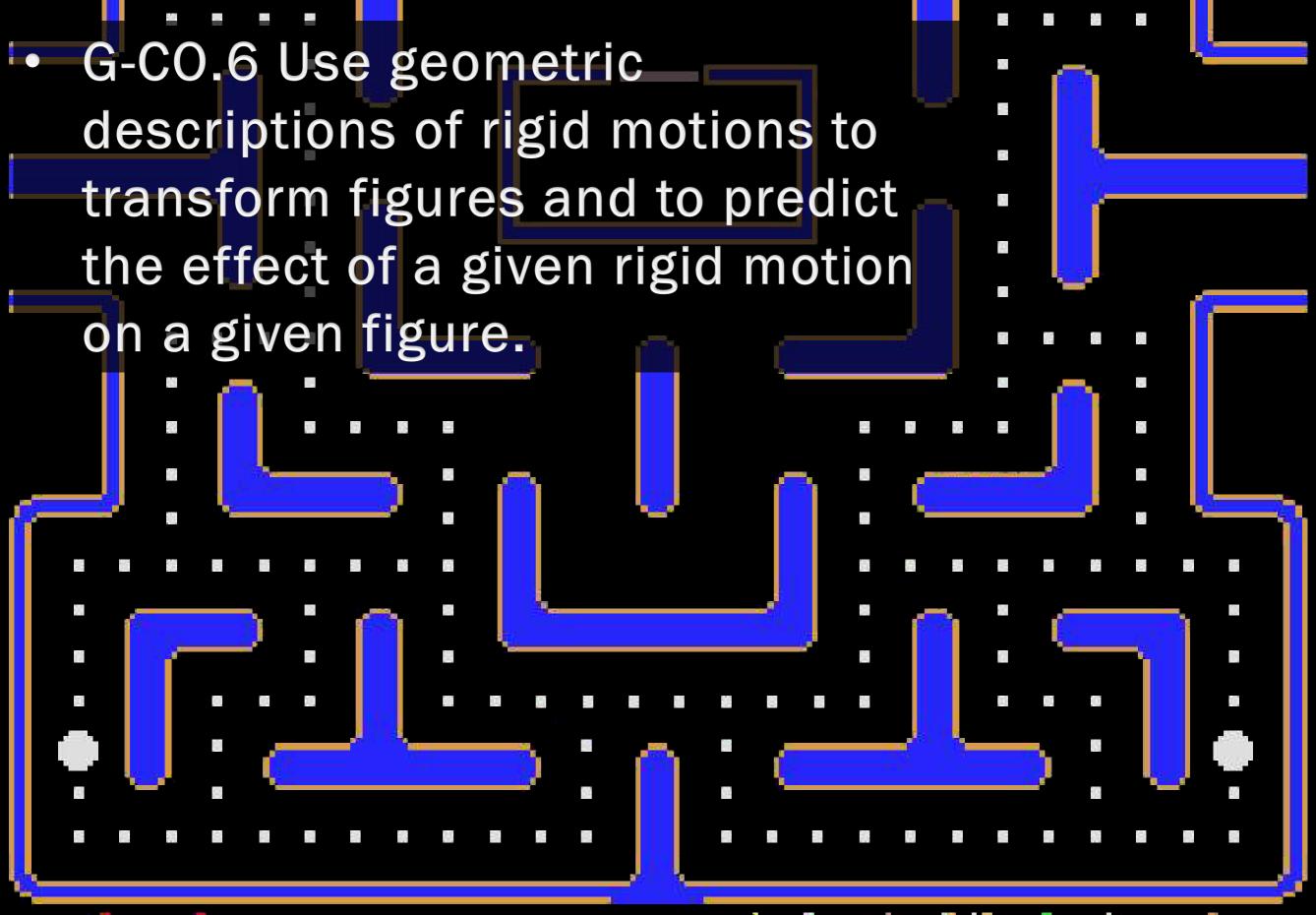


### The Four C's

CommunicationCuriosity

6.G.4 - Represent threedimensional figures using nets made up of rectangles and triangles, and use the nets to find the surface area of these figures. 7.G.6 - Solve real-world and mathematical problems involving area, volume and surface area.

8.G.9 - Know the formulas for the volumes of cones, cylinders, and spheres and use them to solve real-world and mathematical problems. G-GMD.3 - Use volume formulas for cylinders, pyramids, cones, and spheres to solve problems.



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A-CED.1 - Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions. F-IF.7a - Graph linear and quadratic functions and show intercepts, maxima, and minima.

#### 6.RP.2 - Understand the concept of a unit rate

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### The Four C's

Communication
Curiosity
Critical Thinking

#### Problem Solving Framework

Inspired by Geoff Krall's resources at emergentmath.com

ame:	Period: Date:
What problem are you trying to figure out?	What guesses do you have?
What do you already know from the problem?	What do you need to know to solve the problem?
What should we title this lesson?	
What is your conclusion? How did you reach that conclusion?	

## The Four C's

- Communication
- Curiosity
- Critical Thinking
- Content Knowledge

Goals Engaging problem solving Real world problem-based learning Higher depth of knowledge problems Better implementation Improve our ability to ask questions Practice preparing to implement a lesson Figure out how to deal with uncomfortable situations

#### Questioning Scenarios

- The activity begins with teachers in groups of three taking the roles of teacher, student, or observer.
- The individuals playing the role of teacher and student each receive a slip of paper describing their scenario.
- The individual playing the role of observer waits to record all of the teacher's questions to the student.
- Once the activity begins, the teacher will talk to the student in the context of the scenario they read about on the slips of paper.

What did you get for the area of the circle with a radius of 2 units?



## Great. Do you have any questions?



What did you get for the area of the circle with a radius of 2 units?

4 pi

Great. How did you get your answer?

The radius is 2 so I plugged it into 2 pi r and got 4 pi.

Goals Engaging problem solving Real world problem-based learning Higher depth of knowledge problems Better implementation Improve our ability to ask questions Practice preparing to implement a lesson Figure out how to deal with uncomfortable situations





CCSS.MATH.CONTENT.4.MD.A.3 nmand of Apply the area and perimeter formulas for harder or rectangles in real world and mathematical problems. meet the equal intensity, u of each grade: conceptua skills and fluency, and application.

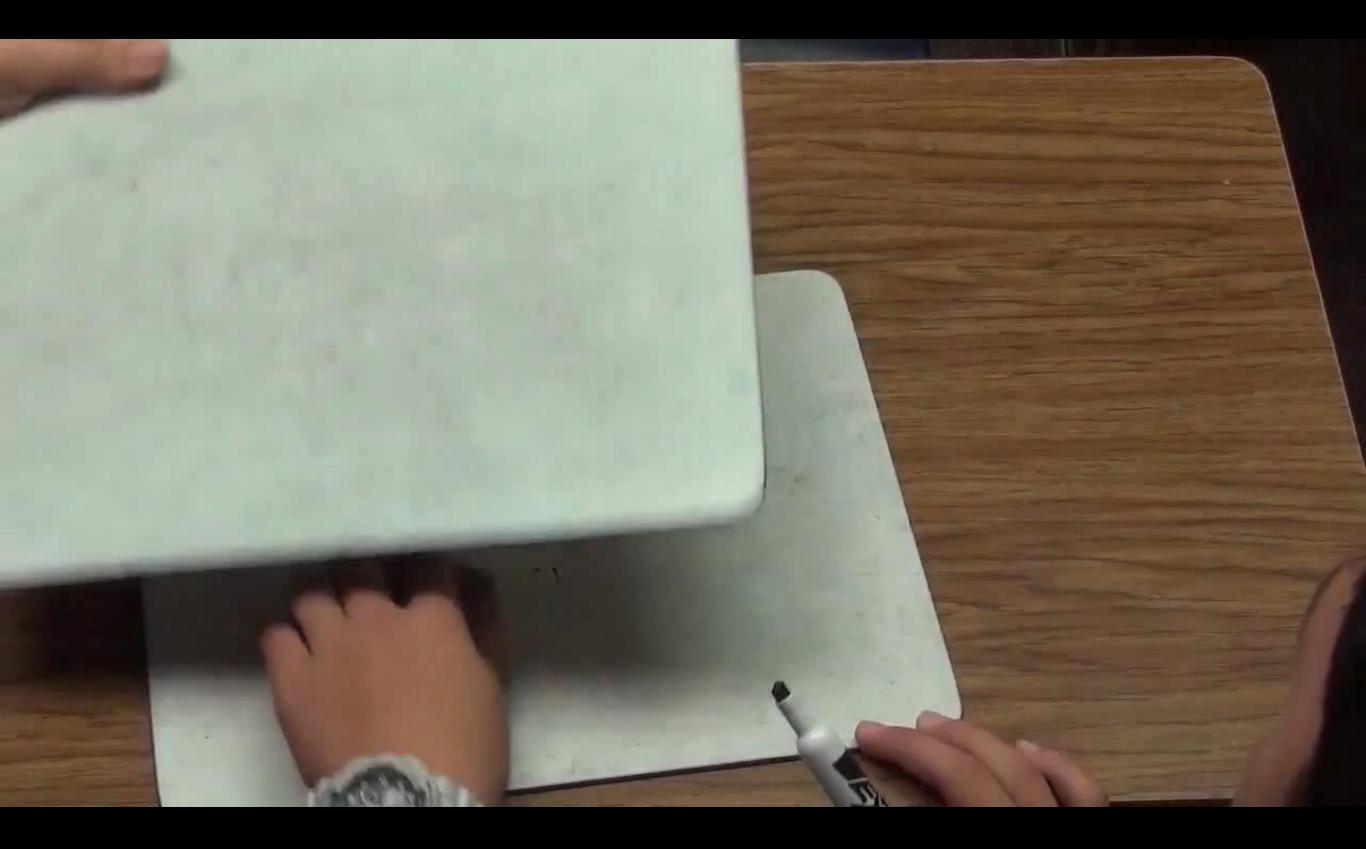
Source: http://www.corestandards.org/other-resources/key-shifts-in-mathematics/

What is the perimeter of a rectangle that measures 8 units by 4 units?





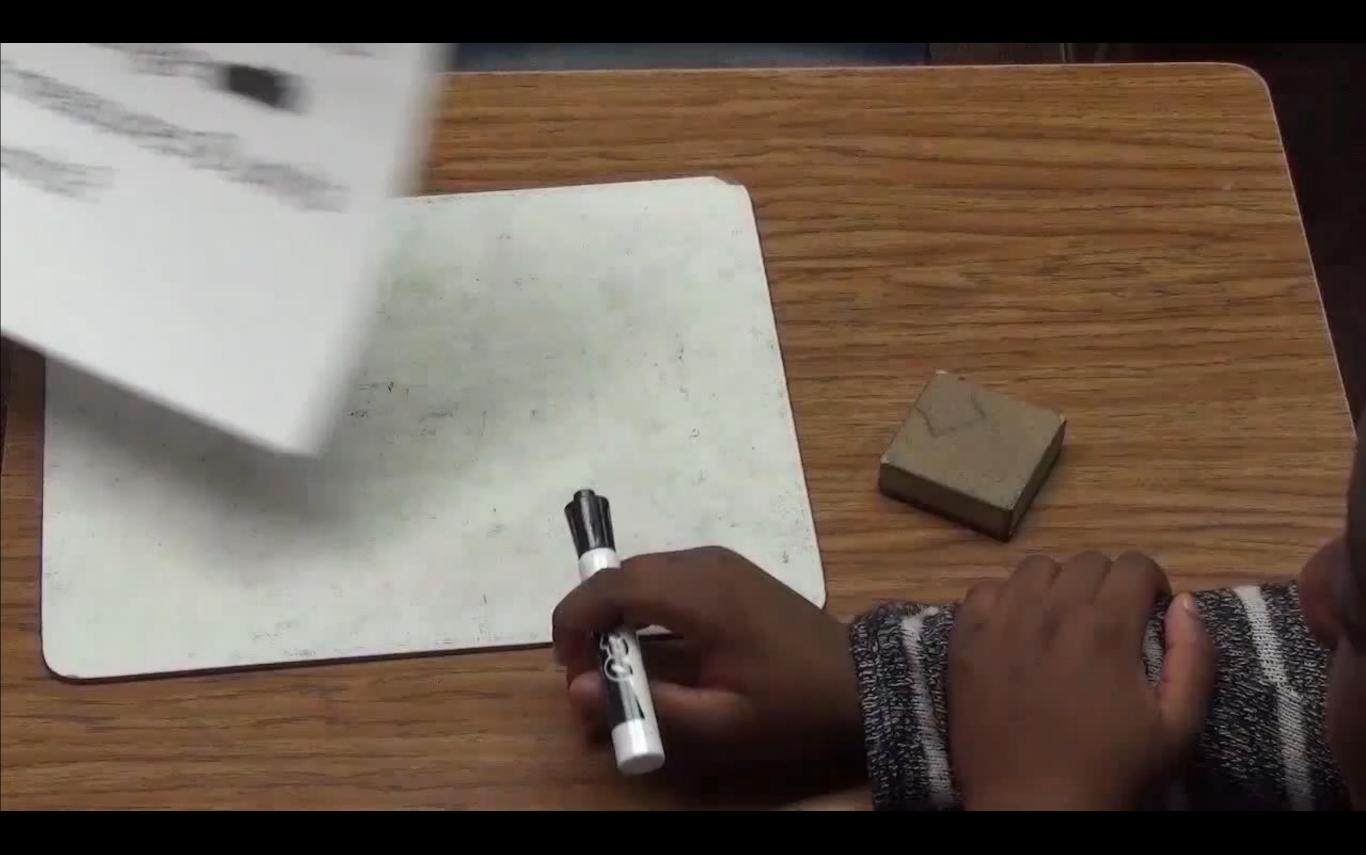
List the dimensions of a rectangle with a perimeter of 24 units.



