Bonita Unified School District

ROBERT KAPLINSKY



@robertkaplinsky

Goals

- Engaging problem solving
 - Real world problem-based learning
 - Higher depth of knowledge problems
- ☐ Better implementation
 - Improve our ability to ask questions
 - Practice preparing to implement a lesson
 - ☐ Figure out how to deal with uncomfortable situations









DOUBLE-DOUBLE Double Meat & 265 CHESEBURGER **1**50 HAMBURGER **FRENCH FRIES 1**05 **1**55 SHAKES Chocolate Strawberry

SM MEI 99 110		X-LG 149
COKE	Classic or Diet	
SEVEN- ROOT E		
DR PEF LEMON		
ICEDTE		



OPEN 10:30 a.m. to 1:00 a.m. Fri. and Sat. until 1:30 a.m.

YOUR GUEST NUMBER IS

IN-N-OUT BURGER LAS VEGAS EASTERN 2004-10-31 165 1 5 98 8:21 PM

Cashier: SAM

GUEST #: 98

Counter-Eat In

98 Meat Pty XChz 2.65 88.20

Counter-Eat In 90.85
Amount Due 97.66

CASH TENDER
Change \$97.66

2004-10-31

Cashier: SAM

GUEST #: 98

Counter-Eat In

98 Meat Pty XChz

88.20

Counter-Eat In TAX 7.50% Amount Due

90.85

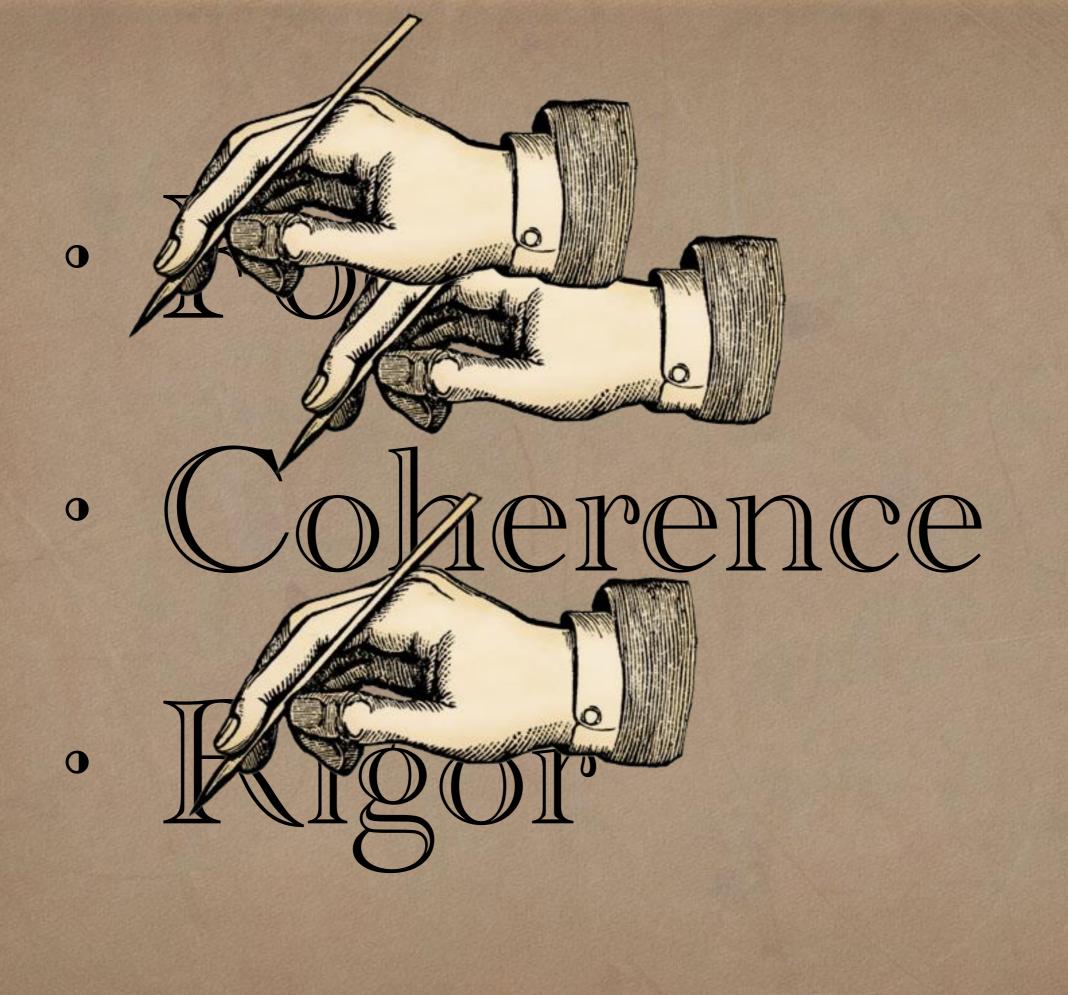
CASH TENDER

\$97.66

2004-10-31

8:21 PM

	Serving Size (g)	Calories
Hamburger w/Onion	243	390
Cheeseburger w/Onion	268	480
Double-Double w/Onion	330	670



Layers	Cost
1	\$1.75
2	\$2.65
3	\$3.55
4	\$4.45
•	•
•	•
20	\$18.85
•	•
•	•
100	\$90.85
•	•
N	\$1.75 + (N-1)*\$0.90

bun + produce + meat + cheese + meat + cheese = \$2.65

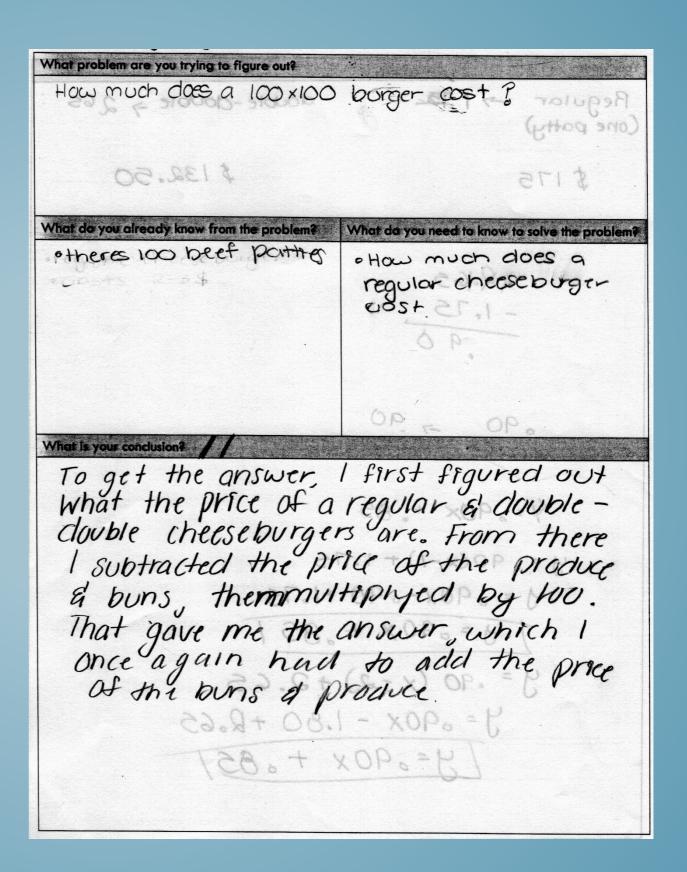
bun + produce + meat + cheese = \$1.75

meat + cheese = \$0.90

The Reality

- Students needed guidance to figure out a layer's cost
- Not every class is ready to go straight to 100x100
- Common wrong answers included:
 - \$175.00 (\$1.75 x 100 cheeseburgers)
 - \$132.50 (\$2.65 x 50 Double-Doubles)
- Students had equations that had more than X patties
- Students were surprised to see three different equations:
 - Starting with a Double-Double
 - Starting with a cheeseburger
 - Starting with produce and bun only

STUDENT WORK



What is your conclusion?

The only difference between a double double and a choeseburger is one patty and one slice of cheese. So you subtract the prices of the two to find the price of only one postty & cheese. You then use that number (.90) & subtract it from the price of all the extra stuff. Multiply by 100

What is your conclusion?

A 100×100 at In-h-out cost \$90.85. To solve that, you start by subtracting the price of a cheese burger from a double double. The answer (.90) is the price of a patty and cheese slice. You multiply (.90) by one less patty than what you want. (x-1), and you add the price of a cheese burger (1.75). You end up with the eq. [y=.90(x-1)+1.75.]. You end up with the eq. [y=.90(x-1)+1.75.]. For the $100\times(00$, you plug in 100 to the (x) and you end up with \$90.85.

2.40 And I Ch I burn

3 355 checke

vith \$90.85.

$$y = .90(100-1) + 1.75$$

 $y = 89.10 + 1.75$
 $y = 90.85$



What is your conclusion?

Figure the price difference from the Double-Double with a cheese burger. Then find out the prize for the produce and cheese-beef.

9et total into \$ 90.85





<u>WHO</u> THINK

THEY HAVE THEIR CHILD IN THE RIGHT SEAT.



KNOW FOR SURE

IF YOUR CHILD IS IN THE RIGHT CAR SEAT.

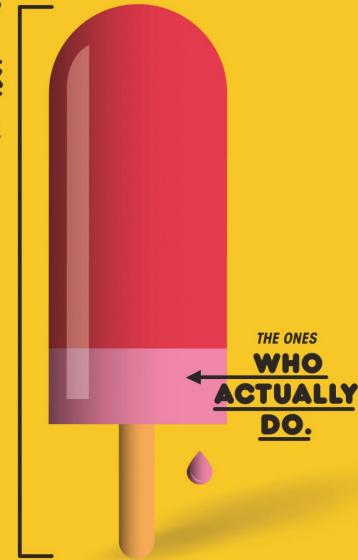








THINK
THEY HAVE
THEIR CHILD
IN THE RIGHT
SEAT.



KNOW FOR SURE

IF YOUR CHILD IS IN THE RIGHT CAR SEAT.

VISIT SAFERCAR.GOV/THERIGHTSEAT







There are 125 sheep and 5 dogs in a flock. How old is the shepherd?

Of the 32 students I interviewed...

- 75% of them gave me numerical responses
- 2 students calculated the answer to be 130 (125 + 5)
- 2 students calculated the answer to be 120 (125 5)
- 12 students calculated the answer to be 25 (125 \div 5)
- 0 students calculated the answer to be 625 (125 x 5)
- 4 students stated that they guessed their answer (90, 5, 42, and 50)
- 4 students tried to divide 125 by 5 but could not correctly implement the procedure

Takeaways

- Making sense of mathematics
- Intellectual autonomy
 - •Intellectual autonomy is about being able to think for yourself and not being dependent on others for the direction and control of one's thinking.

What Does the NHTSA Say?

Key Statistics and Consumer Insights:

Motor vehicle crashes are the leading cause of death for children age 1 through 12 years old.¹

According to a NHTSA study, 3 out of 4 kids are not as secure in the car as they should be because their car seats are not being used correctly.

be reduced by about half if the correct child safety seats were always used.

 $^{^1}$ Source: Based on the latest mortality data currently available from the CDC's National Center for Health Statistics.



- "because they have their child in the right seat"
- "because their car seats are not being used correctly"

IF YOUR CHILD IS IN THE RIGHT CAR SEAT.











WHO THINK

THEIR CAR SEATS ARE BEING USED CORRECTLY.



KNOW FOR SURE

IF YOUR CHILD IS IN THE RIGHT CAR SEAT.











KNOW FOR SURE

IF YOUR CHILD IS IN THE RIGHT CAR SEAT.

VISIT SAFERCAR.GOV/THERIGHTSEAT

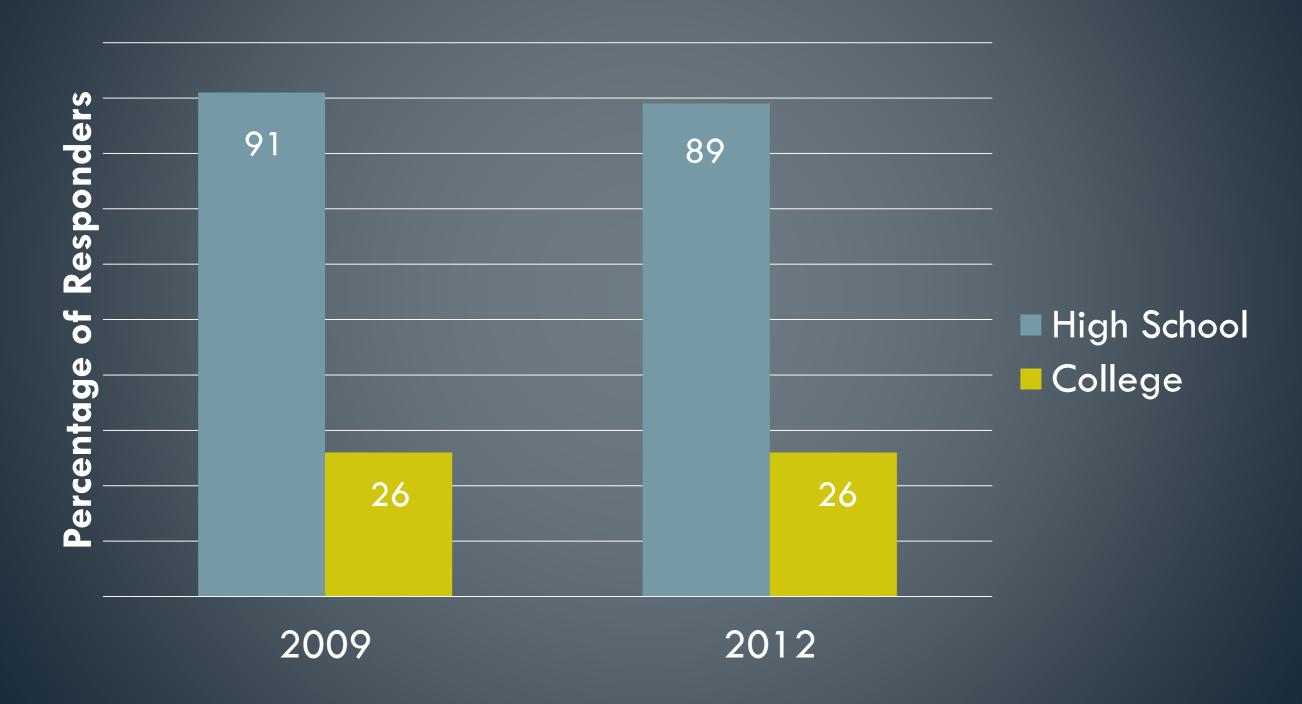




WHAT IS THE PURPOSE OF A K-12 EDUCATION?

- College readiness
 - ACT National CurriculumSurvey
 - Surveyed 9,937 educators

"Well" or "Very Well" Prepared for College



Source: http://www.act.org/research/policymakers/pdf/NCS-PolicySummary2012.pdf

WHAT IS THE PURPOSE OF A K-12 EDUCATION?

