Digging into Depth of Knowledge

ROBERT KAPLINSKY





CCSS.MATH.CONTENT.4.MD.A.3 mand of Apply the area and perimeter formulas for harder or rectangles in real world and mathematical problems. meet the equal intensity, ti of each grade: conceptua skills and fluency, and application.

Source: http://www.corestandards.org/other-resources/key-shifts-in-mathematics/

What is the perimeter of a rectangle that measures 8 units by 4 units?





List the dimensions of a rectangle with a perimeter of 24 units.



Components of Rigor Procedural Skill and Fluency

Conceptual Understanding









List the of a rectangle with a perimeter of 24 units.

Components of Rigor Procedural Skill and Fluency

Conceptual Understanding



Source: http://www.cde.ca.gov/ta/tg/sr/documents/cstrtqmath3.pdf

What is the perimeter of a rectangle **Mathematics** that measures 8 units by 4 units?











Of all the rectangles with a perimeter of 24 units, which one has the most area?

00:00:00:00 Of all the revealed its with a perimeter of 24 units, which one has the mast area?

Components of Rigor Procedural Skill and Fluency

Conceptual Understanding

Defining the Problem

Students appear to demonstrate "deep, authentic command of mathematical concepts" when given commonly used problems. However with more challenging problems, the same students seem to no longer demonstrate that command.

Addressing the Problem

- First, we must have a clear understanding about why these problems are different from one another.
- Next, we need to practice using these problems so that we understand how students may react to them.
- Last, we need a source that can provide us with a variety of free problems.

DOK Distinguishing Between Depth of Knowledge Levels in Mathematics

Topic	Adding Whole Numbers	Money	Fractions on a Number Line	Area and Perimeter	Subtracting Mixed Numbers
CCSS	• 1.NBT.4	 2.MD.8 	• 3.NF.2	• 3.MD.8	• 5.NF.1
Standard(s)	 2.NBT.5 			• 4.MD.3	
DOK 1	Find the sum.	If you have 2	Which point is located at $\frac{7}{12}$	Find the perimeter	Find the difference.
Example		dimes and 3	below?	of a rectangle that	
	44 + 27 =	pennies, how	LM NO	measures 4 units	_1 _2
		many cents	• • • • • • • • • • • • • • • • • • • •	by 8 units.	$5\frac{-}{2}-4\frac{-}{3}=$
		do you have	$0 \frac{1}{2}$ 1		2 5
DOK 2	Fill in the boxes below	Make 47¢ in	Label the point where $\frac{3}{4}$	List the	Create three different mixed
Example	using the whole	three	belongs on the number line	measurements of	numbers that will make the
	numbers 1 through 9,	different	below. Be as precise as	three different	equation true by using the whole
	no more than one time	ways with	possible.	rectangles that	numbers 1 through 9, no more
	each, so that you make	either		each has a	than one time each,. You may
	a true equation.	quarters,		perimeter of 20	reuse the same whole numbers
		dimes,	\leftarrow	units.	for each of the three mixed
	+ 53 =	nickels, or	$\frac{1}{3}$		numbers.
		pennies.			$5\frac{4}{5} - \boxed{3\frac{1}{20}} = 3\frac{1}{20}$
DOK 3	Make the largest sum	Make 47¢	Create 5 fractions using the	What is the	Make the smallest difference by
Example	by filling in the boxes	using exactly	whole numbers 0 through 9	greatest area you	filling in the boxes below using
Example	below using the whole	6 coins with	no more than one time each.	can make with a	the whole numbers 1 through 9.
	numbers 1 through 9,	either	as numerators and	rectangle that has a	no more than one time each.
	no more than one time	quarters,	denominators and correctly	perimeter of 24	
	each.	dimes,	place them all on a number	units?	•••••
		nickels, or	line.		
	= + =	pennies.			

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More free DOK 2 & 3 problems available at openmiddle.com | © 2015 Robert Kaplinsky, robertkaplinsky.com

DOK Distinguishing Between Depth of Knowledge Levels in Mathematics

Topic	Surface Area and Probability		Transformations	Factoring	Quadratics in Vertex		
	Volume			Quadratics	Form		
CCSS	• 6.G.4	• 7.SP.5	• 8.G.1	 A-SSE.3a 	• F-IF.7a		
Standard(s)	• 7.G.6	• 7.SP.7	• G-CO.5				
DOK 1	Find the surface	What is the probability of	Rotate the image below 90°	Find the factors:	Find the roots and		
Example	area of a	rolling a sum of 5 using	counterclockw		maximum of the		
	rectangular prism	two 6-sided dice?	ise and reflect	$2x^2 + 7x + 3$	quadratic equation		
	that measures 3		it across a 🛛 💦 🗸		below.		
	units by 4 units by		horizontal				
	5 units.		line.		$y = -3(x-4)^2 - 3$		
DOK 2	List the	What value(s) have a	List three sequences of	Fill in the blank	Create three		
Example	measurements of	1/12 probability of being	transformations that take pre-	with integers so	equations for		
	three different	rolled as the sum of two	image	that the quadratic	quadratics in vertex		
	rectangular prisms	6-sided dice?	ABCD to	expression is	form that have roots		
	that each has a		image	factorable.	at 3 and 5 but have		
	surface area of 20		A'B'C'D'.		different maximum		
	square units.		Pre-Image Image	$x^2 + x + 4$	and/or minimum		
					values.		
DOK 3	What is the	Fill in the blanks to	What is the fewest number of	Fill the blank by	Create a quadratic		
Example	greatest volume	complete this sentence	transformations needed to take	finding the largest	equation with the		
	you can make with	using the whole numbers	pre-image ABCD to image A'B'C'D'?	and smallest	largest maximum		
	a rectangular	1 through 9, no more	В,	integers that will	value using the		
	prism that has a	than one time each.	A	make the quadratic	whole numbers 1		
	surface area of 20			expression	through 9, no more		
	square units?	Rolling a sum of on		factorable.	than one time each.		
		twosided dice is the					
		same probability as rolling	► В V	$2x^2 + 3x + _$	$y = - \left[(x - \left[\right])^2 + \right]$		
		a sum of on two	Pre-Image Image				
		sided dice.					