# Components of Rigor Procedural Skill and Fluency

#### Conceptual Understanding





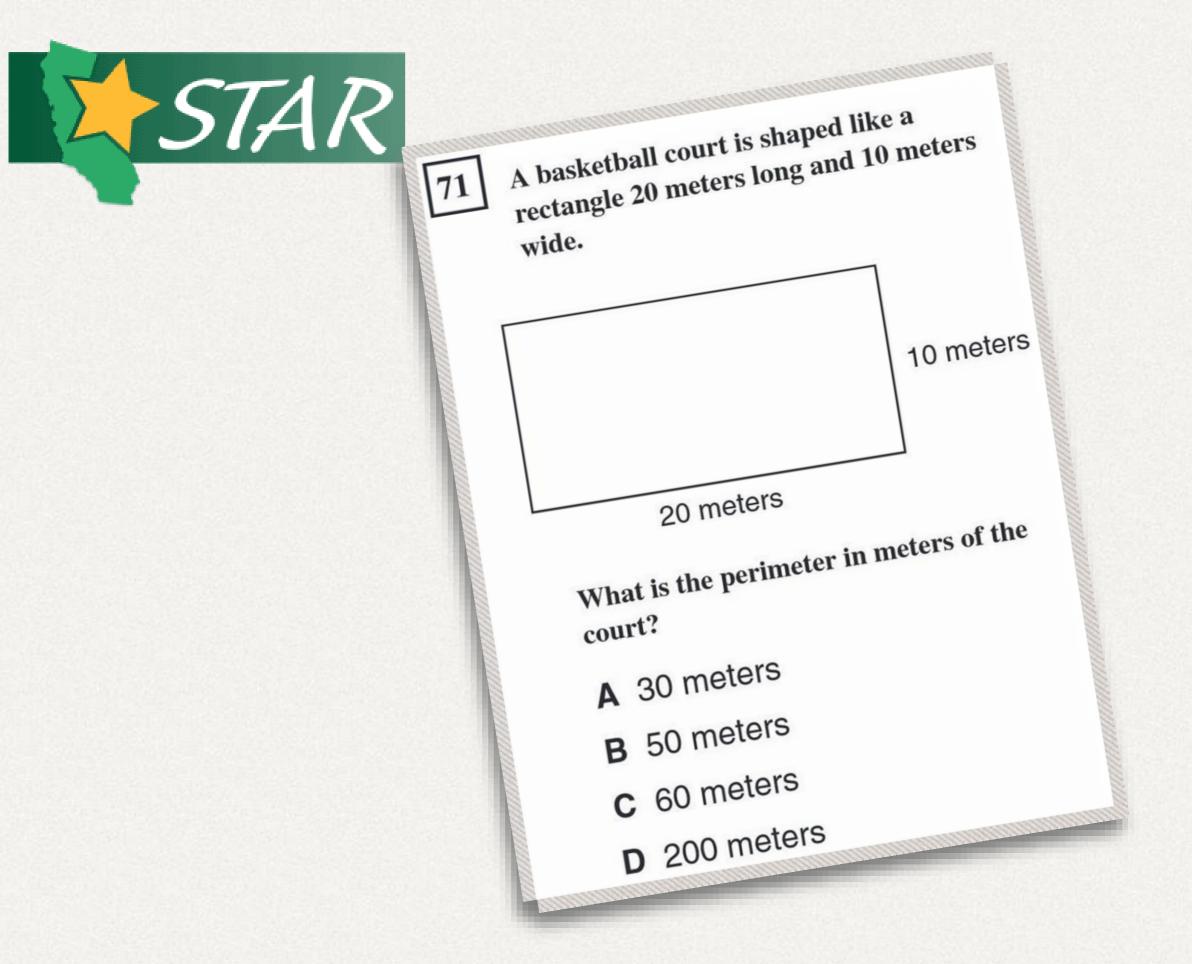




List the of a rectangle with a perimeter of 24 units.

# Components of Rigor Procedural Skill and Fluency

#### Conceptual Understanding

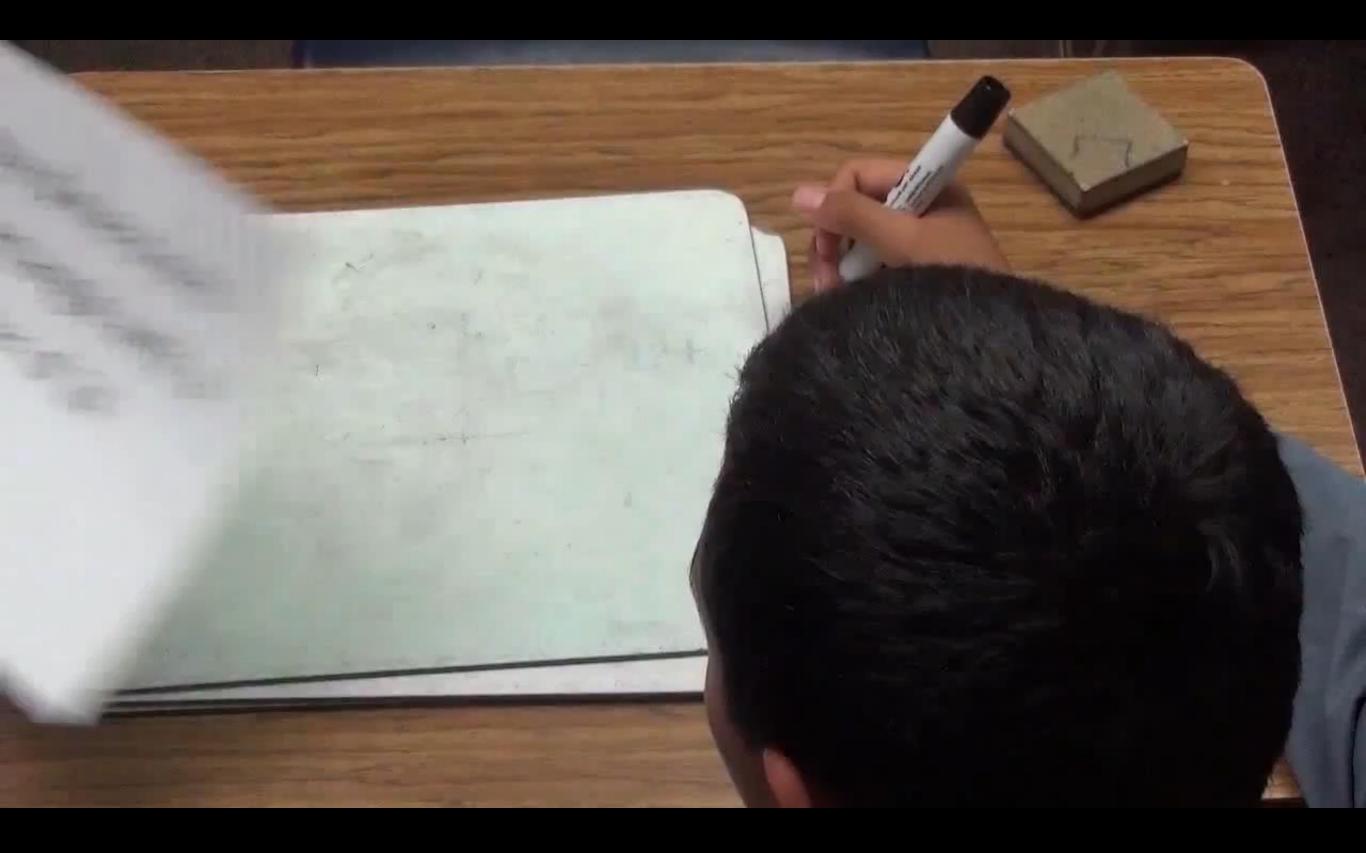


Source: http://www.cde.ca.gov/ta/tg/sr/documents/cstrtqmath3.pdf

What is the perimeter of a rectangle **Mathematics** that measures 8 units by 4 units?











Of all the rectangles with a perimeter of 24 units, which one has the most area?

00:00:00:00 Of all the rectangles with a perimeter of 24 units, which one has the mast area?

# Components of Rigor Procedural Skill and Fluency

### Conceptual Understanding

### Defining the Problem

Students appear to demonstrate "deep, authentic command of mathematical concepts" when given commonly used problems. However with more challenging problems, the same students seem to no longer demonstrate that command.

### Addressing the Problem

- First, we must have a clear understanding about why these problems are different from one another.
- Next, we need to practice using these problems so that we understand how students may react to them.
- Last, we need a source that can provide us with a variety of free problems.

#### DOK Distinguishing Between Depth of Knowledge Levels in Mathematics

Topic	Adding Whole Numbers	Money	Fractions on a Number Line	Area and Perimeter	Subtracting Mixed Numbers
CCSS	• 1.NBT.4	• 2.MD.8	<ul> <li>3.NF.2</li> </ul>	<ul> <li>3.MD.8</li> </ul>	• 5.NF.1
Standard(s)	• 2.NBT.5			• 4.MD.3	
DOK 1 Example	Find the sum. $44 + 27 =$	If you have 2 dimes and 3 pennies, how many cents do you have	Which point is located at $\frac{7}{12}$ below? L M N O ++++++++++++++++++++++++++++++++++++	Find the perimeter of a rectangle that measures 4 units by 8 units.	Find the difference. $5\frac{1}{2} - 4\frac{2}{3} =$
DOK 2 Example	Fill in the boxes below using the whole numbers 1 through 9, no more than one time each, so that you make a true equation. + 53 =	Make 47¢ in three different ways with either quarters, dimes, nickels, or pennies.	Label the point where $\frac{3}{4}$ belongs on the number line below. Be as precise as possible.	List the measurements of three different rectangles that each has a perimeter of 20 units.	Create three different mixed numbers that will make the equation true by using the whole numbers 1 through 9, no more than one time each,. You may reuse the same whole numbers for each of the three mixed numbers. $5\frac{4}{5} - \boxed{\frac{1}{5}} = 3\frac{1}{20}$
DOK 3 Example	Make the largest sum by filling in the boxes below using the whole numbers 1 through 9, no more than one time each.	Make 47¢ using exactly 5 coins with either quarters, dimes, nickels, or pennies.	Create 5 fractions using the whole numbers 0 through 9, no more than one time each, as numerators and denominators and correctly place them all on a number line.	What is the greatest area you can make with a rectangle that has a perimeter of 24 units?	Make the smallest difference by filling in the boxes below using the whole numbers 1 through 9, no more than one time each.

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More free DOK 2 & 3 problems available at openmiddle.com | © 2015 Robert Kaplinsky, robertkaplinsky.com

### DOK Distinguishing Between Depth of Knowledge Levels in Mathematics

Topic	Surface Area and	Probability	Transformations	Factoring	Quadratics in Vertex
	Volume			Quadratics	Form
CCSS	• 6.G.4	• 7.SP.5	• 8.G.1	<ul> <li>A-SSE.3a</li> </ul>	• F-IF.7a
Standard(s)	• 7.G.6	• 7.SP.7	• G-CO.5		
DOK 1	Find the surface	What is the probability of	Rotate the image below 90°	Find the factors:	Find the roots and
Example	area of a	rolling a sum of 5 using	counterclockwise and reflect it		maximum of the
	rectangular prism	two 6-sided dice?	across a	$2x^2 + 7x + 3$	quadratic equation
	that measures 3		horizontal		below.
	units by 4 units by		line.		
	5 units.		B		$y=3(x-4)^2-3$
DOK 2	List the	What value(s) have a	List three sequences of	Fill in the blank	Create three
Example	measurements of	1/12 probability of being	transformations that take pre-	with integers so	equations for
	three different	rolled as the sum of two	image	that the quadratic	quadratics in vertex
	rectangular prisms	6-sided dice?	ABCD to	expression is	form that have roots
	that each has a		image	factorable.	at 3 and 5 but have
	surface area of 20		A'B'C'D'.	2	different maximum
	square units.		Pre-Image Image	$x^2 + x + 4$	and/or minimum
DOK 3	What is the	Fill in the blanks to	What is the fewest number of	Fill the blank by	values. Create a quadratic
Example	greatest volume	complete this sentence	transformations needed to take	finding the largest	equation with the
Lxample	you can make with	using the whole numbers	pre-image ABCD to image A'B'C'D'?	and smallest	largest maximum
	a rectangular	1 through 9, no more	pre image Abeb to image Abeb i	integers that will	value using the
	prism that has a	than one time each.	B	make the quadratic	whole numbers 1
	surface area of 20			expression	through 9, no more
	square units?	Rolling a sum of on	$\geq$ $\sim$	factorable.	than one time each.
		twosided dice is the			
		same probability as rolling	∼в ∨	$2x^2 + 3x + $	$y = -[(x-[)^2 + [])^2$
		a sum of on two	ن Pre-Image Image		Andre
		sided dice.			

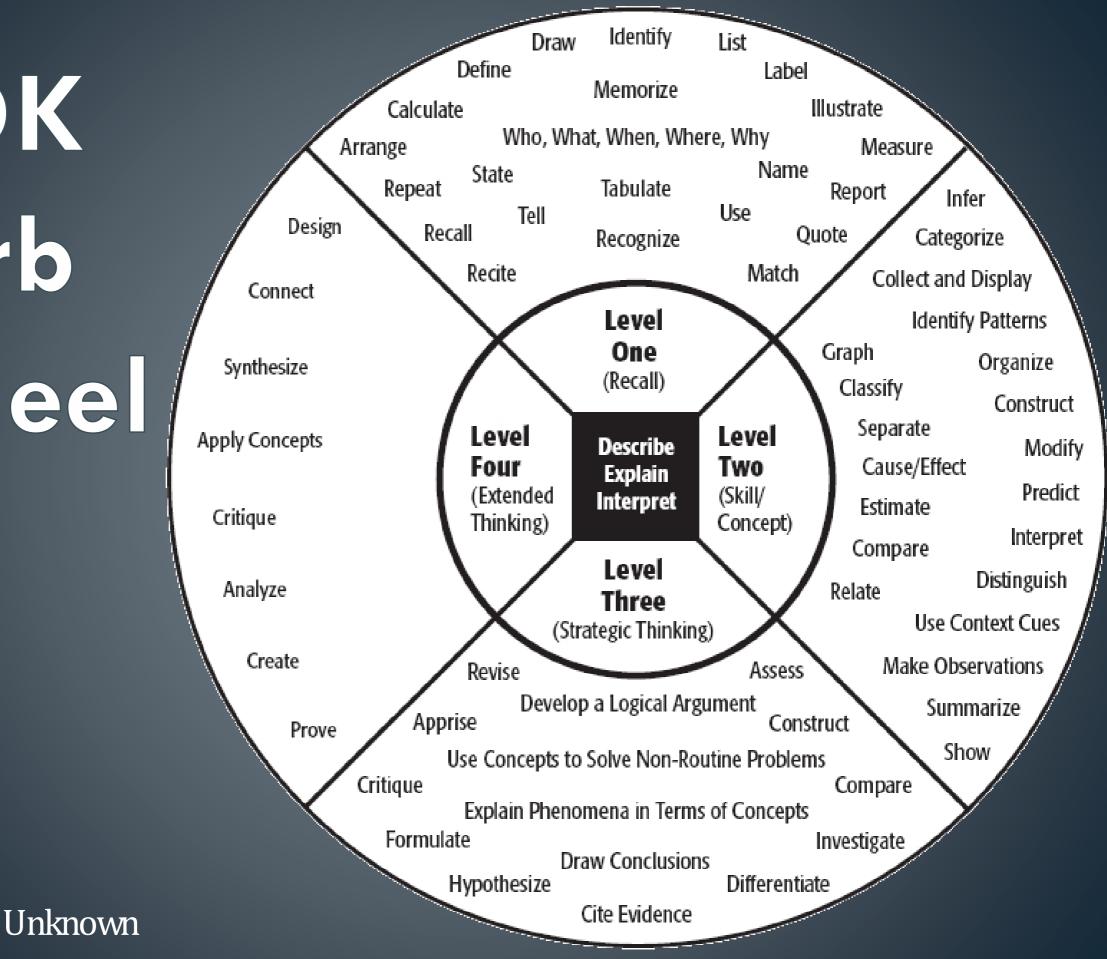
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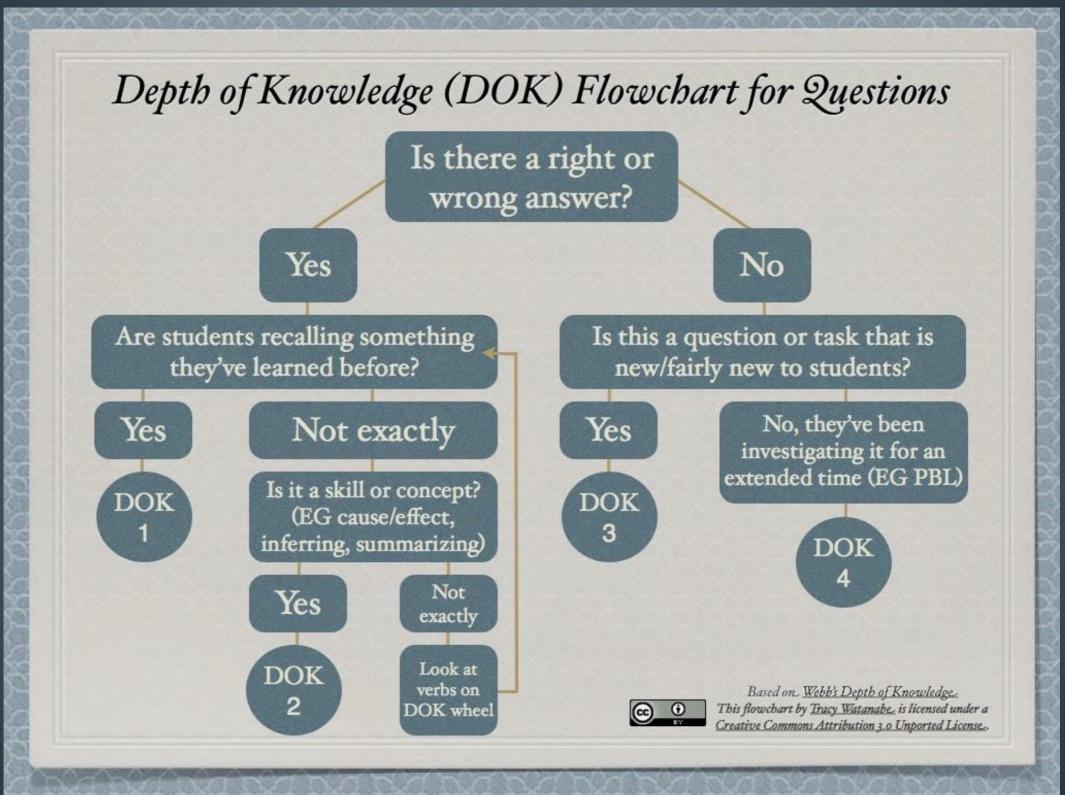
# Complicated or Complex?