- College readiness
- Career readiness
 - Association of AmericanColleges and Universitiessurvey
 - Surveyed over 300
 employers with at least 25
 employees and many new hires

Critical thinking and analytical reasoning skills

Analyzing and solving complex problems

Communicating effectively orally and in writing

Applying knowledge and skills to real-world setting

Working w/ numbers and understanding statistics

Source: http://www.aacu.org/leap/documents/2013 EmployerSurvey.pdf









Sinkhole Dimensions

- National Geographic: "60 feet (18 meters) wide and about 30 stories deep"
- Time Magazine: "runs some 200 ft. deep"
- CNN: "The 20-meter (about 66 feet)
 diameter sinkhole is about 30 meters (about 100 feet) deep."
- Slate: "A sinkhole, 65 feet across and 100 feet deep"

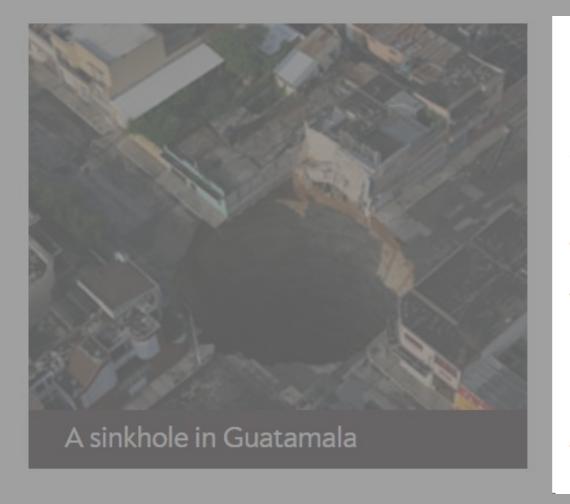


How To Fix a Giant Sinkhole

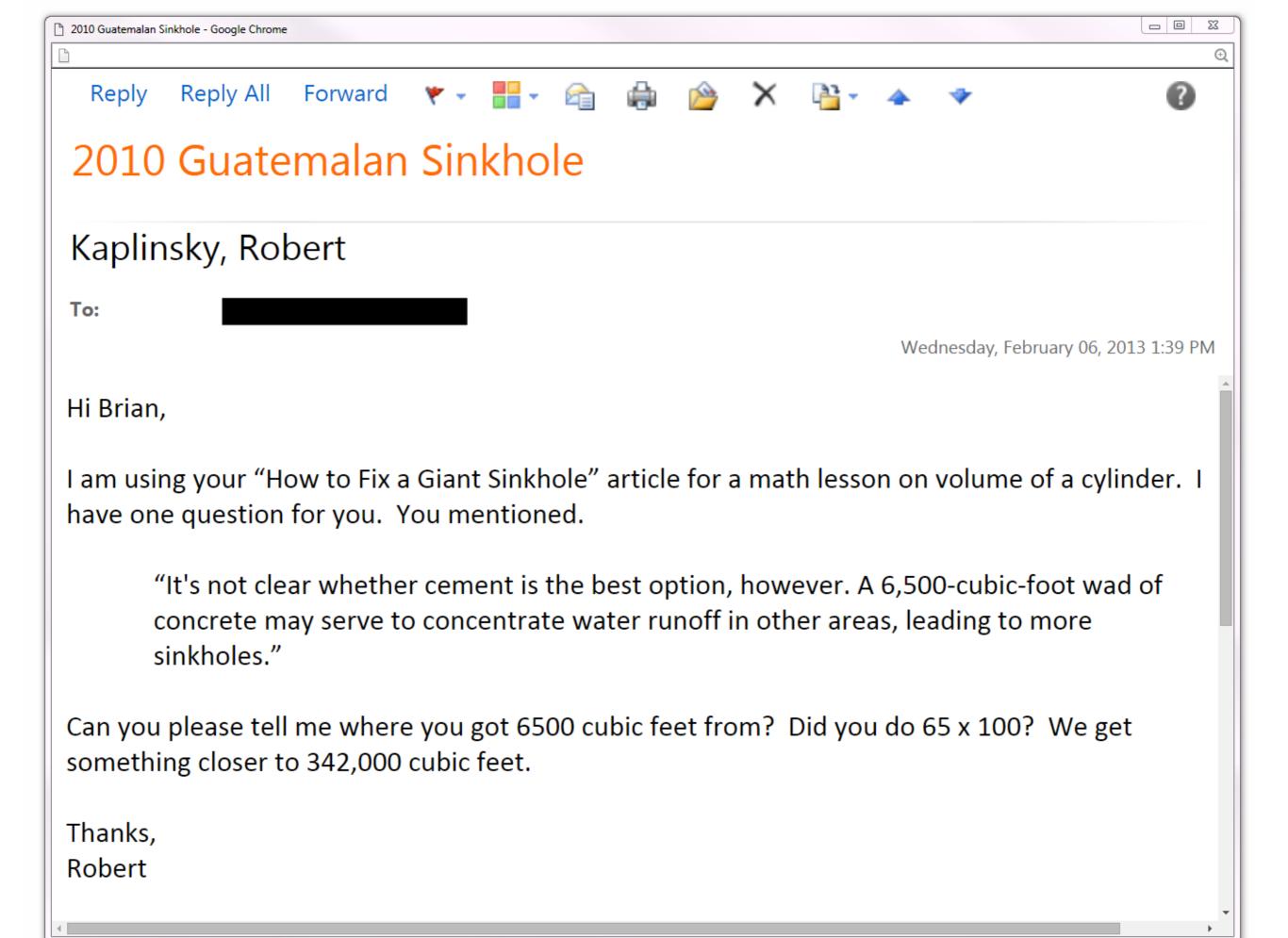
The cement method vs. the graded-filter technique.

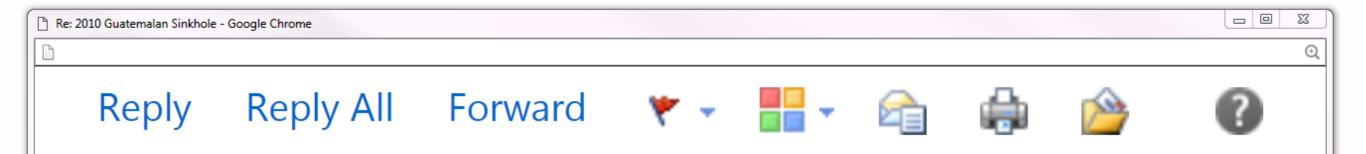


By Brian Palmer



It's not clear whether cement is the best option, however. A 6,500-cubic-foot wad of concrete may serve to concentrate water runoff in other areas, leading to more sinkholes. Many engineers prefer the **graded-filter technique**, in which the hole is filled with a layer of boulders, then a layer of smaller rocks, and, finally, a layer of gravel. This fills the hole, more or less, while permitting water to drain through the area.





Re: 2010 Guatemalan Sinkhole

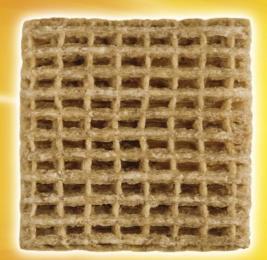
Brian Palmer

To: Kaplinsky, Robert

Wednesday, February 06, 2013 2:01 PM

Apparently you picked the wrong article for a math lesson! I apologize. It appears you are correct. I can't find anything in my notes to save myself-- I think I just screwed up. Dunce cap for me.





OLD (Boring)

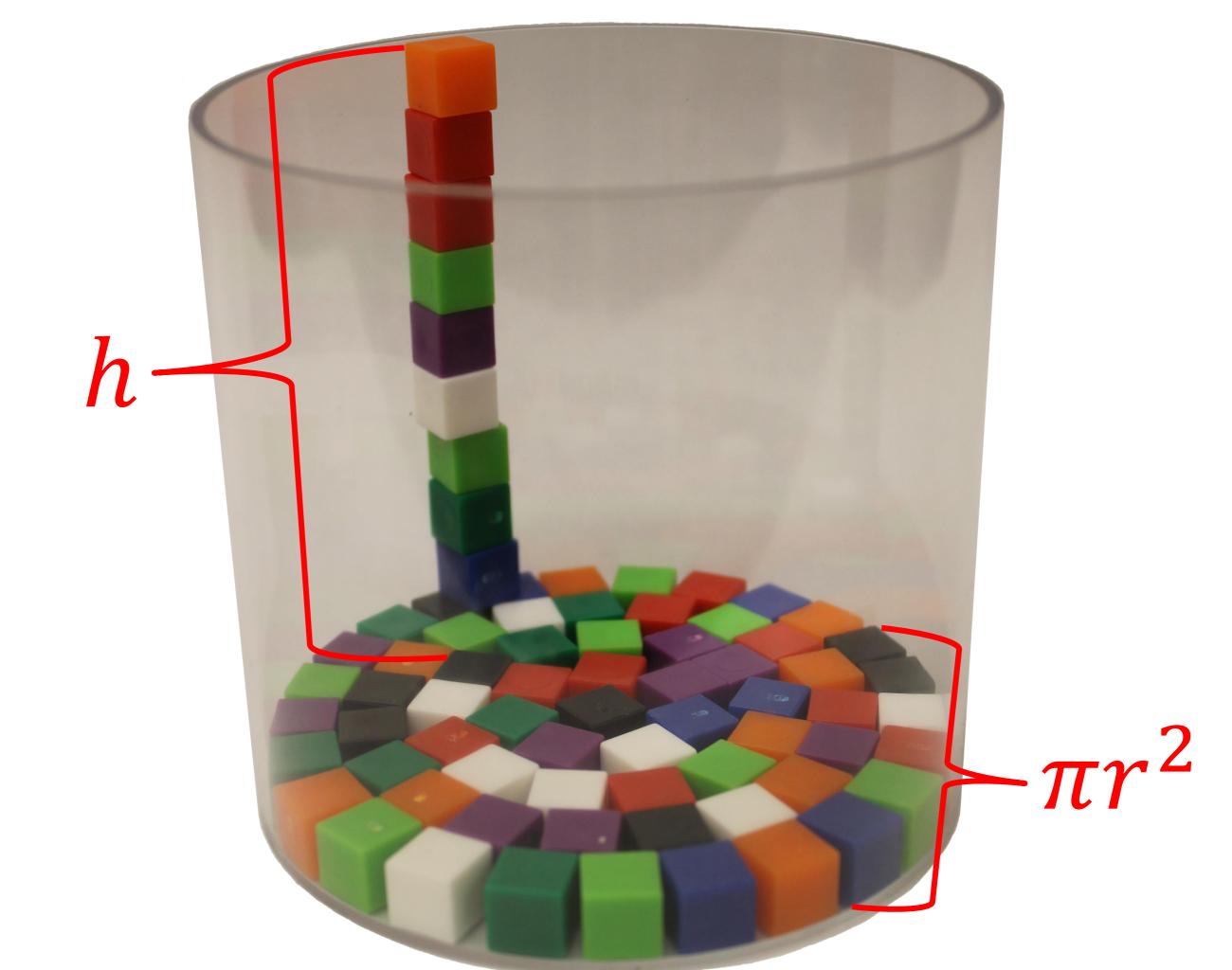
NEW Diamond Shreddies

Cereal





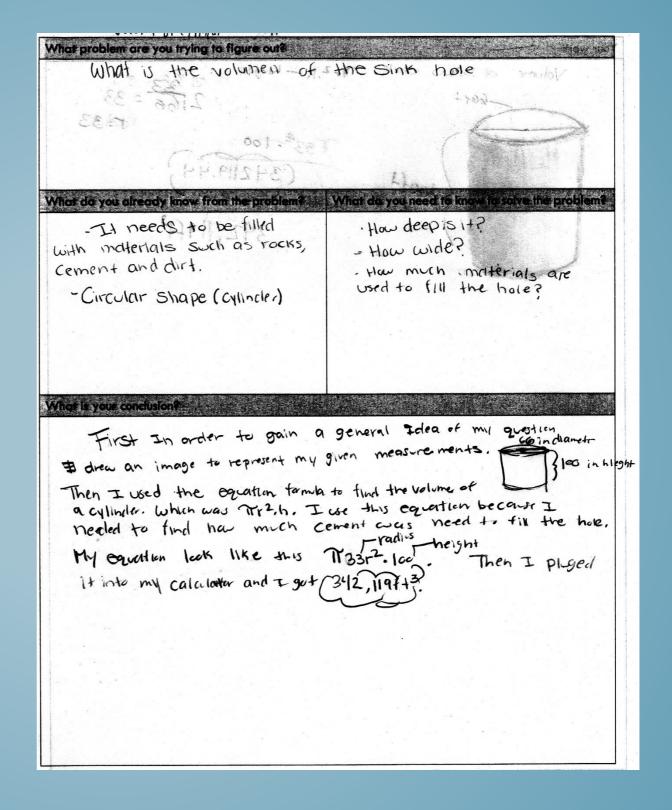




The Reality

- Some students felt anxious about not having the exact dimensions.
- Depending on how much extra information I gave them, students modeled the problem differently:
 - Cylinder
 - Semi-sphere
 - Truncated cone
- Students struggled with precision when dealing with multiple units:
 - feet vs. square feet vs. cubic feet
 - feet vs. meters vs. stories
- Many students doubted themselves when they saw that the "answer" was 6,500 cubic feet.

STUDENT WORK



What is your conclusion?

In order to solve this problem, you need the width and the height of the hole. Once you have it you plus them into the equation r27. In which is to find the volume. Once you find the volume you will know how much come you will need to order so that you could fill that the hole, which in this case would be 3412, 119 feet of cement.

What is your conclusion?

This particular sinkhole in Guatemala City, was about 20 meters (66 feet) indiameter and about 30 meters (100 feet) deep. We are trying to find the volume of the hole to figure out how much material is needed to fill it. I used the cylinder volume formula (v= mr2h). When you plug in the radius and the height, you get v= 1 (33)2 (100). I did not use bb as my radius, because that is my diameter. Radius is half of the diameter. After ger solve, ger are left with 342, 119.44 ft? You don't use ft or ft because the hole 13 3 dimensional. From here on, you just use the material cost and amount to find the price of

In order to fill the smkhde with coment. They will need 342,119 ft3 of cement. How is this possible? Donneter- cele feet, but we are working for radius. 66/5 = 133) Non me day our nagin my 35°

1=33) So we have a nadrus and height. Depth=100 feet.) We can use the volume of a cylinder formula. which is $v = Pr^2h$

> V=74(33)2 - 100 U= 74 (10004) = 100 V= 3421.20 1 V= 345119.44

WHAT ISN'T MATHEMATICAL MODELING?

- It is not modeling in the sense of,
 "I do; now you do."
- It is not modeling in the sense of using manipulatives to represent mathematical concepts.
- It is not modeling in the sense of a "model" being just a graph, equation, or function.
- It is not just starting with a real world situation and solving a math problem.
- It is not beginning with the mathematics and then moving to the real world.

Source: http://www.cde.ca.gov/ci/ma/cf/documents/aug2013apxdmathmodel.pdf

Content and Language Objectives using

Content Objective Example:

SWBAT apply the mathematics they know to solve problems arising in everyday life, society, and the workplace. (MP4)

Language Objective Example:

SWBAT understand and use stated assumptions, definitions, and previously established results in constructing arguments. (MP3)

example:

- In early grades, this might be as simple as writing an addition equation to describe a situation. (MP4)
- In middle grades, a student might apply proportional reasoning to plan a school event or analyze a problem in the community. (MP4)
- By high school, a student might use geometry to solve a design problem or use a function to describe how one

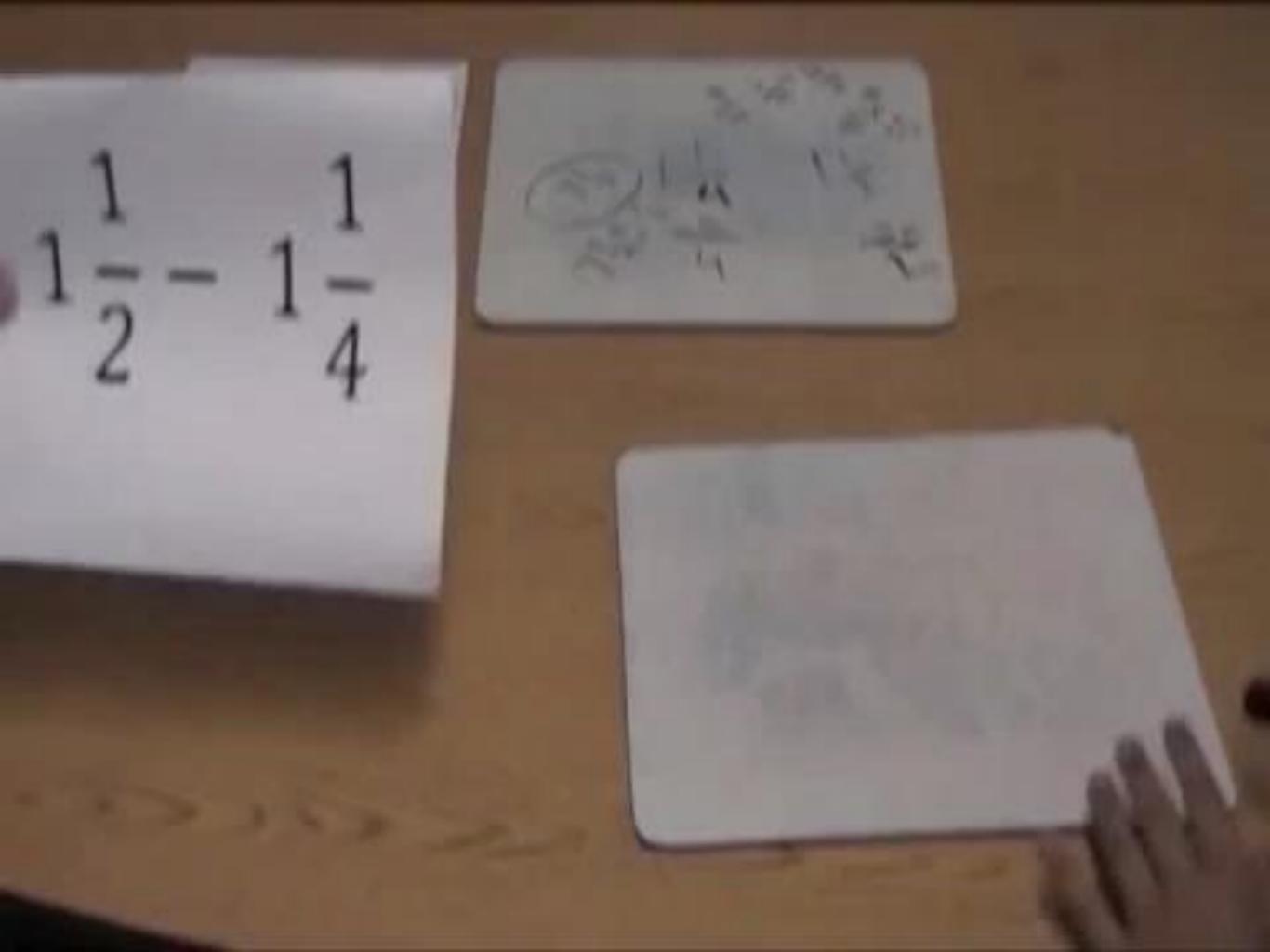
WHAT DOES IT LOOK LIKE...

- when students have procedural skill but not conceptual understanding or the ability to apply mathematics?
- when students <u>can</u> work with numbers but <u>cannot</u>:
 - critically think
 - applying knowledge and skills to real-world settings
 - analyze and solve complex problems

How far apart are the exits on this freeway: Jct 90 and Jefferson Blvd?



