CHALLENGING PROBLEMS

WORTH SOLVING

ROBERT KAPLINSKY

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@robertkaplinsky

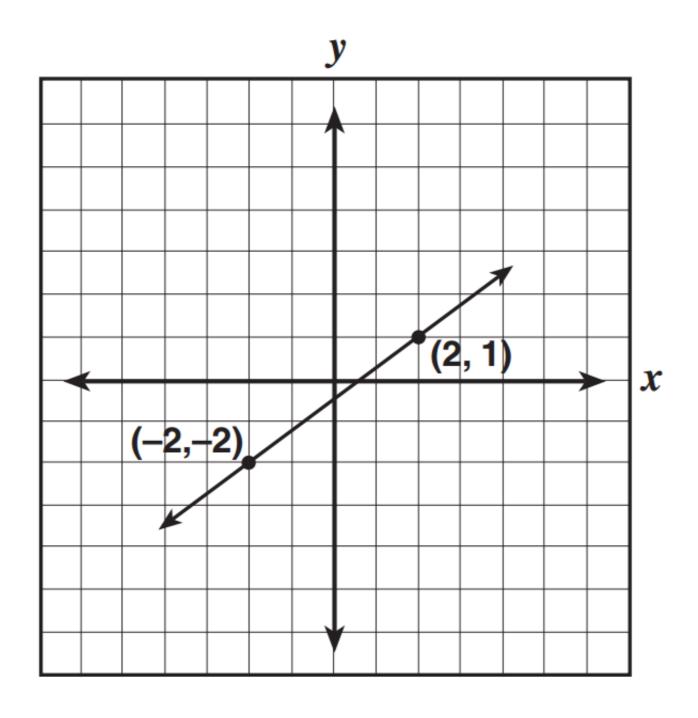


GOALS

- ☐ WHY DO WE NEED THEM?
- **WHY ARE THEY DIFFERENT?**
- ☐ HOW DO YOU IMPLEMENT THEM?
- ☐ HOW DO YOU CREATE YOUR OWN?
- ☐ WHERE DO YOU GET OTHERS?

				Mathematics Clusters									
						(Clus	ters where th	e percent cor	ect is shown	in bold repres	sent proficien	cy for that clu	ıster.)
								Quant	itative				
								relations	ships and	Multi-step	problems,		
						Exponent	s, powers,	evalu	ıating	graphi	ng, and	Measure	ment a
				Rational	numbers	and	roots	expre	ssions	func	tions	geor	metry
		Perf.	Scaled	Number	Percent	Number	Percent	Number	Percent	Number	Percent	Number	Perc
Student Name	ID Number	Level	Score	Correct	Correct	Correct	Correct	Correct	Correct	Correct	Correct	Correct	Con
KON, KITHE	575,058	ADV	476	13	93%	8	100%	8	80%	14	93%	12	92
acception, research at	572560	ADV	464	13	93%	7	88%	8	80%	15	100%	11	85
Marcallo, San Charles	575540	ADV	453	10	71%	8	100%	10	100%	14	93%	11	85
RESEA, DECREA	100,7567	ADV	453	13	93%	8	100%	9	90%	12	80%	11	85
CHECKS, C. SECTION	17862	ADV	444	14	100%	7	88%	8	80%	13	87%	10	77
THERMAN, MICH.	57,7940	ADV	444	12	86%	8	100%	8	80%	15	100%	10	77
HUNCHLA, DARRIE	100000	ADV	444	13	93%	8	100%	8	80%	14	93%	9	69
SECURE, SCORE	1007740	ADV	435	12	86%	6	75%	9	90%	14	93%	10	77
ROSC, ADROVA	579804	ADV	435	12	86%	6	75%	8	80%	14	93%	11	85
SHEETE, MITTER	17,0940	ADV	435	13	93%	7	88%	9	90%	12	80%	10	77
BOARDON, SERVICE	576000	ADV	427	13	93%	6	75%	9	90%	12	80%	10	77
CHARGO, UNK	1771088	ADV	427	13	93%	7	88%	6	60%	13	87%	11	85
HOME BROKET	1000	ADV	427	14	100%	5	63%	7	70%	14	93%	10	77
ACCRETA, DANSES.	Maria and the	ADV	421	13	93%	6	75%	6	60%	14	93%	10	77
MINISTER, MINISTER	800,004	ADV	421	11	79%	5	63%	9	90%	13	87%	11	85
HARCIL, HARCIDA	17,080,08	ADV	414	12	86%	6	75%	8	80%	11	73%	11	85
BETTE, THEO, THE	572300	ADV	414	12	86%	8	100%	8	80%	13	87%	8	62
BANKS, SPERMIT	17 (1988)	PRO	408	11	79%	6	75%	9	90%	11	73%	10	77
ACTION, SECTION	577274	PRO	402	12	86%	8	100%	9	90%	8	53%	11	85
SUPERIOR CO., ADMINISTRA	572796	PRO	402	8	57%	7	88%	8	80%	13	87%	10	77
RETRIENCE, GRACE	572796	PRO	402	13	93%	6	75%	7	70%	13	87%	8	62
DESCRIPTION OF STREET	572 995	PRO	402	11	79%	5	63%	7	70%	11	73%	12	92
ALTERNATION AND THE	572998	PRO	402	13	93%	7	88%	9	90%	10	67%	7	54
ROBERT SERVICE SERVICES	5729605	PRO	402	13	93%	7	88%	7	70%	11	73%	8	62
AUTHOR, DANSOLA	9907536	PRO	396	10	71%	6	75%	9	90%	14	93%	7	54
MICA, HICHMON	572400	PRO	396	12	86%	8	100%	6	60%	9	60%	11	85
MINERAL DANSE.	575385	PRO	380	10	71%	7	88%	8	80%	11	73%	7	54
NAMED OF TAXABLE PARTY.	577567	PRO	375	14	100%	5	63%	6	60%	10	67%	6	46
MARKET, TOWNS	1007000	PRO	375	8	57%	7	88%	8	80%	11	73%	8	62
	6000700.2	PRO	375	10	71%	5	63%	8	80%	11	73%	8	62
STREET, SCHOOLS	57,7803	PRO	375	12	86%	4	50%	6	60%	12	80%	7	54