# DOK Verb Wheel

Source:



### **DOK Flowchart for Questions**



Source: Tracy Watanabe - @tracywatanabe

# DOK Level Differences

#### Level 1: Recall & Reproduction

- Often a trivial application of facts.
- Requires little to no cognitive effort beyond remembering the right formula.
- Usually only one answer.

#### Level 2: Skills & Concepts

- Usually requires more than one step to solve.
- Often multiple answers.

#### Level 3: Strategic Thinking

- Usually requires critical thinking about the best way to approach a problem.
- May be multiple answers or a single optimal answer.
- Often challenging enough to make your head hurt.

#### Level 4: Extended Thinking

In mathematics these are generally represented by performance tasks or problem-based lessons.

# **Probability** What is the probability of rolling a sum of 5 using two 6sided dice?

# Probability What value(s) have a $\frac{1}{12}$ probability of being rolled as the sum of two 6-sided dice?

**Author: Daniel Luevanos** 

# Probability

Fill in the blanks to complete this sentence using the whole numbers 1 through 9, no more than one time each.

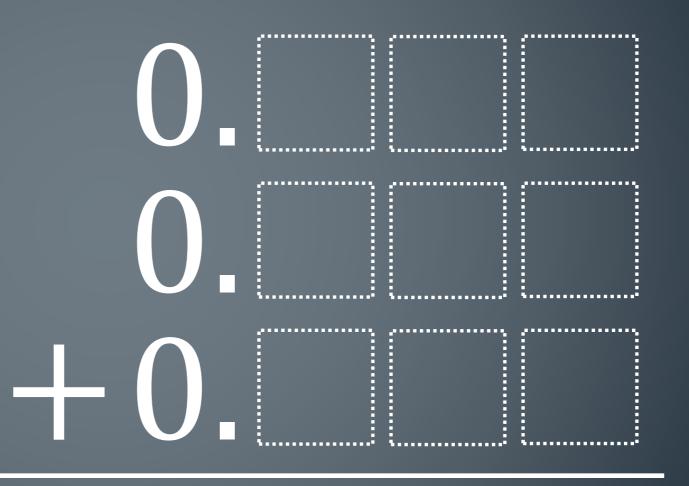
Rolling a sum of \_\_\_\_\_ on two \_\_\_\_\_-sided dice is the same probability as rolling a sum of \_\_\_\_\_ on two \_\_\_\_\_-sided dice.

Authors: Audrey Mendivil, Daniel Luevanos, and Robert Kaplinsky

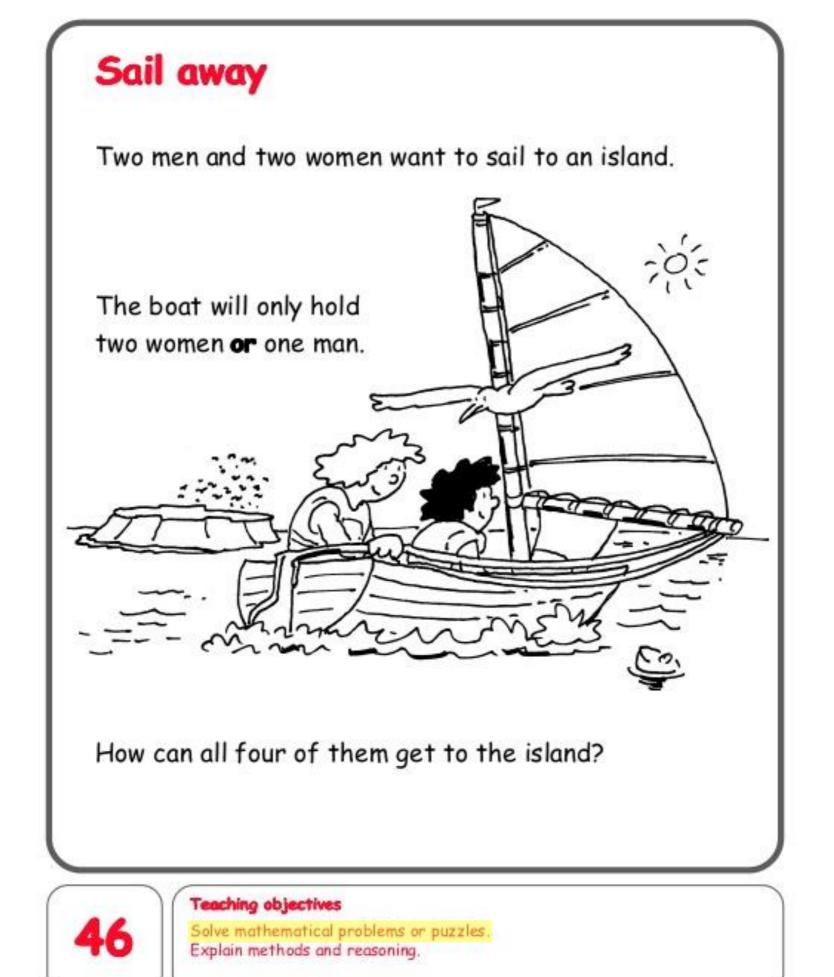


# Adding Decimals

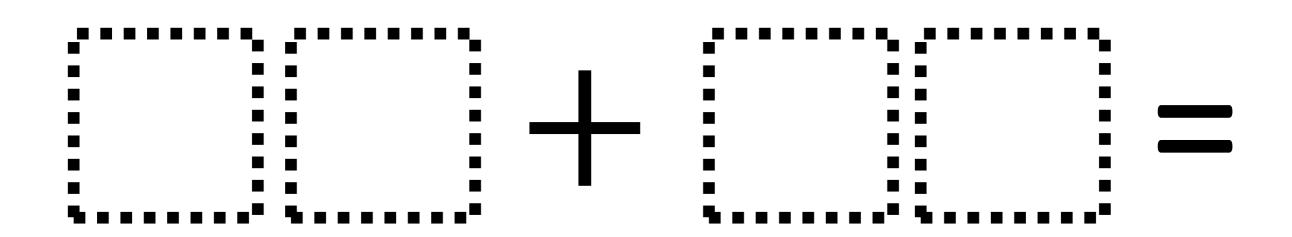
Use the numbers 1 through 9, at most one time each, to fill in the boxes and make three decimals whose sum is as close to 1 as possible.



# 



Make the largest sum by filling in the boxes below using the whole numbers 1 through 9, no more than one time each.









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**Follow** 

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@fawnpnguyen @robertkaplinsky @openmiddle I agree OMP allow for multiple approaches and/or solutions where BT seemed closed most of the time 1:44 PM - 4 May 2015



### Depth of Knowledge – Level One

What is the circle's circumference?  $\pi \approx 3.14$ 

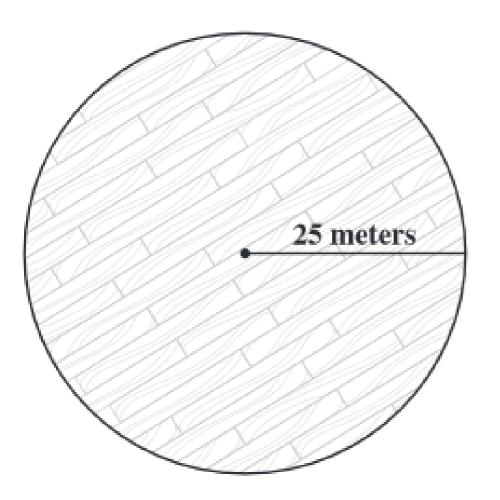
10 units /

What is the circle's area?  $\pi \approx 3.14$ 

10 units



#### This circular stage has a radius of 25 meters.

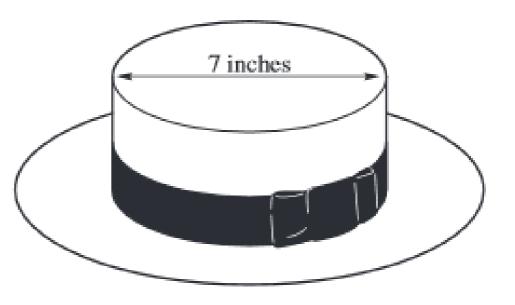


Which equation could be used to find the area of the stage in square meters?

- A  $A = 25\pi$
- $\mathbf{B} = A = 50\pi$
- $C \quad A = \pi \cdot 25^2$
- $\mathbf{D} \quad A = \pi \bullet 50^2$



The top part of this hat is shaped like a cylinder with a diameter of 7 inches.



Which measure is *closest* to the length of the band that goes around the outside of the hat?

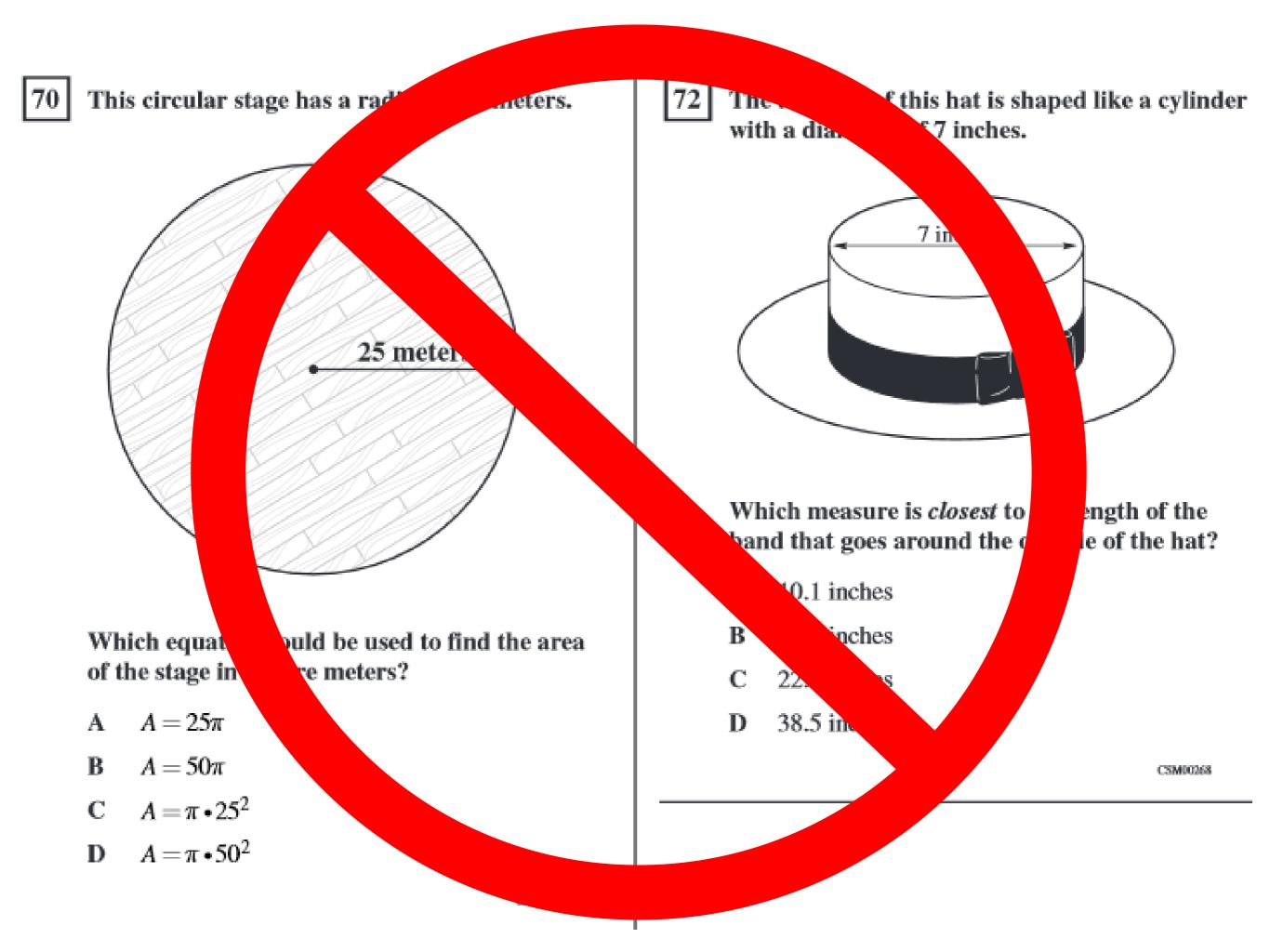
- A 10.1 inches
- B 11.0 inches
- C 22.0 inches
- D 38.5 inches

CSM00268

Source: 6<sup>th</sup> Grade CST Released Test Questions - http://www.cde.ca.gov/ta/tg/sr/documents/cstrtqmath6.pdf

## Student Data Facts

- 396 seventh grade students were assessed
- 68.26% correctly answered the circumference question
- 78.59% correctly answered the area question



Depth of Knowledge – Level Two Which circle is bigger? How do you know? Circle A Circle B Area =  $36 \text{ units}^2$  Circumference =  $36 \text{ units}^2$  $A = \pi \cdot r^2$  $C = \pi \cdot 2 \cdot r$  $A \approx 3.14 \cdot 5.73^2$  $36 \approx 6.28 \cdot r$  $A \approx 3.14 \cdot 32.83$ 36  $\overline{6.28} \approx r$  $A \approx 103.15 \text{ units}^2$ 5.73 units  $\approx r$ 

### **SBAC Constructed Response Rubric**

- For full credit (2 points):
  - Student reaches the correct conclusion.
    - AND
  - Student provides sufficient reasoning to support this conclusion.
- For partial credit (1 point):
  - Student reaches the correct conclusion but does not provide sufficient reasoning to support this conclusion.
     OR
  - Student does not reach the correct conclusion but provides reasoning to support this conclusion that contains a minor conceptual or computation error.