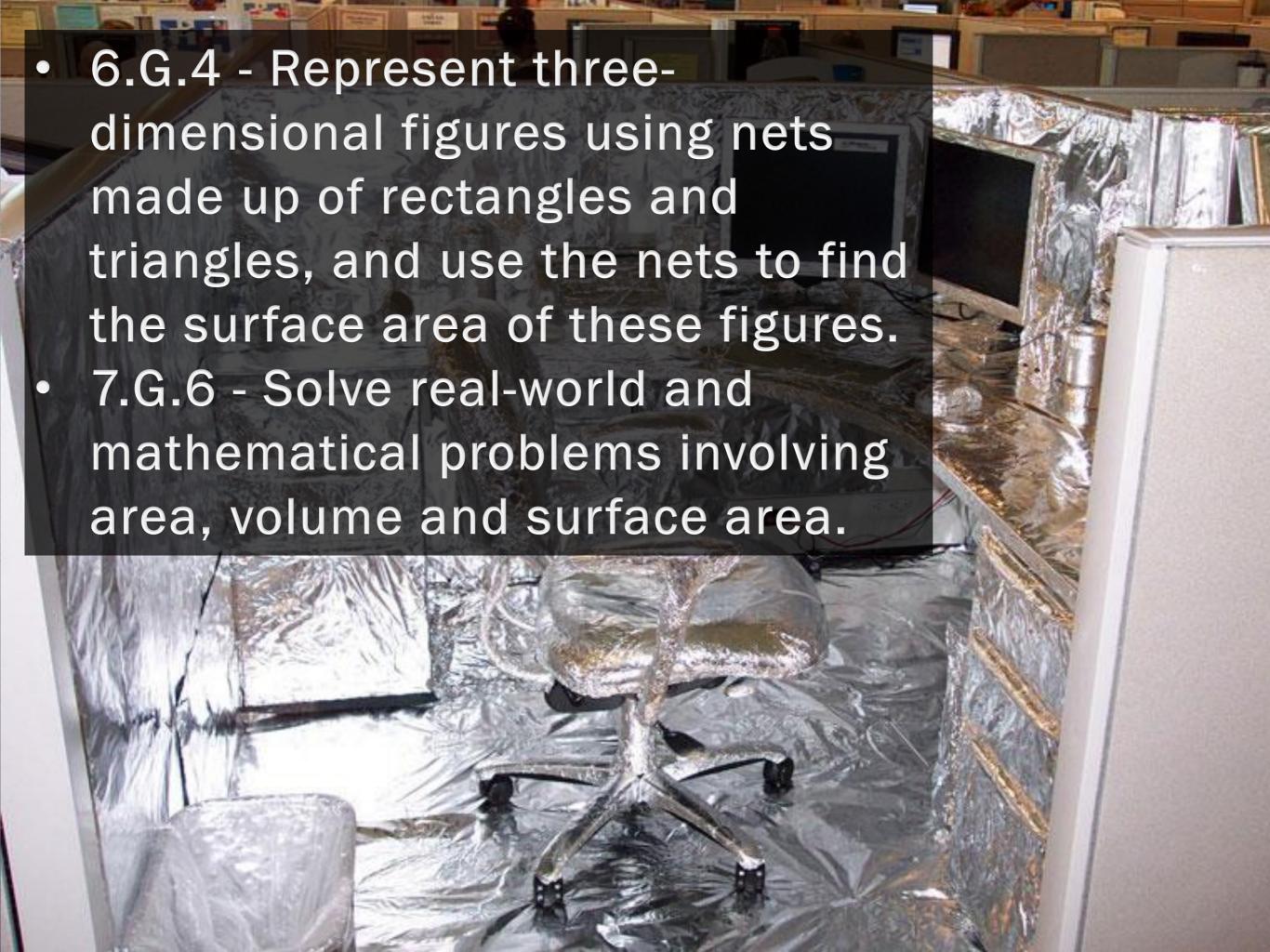


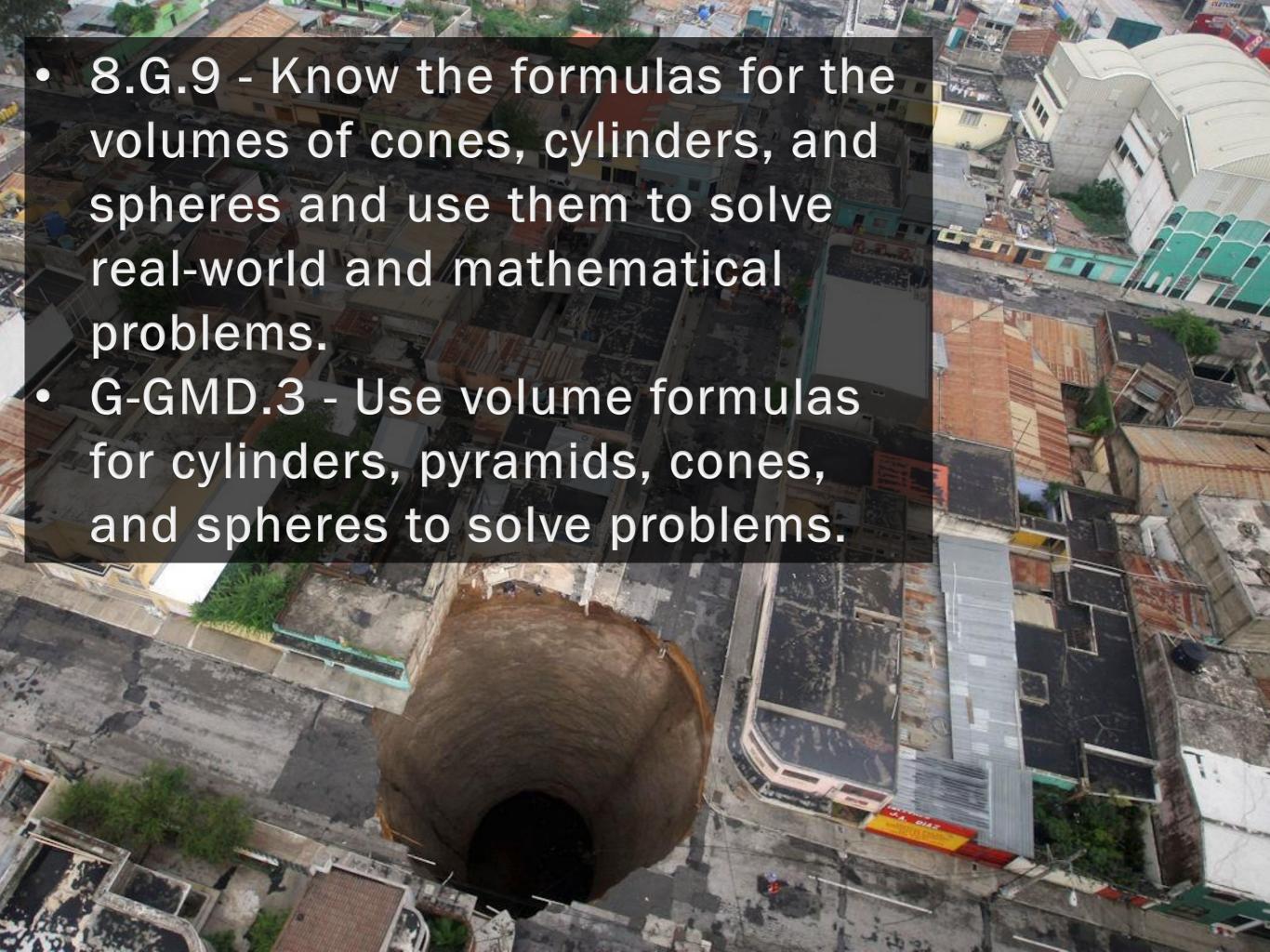




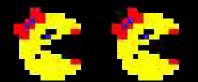
The Four C's

- Communication
- Curiosity





- 8.G.3 Describe the effect of dilations, translations, rotations, and reflections on twodimensional figures using coordinates.
- G-CO.6 Use geometric descriptions of rigid motions to transform figures and to predict the effect of a given rigid motion on a given figure.













A-CED.1 - Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions. F-IF.7a - Graph linear and quadratic functions and show intercepts, maxima, and minima.



The Four C's

- Communication
- Curiosity
- Critical Thinking

Problem Solving Framework

Inspired by Geoff Krall's resources at emergentmath.com

Name:	Period:	Date:	
What problem are you trying to figure out?	What quess	es do you have?	
The production and you trying to triget a con-	Janes Gana		
What do you already know from the problem?	What do yo	u need to know to solv	e the problem?
What should we title this lesson?			
TYTICA STOCICA WE TITLE THIS TESSOT!			
What is your conclusion? How did you reach that conclusion?			

The Four C's

- Communication
- Curiosity
- Critical Thinking
- Content Knowledge

Goals

- Engaging problem solving
 - Real world problem-based learning
 - Higher depth of knowledge problems
- ☐ Better implementation
 - Improve our ability to ask questions
 - Practice preparing to implement a lesson
 - ☐ Figure out how to deal with uncomfortable situations

Questioning Scenarios

- The activity begins with teachers in groups of three taking the roles of teacher, student, or observer.
- The individuals playing the role of teacher and student each receive a slip of paper describing their scenario.
- The individual playing the role of observer waits to record all of the teacher's questions to the student.
- Once the activity begins, the teacher will talk to the student in the context of the scenario they read about on the slips of paper.

What did you get for the area of the circle with a radius of 2 units?

4 pi

Great. Do you have any questions?



What did you get for the area of the circle with a radius of 2 units?

4 pi

Great. How did you get your answer?

The radius is 2 so I plugged it into 2 pi r and got 4 pi.



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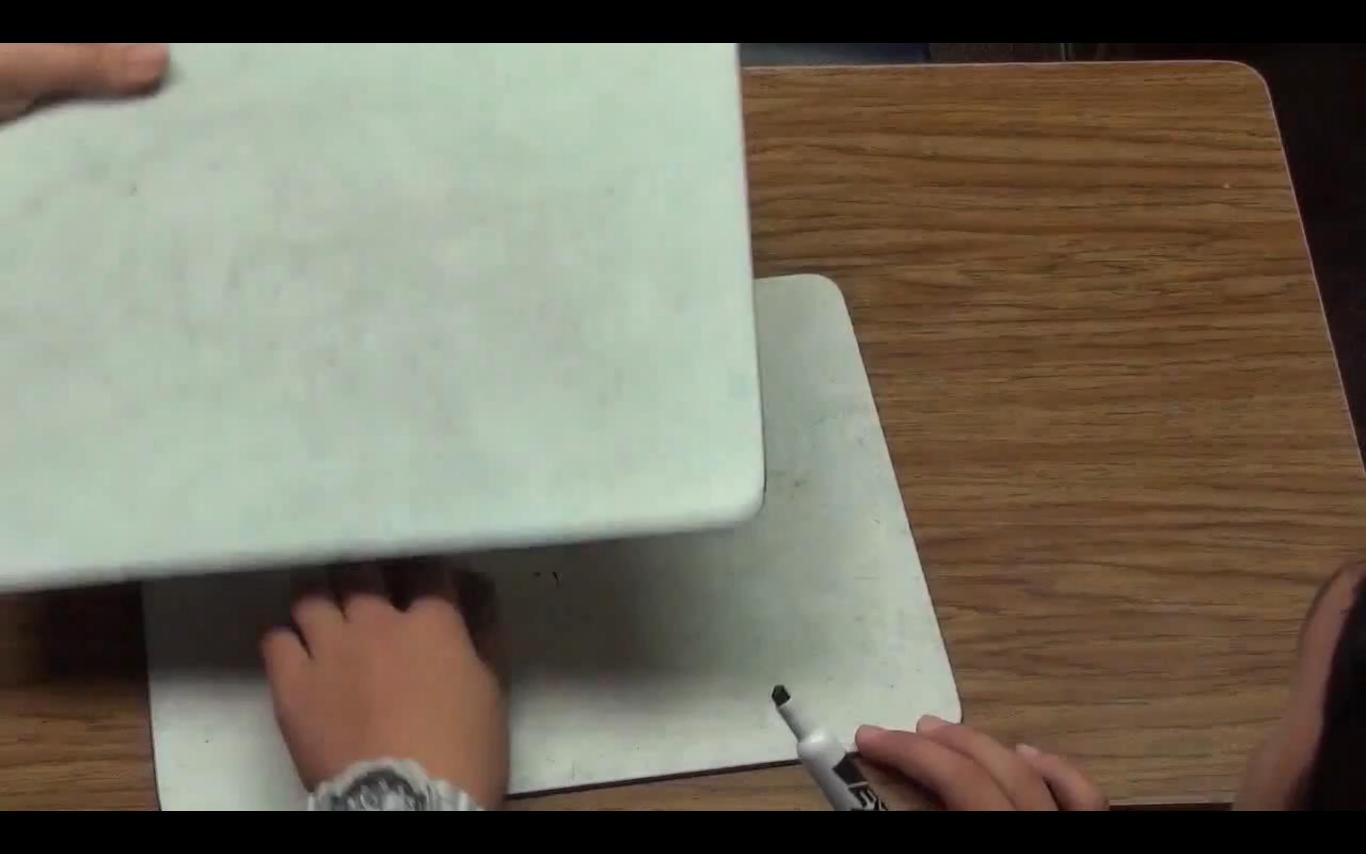
CCSS.MATH.CONTENT.4.MD.A.3 Apply the area and perimeter formulas for rectangles in real world and mathematical problems. equal intensity, th of each grade: conceptua skills and fluency, and application.

Source: http://www.corestandards.org/other-resources/key-shifts-in-mathematics/

What is the perimeter of a rectangle that measures 8 units by 4 units?

Procedural Skill and Fluency

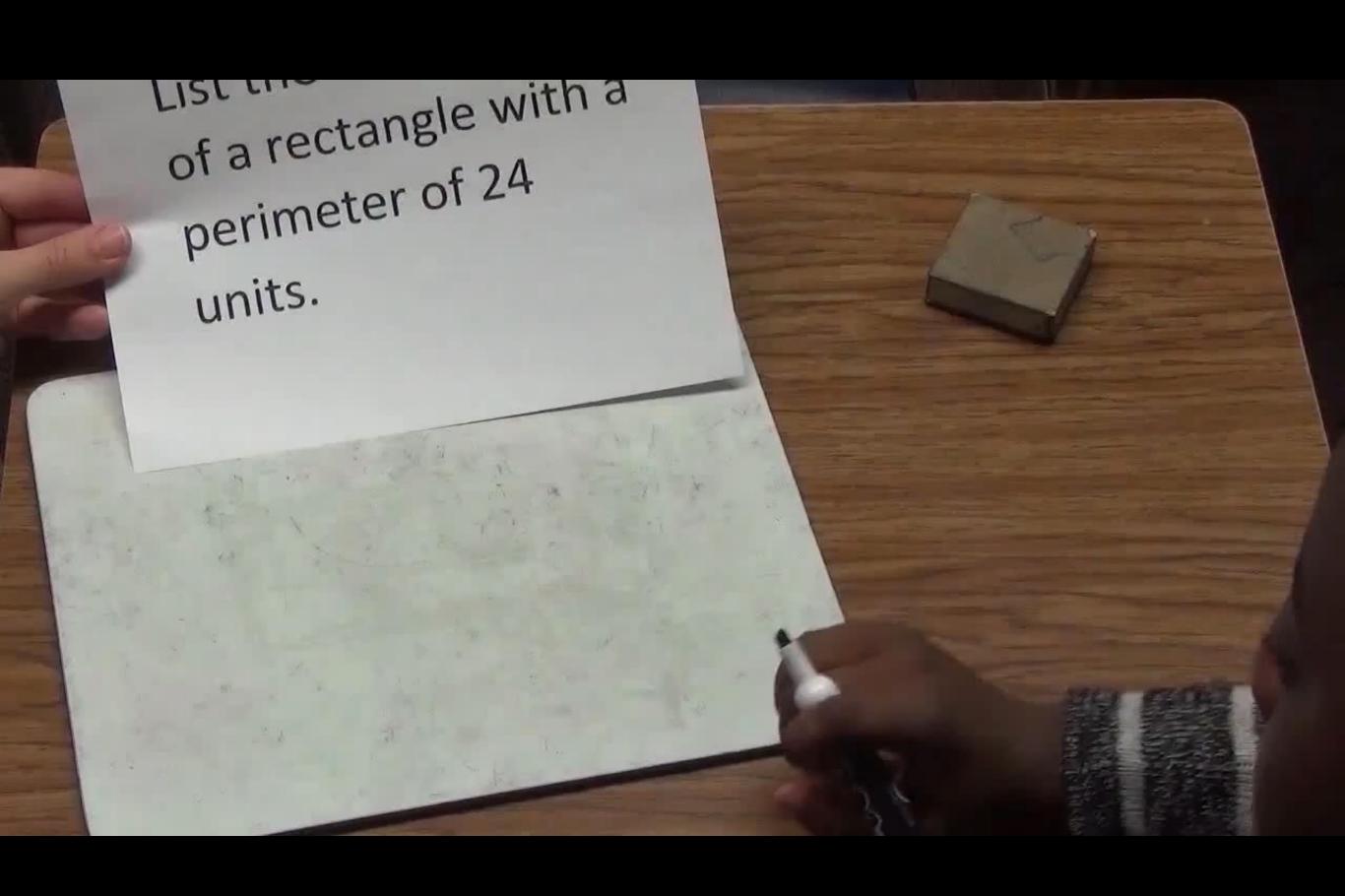
List the dimensions of a rectangle with a perimeter of 24 units.