What is the slope of this line?



- $\mathbf{A} = \frac{1}{2}$
- $\mathbf{B} = \frac{3}{4}$
- **C** 1
- $\mathbf{D} = \frac{4}{3}$



			Mathematics Clusters									
				(Clusters where the percent correct is shown in bold represent proficiency for that cluster.)								
							Quant	itative				
							relations	ships and	Multi-step	problems,		
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			Rational	numbers	and	roots	expre	ssions	func	tions	geoi	metry
	Perf.	Scaled	Number	Percent	Number	Percent	Number	Percent	Number	Percent	Number	Perc
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MORE, METHER, STAGE	ADV	476	13	93%	8	100%	8	80%	14	93%	12	92
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Manager, convictions 5759	ADV	453	10	71%	8	100%	10	100%	14	93%	11	85
60°01, 240'0604 5675	ADV	453	13	93%	8	100%	9	90%	12	80%	11	85
CHARLES OF THE PARTY OF T	ADV	444	14	100%	7	88%	0	000/	13	87%	10	77
Transferring, Million P.				86%	8					%	10	77
										6	9	69
										<i>√</i> / ₀	10	77
				U						93%	11	85
	ADV			3%						80%	10	77
MONANCE CO. SERVICE	ADV			93%			D			80%	10	77
	VOV			93%						87%	11	85
				100%	5					93%	10	77
				93%	6					93%	10	77
				79%	5					87%	11	85
			12	86%	6				1	73%	11	85
MCCCC, TORONO COM			12	86%	8	100%			13	87%	8	62
Appetical, Commander	PRO	408	11	79%	6	75%	9	90%	11	73%	10	77
ALTHROUGH STOP	PRO	402	12	86%	8	100%	9	90%	8	53%	11	85
CONTRACTOR AND ADMINISTRAL P.	PRO	402	8	57%	7	88%	8	80%	13	87%	10	77
HERMANICO, GRACE \$757	PRO	402	13	93%	6	75%	7	70%	13	87%	8	62
AMERICANA, CASCATTON	PRO	402	11	79%	5	63%	7	70%	11	73%	12	92
ROMEOUT, MARKET \$750.	PRO	402	13	93%	7	88%	9	90%	10	67%	7	54
Bollow, Calle, Garrelle Trans.	PRO	402	13	93%	7	88%	7	70%	11	73%	8	62
ALTHOUGH THEFTILE	PRO	396	10	71%	6	75%	9	90%	14	93%	7	54
MISSA, HECHARD, STORY	PRO	396	12	86%	8	100%	6	60%	9	60%	11	85
MINISTRA, DANIEL. STORY	PRO	380	10	71%	7	88%	8	80%	11	73%	7	54
ALLEGO PARKETON TO STORY	PRO	375	14	100%	5	63%	6	60%	10	67%	6	46
Married Marrie	PRO	375	8	57%	7	88%	8	80%	11	73%	8	62
SCHOOL CONTRACTOR CONT	PRO	375	10	71%	5	63%	8	80%	11	73%	8	62
STATE OF THE PARTY NAMED IN COLUMN 1979	PRO	375	12	86%	4	50%	6	60%	12	80%	7	54