## Student Data Facts

- Of the 396 seventh grade students who were assessed, 12.12% earned two points on the DOK 2 question.
- 97.92% of the students who correctly answered the DOK 2 question also correctly answered both of the two DOK 1 questions.
- 10.61% of the students who correctly answered both of the two DOK 1 questions also correctly answered the DOK 2 question.

# More Student Data Facts

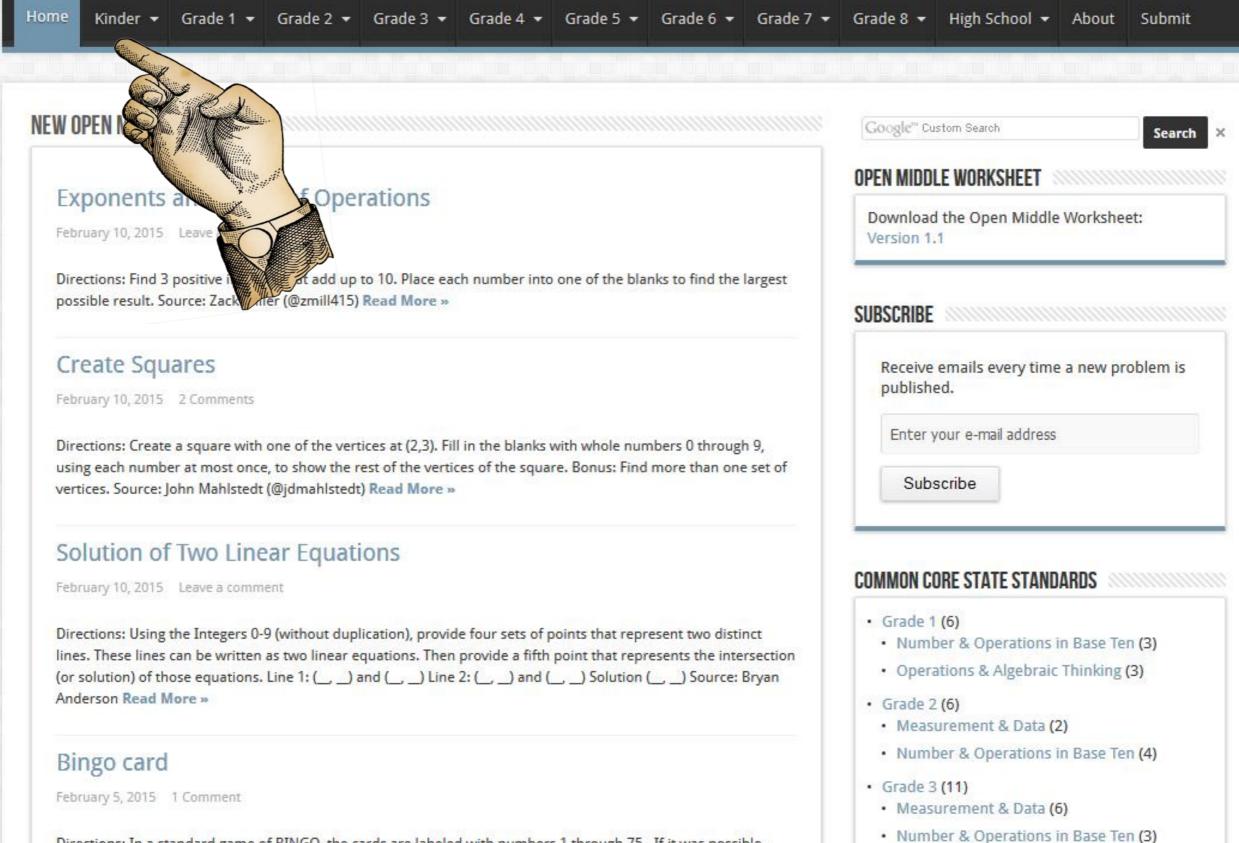
- 28.28% of the students earned only one point.
- All of them earned one point by choosing Circle B and providing insufficient reasoning.
- 59.59% of the students earned no points.

DOK FAQ

- When will students ever use this?
- What DOK level should I start students off with?
- How do teachers fit these problems into their pacing?
- How do I help prevent students from giving up after trying the problem once or twice?
- Where can I find other DOK 2 and DOK 3 problems or submit ones I've made?

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### Open Middle Challenging math problems worth solving

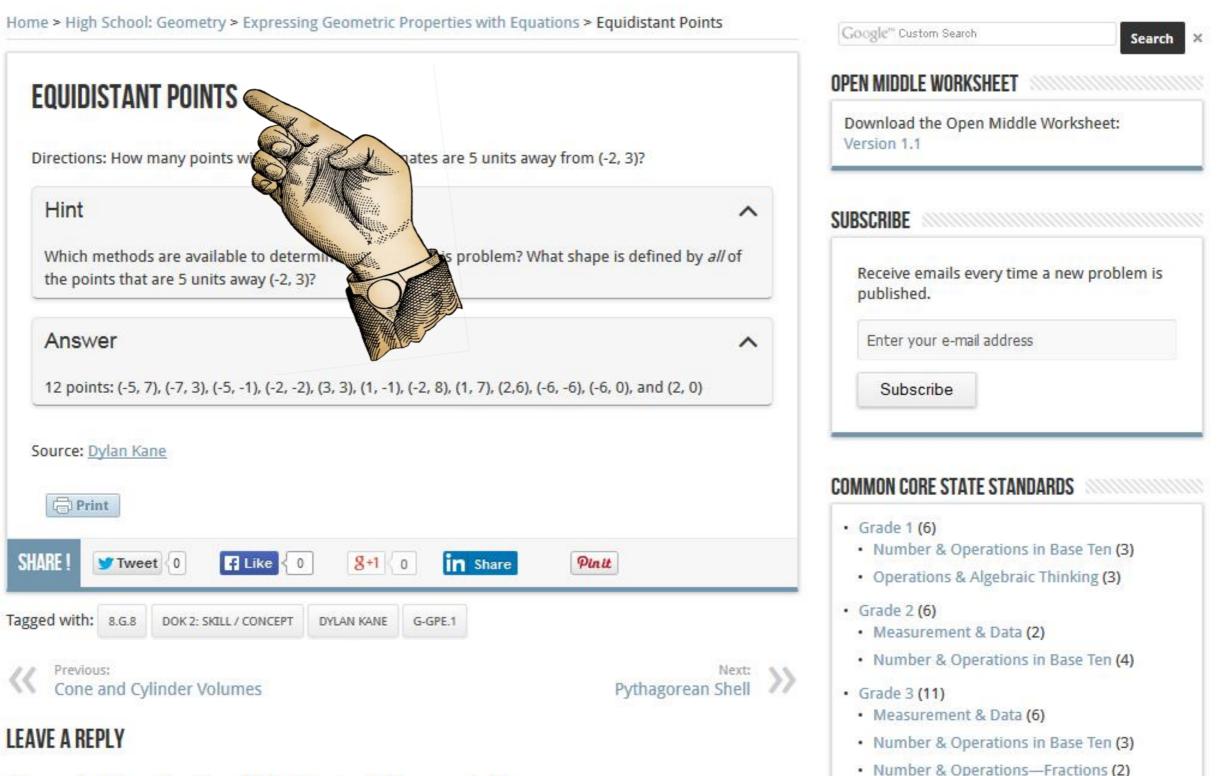


Number & Operations—Fractions (2)

Directions: In a standard game of BINGO, the cards are labeled with numbers 1 through 75. If it was possible, which card would you choose: a card with all of the same number or a standard bingo card? Source: Nanette

### Open Middle Challenging math problems worth solving

Home	Kinder 🔻	Grade 1 🝷	Grade 2 🔻	Grade 3 🔻	Grade 4 🔻	Grade 5 🔻	Grade 6 🔻	Grade 7 🔻	Grade 8 🔻	High School 🔻	About	Submit	
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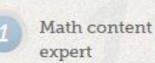


### **Problem-Based Lesson Resources**

- Problem-based lesson search engine: <u>http://robertkaplinsky.com/prbl-search-engine/</u>
- My lessons: <a href="http://www.robertkaplinsky.com/lessons">http://www.robertkaplinsky.com/lessons</a>
- Dan Meyer: <u>http://threeacts.mrmeyer.com</u>
- Andrew Stadel: <u>http://tinyurl.com/mrstadel</u>
- Geoff Krall: <u>http://tinyurl.com/PrBLmaps</u>
- Dan Meyer's TED talk: <u>http://tinyurl.com/meyer-TED</u>



#### Why Choose Us?



Robert graduated from University of California, Los Angeles (UCLA) with a Bachelors of Science in Mathematics. He has taught mathematics to students at the elementary, middle, and high school levels. As

#### Lessons









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All	2nd	3rd	4th	5th	6th	7th	8th	Algebra	Functions	Geometry	Modeling	Numb & Quant	Stats & Prob	
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How Much Is One Third Of A Cup Of Butter?



How Do Skytypers Write Messages?





#### Robert Kaplinsky's Problem-Based Lessons ☆ 🖿

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	A	В	С	D	Е	F	
1	Task Name	Concept / Skill	Standard 1	Standard 2	Standard 3	Standard 4	Sta
2	How Can We Water All Of The Grass?	Circles, Pythagorean Theorem, trigonometric ratios	7.G.4	8.G.7	G-SRT.8	G-MG.1	G-I
	How Much Money IS That?!	Volume of rectangular prism	5.MD.3	5.MD.4	5.MD.5	5.MD.5b	5.N
	How Much Money Should Dr. Evil Demand?	Exponential Growth	N-RN.2	A-SSE.1	A-SSE.3c	A-SSE.4	A-F
	How Tall Is Mini-Me?	Scale and Dividing Decimals	5.NF.5	5.NF.5a	5.NF.5b	6.NS.3	
	How Did They Make Ms. Pac-Man?	Transformations (Rotations, Reflections, and Translations)	8.G.1	8.G.2	8.G.3	8.G.4	G-5
	Which Ticket Option Is The Best Deal?	Unit Rates and Ratios	6.RP.2	6.RP.3	6.RP.3a	6.RP.3b	
	How Far Apart Are The Freeway Exits?	Fractions on a Number Line and Subtracting Fractions	3.NF.2	3.NF.2b	4.NF.2	4.NF.3a	4.N
	Do We Have Enough Paint?	Area	3.MD.5	3.MD.6	3.MD.7		_
	How Many Stars Are There In The Universe?	Scientific Notation	8.EE.3	8.EE.4			
11	What Rides Can You Go On?	Inequalities and Measurement	2.MD.1	6.NS.7a	6.NS.7b		
	Do You Have Enough Money?	Money	2.MD.8				
13	Which Bed Bath & Beyond Coupon Should You Use?	Percent Discount	7.RP.3				
14	Is Gas Cheaper With Cash Or Credit Card?	Percent Discount	7.RP.3				
15	Where's The Nearest Toys R Us?	Pythagorean Theorem (Distance in coordinate system)	8.G.8	G-SRT.8	G-GPE.7		
16	How Sharp Is The iPhone 5's Retina Display?	Pythagorean Theorem (Length of a side)	8.G.7	G-SRT.8	G-GPE.7		
17	When Should She Take Her Medicine?	Operations with Time Intervals	4.MD.2				
18	How Big Are Sunspots?	Converting Units, Proportions, and Scientific Notation	5.MD.1	7.RP.2	7.G.4	8.EE.4	G-I
19	What Michael's Coupon Should I Use?	Percent Discount	7.RP.3	A-CED.3			
20	Is It Cheaper To Pay Monthly or Annually?	Decimal Operations and/or Systems of Equations	5.NBT.7	8.EE.8c	A-CED.3	A-REI.11	F-E
21	How Big Is The 2010 Guatemalan Sinkhole?	Volume of Cylinder	5.MD.3	5.MD.4	5.MD.5	8.G.9	G-(
22	How Can You Win Every Prize At Chuck E. Cheese's?	Decomposing Numbers and/or Systems of Equations	2.NBT.7	3.NBT.2	3.NBT.3	8.EE.8c	A-C
23	How Many Royal Flushes Will You Get?	Probability	7.SP.5	7.SP.6	7.SP.7	S-MD.5	S-N
24	How Much Does The Paint On A Space Shuttle Weigh?	Surface Area	6.G.4	7.G.6	8.G.7	G-MG.1	G-I
25	How Did Motel 6 Go From \$6 to \$66?	Percent Increase and Compound Interest	7.RP.3	A-SSE.1b	F-BF.1	F-IF.8b	F-L
26	How Much Does The Aluminum Foil Prank Cost?	Surface Area and Unit Rates	6.G.4	6.RP.2	6.RP.3	7.G.6	
27	How Many Laps Is A 5k Race?	Perimeter	4.MD.3				
28	Which Toilet Uses Less Water?	Systems of Equations/Inequalities	8.EE.8c	A-CED.3	A-REI.11	F-BF.1	
29	How Did Someone Get A \$103,000 Speeding Ticket In Finland?	Linear Equations	A-CED.2	F-BF.1	F-IF.4	F-IF.6	
30	Which Pizza Is A Better Deal?	Area or Circle, Square, and Unit Rates	3.MD.5	3.MD.6	3.MD.7	4.MD.3	6.F
31	How Big Is The World's Largest Deliverable Pizza?	Area of Square	3.MD.5	3.MD.6	3.MD.7	4.NBT.3	4.N
32	How Many Sheets Do You Need To Break Out Of Prison?	Integer Operations	5.NBT.6				
33	Do Hybrid Cars Pay For Themselves?	Systems of Equations or Rates	6.RP.2	6.RP.3	8.EE.8c	A-CED.3	F-E
34	How Many Hot Dogs Did They Eat?!	Linear and Quadratic Functions	8.F.3	8.F.4	F-BF.1	F-BF.2	F-II
35	How Much Purple Ribbon Will You Need?	Perimeter & Circumference	3.MD.8	4.MD.3	7.G.4		
36	Are We There Yet?	Adding Times	3.MD.1	4.MD.2			
37	Which Chinese Food Coupon Should I Use?	Percent Discount	7.RP.3				
38	How Big Is The Vehicle That Uses Those Tires?	Ratio and Proportions	7.RP.2				
39	Where Would The Angry Birds Have Landed?	Create Equation From Quadratic Graph	A-CED.1	F-BF.1	F-IF.4	F-IF.7a	F-L
40	How Many Movies Can You See In One Day?	Adding Times	3.MD.1	4.MD.2			
41	Which Carrots Should You Buy?	Unit Rates	6.RP.1	6.RP.2	6.RP.3		
42	How Fast Can You Throw A Baseball?	Converting Units and Unit Rates	5.MD.1	6.RP.2			

Go	ogle	
 Google Search	I'm Feeling Lucky	

#### Problem-Based Lesson Search Engine

This search engine searches all of the sites below to quickly help you find a problem-based lesson (also called 3-Act Task, mathematical modeling, or application problem):