Procedural Skill and Fluency

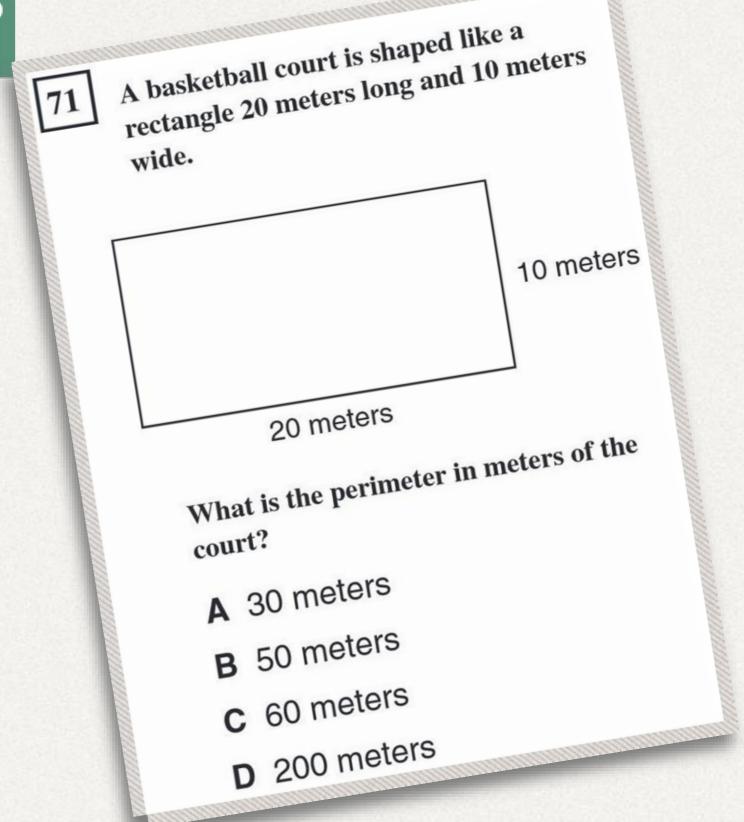


Procedural Skill and Fluency

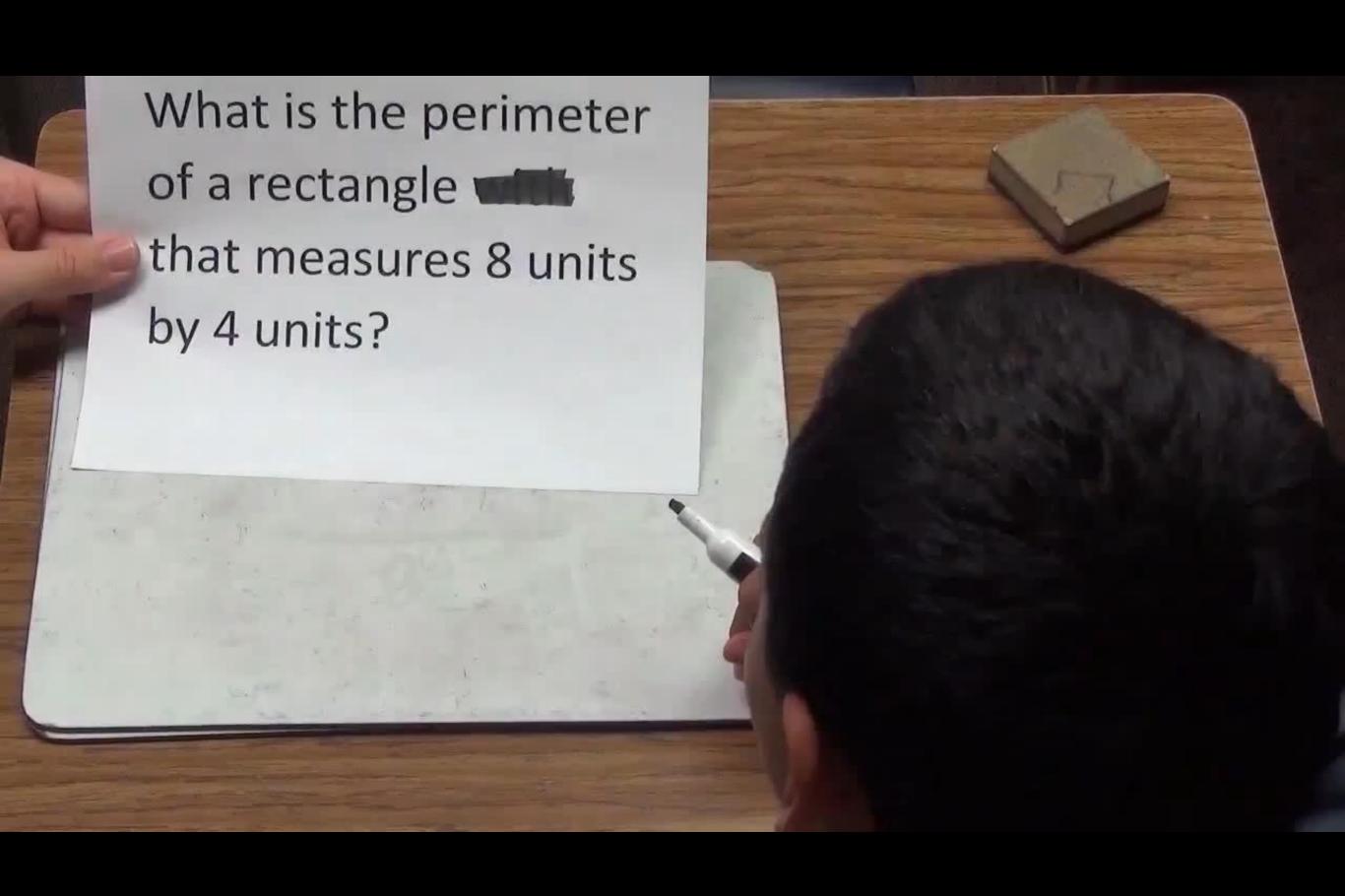


Procedural Skill and Fluency

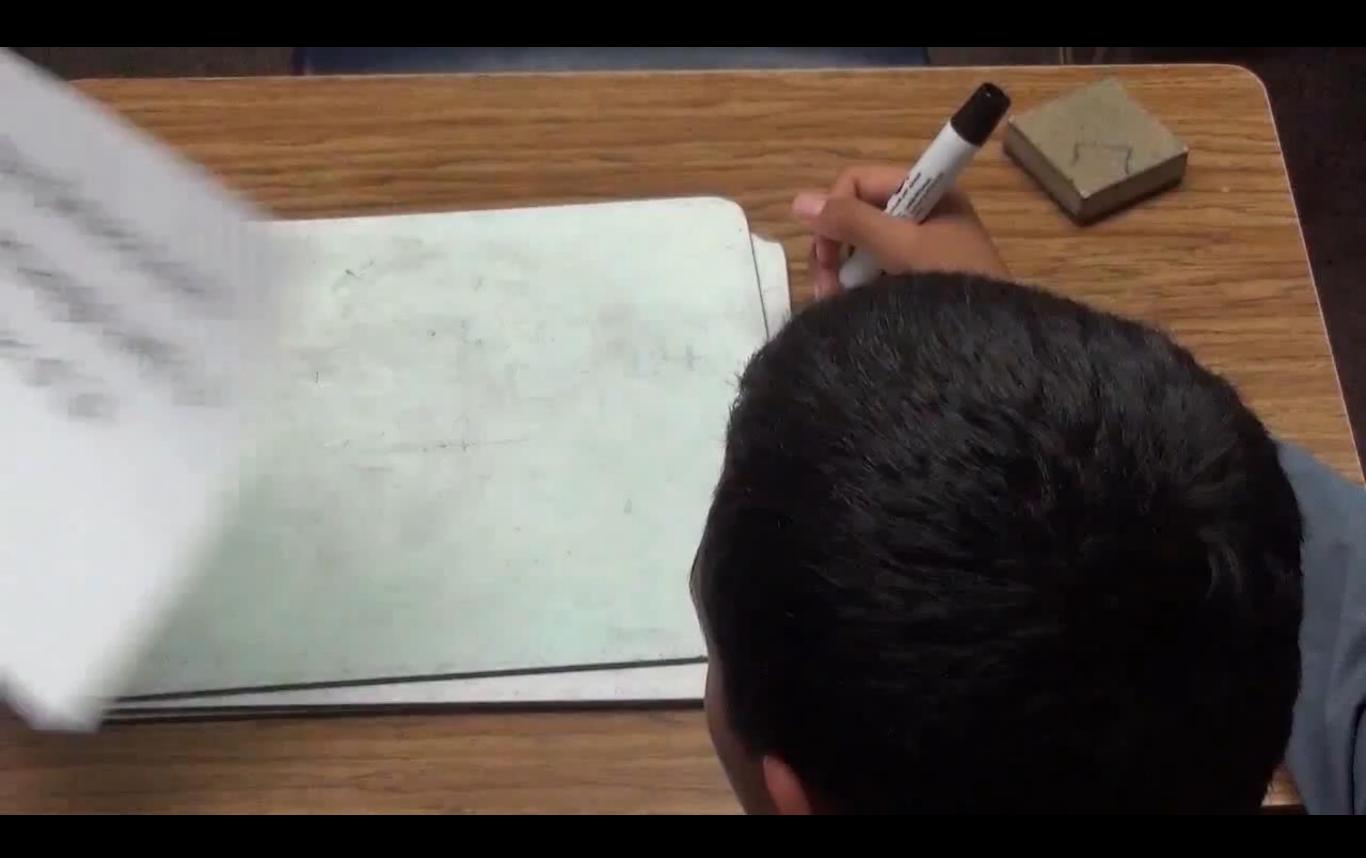




Source: http://www.cde.ca.gov/ta/tg/sr/documents/cstrtqmath3.pdf

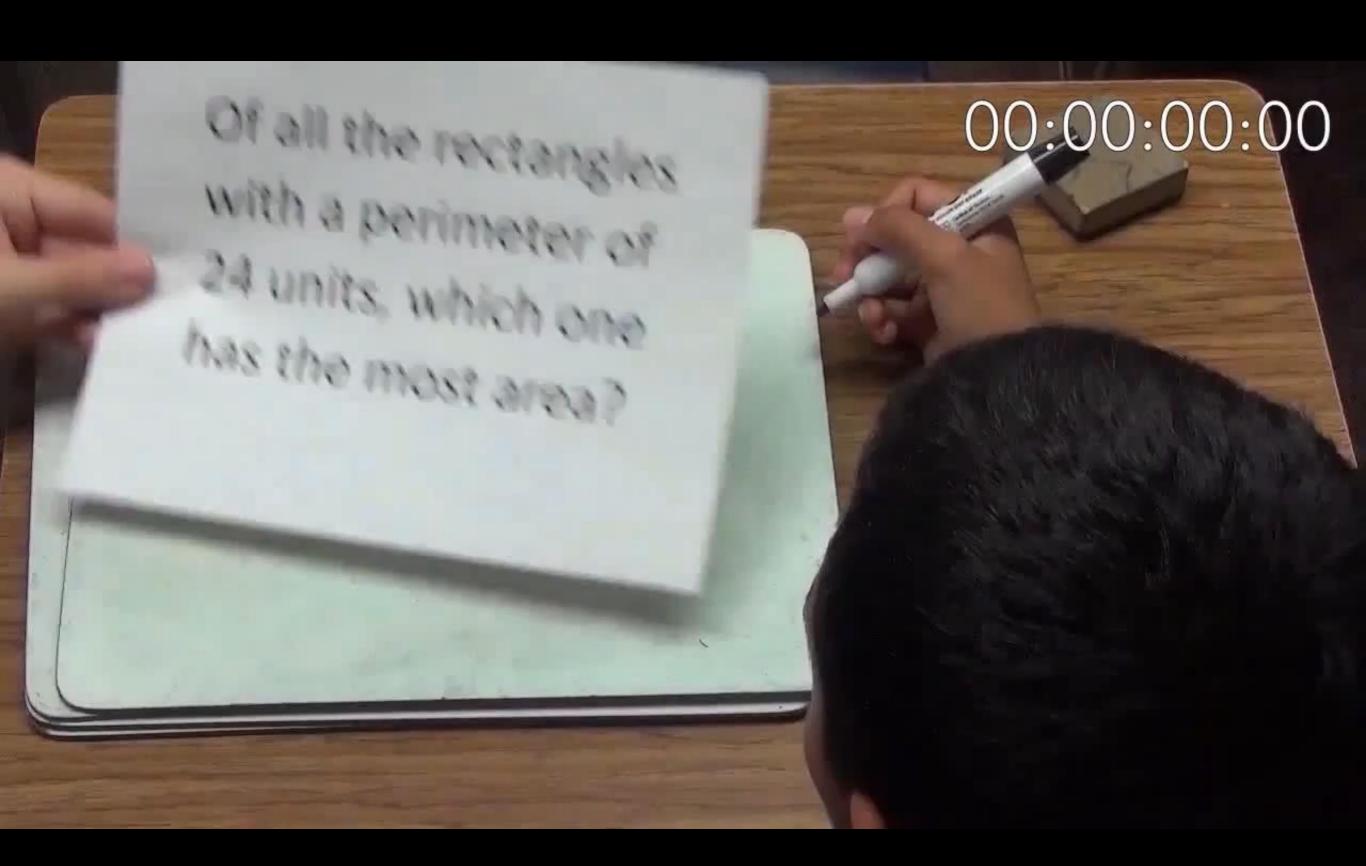


Procedural Skill and Fluency



Procedural Skill and Fluency

Of all the rectangles with a perimeter of 24 units, which one has the most area?



Procedural Skill and Fluency

Defining the Problem

- Students appear to demonstrate "deep, authentic command of mathematical concepts" when given commonly used problems.
- However with more challenging problems, the same students seem to no longer demonstrate that command.

Addressing the Problem

- First, we must have a clear understanding about why these problems are different from one another.
- Next, we need to practice using these problems so that we understand how students may react to them.
- Last, we need a source that can provide us with a variety of free problems.

DOK Distinguishing Between Depth of Knowledge Levels in Mathematics

Topic	Adding Whole Numbers	Money	Fractions on a Number Line	Area and Perimeter	Subtracting Mixed Numbers
CCSS	• 1.NBT.4	• 2.MD.8	• 3.NF.2	• 3.MD.8	• 5.NF.1
Standard(s)	• 2.NBT.5			• 4.MD.3	
DOK 1	Find the sum.	If you have 2	Which point is located at $\frac{7}{12}$	Find the perimeter	Find the difference.
Example	44 + 27 =	dimes and 3 pennies, how many cents do you have	below? L M N O 12 12 12 13 14 15 16 17 18 19 19 19 10 10 10 11 10 11 10 11 10 11 10 11 1	of a rectangle that measures 4 units by 8 units.	$5\frac{1}{2} - 4\frac{2}{3} =$
DOK 2 Example	Fill in the boxes below using the whole numbers 1 through 9, no more than one time each, so that you make a true equation.	Make 47¢ in three different ways with either quarters, dimes, nickels, or pennies.	Label the point where $\frac{3}{4}$ belongs on the number line below. Be as precise as possible.	List the measurements of three different rectangles that each has a perimeter of 20 units.	Create three different mixed numbers that will make the equation true by using the whole numbers 1 through 9, no more than one time each,. You may reuse the same whole numbers for each of the three mixed numbers. $5\frac{4}{5} - = 3\frac{1}{20}$
DOK 3 Example	Make the largest sum by filling in the boxes below using the whole numbers 1 through 9, no more than one time each.	Make 47¢ using exactly 6 coins with either quarters, dimes, nickels, or pennies.	Create 5 fractions using the whole numbers 0 through 9, no more than one time each, as numerators and denominators and correctly place them all on a number line.	What is the greatest area you can make with a rectangle that has a perimeter of 24 units?	Make the smallest difference by filling in the boxes below using the whole numbers 1 through 9, no more than one time each.

ROBERT KAPLINSKY



DOK Distinguishing Between Depth of Knowledge Levels in Mathematics

Topic	Surface Area and	Probability	Transformations	Factoring	Quadratics in Vertex
	Volume	,		Quadratics	Form
CCSS	• 6.G.4	• 7.SP.5	• 8.G.1	A-SSE.3a	• F-IF.7a
Standard(s)	• 7.G.6	• 7.SP.7	• G-CO.5		
DOK 1	Find the surface	What is the probability of	Rotate the image below 90°	Find the factors:	Find the roots and
Example	area of a	rolling a sum of 5 using	counterclockw		maximum of the
	rectangular prism	two 6-sided dice?	ise and reflect	$2x^2 + 7x + 3$	quadratic equation
	that measures 3		it across a		below.
	units by 4 units by		horizontal		04 402 0
	5 units.		line.		$y = -3(x-4)^2 - 3$
DOK 2	List the	What value(s) have a	List three sequences of	Fill in the blank	Create three
Example	measurements of	1/12 probability of being	transformations that take pre-	with integers so	equations for
	three different	rolled as the sum of two	image "	that the quadratic	quadratics in vertex
	rectangular prisms	6-sided dice?	ABCD to	expression is	form that have roots
	that each has a		image \\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	factorable.	at 3 and 5 but have
	surface area of 20		A'B'C'D'.		different maximum
	square units.		Pre-Image Image	$x^2 + _x x + 4$	and/or minimum
					values.
DOK 3	What is the	Fill in the blanks to	What is the fewest number of	Fill the blank by	Create a quadratic
Example	greatest volume	complete this sentence	transformations needed to take	finding the largest	equation with the
	you can make with	using the whole numbers	pre-image ABCD to image A'B'C'D'?	and smallest	largest maximum
	a rectangular	1 through 9, no more	В'	integers that will	value using the
	prism that has a	than one time each.	Â	make the quadratic	whole numbers 1
	surface area of 20			expression	through 9, no more
	square units?	Rolling a sum of on	~ CM ~ N	factorable.	than one time each.
		twosided dice is the	· N		
		same probability as rolling	В У	$2x^2 + 3x + $	$y = -[(x-[)^2 + [$
		a sum of on two	Pre-Image Image		
		sided dice.			