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Complicated or Complex?

Gookie Monster Gupcakes



DOK Verb Wheel

Source: Unknown



DOK Flowchart for Questions



Source: Tracy Watanabe - @tracywatanabe



DOK 2								
Conce	ptual	Thinking						
Can you explain how								
compare	classify	categorize						
measure	graph	distinguish						
predict	modify	construct						
interpret	make ob	servations						
DOK 4								
Extend	ded Re	easoning						

- Write a research paper.
- What information can you gather to support your idea
- about ?
- Write a thesis, drawing conclusions from multiple sources.
- Apply information from one text to another to develop an persuasive argument.

design	connect	prove
analyze	critique	synthesize
create	apply con	ncepts

DOK Posters

Source: Penny Lund http://isntitelementary.blogspot.com/

Created by Penny Lund 2013

DOK Level Differences

Level 1: Recall & Reproduction

- Often a trivial application of facts.
- Generally requires little to no cognitive effort beyond remembering the right formula.
- Usually only one answer.

Level 2: Skills & Concepts

- Usually requires more than one step to solve.
- Often multiple answers.

Level 3: Strategic Thinking

- Usually requires critical thinking about the best way to approach a problem.
- May be multiple answers or a single optimal answer.
- Often challenging enough to make your head hurt.

Level 4: Extended Thinking

In mathematics these are generally represented by performance tasks or problem-based lessons.

Probability What is the probability of rolling a sum of 5 using two 6sided dice?

Probability What value(s) have a $\frac{1}{12}$ probability of being rolled as the sum of two 6-sided dice?

Author: Daniel Luevanos

Probability

Fill in the blanks to complete this sentence using the whole numbers 1 through 9, no more than one time each.

Rolling a sum of _____ on two _____-sided dice is the same probability as rolling a sum of _____ on two _____-sided dice.

Authors: Audrey Mendivil, Daniel Luevanos, and Robert Kaplinsky





Make the largest sum by filling in the boxes below using the whole numbers 1 through 9, no more than one time each.









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ave

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 difference. OMP are designed to learn important math. BT are
 designed to trick!
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Adding Decimals

Use the numbers 1 through 9, exactly one time each, to fill in the boxes and make three decimals whose sum is as close to 1 as possible.





Fourth attempt: Points: /2 explanation /2 attempt tematic St notionalaxe S\ 10110110 21 What did you learn from this attempt? How will your strategy change on your next attempt? The perimeter is 24, but the alreg is it and Strategy: use #'s with more than one row. Fifth attempt: Points: ____/2 attempt /2 explanation ris /2 offengt /2 explorention Second attempt What did you learn from this attempt? How will your strategy change on your next attempt? What did you learn from this oftempt? How will your strategy change on your next atten

DOK FAQ

- When will students ever use this?
- What DOK level should I start students off with?
- How do teachers fit these problems into their pacing?
- How do I help prevent students from giving up after trying the problem once or twice?
- Where can I find other DOK 2 and DOK 3 problems or submit ones I've made?

Open Middle Challenging math problems worth solving

Number & Operations—Fractions (2)

Directions: In a standard game of BINGO, the cards are labeled with numbers 1 through 75. If it was possible, which card would you choose: a card with all of the same number or a standard bingo card? Source: Nanette

Open Middle Challenging math problems worth solving

Home	Kinder 🔻	Grade 1 🝷	Grade 2 🔻	Grade 3 🔻	Grade 4 🔻	Grade 5 🔻	Grade 6 🔻	Grade 7 🔻	Grade 8 🔻	High School 🔻	About	Submit
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Total Open Middle Problems

Open Middle Author Percentages

Open Middle Author Percentages

Problems by DOK Level

DOK 2

DOK 1

DOK 3

Note: Data as of February 2016

Problems by Grade Band

9-12

Note: Data as of February 2016

Rigor refers to deep, authentic command of mathematical concepts, not making math harder or introducing topics at earlier grades. To help students meet the standards, educators will need to pursue, with equal intensity, three aspects of rigor in the major work of each grade: conceptual understanding, procedural skills and fluency, and application.

Source: http://www.corestandards.org/other-resources/key-shifts-in-mathematics/

Call to Action

- Commit to one of these choices:
 - Implement a single DOK 2 or DOK 3 problem from openmiddle.com in your classes within the week.
 - Put a DOK 2 question from openmiddle.com on your next assessment.