GOALS

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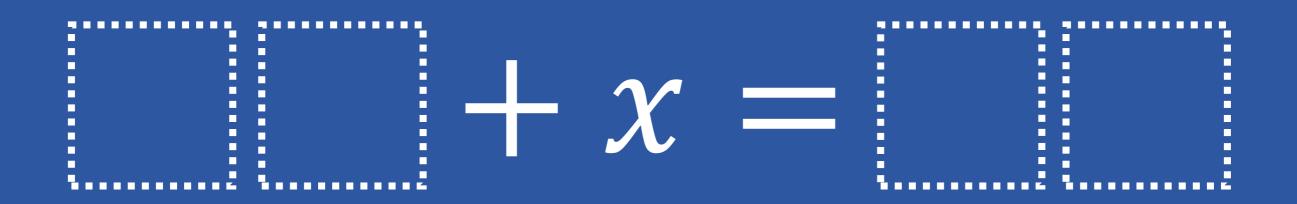
PROBLEM ONE

Solve for x.

$$21 + x = 70$$

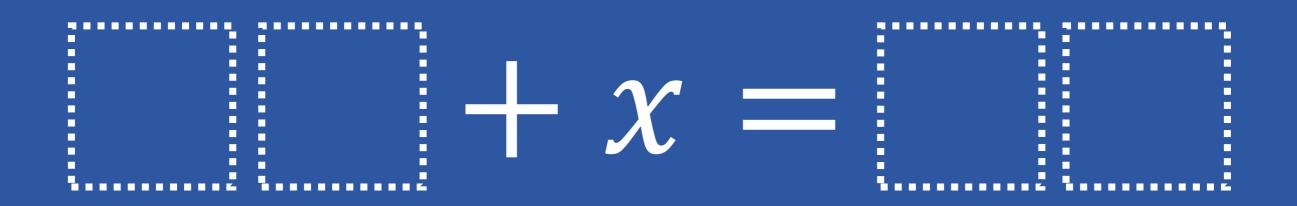
PROBLEM TWO

Using the digits 1 to 9, at most one time each, create two equations: one where x has a positive value and one where x has a negative value.



PROBLEM THREE

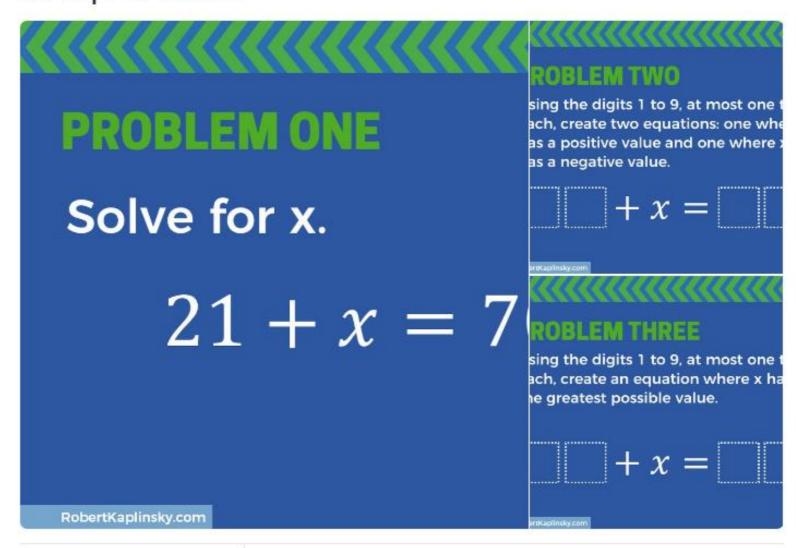
Using the digits 1 to 9, at most one time each, create an equation where x has the greatest possible value.





MS & HS #MTBoS Ts, please ask your Ss these 3 ?s and put the % who answered correctly here:

docs.google.com/forms/d/e/1FAI Answers at top of form.