Complicated or Complex?



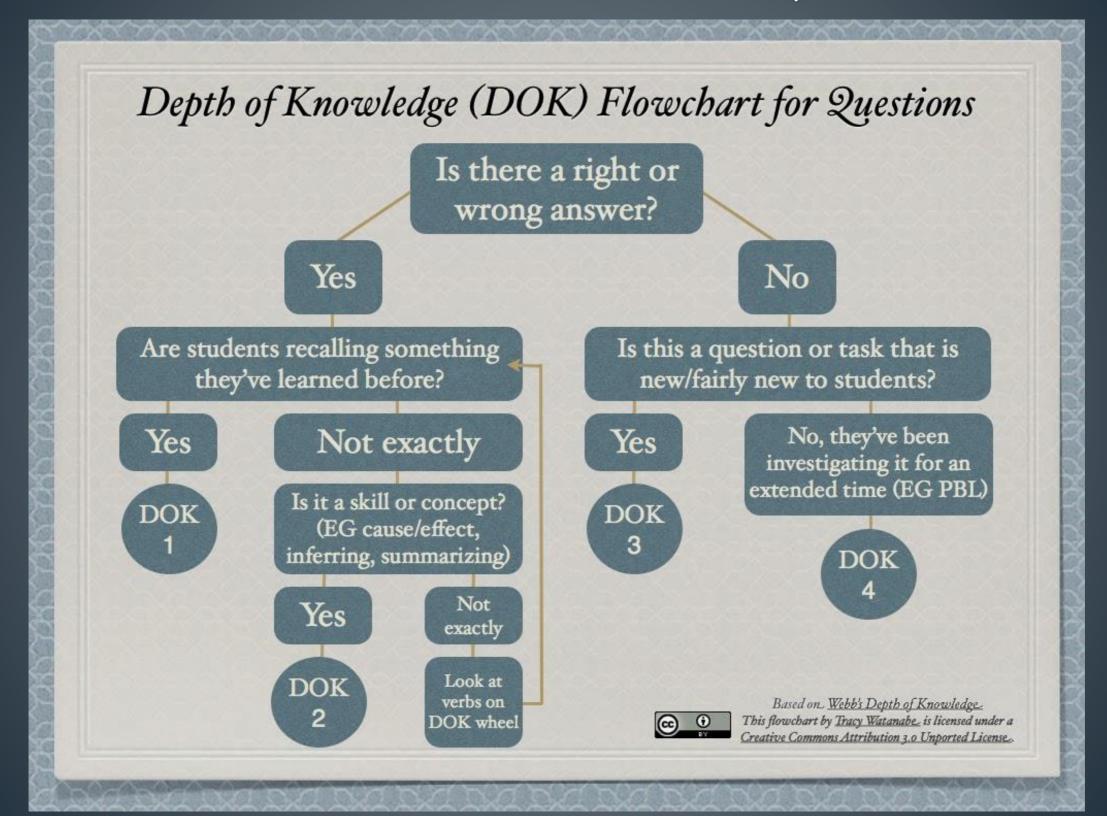


DOK Verb Wheel



Source: Unknown

DOK Flowchart for Questions



Source: Tracy Watanabe - @tracywatanabe

DOK 1

Routine Thinking

- Can you recall
- Can you identify _____
- How would you describe
- What might you include on a list about
- Can you select
- -How can you find the meaning

arrange calculate memorize measure name recognize recall repeat identify illustrate match label state

DOK 2

Conceptual Thinking

- -Can you explain how affected ?
- -How would you apply what you learned to develop ?
- -How would you summarize
- What do you notice about
- How would you estimate
- How could you organize

compare classify categorize measure graph distinguish predict modify construct organize infer summarize interpret make observations

DOK 3

Strategic Reasoning

- How is related to
- What conclusions can be drawn?
- Can you elaborate on ?
- -How would you test___?
- What evidence supports
- What would happen if ___?
- · Why is that the best answer?

assess compare construct
apprise revise hypothesize
critique investigate
draw conclusions

develop a logical argument

DOK 4

Extended Reasoning

- Write a research paper.
- What information can you gather to support your idea about
- Write a thesis, drawing conclusions from multiple sources.
- Apply information from one text to another to develop an persuasive argument.

design connect prove analyze critique synthesize create apply concepts

Created by Penny Lund 2013

DOK Posters

Source: Penny Lund http://isntitelementary.blogspot.com/

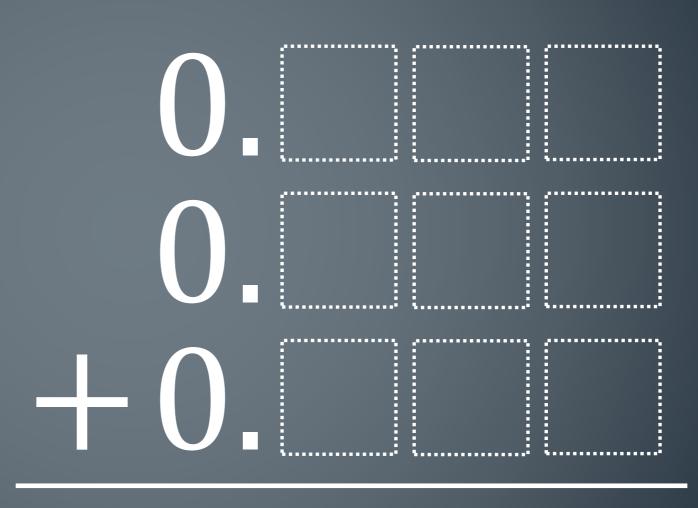
DOK Level Differences

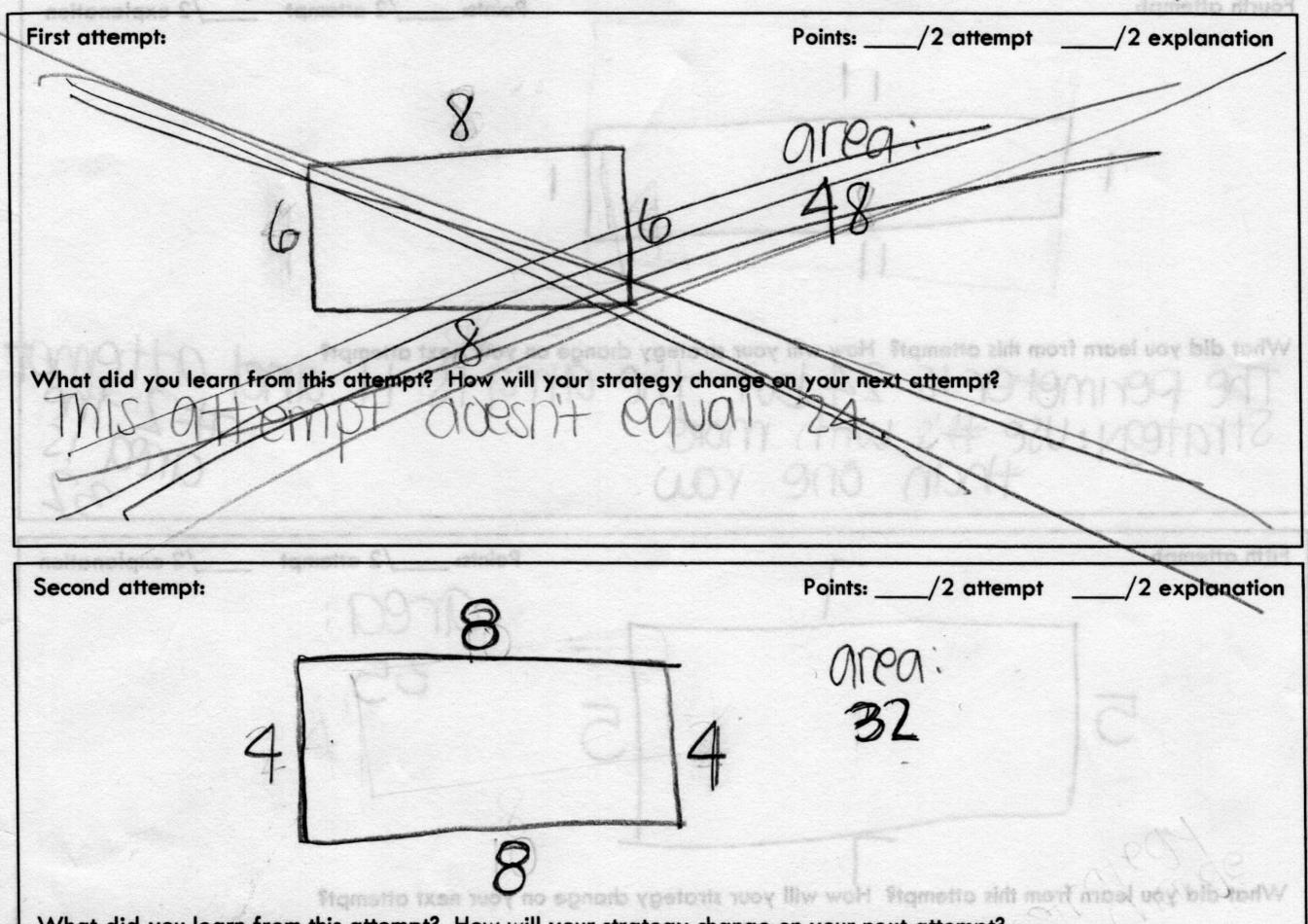
- Level 1: Recall & Reproduction
 - Often a trivial application of facts.
 - Generally requires little to no cognitive effort beyond remembering the right formula.
 - Usually only one answer.
- Level 2: Skills & Concepts
 - Usually requires more than one step to solve.
 - Often multiple answers.

- Level 3: Strategic Thinking
 - Usually requires critical thinking about the best way to approach a problem.
 - May be multiple answers or a single optimal answer.
 - Often challenging enough to make your head hurt.
- Level 4: Extended Thinking
 - In mathematics these are generally represented by performance tasks or problem-based lessons.

Adding Decimals

Use the numbers 1 through 9, exactly one time each, to fill in the boxes and make three decimals whose sum is as close to 1 as possible.





What did you learn from this attempt? How will your strategy change on your next attempt?

Fourth attempt:	Points:/2 attempt/2 explanation
No. of the second secon	
What did you learn from this attempt? How will y The perimeter is 24, bu Strategy: Use #1's with than one	more row.
Fifth attempts noting add que \$\\	Points:/2 attempt/2 explanation
APPA.	

5 5

What did you learn from this attempt? How will your strategy change on your next attempt?

DOK FAQ

- When will students ever use this?
- What DOK level should I start students off with?
- How do teachers fit these problems into their pacing?
- How do I help prevent students from giving up after trying the problem once or twice?
- Where can I find other DOK 2 and DOK 3 problems or submit ones I've made?



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Open Middle Challenging math problems worth solving

Home Grade 1 ▼ Grade 2 ▼ Grade 3 ▼ Grade 4 ▼ Grade 5 ▼ Grade 6 ▼ Grade 7 ▼ Grade 8 ▼ High School ▼ About Submit NEW OPEN N Google™ Custom Search Search OPEN MIDDLE WORKSHEET **Coperations** Exponents a Download the Open Middle Worksheet: February 10, 2015 Leave Version 1.1 Directions: Find 3 positive it at add up to 10. Place each number into one of the blanks to find the largest possible result. Source: Zack liter (@zmill415) Read More » SUBSCRIBE

Create Squares

February 10, 2015 2 Comments

Directions: Create a square with one of the vertices at (2,3). Fill in the blanks with whole numbers 0 through 9, using each number at most once, to show the rest of the vertices of the square. Bonus: Find more than one set of vertices. Source: John Mahlstedt (@jdmahlstedt) Read More »

Solution of Two Linear Equations

February 10, 2015 Leave a comment

Directions: Using the Integers 0-9 (without duplication), provide four sets of points that represent two distinct lines. These lines can be written as two linear equations. Then provide a fifth point that represents the intersection (or solution) of those equations. Line 1: (_, _) and (_, _) Line 2: (_, _) and (_, _) Solution (_, _) Source: Bryan Anderson Read More »

Bingo card

February 5, 2015 1 Comment

Directions: In a standard game of BINGO, the cards are labeled with numbers 1 through 75. If it was possible, which card would you choose: a card with all of the same number or a standard bingo card? Source: Nanette

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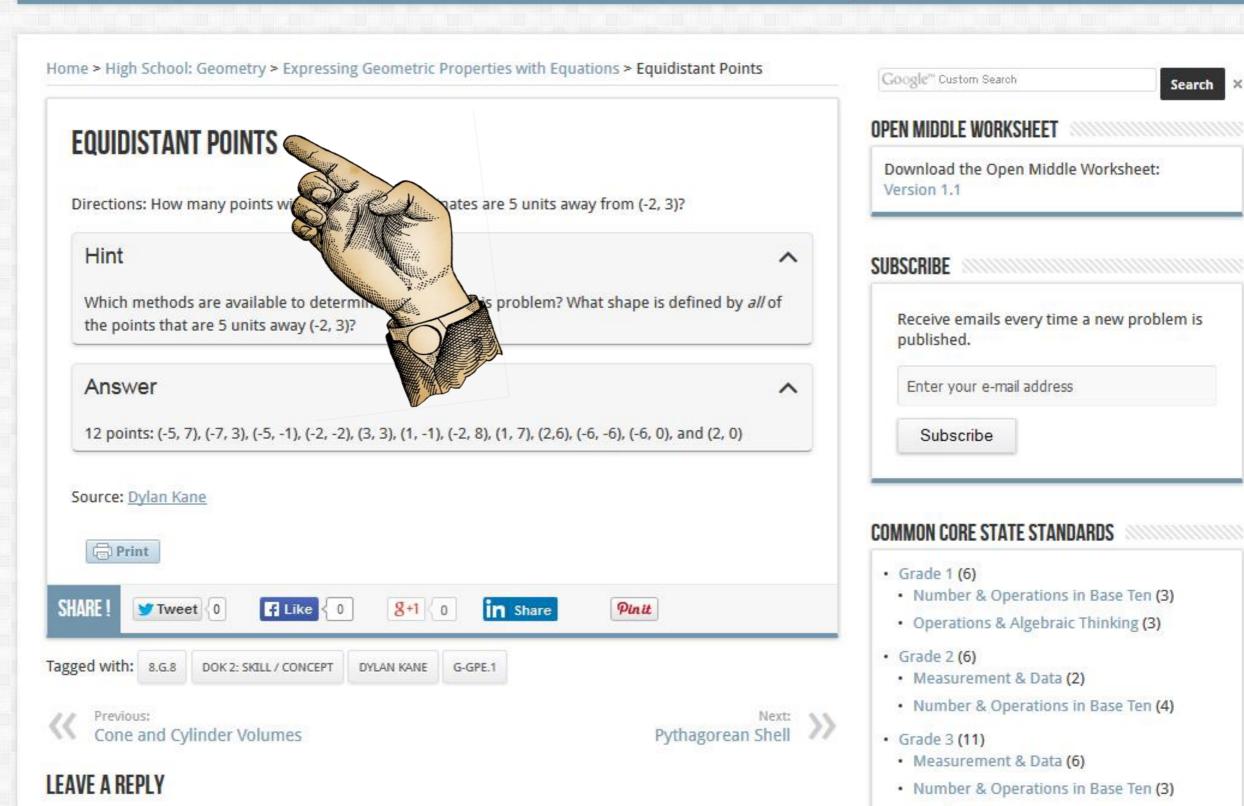
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 - Number & Operations in Base Ten (3)
- · Operations & Algebraic Thinking (3)
- Grade 2 (6)
 - Measurement & Data (2)
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- Andrew Stadel: http://tinyurl.com/mrstadel
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- Geoff Krall: http://tinyurl.com/PrBLmaps
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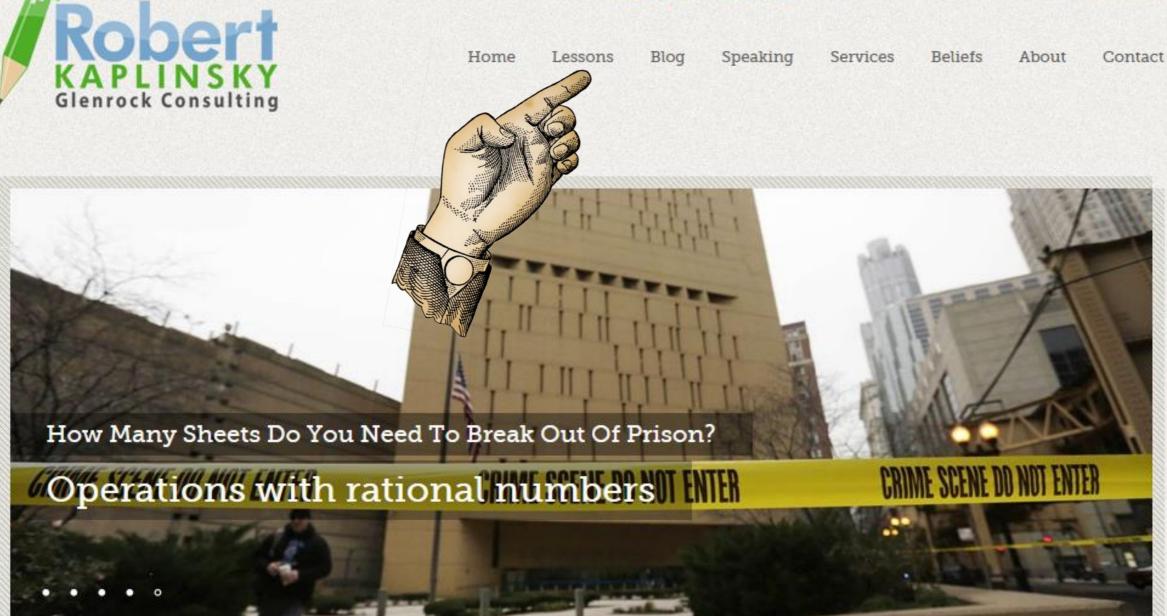












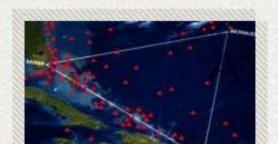
Why Choose Us?