Submit

The links below are the pages that are being searched by the search engine:

- 101 Questions
- Andrew Stadel
- Dan Meyer
- Dane Ehlert
- Emergent Math's Problem Based Curriculum Maps
- Estimation180
- Geoff Krall

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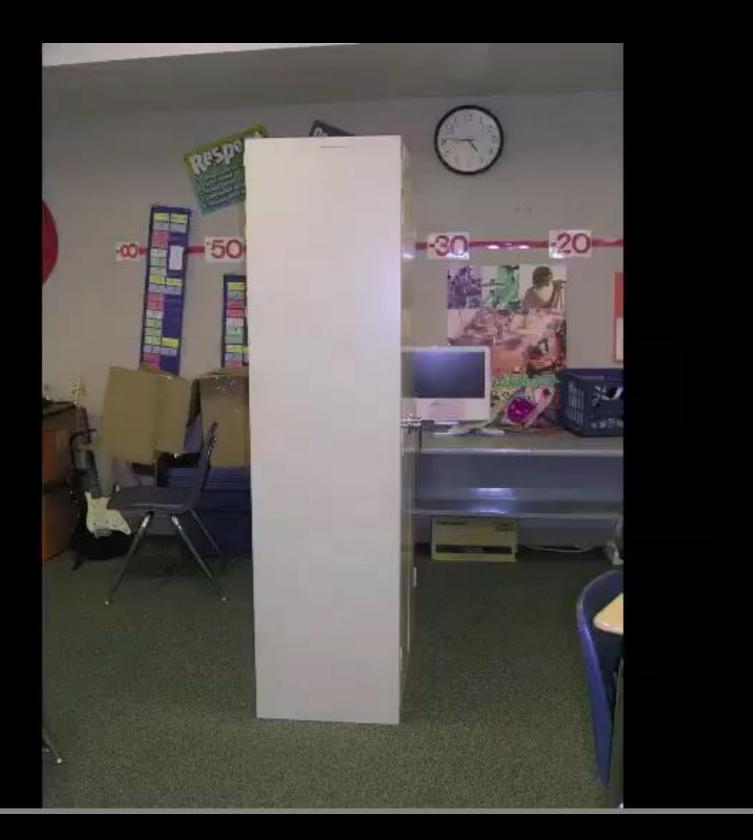
Problem Based Curriculum Maps



# Wentzville School District

**ROBERT KAPLINSKY** 





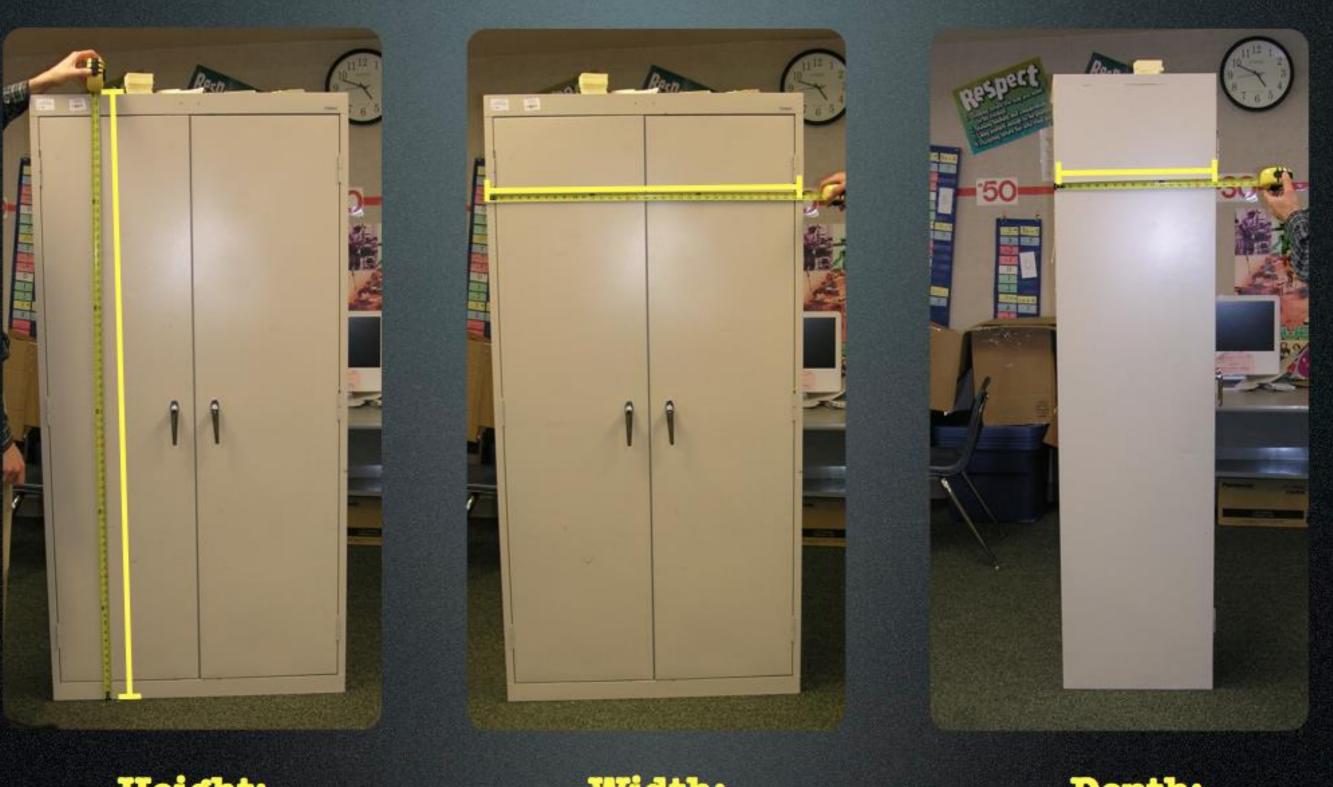


#### Height: 72 inches



#### Height: 72 inches

Width: 36 inches



#### Height: 72 inches

Width: 36 inches Depth: 18 inches

#### Sticky note

Recycled Self Stick Notes Notas autoadhesivas reciclados Notes autocollantes recyclés

- 18 pads / blocs
- 100 sheets per pad / hojas por bloc / f
  Total 1800 sheets / hojas / feuillets
- · 3 in x 3 in (76,2 mm x 76,2 mm)

#### **Dimensions:** 3" x 3"



### PERFORMANCE TASK

#### **CEREAL BOXES**

A cereal company uses cereal boxes that are rectangular prisms The boxes have the dimensions shown.

- 12 inches high
- 8 inches wide
- 2 inches deep

The managers of the company want a new size for their cereal boxes. The new boxes have to be rectangular prisms. You will evaluate one box design the company proposed. Then you will create and propose your own design for the company.

Requirements for the new boxes:

• The new boxes have to use less cardboard than the

		•
+ •	•	

1

2



Determine the volume of the current cereal box with the dimensions 12 inches high, 8 inches wide, and 2 inches deep.

Find the volume, V, in cubic inches, of each box.

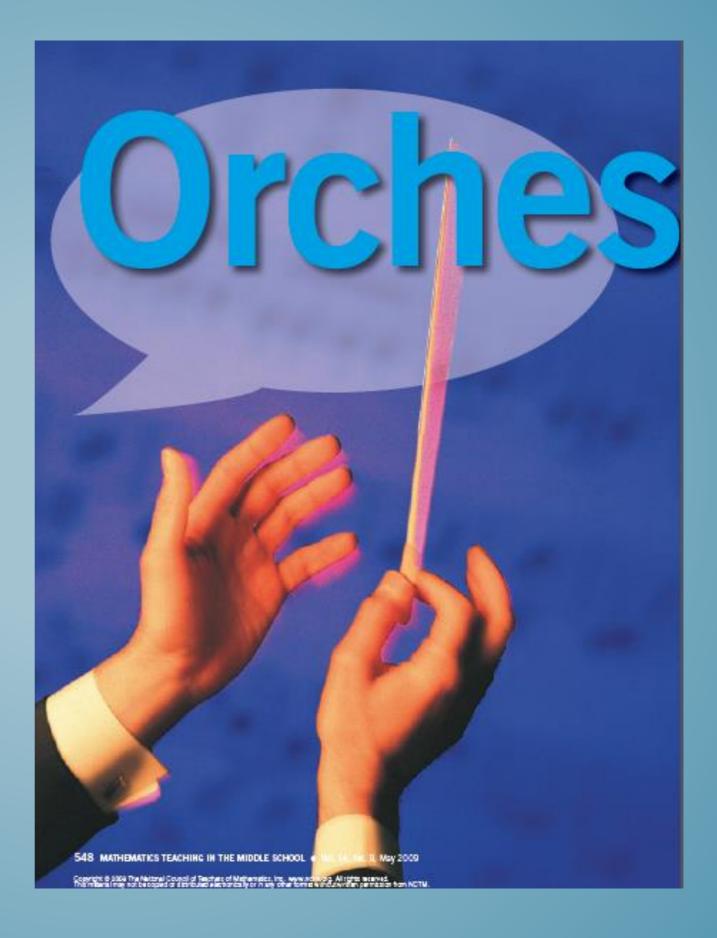
Volume of Original Box:  $V = \_$  in<sup>3</sup>

123
4 5 6
789
0

Label the dimensions of the net for the current cereal box with dimensions 12 inches high, 8 inches wide, and 2 inches deep.

12 in	🖲 Delete	×

### **FIVE PRACTICES**



# Discussion Questions

- "Giving students too much or too little support, or too much direction, can result in a decline in the cognitive demands of the task." (p. 550) Why?
- "By making purposeful choices about the order in which students' work is shared, teachers can maximize the chances that their mathematical goals for the discussion will be achieved." (p. 554) What ways do teachers currently select students? How would you suggest they change their selection process after reading this?
- What challenges might teachers have when trying to "connect" student solutions? (p. 554)

## Implementing the Five Practices

- Anticipate potential student responses to the file cabinet problem.
- 2. Review the ten student work samples that represent students in your classroom.
- 3. Figure out which students you would have share their mathematical work.
- 4. Determine the order you would have those students present their work.
- 5. Decide on which connections you would emphasize between the students' work and mathematical ideas.

# Posters

- At the top of the poster, list the selection strategy used by your group. For example:
  - Starting with the most commonly used strategy and moving to one that few students used.
  - Starting with a strategy that is more concrete and moving to strategies that are more abstract.
  - Incorporating wrong answers to address common misconceptions.
- Attach those students' work to the poster in the order that you would present it.
- Next to the student work list the questions you would ask the student(s) or ideas that you would want to come out as a result of showing that student's work.



struggle: none feedback: none reward: none

### struggle: low feedback: low reward: high

struggle: medium feedback: high reward: medium

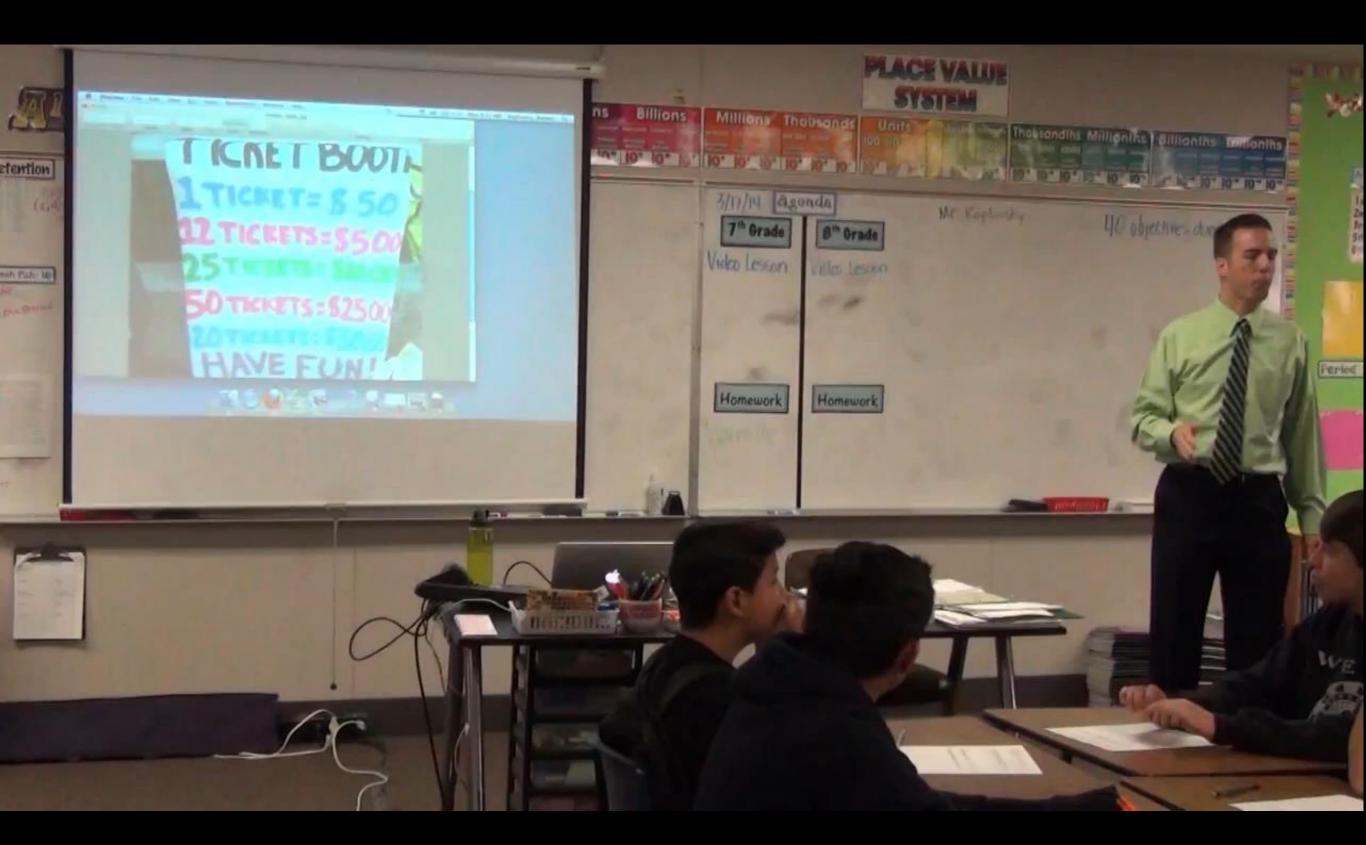
struggle: high feedback: high reward: high Gods Engaging problem solving Real world problem-based learning Higher depth of knowledge problems Better implementation Improve our ability to ask questions Practice preparing to implement a lesson Figure out how to deal with uncomfortable situations