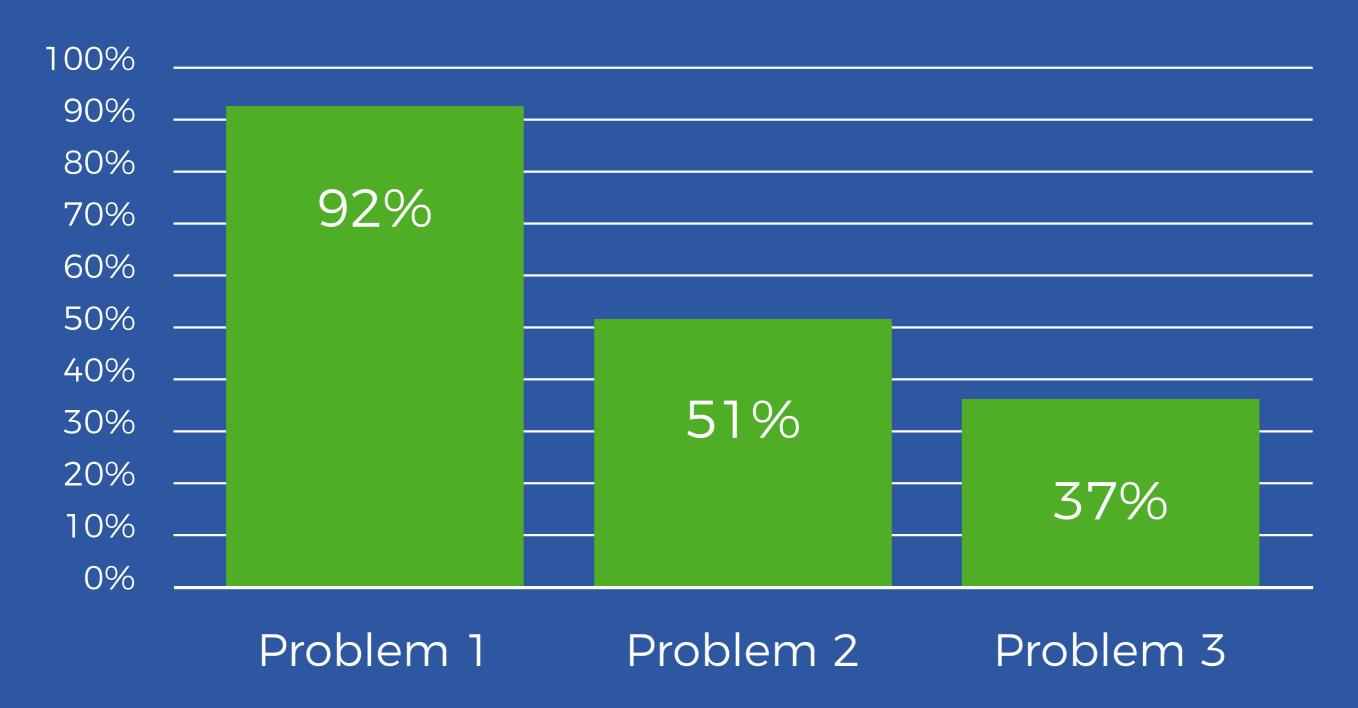








PROBLEM RESULTS



Depth of Knowledge Matrix - Secondary Math

Topic	Dividing Fractions	Solving One-Step Equations	Exponents	Solving Equations with
				Variables on Both Sides
CCSS	• 6.NS.1	• 7.EE.4a	• 8.EE.1	• 8.EE.8
Standard(s)				A-REI.3
DOK 1	Evaluate.	Solve for x.	Evaluate.	Solve for x.
Example	$\frac{4}{9} \div \frac{2}{5}$	21 + x = 70	3 ⁴	3x + 2 = -2x + 4
DOK 2 Example	Use the digits 1 to 9, at most one time each, to fill in the boxes to make two different pairs of fractions that have a quotient of $2/3$. $\frac{2}{3} \div \frac{2}{3}$	Use the digits 1 to 9, at most one time each, to create two equations: one where x has a positive value and one where x has a negative value.	Use the digits 1 to 9, at most one time each, to fill in the boxes to make two true number sentences. = 64	Use the digits 1 to 9, at most two times each, to fill in the boxes to make an equation with no solutions. $x + y = x + y$
DOK 3 Example	Use the digits 1 to 9, at most one time each, to fill in the boxes to make two fractions that have a quotient that is as close to 4/11 as possible.	Use the digits 1 to 9, at most one time each, to create an equation where x has the greatest possible value. $+ x =$	Use the digits 1 to 9, at most one time each, to fill in the boxes to make a result that has the greatest value possible.	Use the digits 1 to 9, at most one time each, to fill in the boxes so that the solution is closest to zero. $x + y = x + y$