Math content expert

Robert graduated from University of California, Los Angeles (UCLA) with a Bachelors of Science in Mathematics. He has taught mathematics to students at the elementary, middle, and high school levels. As an instructor for UCLA, he also taught math

Lessons







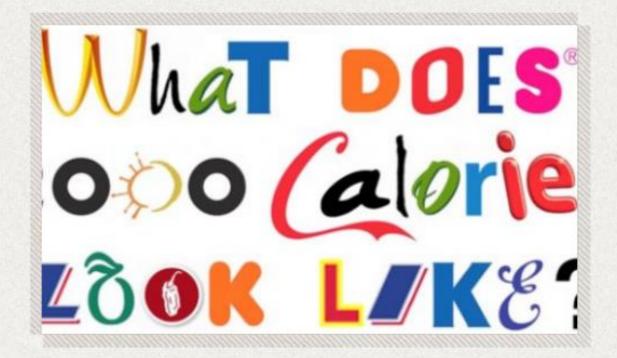


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How Many Hot Dogs And Buns Should He Buy?



What Does 2000 Calories Look Like?





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	A	В	С	D	E	F	
1	Task Name	Concept / Skill	Standard 1	Standard 2	Standard 3	Standard 4	Sta
2	How Can We Water All Of The Grass?	Circles, Pythagorean Theorem, trigonometric ratios	7.G.4	8.G.7	G-SRT.8	G-MG.1	G-I
3	How Much Money IS That?!	Volume of rectangular prism	5.MD.3	5.MD.4	5.MD.5	5.MD.5b	5.1
4	How Much Money Should Dr. Evil Demand?	Exponential Growth	N-RN.2	A-SSE.1	A-SSE.3c	A-SSE.4	A-F
5	How Tall Is Mini-Me?	Scale and Dividing Decimals	5.NF.5	5.NF.5a	5.NF.5b	6.NS.3	
6	How Did They Make Ms. Pac-Man?	Transformations (Rotations, Reflections, and Translations)	8.G.1	8.G.2	8.G.3	8.G.4	G-
7	Which Ticket Option Is The Best Deal?	Unit Rates and Ratios	6.RP.2	6.RP.3	6.RP.3a	6.RP.3b	
8	How Far Apart Are The Freeway Exits?	Fractions on a Number Line and Subtracting Fractions	3.NF.2	3.NF.2b	4.NF.2	4.NF.3a	4.1
9	Do We Have Enough Paint?	Area	3.MD.5	3.MD.6	3.MD.7		
10	How Many Stars Are There In The Universe?	Scientific Notation	8.EE.3	8.EE.4			
11	What Rides Can You Go On?	Inequalities and Measurement	2.MD.1	6.NS.7a	6.NS.7b		
12	Do You Have Enough Money?	Money	2.MD.8				
13	Which Bed Bath & Beyond Coupon Should You Use?	Percent Discount	7.RP.3				
14	Is Gas Cheaper With Cash Or Credit Card?	Percent Discount	7.RP.3				
15	Where's The Nearest Toys R Us?	Pythagorean Theorem (Distance in coordinate system)	8.G.8	G-SRT.8	G-GPE.7		
16	How Sharp Is The iPhone 5's Retina Display?	Pythagorean Theorem (Length of a side)	8.G.7	G-SRT.8	G-GPE.7		
17	When Should She Take Her Medicine?	Operations with Time Intervals	4.MD.2				
18	How Big Are Sunspots?	Converting Units, Proportions, and Scientific Notation	5.MD.1	7.RP.2	7.G.4	8.EE.4	G-I
19	What Michael's Coupon Should I Use?	Percent Discount	7.RP.3	A-CED.3			
20	Is It Cheaper To Pay Monthly or Annually?	Decimal Operations and/or Systems of Equations	5.NBT.7	8.EE.8c	A-CED.3	A-REI.11	F-E
21	How Big Is The 2010 Guatemalan Sinkhole?	Volume of Cylinder	5.MD.3	5.MD.4	5.MD.5	8.G.9	G-(
22	How Can You Win Every Prize At Chuck E. Cheese's?	Decomposing Numbers and/or Systems of Equations	2.NBT.7	3.NBT.2	3.NBT.3	8.EE.8c	A-0
23	How Many Royal Flushes Will You Get?	Probability	7.SP.5	7.SP.6	7.SP.7	S-MD.5	S-I
24	How Much Does The Paint On A Space Shuttle Weigh?	Surface Area	6.G.4	7.G.6	8.G.7	G-MG.1	G-I
25	How Did Motel 6 Go From \$6 to \$66?	Percent Increase and Compound Interest	7.RP.3	A-SSE.1b	F-BF.1	F-IF.8b	F-L
26	How Much Does The Aluminum Foil Prank Cost?	Surface Area and Unit Rates	6.G.4	6.RP.2	6.RP.3	7.G.6	
27	How Many Laps Is A 5k Race?	Perimeter	4.MD.3				
28	Which Toilet Uses Less Water?	Systems of Equations/Inequalities	8.EE.8c	A-CED.3	A-REI.11	F-BF.1	
29	How Did Someone Get A \$103,000 Speeding Ticket In Finland?	Linear Equations	A-CED.2	F-BF.1	F-IF.4	F-IF.6	
30	Which Pizza Is A Better Deal?	Area or Circle, Square, and Unit Rates	3.MD.5	3.MD.6	3.MD.7	4.MD.3	6.F
31	How Big Is The World's Largest Deliverable Pizza?	Area of Square	3.MD.5	3.MD.6	3.MD.7	4.NBT.3	4.1
32	How Many Sheets Do You Need To Break Out Of Prison?	Integer Operations	5.NBT.6				
33	Do Hybrid Cars Pay For Themselves?	Systems of Equations or Rates	6.RP.2	6.RP.3	8.EE.8c	A-CED.3	F-E
34	How Many Hot Dogs Did They Eat?!	Linear and Quadratic Functions	8.F.3	8.F.4	F-BF.1	F-BF.2	F-I
35	How Much Purple Ribbon Will You Need?	Perimeter & Circumference	3.MD.8	4.MD.3	7.G.4		
36	Are We There Yet?	Adding Times	3.MD.1	4.MD.2			
37	Which Chinese Food Coupon Should I Use?	Percent Discount	7.RP.3				
38	How Big Is The Vehicle That Uses Those Tires?	Ratio and Proportions	7.RP.2				
39	Where Would The Angry Birds Have Landed?	Create Equation From Quadratic Graph	A-CED.1	F-BF.1	F-IF.4	F-IF.7a	F-L
40	How Many Movies Can You See In One Day?	Adding Times	3.MD.1	4.MD.2			
41	Which Carrots Should You Buy?	Unit Rates	6.RP.1	6.RP.2	6.RP.3		
42	How Fast Can You Throw A Baseball?	Converting Units and Unit Rates	5.MD.1	6.RP.2			



Problem-Based Lesson Search Engine

This search engine searches all of the sites below to quickly help you find a problem-based lesson (also called 3-Act Task, mathematical modeling, or application problem):

Submit

The links below are the pages that are being searched by the search engine:

- 101 Questions
- Andrew Stadel
- Dan Meyer
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productive struggle

unproductive struggle



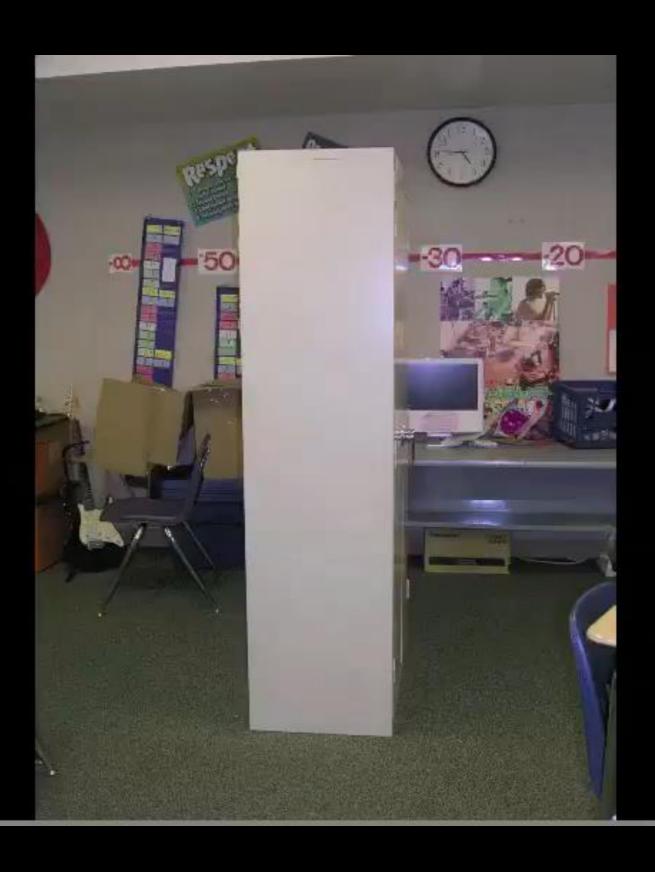
productive struggle

unproductive struggle

Goals

- Engaging problem solving
 - Real world problem-based learning
 - Higher depth of knowledge problems
- ☐ Better implementation
 - Improve our ability to ask questions
 - Practice preparing to implement a lesson
 - ☐ Figure out how to deal with uncomfortable situations











Height: 72 inches







Height: 72 inches

Width: 36 inches







Height: 72 inches

Width: 36 inches

Depth: 18 inches



Recycled Self Stick Notes Notas autoadhesivas reciclados Notes autocollantes recyclés

- 18 pads / blocs
- 100 sheets per pad/hojas por bloc/f
 Total 1800 sheets/hojas/feuillets
- · 3 in x 3 in (76,2 mm x 76,2 mm)

Sticky note

Dimensions: 3" x 3"



PERFORMANCE TASK

CEREAL BOXES

A cereal company uses cereal boxes that are rectangular prisms The boxes have the dimensions shown.

- 12 inches high
- 8 inches wide
- 2 inches deep

The managers of the company want a new size for their cereal boxes. The new boxes have to be rectangular prisms. You will evaluate one box design the company proposed. Then you will create and propose your own design for the company.

Requirements for the new boxes:

• The new boxes have to use less cardboard than the

Determine the volume of the current cereal box with the dimensions 12 inches high, 8 inches wide, and 2 inches deep.

Find the volume, \(\mu, \) in cubic inches, of each box.

Volume of Original Box: \(\mu = _{\text{in}}^{3} \)

Label the dimensions of the net for the current cereal box with dimensions 12 inches high, 8 inches wide, and 2 inches deep.

12 in



DOK

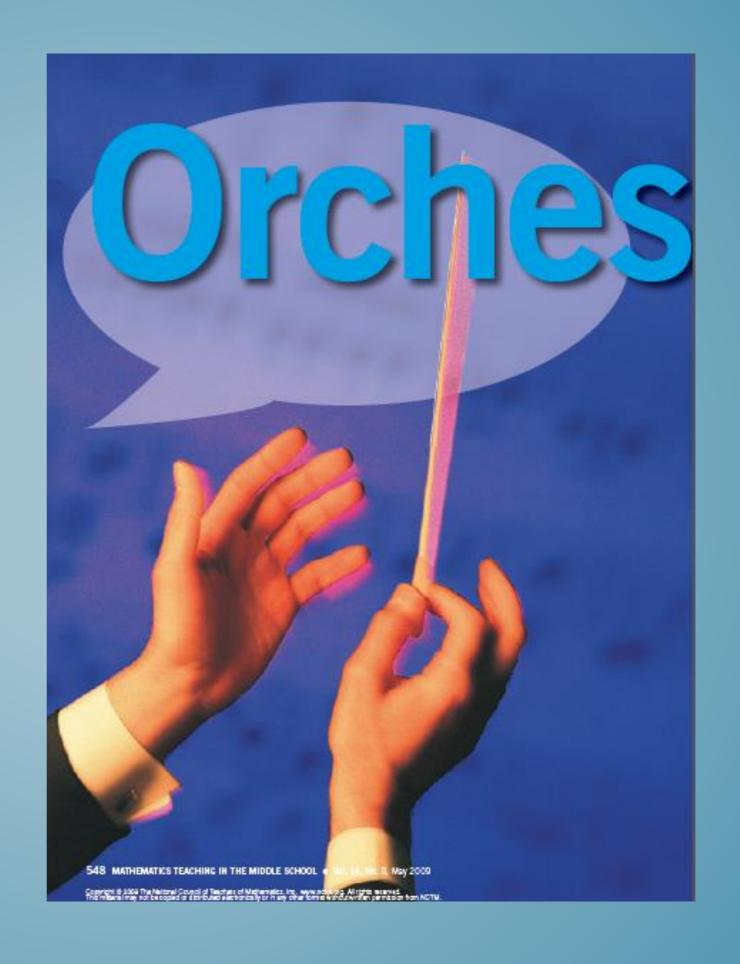
Distinguishing Between Depth of Knowledge Levels in Mathematics

Topic	Surface Area and	Probability	Transformations	Factoring	Quadratics in Vertex
	Volume	, , , , , , , , , , , , , , , , , , , ,		Quadratics	Form
CCSS	• 6.G.4	• 7.SP.5	• 8.G.1	A-SSE.3a	F-IF.7a
Standard(s)	• 7.G.6	• 7.SP.7	• G-CO.5		
DOK 1	Find the surface	What is the probability of	Rotate the image below 90°	Find the factors:	Find the roots and
Example	area of a	rolling a sum of 5 using	counterclockw		maximum of the
	rectangular prism	two 6-sided dice?	ise and reflect	$2x^2 + 7x + 3$	quadratic equation
	that measures 3		it across a		below.
	units by 4 units by		horizontal		
	5 units.		line.		$y = -3(x-4)^2 - 3$
DOK 2	List the	What value(s) have a	List three sequences of	Fill in the blank	Create three
Example	measurements of	1/12 probability of being	transformations that take pre-	with integers so	equations for
	three different	rolled as the sum of two	image	that the quadratic	quadratics in vertex
	rectangular prisms	6-sided dice?	ABCD to	expression is	form that have roots
	that each has a		image $\sum_{i \geq 1} \sum_{i = 1}^{N} \sum_{i = 1}^{N}$	factorable.	at 3 and 5 but have
	surface area of 20		A'B'C'D'.		different maximum
	square units.		0' Pre-Image Image	$x^2 + \underline{\hspace{1cm}} x + 4$	and/or minimum
					values.
DOK 3	What is the	Fill in the blanks to	What is the fewest number of	Fill the blank by	Create a quadratic
Example	greatest volume	complete this sentence	transformations needed to take	finding the largest	equation with the
	you can make with	using the whole numbers	pre-image ABCD to image A'B'C'D'?	and smallest	largest maximum
	a rectangular	1 through 9, no more	B'	integers that will	value using the
		than one time each.		make the quadratic	whole numbers 1
	surface area of 20	Rolling a sum of on	$\sim > \leq \sim \sim \sim$	expression factorable.	through 9, no more than one time each.
	square units?	twosided dice is the	$c \ge c $ $c'' \setminus A'$	lactorable.	ulan one ume each.
		same probability as rolling	В	$2x^2 + 3x +$	$y = -[(x-[)^2 + []$
		a sum of on two	Dro Imago	2.4 1 0.7 1	, m, m, m
I		sided dice.	Pre-Image Image		
I					

Discussion Questions

- How will problem-based lessons like these prepare students for a performance task like the Cereal Box?
- What skills might students still be lacking to be successful with a problem like this?

FIVE PRACTICES



Discussion Questions

- "Giving students too much or too little support, or too much direction, can result in a decline in the cognitive demands of the task." (p. 550) Why?
- "By making purposeful choices about the order in which students' work is shared, teachers can maximize the chances that their mathematical goals for the discussion will be achieved." (p. 554) What ways do teachers currently select students? How would you suggest they change their selection process after reading this?
- What challenges might teachers have when trying to "connect" student solutions? (p. 554)

Implementing the Five Practices

- 1. Pick a selection strategy you anticipate using before looking at the student work.
- 2. Next, review the student work to simulate the reality that you won't know what students will actually do.
- 3. Figure out which students you would have share their mathematical work.
- 4. Determine the order you would have those students present their work.
- 5. Decide on which connections you would emphasize between the students' work and mathematical ideas.