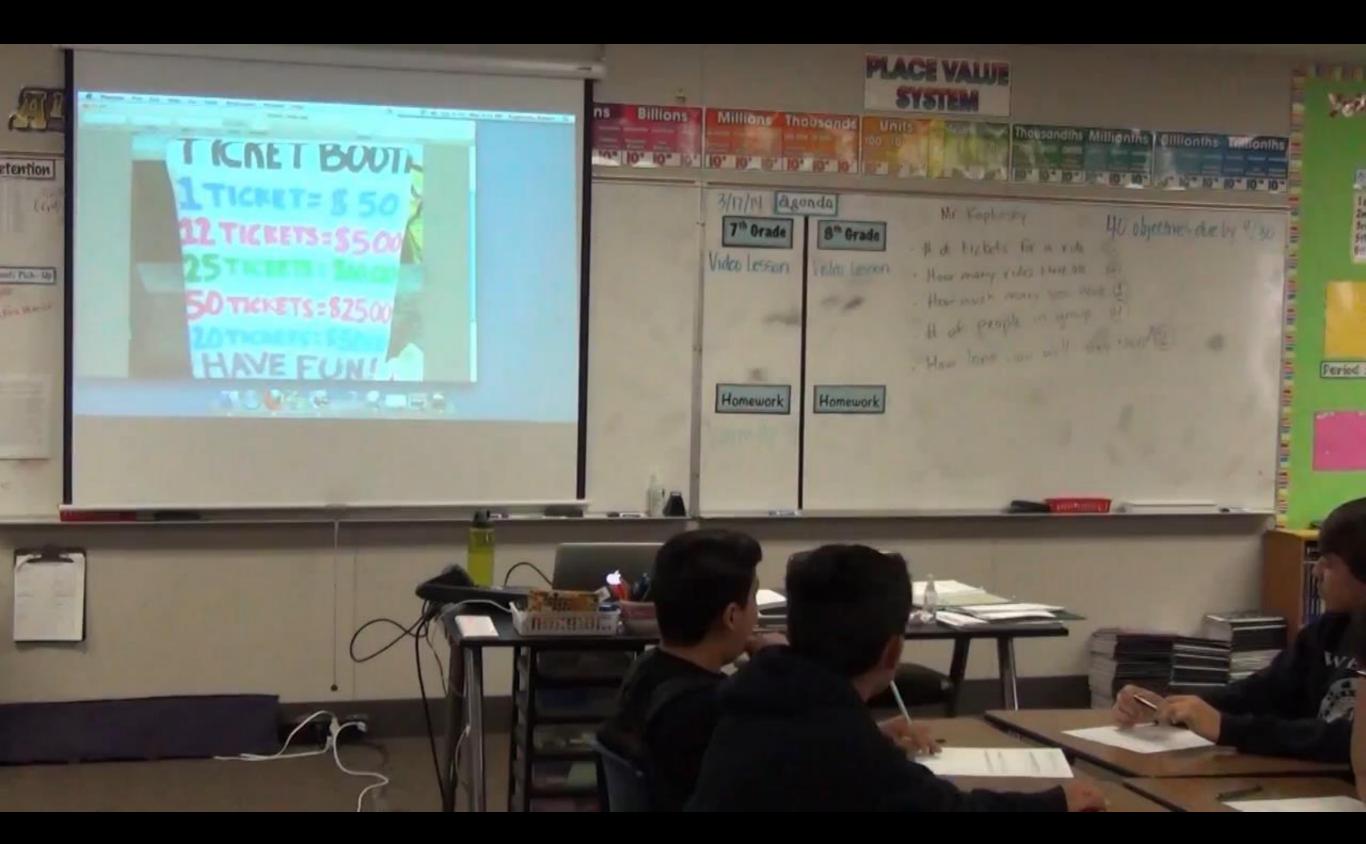


# Setting Up The Problem

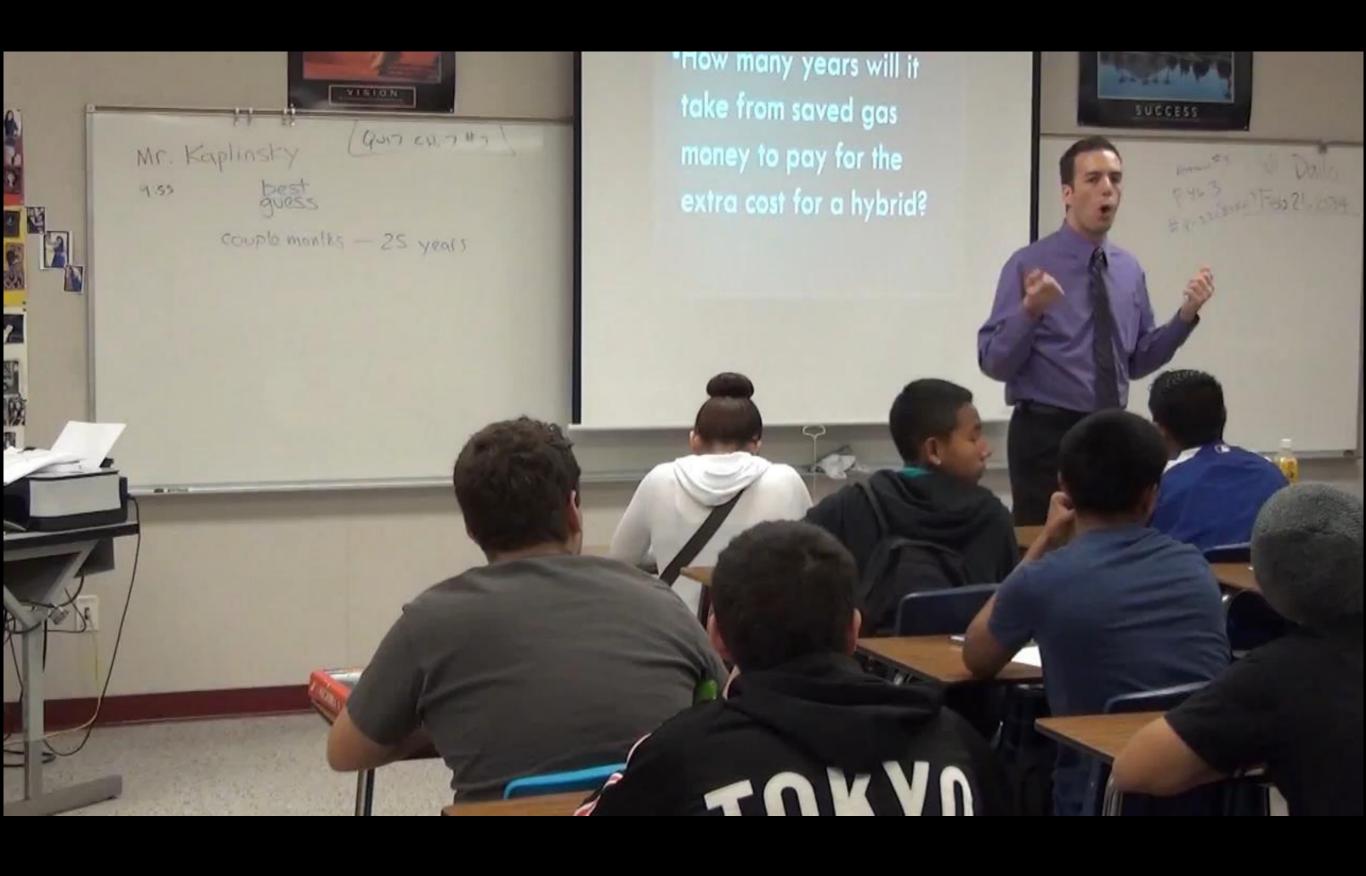
- What do you do when students ask for data/information I don't have, hadn't considered, or forgot to get?
- What do you do when students ask for information that is probably not important or that they don't actually need?