Depth of Knowledge Matrix - Secondary Math

Topic	Geometric Proofs	Complex Numbers	Trigonometric Functions	Definite Integral
CCSS	• G-CO.11	• N-CN.2	• F-TF.3	• N/A
Standard(s)				
DOK 1	Add one geometric marking to	Multiply the binomials.	Evaluate.	Solve.
Example	demonstrate the quadrilateral			
	is a square.	(3+4i)(2+3i)	$\sin\frac{\pi}{3}$	$\int_{2}^{6} x^{3} dx$
DOK 2	Use exactly 5 geometric	Use the integers -9 to 9, at	Use the digits 1 to 9, at most	Use the digits 1 to 9, at most
Example	markings to show that a	most one time each, to fill in	one time each, to fill in the	one time each, to fill in the
	quadrilateral is a square.	the boxes twice: once to make	boxes and make two true	boxes and make a positive and
		a positive real number product	number sentences.	a negative solution.
		and once to make a negative real number product. $(+ i)(+ i)$	$\sin\frac{\pi}{\pi} = 1$	$\int_{-\infty}^{\infty} x^{-1} dx$
DOK 3	What is the least number of	Use the integers -9 to 9, at	Use the digits 1 to 9, at most	Use the digits 1 to 9, at most
Example	geometric markings needed to	most one time each, to fill in	one time each, to fill in the	one time each, to fill in the
	demonstrate that a	the boxes and make a real	boxes to make two true	boxes and make a solution
	quadrilateral is a square?	number product with the	number sentences.	that is as close to 100 as
		greatest value. $ (+ i) (+ i) $	$\sin\frac{\pi}{\pi} = \frac{\sqrt{\pi}}{\pi}$	possible. $\int_{-\infty}^{\infty} x^{-1} dx$



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IMPLEMENTATION

Open Middle Worksheet

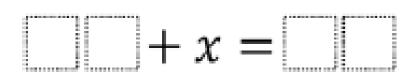
First attempt:	Points:	/2 attempt	/2 explanation
What did you learn from this attended in the next attempt?	empt? Hov	v will your strat	tegy change on your

IMPLEMENTATION

- Open Middle Worksheet
- Classwork
 - Single problem for entire class
 - Extensions menu

QUESTION#1

Use the digits 1 to 9, at most one time each, to create an equation where x has the greatest possible value.



4 points

QUESTION#4

Use the digits 1 to 9, at most one time each, to make each equation true.

QUESTION #2

Solve for x.

$$3x + 7 = 19$$

1 point

SOLVING EQUATIONS EXTENSION MENU

You must earn <u>at least 12</u>
<u>points</u> by doing the
problems of your choice.
Circle the questions you
have answered.

QUESTION #3

Use the digits 1 to 9, at most one time each, to create two equations: one where x has a positive value and one where x has a negative value.

$$+x=$$
 2 points

OUESTION #5

Use the digits 1 to 9, at most one time each, to create an equation where x has the greatest possible value.

/ mainte

IMPLEMENTATION

- Open Middle Worksheet
- Classwork
 - Single problem for entire class
 - Extensions menu
- Homework
- Assessments

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STEP ONE

- Find a One-Operation Problem
 - Addition
 - Subtraction
 - Multiplying
 - Dividing
 - Exponents (including square root)
 - Trigonometric functions

ADDING 2-DIGIT NUMBERS Solve.

$$41 + 36 =$$

MULTIPLYING FRACTIONS

Solve.

TRIGONOMETRY

Solve.

$$\sin\frac{\pi}{3} =$$

STEPTWO

- Go from DOK 1 to DOK 2
 - Strategically remove some information from the problem to prevent immediate calculation
 - Increase the quantity of solutions needed to increase the need to look for patterns

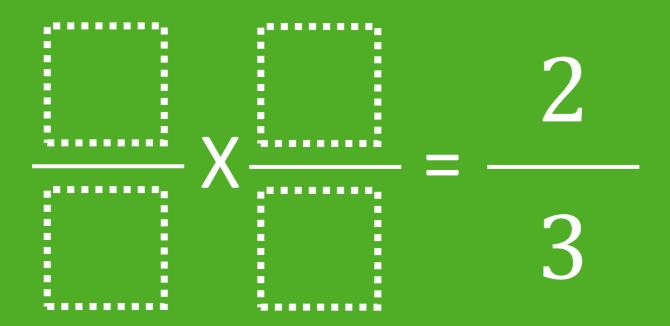
ADDING 2-DIGIT NUMBERS

Using the digits 1 to 9, at most one time each, fill in the boxes to make two different pairs of two-digit numbers that have a sum of 71.

$$+ = 71$$

MULTIPLYING FRACTIONS

Using the digits 1 to 9, at most one time each, fill in the boxes to make two different pairs of fractions that have a product of 2/3.