Posters

- At the top of the poster, list the selection strategy used by your group. For example:
 - Starting with the most commonly used strategy and moving to one that few students used.
 - Starting with a strategy that is more concrete and moving to strategies that are more abstract.
 - Incorporating wrong answers to address common misconceptions.
- Attach those students' work to the poster in the order that you would present it.
- Next to the student work list the questions you would ask the student(s) or ideas that you would want to come out as a result of showing that student's work.











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 - Improve our ability to ask questions
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Pre-Mortem

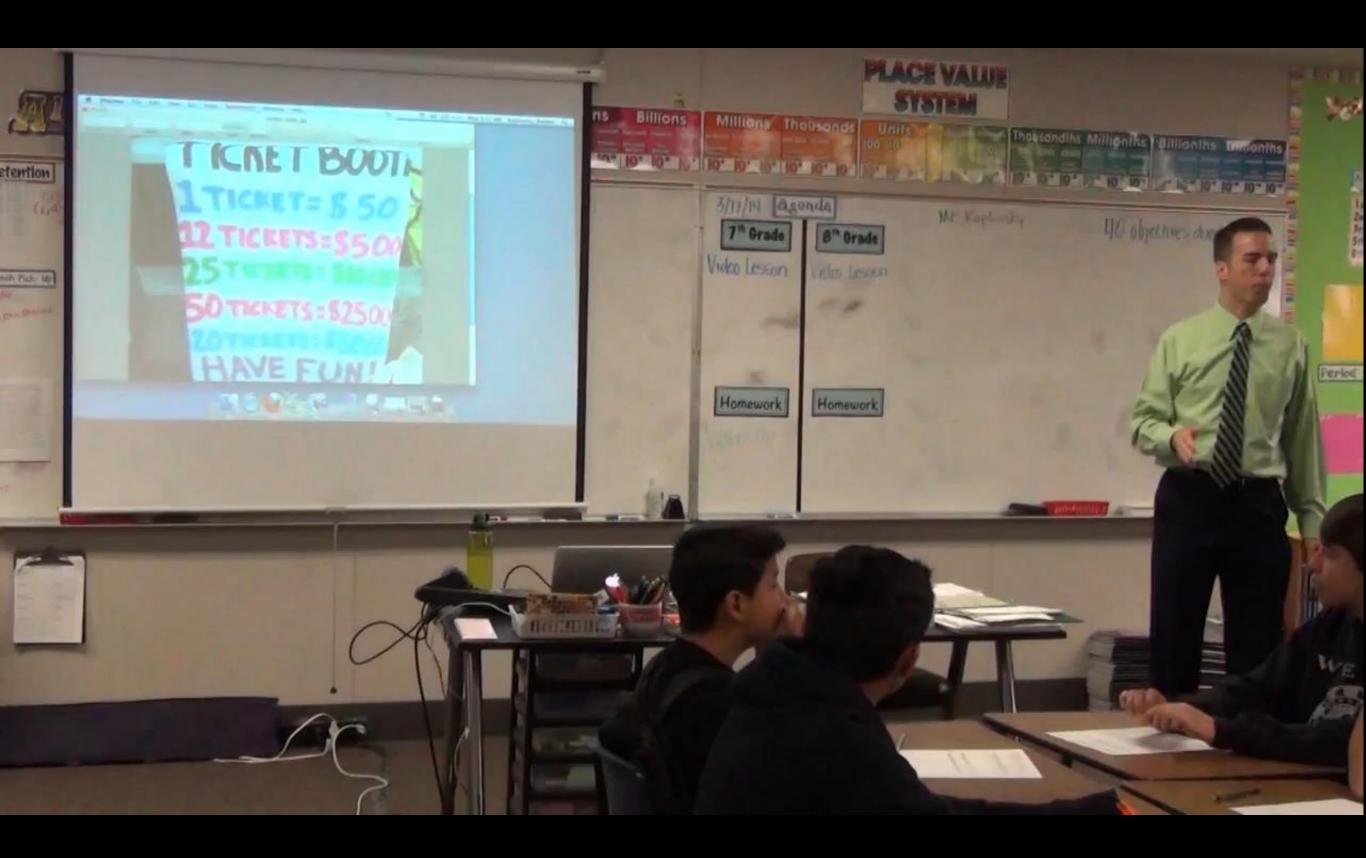
- The lesson flopped. What went wrong?
- You have sixty seconds to write down all the reasons the lesson did not go well.
- Create a combined list with your neighbors.
- Then discuss "less helpful" and "more helpful" was you could address them if they do happen.

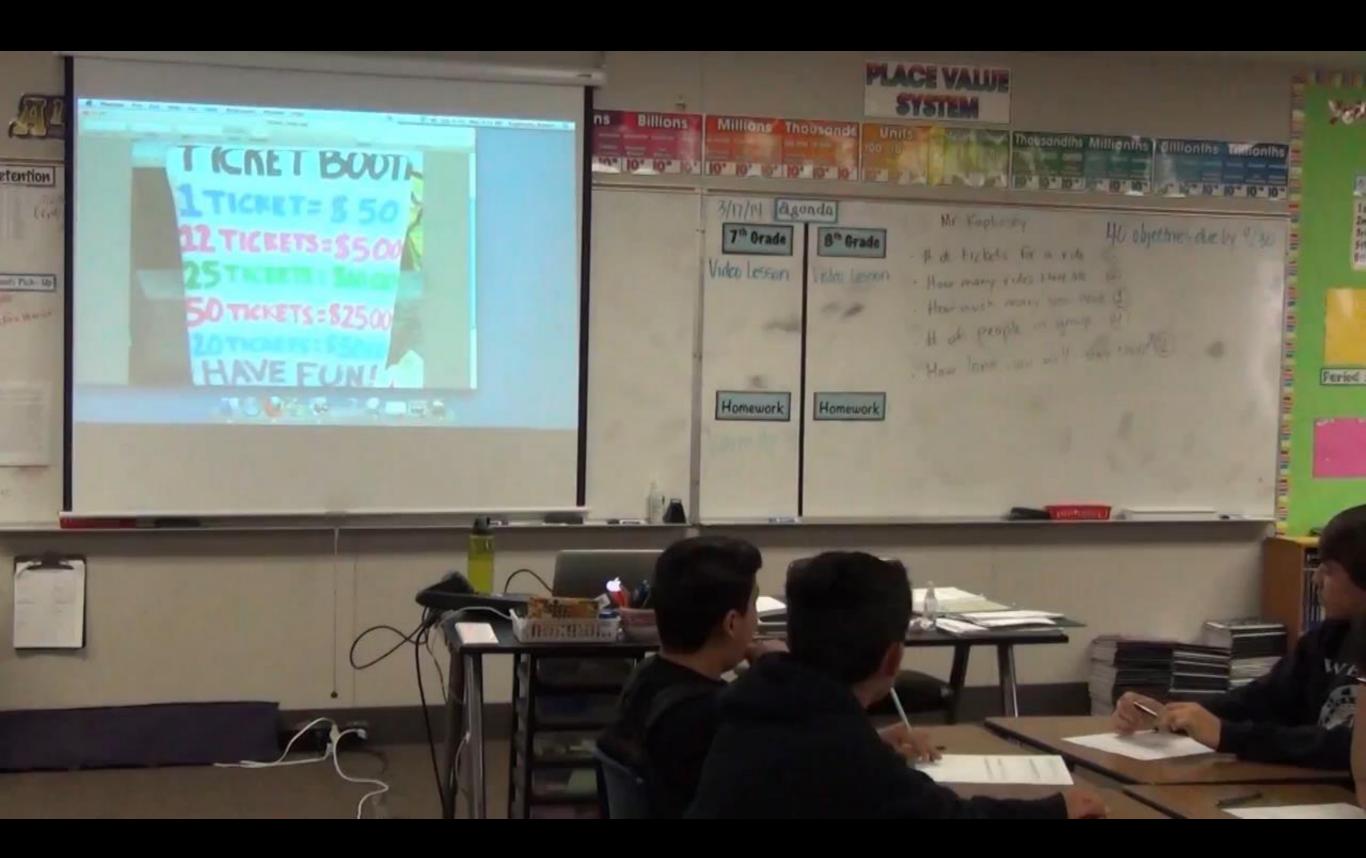


Setting Up The Problem

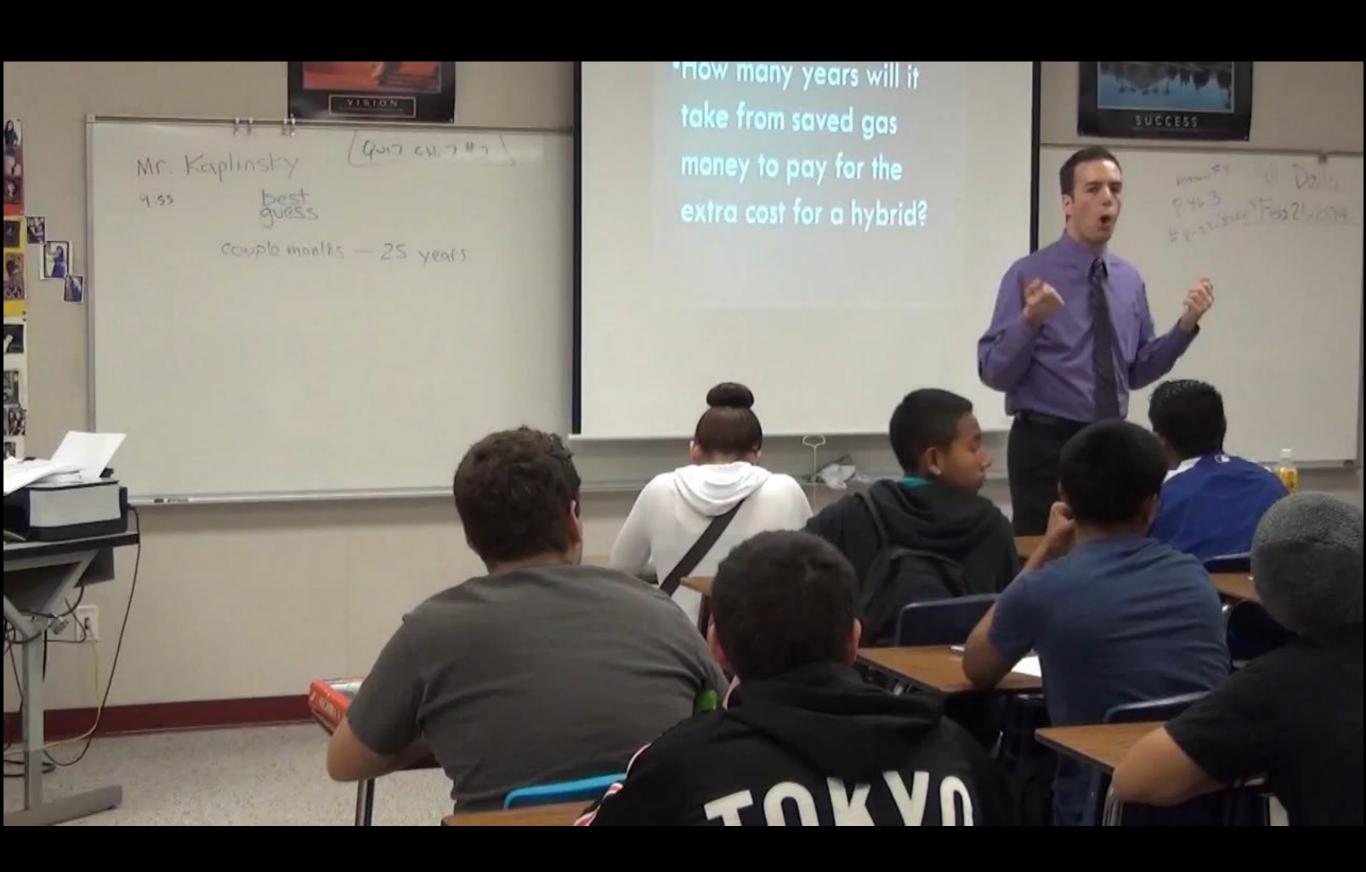
- What do you do when students ask for data/information I don't have, hadn't considered, or forgot to get?
- What do you do when students ask for information that is probably not important or that they don't actually need?

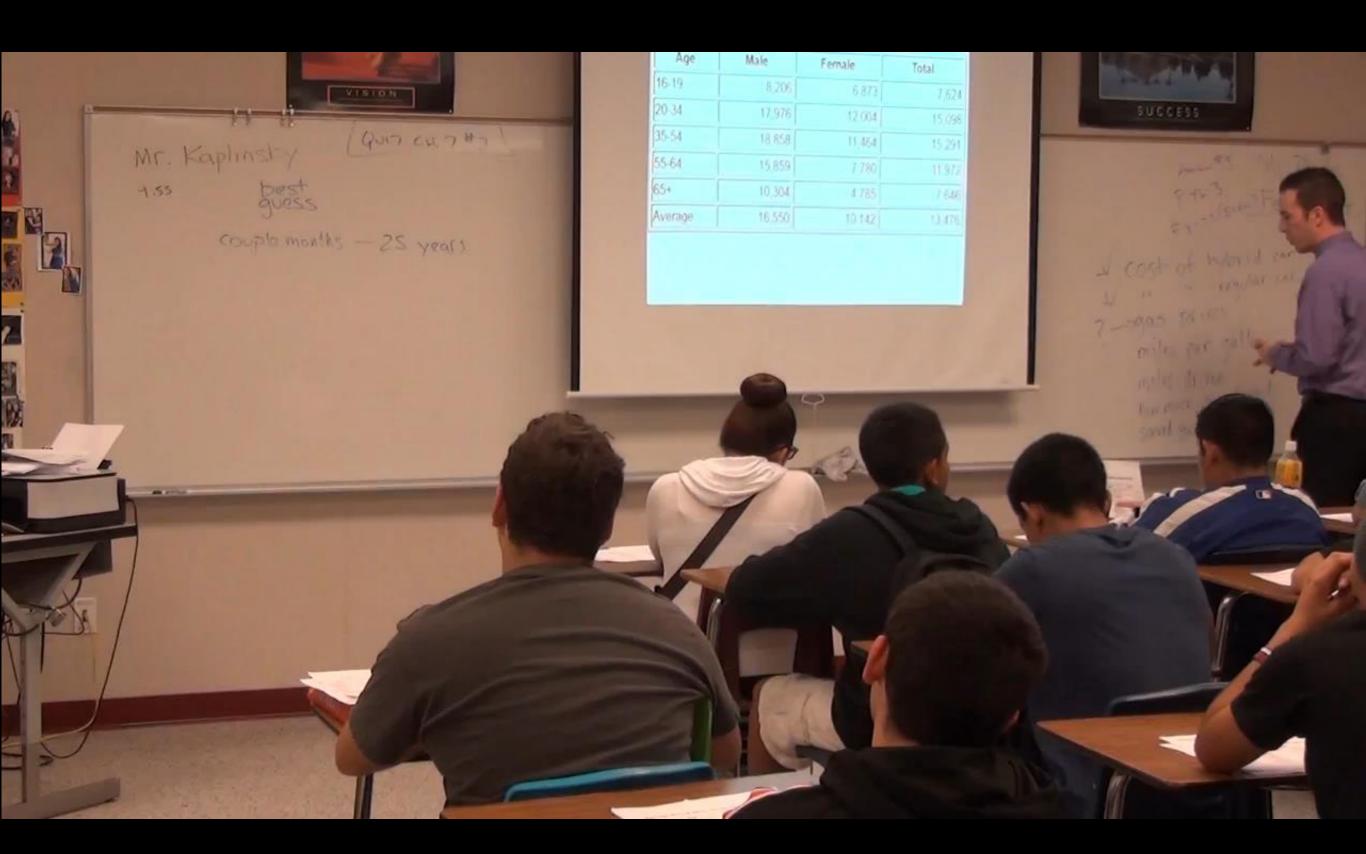




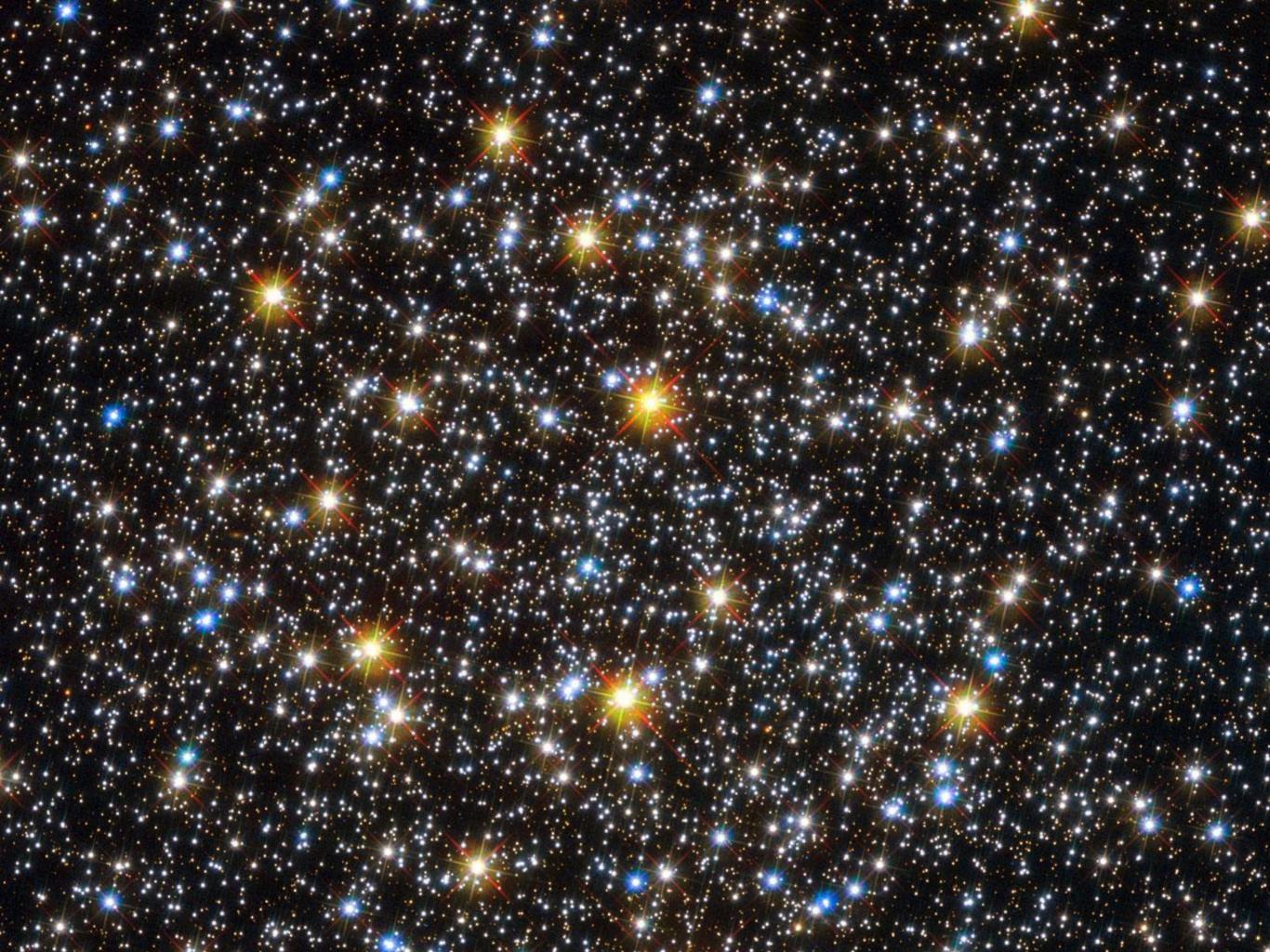


Does a hybrid car boy for itself?