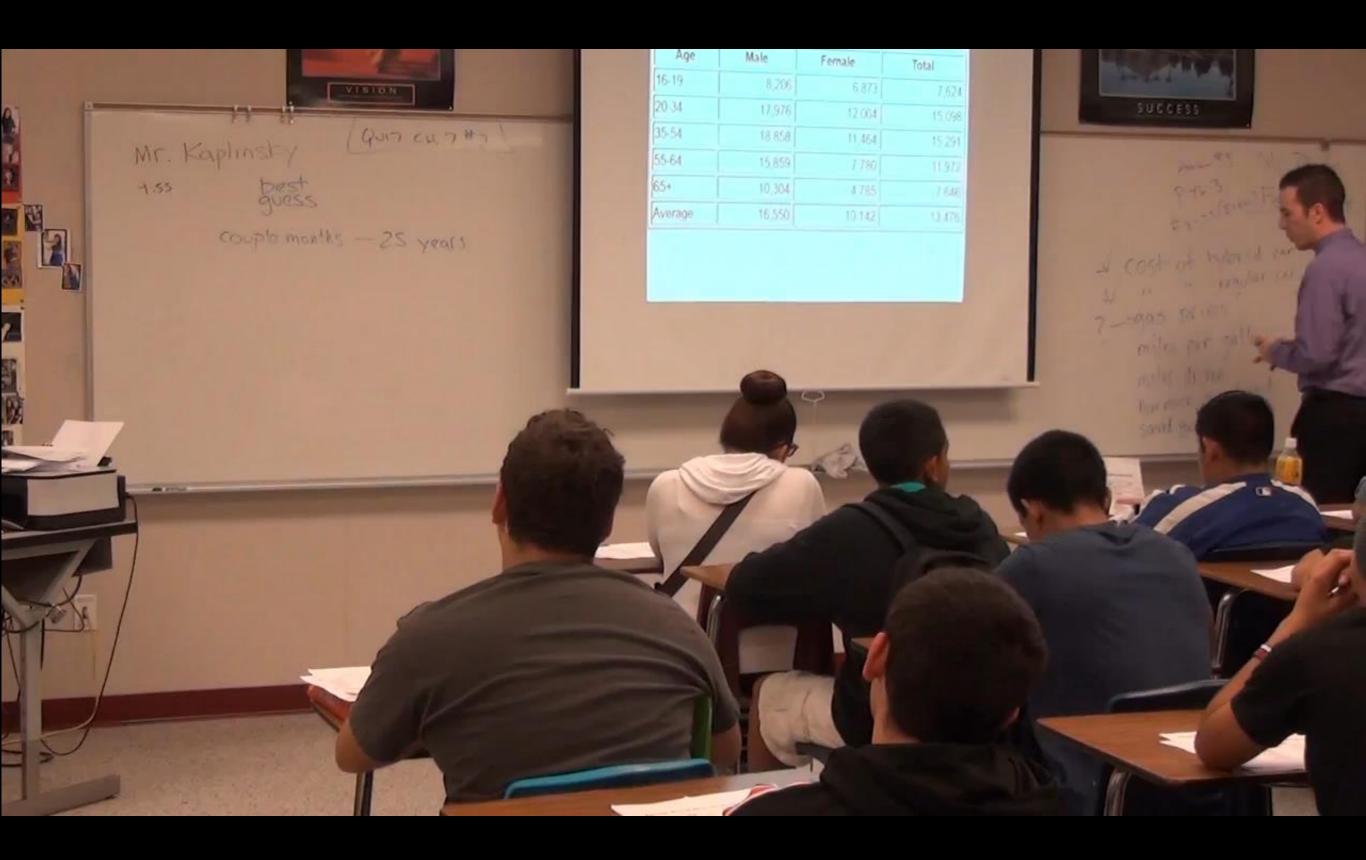




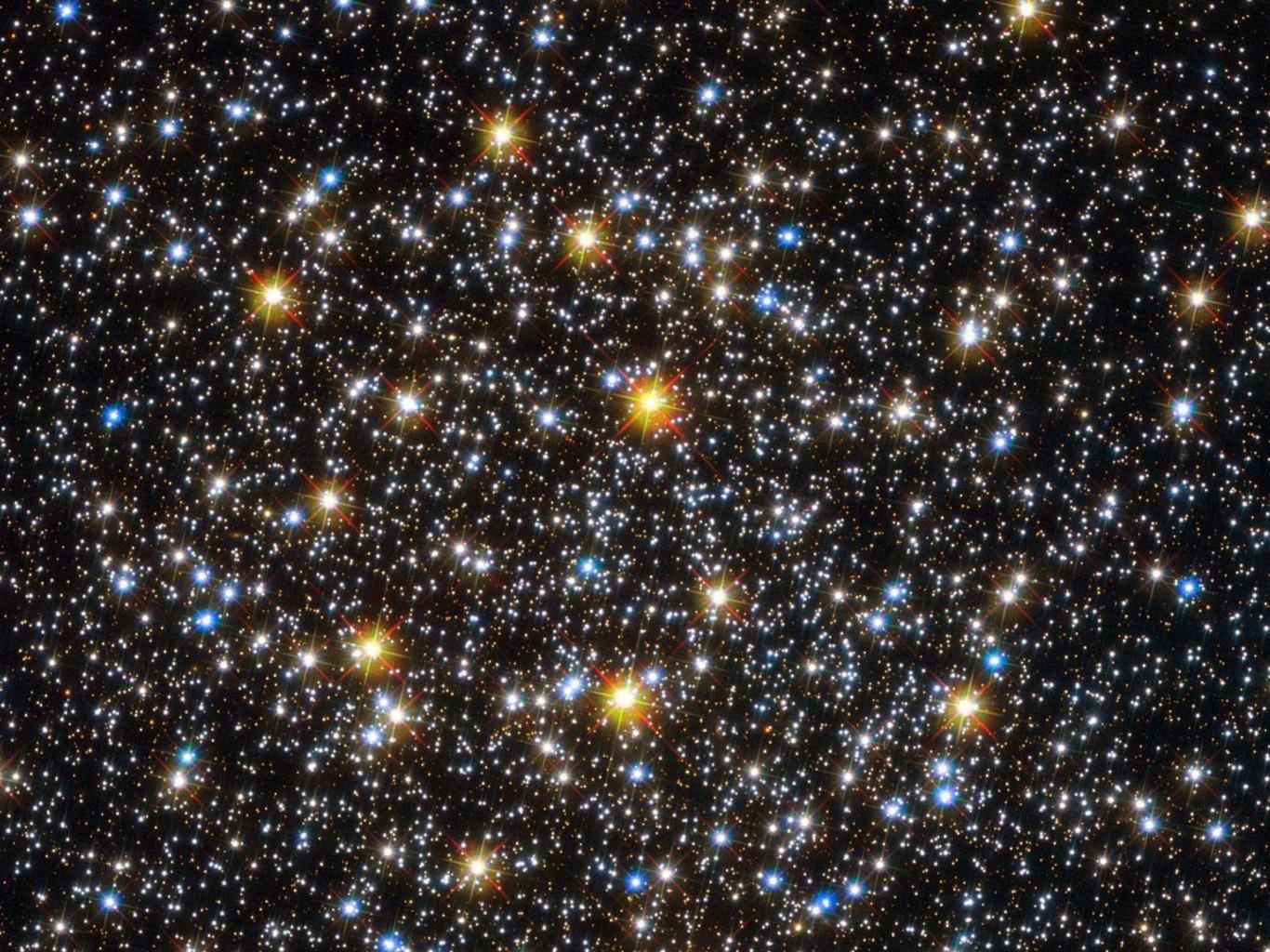


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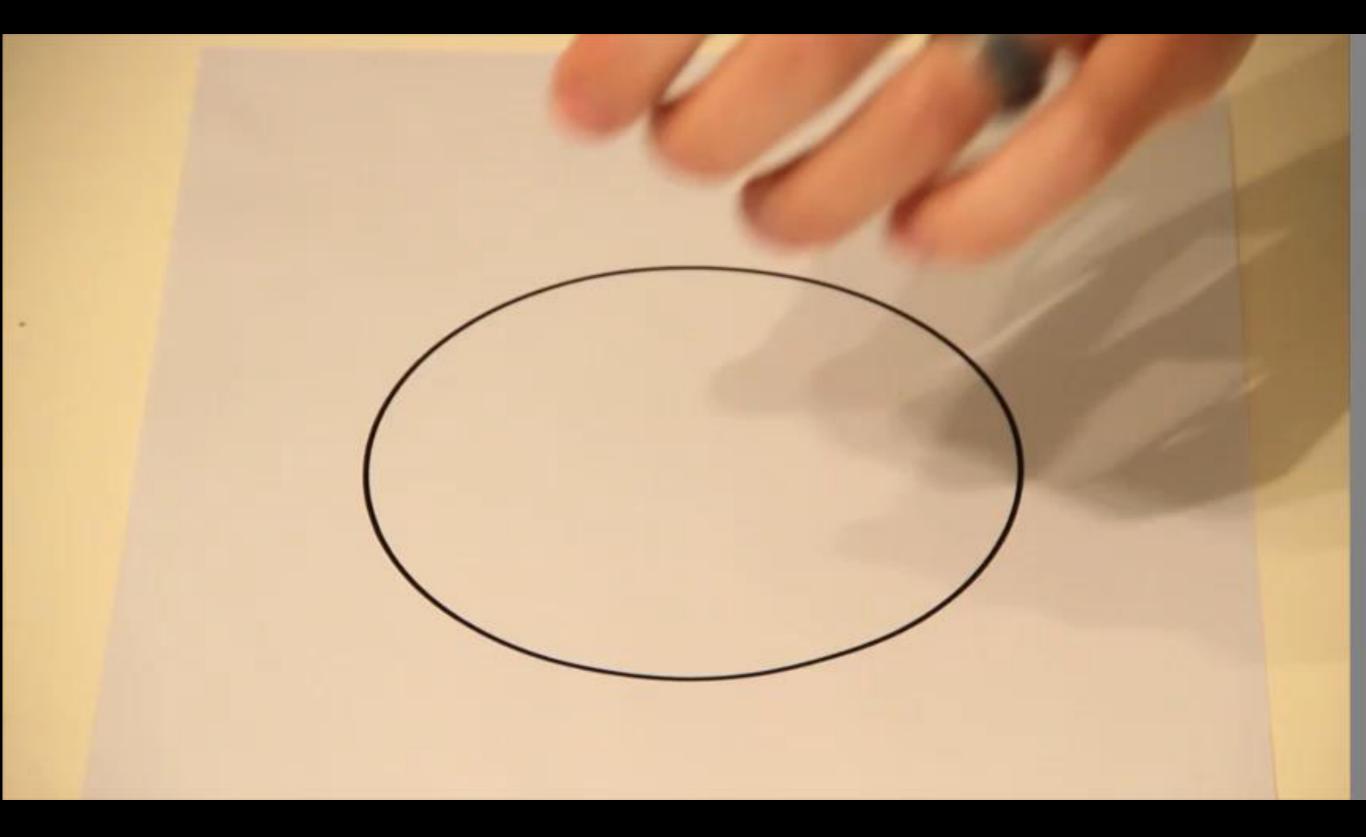






# Setting Up The Problem

- What do you do when students ask for data/information I don't have, hadn't considered, or forgot to get?
- What do you do when students ask for information that is probably not important or that they don't actually need?
- What do you do when students don't know what to write for what they know and don't know?
- What do you do when you ask for a guess and they don't know?
- What do you do when they don't ask you for information that they need to solve the problem?



 What do you do when students don't use the strategy you anticipated they would use?





#### American Standard

#### Clean™ Cadet® 3

Elongated

18.5 in

Overall dimensions: 15 in W x 31 in H x 29-3/4 in D Rough-in dimensions: 12 in Trapway size: 2 in

Dimensiones generales: 38,10 cm de ancho x 78,74 cm de alto x 75,57 cm de profundidad Dimensiones aproximadas: 30,48 cm Tamaño de canal de siñón: 5,08 cm



Item | Artículo: 84065 Model | Modelo: 3381.216.020

> Reorder # P117364

High-efficiency, dual flush toilet—1.6 gal. or 1.0 gal. flush
 Stays cleaner longer with EverClean<sup>®</sup> surface & PowerWash<sup>™</sup> flush
 Features No Tools<sup>™</sup> installation
 ADA approved chair height

Inodoro de descarga doble de alta eficiencia con descarga de 6.06 litros o 3.79 litros
 Permanece limpio por más tiempo con la superficie EverClean® y la descarga PowerWash™
 Cuenta con instalación No Tools™
 Altura de silla aprobada por ADA



American Standard

#### Clean™ Cadet® 3

Overall dimensions: 15-3/4 in W x 30-3/4 in H x 30-1/4 in D Rough-in dimensions: 12 in Trapway size: 2-1/16 in

Dimensiones generales: 40,01 cm de ancho x 78,11 cm de alto x 76,84 cm de profundidad Dimensiones aproximadas: 30,48 cm Tamaño de canal de siñon: 5,24 cm



Item | Artículo: 88575 Model | Modelo: 2514.101.020

Smooth-sided toilet design
 Stays cleaner longer with EverClean<sup>®</sup> surface & PowerWash™ flush
 Features No Tools™ installation
 ADA approved chair height

Diseño de inodoro de lados lisos
 Permanece âmpio por más tiempo con la superficie EverClean® y la descarga PowerWash™
 Cuenta con instateción No Tools™
 Altura de silla aprobada por ADA



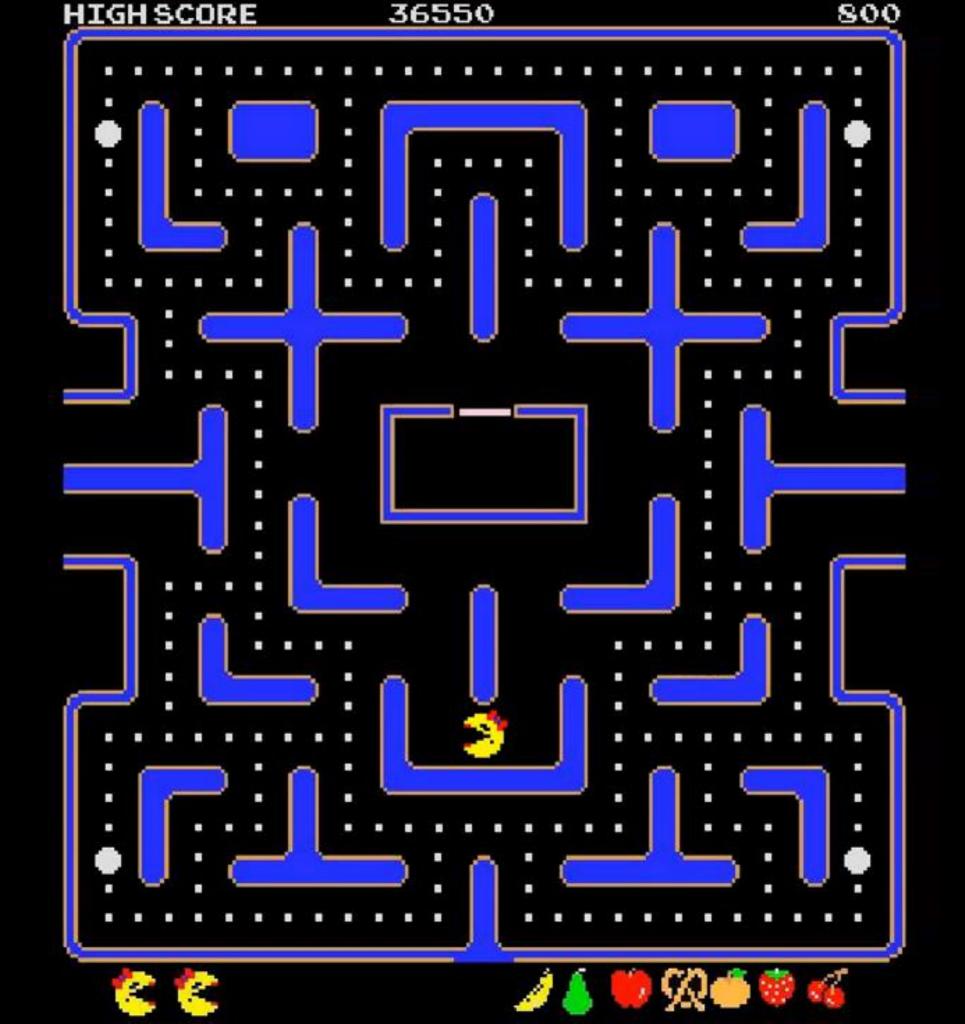
Year

**Limited Warranty** 



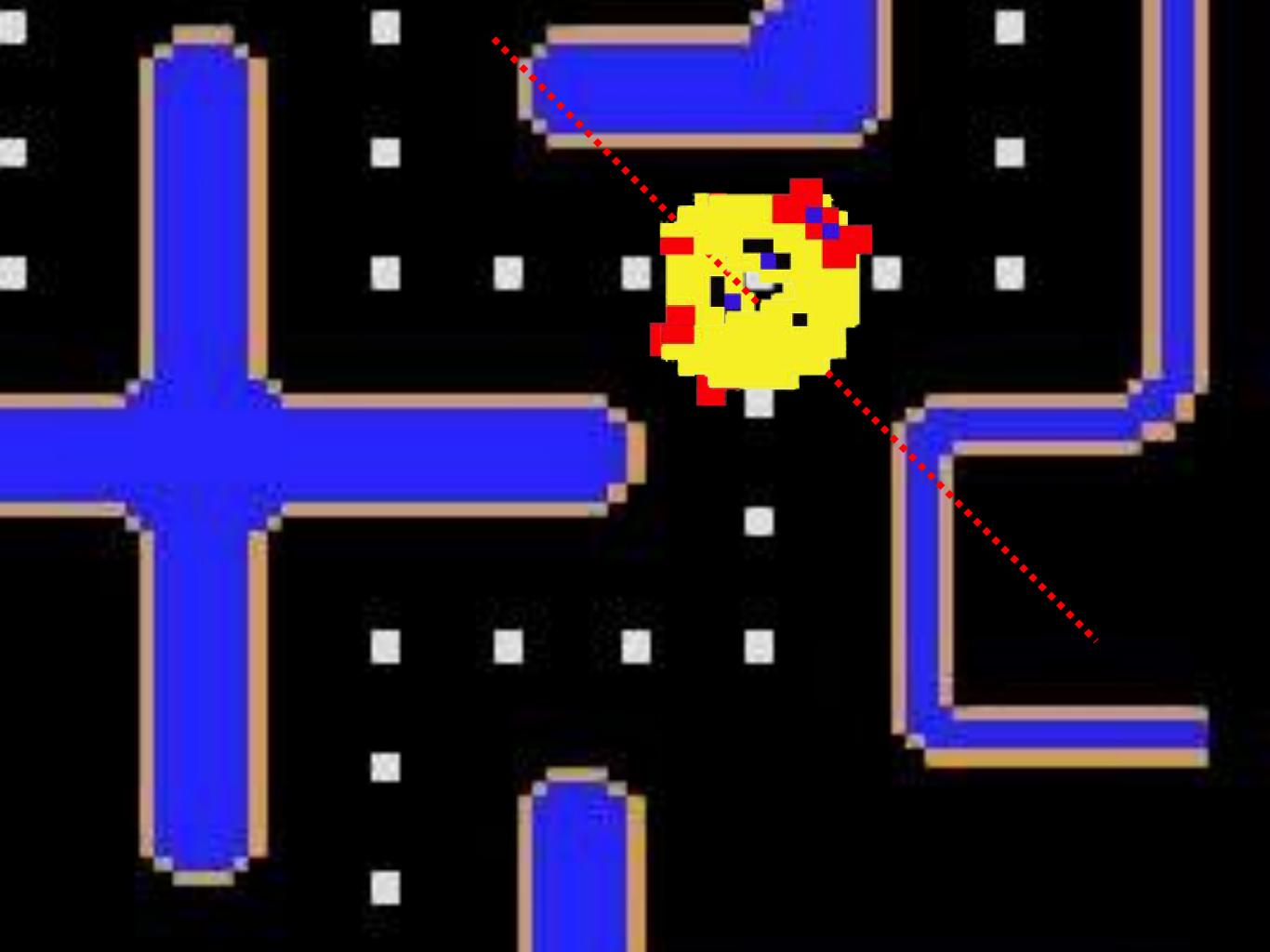


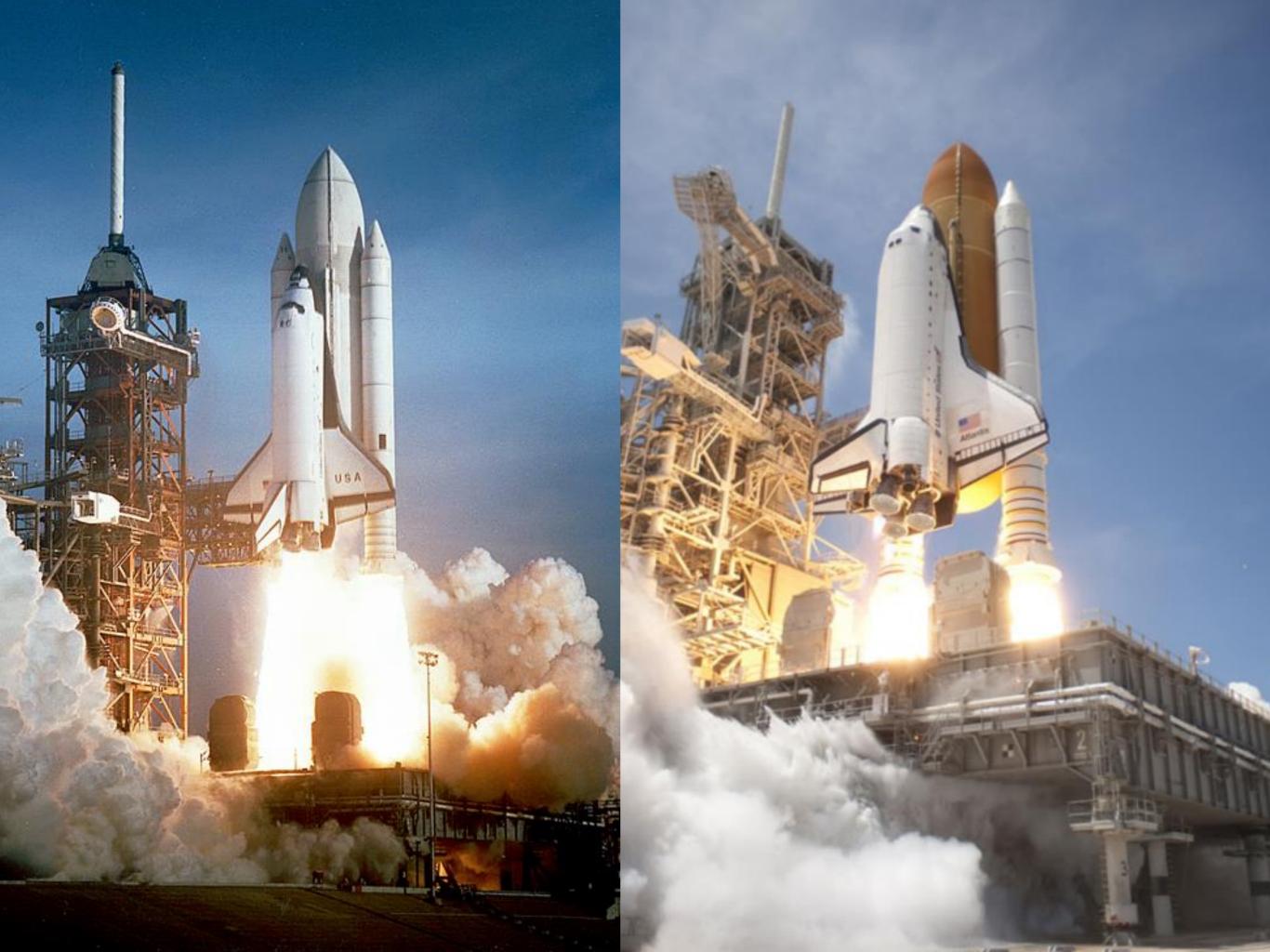
- What do you do when students don't use the strategy you anticipated they would use?
- What do you do when a student comes up with a strategy for solving the problem that I do not understand?