TRIGONOMETRY

Using the digits 1 to 9, at most one time each, fill in the boxes to make two true number sentences.

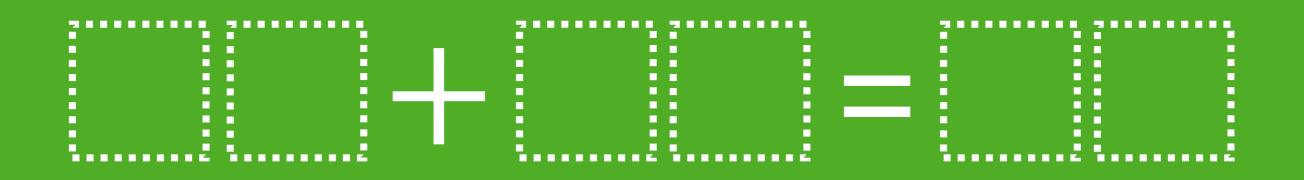
$$\sin \frac{\pi}{\pi} = 0$$

STEP THREE

- Go from DOK 2 to DOK 3
 - Introduce the need to optimize the solution by making the greatest or least product / sum / difference / quotient / answer.
 - Another optimization option is make the answer closest to a specific value.

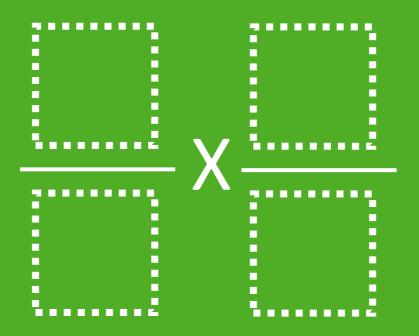
ADDING 2-DIGIT NUMBERS

Using the digits 1 to 9, at most one time each, fill in the boxes to make the smallest sum.



MULTIPLYING FRACTIONS

Using the digits 1 to 9, at most one time each, fill in the boxes to make two fractions that have a product that is as close to 4/11 as possible.



TRIGONOMETRY

Using the digits 1 to 9, at most one time each, fill in the boxes to make two true number sentences.

$$\sin \frac{\pi}{\pi} = \frac{\sqrt{\pi}}{\pi}$$

3 Steps to Increase Math DOK Levels

Step 1: Find a One-Operation Problem

- Procedural problems with one operation are easiest to modify.
- Other problems may also be modified but may not be as easy.

Adding 2-Digit Numbers Solve.

Multiplying Fractions
Solve.

$$\frac{3}{7} \times \frac{2}{9} =$$

Trigonometry

$$\sin\frac{\pi}{3} =$$

Step 2: Go from DOK 1 to DOK 2

- Strategically remove some information from the problem to prevent immediate calculation
- Increase the quantity of solutions needed to increase the need to look for patterns

Adding 2-Digit Numbers
Using the digits 1 to 9, at most one time each, fill in the boxes to make two different pairs of two-digit numbers that have a sum of 71.

Multiplying Fractions
Using the digits 1 to 9, at most one time each, fill in the boxes to make two different pairs of fractions that have a product of 2/3.

$$x = \frac{2}{3}$$

Trigonometry

Using the digits 1 to 9, at most one time each, fill in the boxes to make two true number sentences.