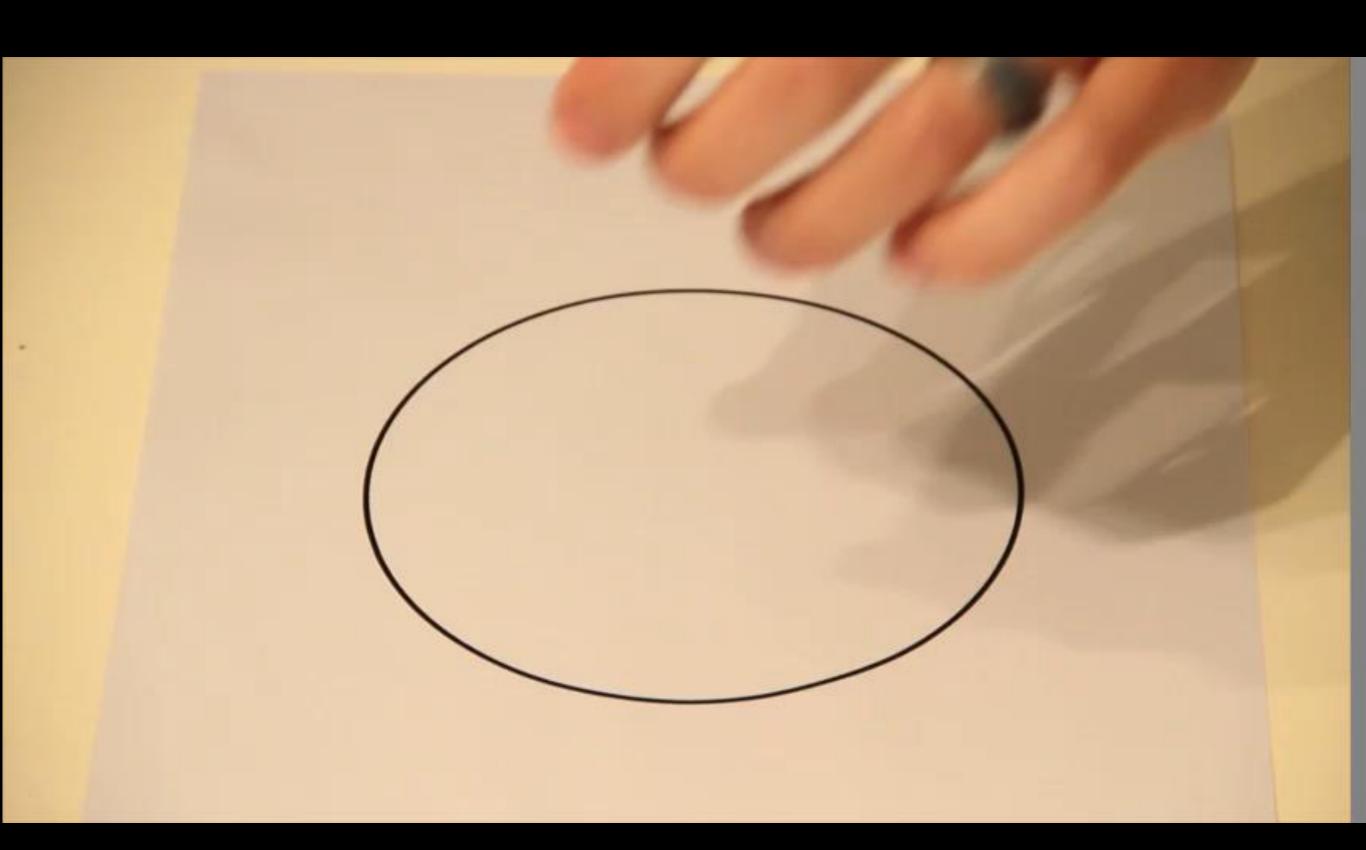






Setting Up The Problem

- What do you do when students ask for data/information I don't have, hadn't considered, or forgot to get?
- What do you do when students ask for information that is probably not important or that they don't actually need?
- What do you do when students don't know what to write for what they know and don't know?
- What do you do when you ask for a guess and they don't know?
- What do you do when they don't ask you for information that they need to solve the problem?



 What do you do when students don't use the strategy you anticipated they would use?





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Overall dimensions: 15 in W x 31 in H x 29-3/4 in D Rough-in dimensions: 12 in

Trapway size: 2 in

Dimensiones generales: 38,10 cm de ancho x 78,74 cm de alto x 75,57 cm de profundidad Dimensiones aproximadas: 30,48 cm Tamaño de canal de sirán: 5,08 cm







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- · ADA approved chair height
- Inodoro de descarga doble de alta eficiencia con descarga de 6,06 litros o 3,79 litros
 Permanece limpio por más tiempo con la superficie EverClean® y la descarga PowerWash™
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 Altura de sila aprobada por ADA







Item | Articulo: 88575 Model | Modelo: 2514.101.020

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Overall dimensions: 15-3/4 in W x 30-3/4 in H x 30-1/4 in D Rough-in dimensions: 12 in

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Dimensiones generales: 40.01 cm de ancho x 78,11 cm de alto x 76,84 cm de profundidad Dimensiones aproximadas: 30,48 cm Tamaño de canal de siñon: 5,24 cm







Smooth-sided toilet design
 Stays cleaner longer with EverClean[®] surface & PowerWash™ flush
 Features No Tools™ installation

· ADA approved chair height

Permanece limpio por más tiempo con la s
Cuenta con instalación No Tools™
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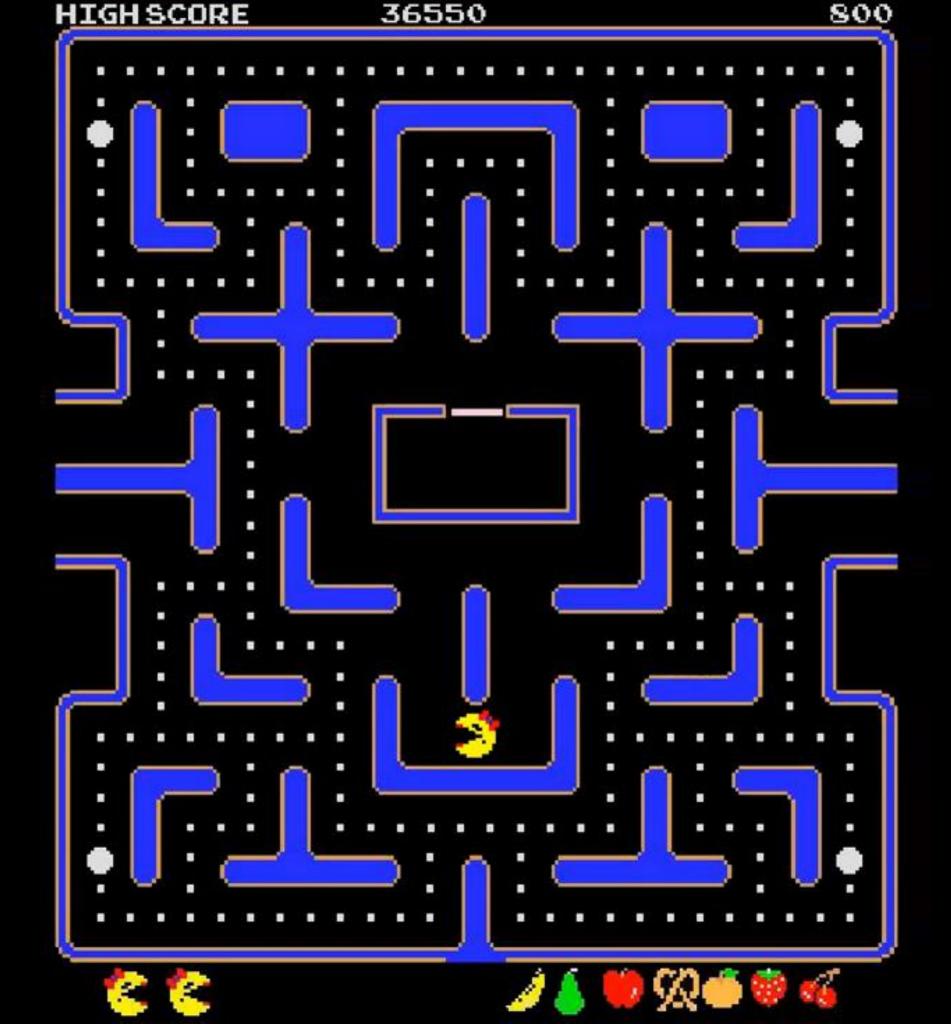
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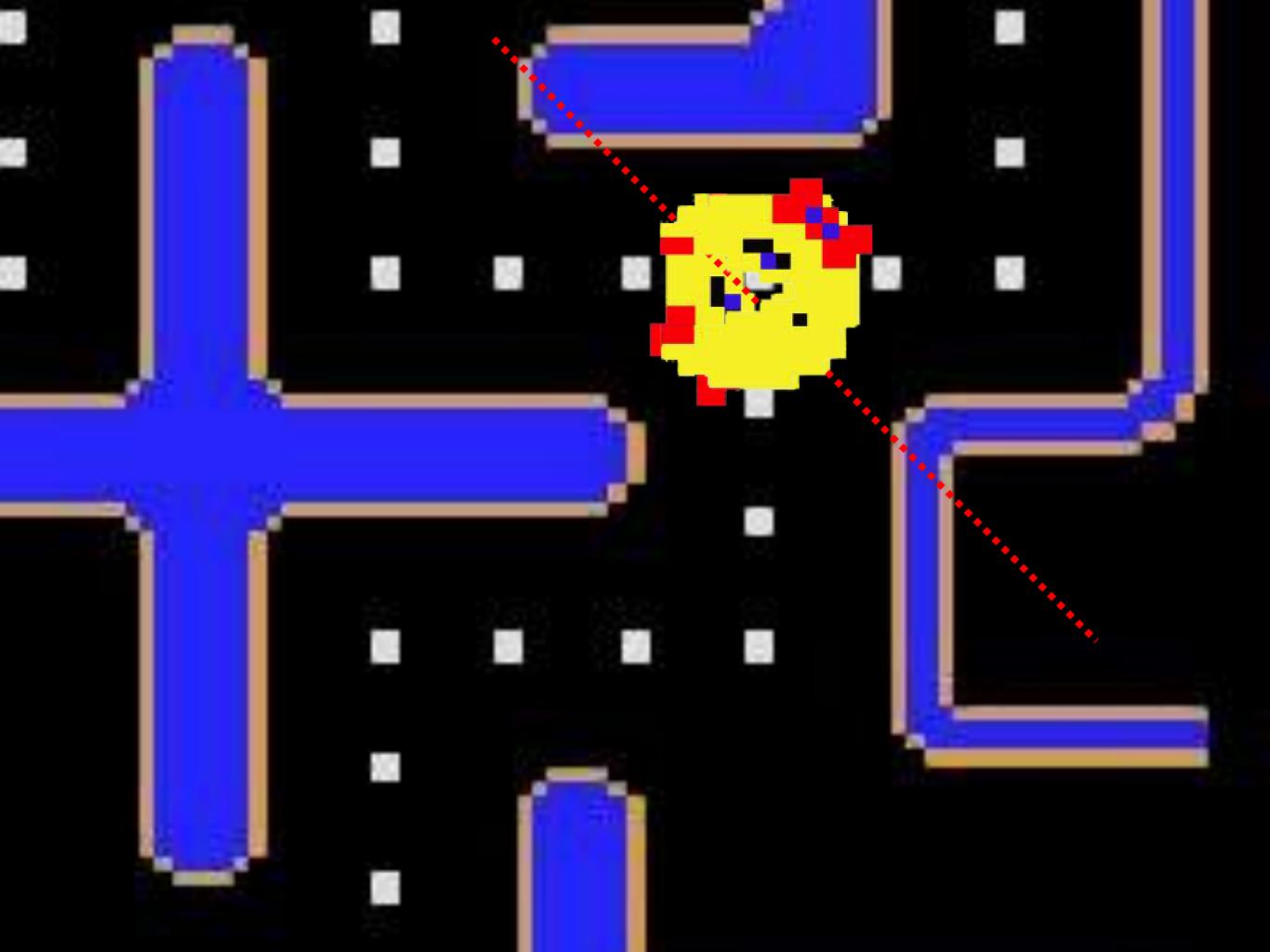


- What do you do when students don't use the strategy you anticipated they would use?
- What do you do when a student comes up with a strategy for solving the problem that I do not understand?











- What do you do when students don't use the strategy you anticipated they would use?
- What do you do when a student comes up with a strategy for solving the problem that I do not understand?
- What do you do when the answer we calculate does not match with the actual answer?
- What do you do when students get stuck during the problem solving process and are not sure what to do?

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- What do you do when students get stuck during the problem solving process and are not sure what to do?
- What do you do when you ask students questions and few to no people are ready to respond?
- What do you do when the student conclusions are low quality and/or effort?



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IA Conclusion each conclusion Each Itemis good for different Items

What is your conclusion? How did you reach that a	。1986年中,中国中国共和国共和国共和国共和国共和国共和国共和国共和国共和国共和国共和国共和国共和国
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23-5=(8)	18 vs 18.40
23-20% = 28,40	'

in store purchase, exclusions

10	Orange Chicken	5.25	F Eggplant with Garlic Sauce	5.25
	Chicken Lo Mein	5.25	✓ Ma Po Tofu	5.25
1	Cashew Nut Chicken	5.25		5.25
-	Pungent Chicken	5.25	String Bean with Garlic Sauce	5.25
	Sweet & Sour Chicken	5.25	Vegetable Delight	5.25
	Curry Chicken	5.25	Bamboo Fungus Tofu	5.25
	Lemon Chicken	5.25	Shrimp with Asparagus	6.25
	Vegetable Chicken	5.25	Shrimp with Lobster Sauce	6.25
	Mongolian Beef	5.25	Fish Fillet with Szuchuan Sauce	6.25
	Broccoli Beef	5.25	Fish Fillet with Black Bean Sauce	6.25
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	Sweet & Sour Pork	5.25	Sweet & Sour Shrimp	6.25



Free topp chiken lomein its pended 125 and not redermand on lunch special dinners and party I tems onein, answour condusions how old you leach thorscondus The 10% coupon is Best with high Prices and small orders is best with the free chicken lamein on chesse war What is your conclusion? How did you reach that conclusion?

You can use the 10% off when you pay 20-2499 or more the free chicken to Mein when you pay 25-49.99 or more and the free orange Chiken when you pay 50 or more

Goals

- Engaging problem solving
 - Real world problem-based learning
 - Higher depth of knowledge problems
- Better implementation
 - Improve our ability to ask questions
 - Practice preparing to implement a lesson
 - Figure out how to deal with uncomfortable situations

Construction

• Pick two:



Fast High Quality

Family

• Pick two:



Kids or Pets

Clean House

Problem-Based Learning

• Pick two:



Student-Centered Learning

Predictability

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