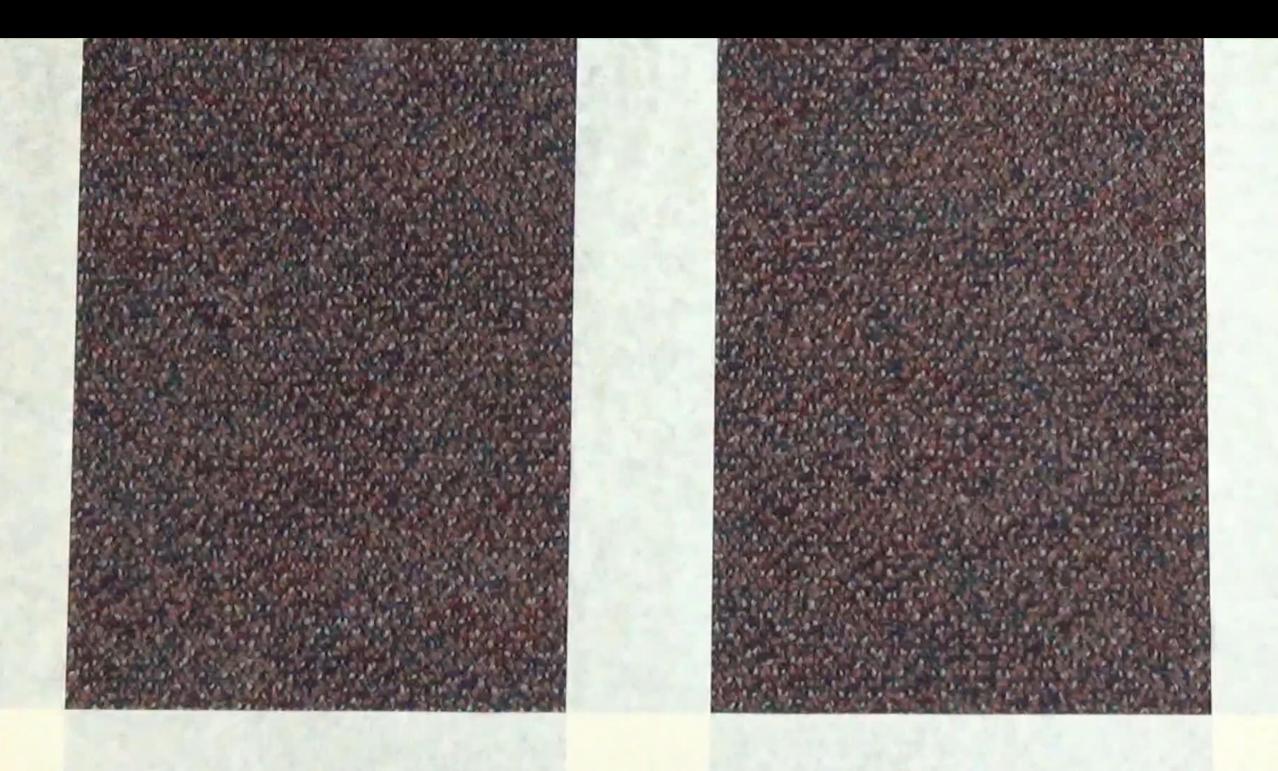




- What do you do when students don't use the strategy you anticipated they would use?
- What do you do when a student comes up with a strategy for solving the problem that I do not understand?
- What do you do when the answer we calculate does not match with the actual answer?
- What do you do when students get stuck during the problem solving process and are not sure what to do?

#### **NON-STAGGERED**

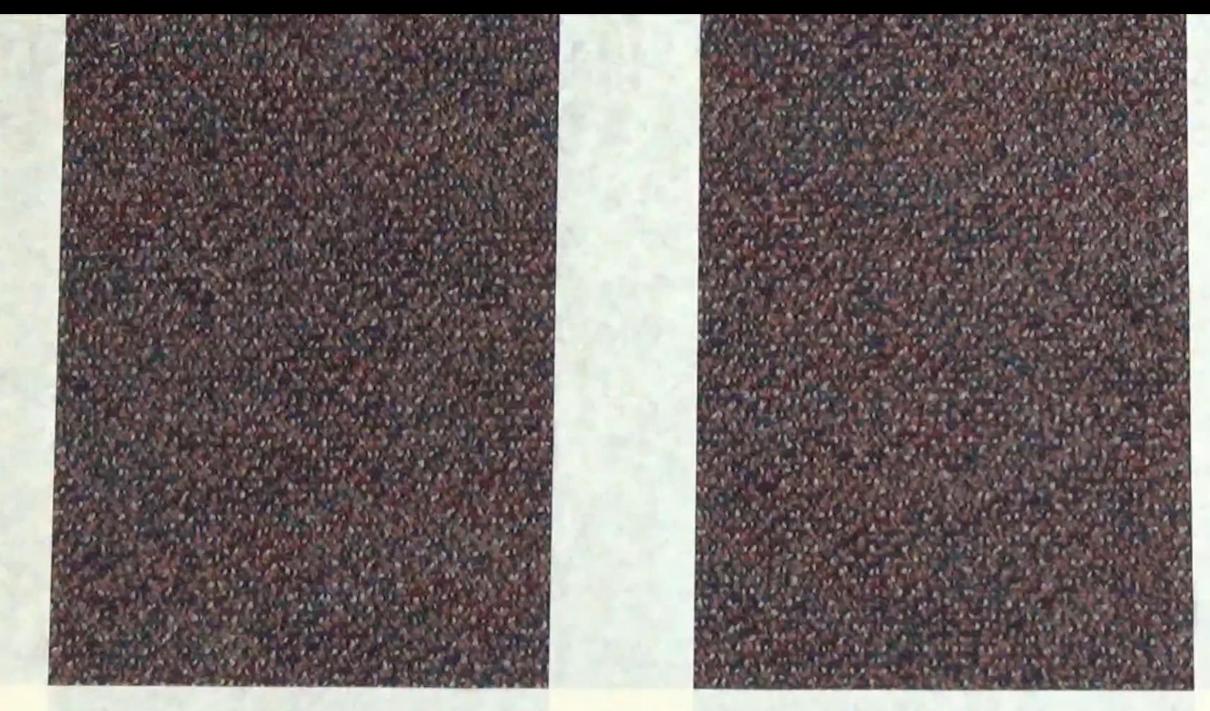




How much shorter are 20 layers of staggered pipe stacks?







#### Layers: 0



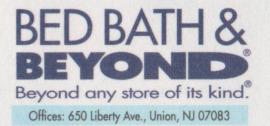


- What do you do when students don't use the strategy you anticipated they would use?
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- What do you do when students don't use the strategy you anticipated they would use?
- What do you do when a student comes up with a strategy for solving the problem that I do not understand?
- What do you do when the answer we calculate does not match with the actual answer?
- What do you do when students get stuck during the problem solving process and are not sure what to do?
- What do you do when you ask students questions and few to no people are ready to respond?
- What do you do when the student conclusions are low quality and/or effort?

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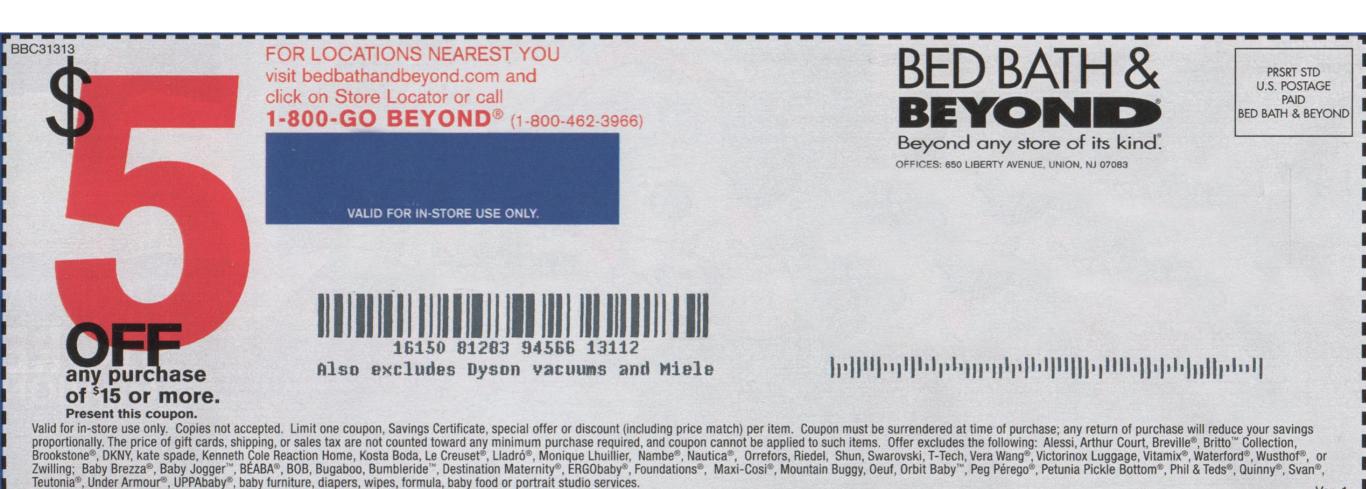
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73283 94566 13028 Also excludes Starbucks Also excludes Dyson vacuums and Miele

Present this coupon.

Valid for in-store use only. Copies not accepted. Limit one coupon, Savings Certificate, special offer or discount (including price match) per item. Coupon must be surrendered at time of purchase; any return of purchase will reduce your savings proportionally. The discount cannot be applied to gift cards, shipping, or sales tax. Offer excludes the following: Alessi, Arthur Court, Breville®, Britto<sup>™</sup> Collection, Brookstone®, DKNY, kate spade, Kenneth Cole Reaction Home, Kosta Boda, Le Creuset<sup>®</sup>, Lladró<sup>®</sup>, Monigue Lhuillier, Nambe<sup>®</sup>, Nautica<sup>®</sup>, Orrefors, Riedel, Shun, Starbucks<sup>®</sup> Electrics, Swarovski, T-Tech, Vera Wang<sup>®</sup>, Victorinox Luggage, Vitamix, Waterford<sup>®</sup>, Wusthof®, or Zwilling; Argington®, babybrezza™, Baby Jogger™, BÉABA®, BOB, Bugaboo, Bumbleride™, ERGObaby®, Foundations®, iCandy®, Maxi-Cosi®, Mountain Buggy, Oeuf, Orbit Baby™, Peg Pérego®, Phil & Teds®, Plan Toys®, Quinny®, Svan®, Teutonia®, Under Armour®, UPPAbaby®, baby furniture, diapers, wipes, formula, baby food or portrait studio services. G47QR-V2



# IA conclusion each conclusion Each Itemis good for different Items

What is your condusion? How ald you reach that conclusion?

in store purchase, exclusions What is your conclusion? How did you reach that conclusion? Ff the Item is \$15 use the \$5 off because 19-5=\$10 and IF the Ftem is 447 it is better to use the 20% offcoupon because U7 - 5 = 647 - 77 - 20% = 37.60 $y_{2vs} 37.60$ \$50ff 20%0ff 18 vs 18.40 23-5=(18) 23-20% =28.40

10	Orange Chicken	5.25	Eggplant with Garlic Sauce	5.25
	Chicken Lo Mein	5.25	Ma Po Tofu	5.25
	Cashew Nut Chicken	5.25	Broccoli with Garlic Sauce	5.25
	Pungent Chicken	5.25	String Bean with Garlic Sauce	5.25
	Sweet & Sour Chicken	5.25	Vegetable Delight	5.25
	Curry Chicken	5.25	Bamboo Fungus Tofu	5.25
	Lemon Chicken	5.25	Shrimp with Asparagus	6.25
	Vegetable Chicken	5.25	Shrimp with Lobster Sauce	6.25
	Mongolian Beef	5.25	Fish Fillet with Szuchuan Sauce	6.25
	Broccoli Beef	5.25	Fish Fillet with Black Bean Sauce	6.25
,	Pungent Beef	5.25	Crab meat with Asparagus	6.25
	Sweet & Sour Pork	5.25	Sweet & Sour Shrimp	6.25



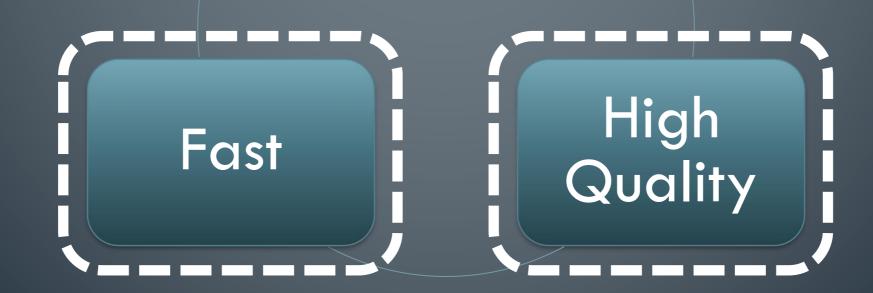
Free to an chiken lomein ifspended \$25 and not redeemake on lunch special dinnersand make party I tems Men 10 men, at is your conclusione how all you reach than conclus The 10% carpon is Best with high Prices and small orders is best with the free chicken lamein out chesse wor

What is your conclusion? How did you reach that conclusion? \$200 can use the 10% off when you pay 20-2499 or more the Free chicken to Mein when you pay 35-49.99 or more and the Free orange Chiten when you pay 50 or more Gods Engaging problem solving Real world problem-based learning Higher depth of knowledge problems **Better** implementation Improve our ability to ask questions Practice preparing to implement a lesson Figure out how to deal with uncomfortable situations

# Construction



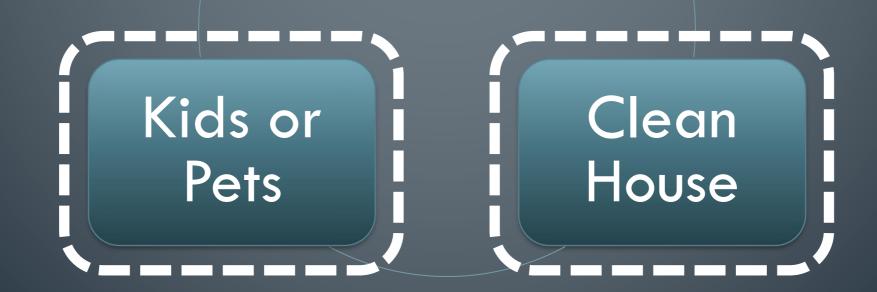












## Problem-Based Learning