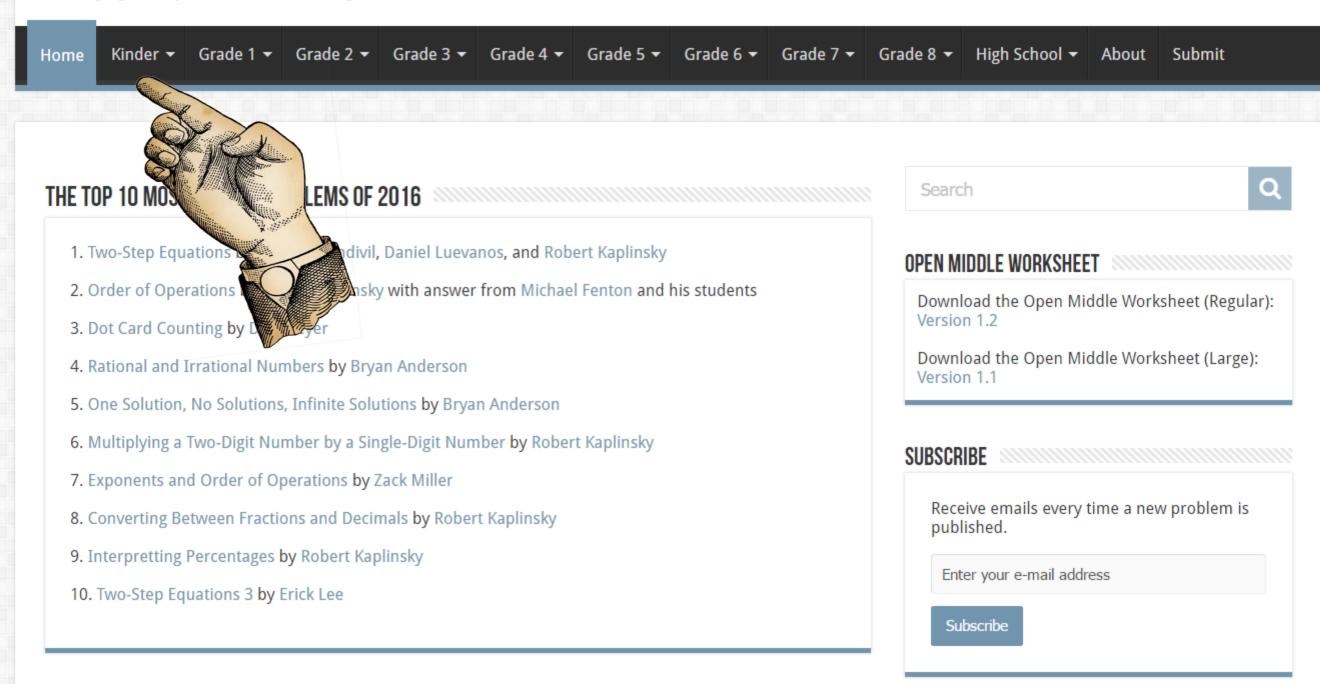
$$\sin\frac{\pi}{\pi} = 0$$

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Open Middle

Challenging math problems worth solving



WHAT ARE PEOPLE SAYING ABOUT OPEN MIDDLE?





Have you checked out openmiddle.com @openmiddle Should

BROWSE BY COMMON CORE STATE STANDARDS

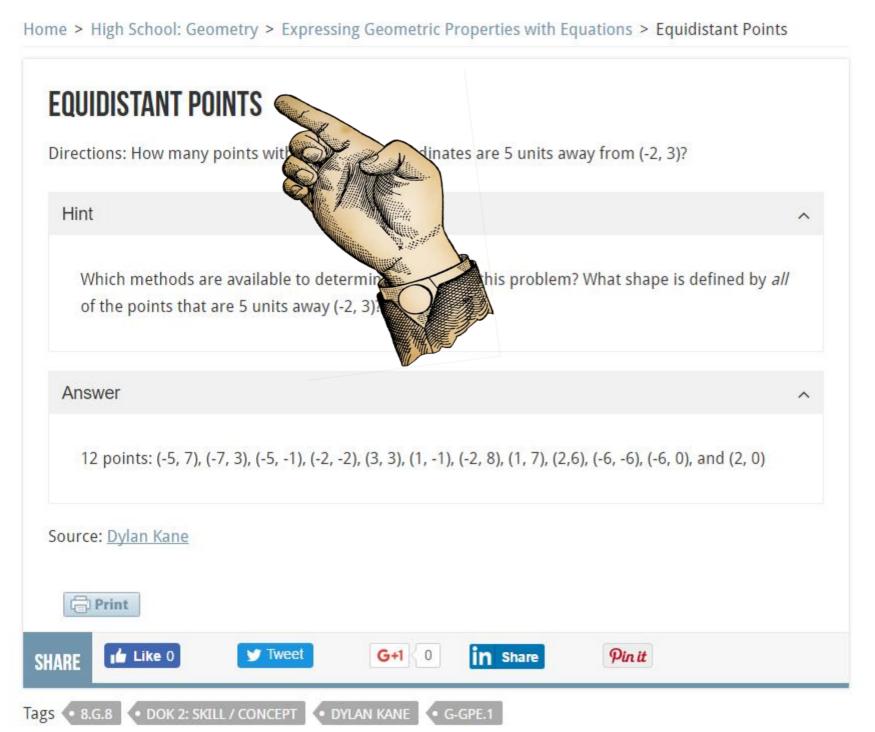
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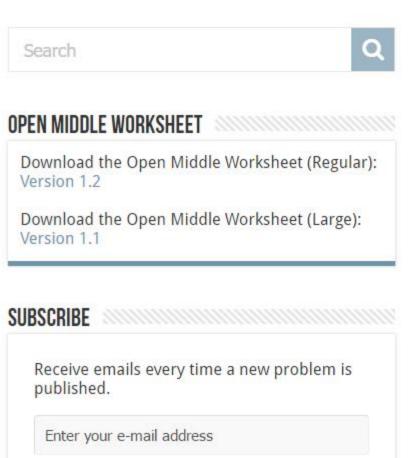
- Counting & Cardinality (2)
- □ Number & Operations in Base Ten (1)
- Operations & Algebraic Thinking (3)

Open Middle

Challenging math problems worth solving

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Home



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How I Can Help You



Real World Problems

My workshops help teachers implement problem-based lessons by helping them experience them from both student and teacher perspective, leading to increase students' success



Depth of Knowledge

Problems at higher depth of knowledge levels have the potential to challenge the most gifted students yet remain accessible to struggling students. I can help teachers develop best practices for

What People Are Saying

Robert was a dynamic trainer who presented information in an unassuming, learner-centered way, allowing teacher participants to think about their own teaching and apply the new strategies accordingly. Throughout the two days, Robert modeled sound instructional strategies as he explained the why, the what, and the how of implementing this approach to math instruction. He provided research-based excerpts, short videos, and



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States, enter your zip code and I'll use it
to let you know about events near you.
First Name
Last Name
Email address
Zip Code

How Can We Make Stronger

Passwords?





How Many Chip Bags Will There

Be?

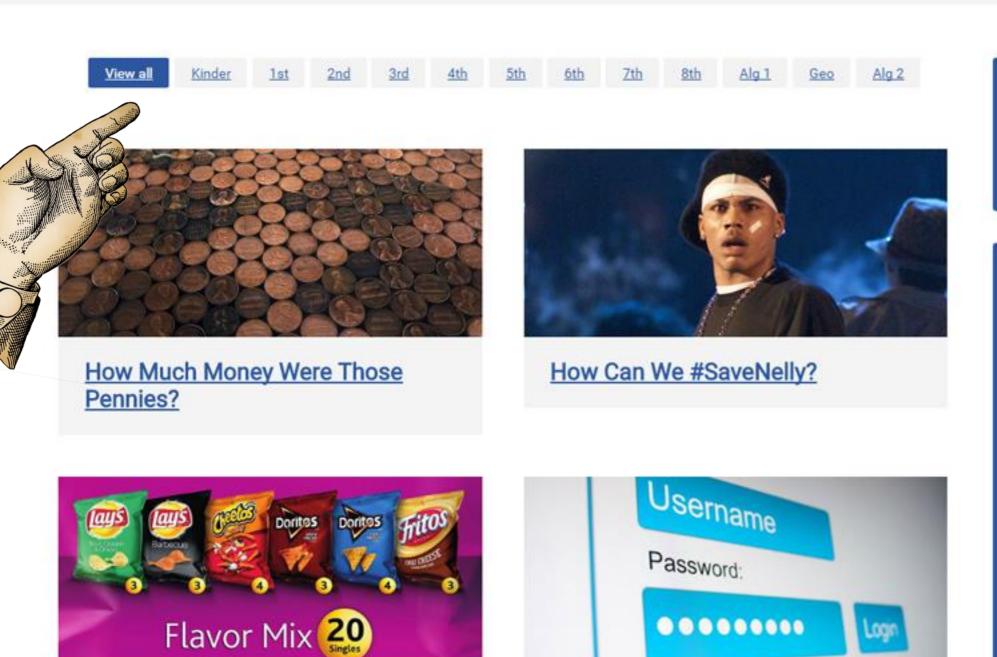
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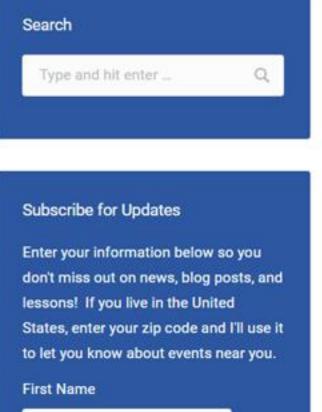
Last Name

Email address

Zip Code

Lessons





CHALLENGING PROBLEMS

WORTH SOLVING

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