

WHAT DO WE KNOW ABOUT EDUCATION?

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paradigm shift

142

FAIRBANKS CITY TRANSIT SYSTEM





GOALS

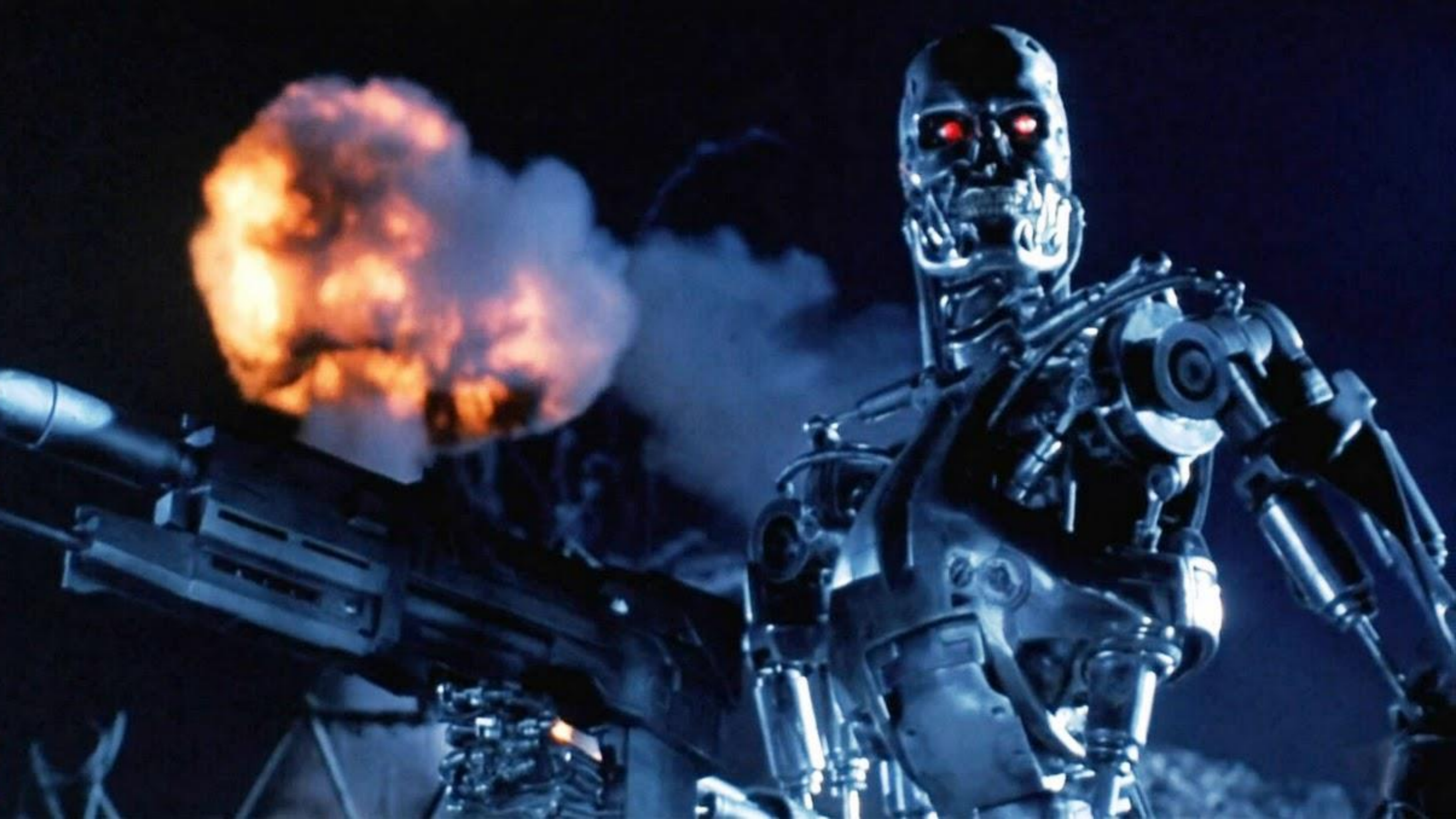
WHAT IS INTELLIGENCE?

WHY DON'T STUDENTS REMEMBER?

WHAT MATHEMATICS IS IMPORTANT?

WHAT MIGHT IT LOOK LIKE?

WHAT ABOUT WHAT WE USED TO DO?





11 a 12 a 13 o i 14 a i 15 o i 16 b 17 f

21 k 22 d 23 v 24 o i 25 m 26 f 27 g

31 f 32 i 33 i o 34 i j 35 k 36 l 37 m

41 w 42 o 43 o 44 g 45 a 46 e 47 f

54 p 55 p 56 p 57 l

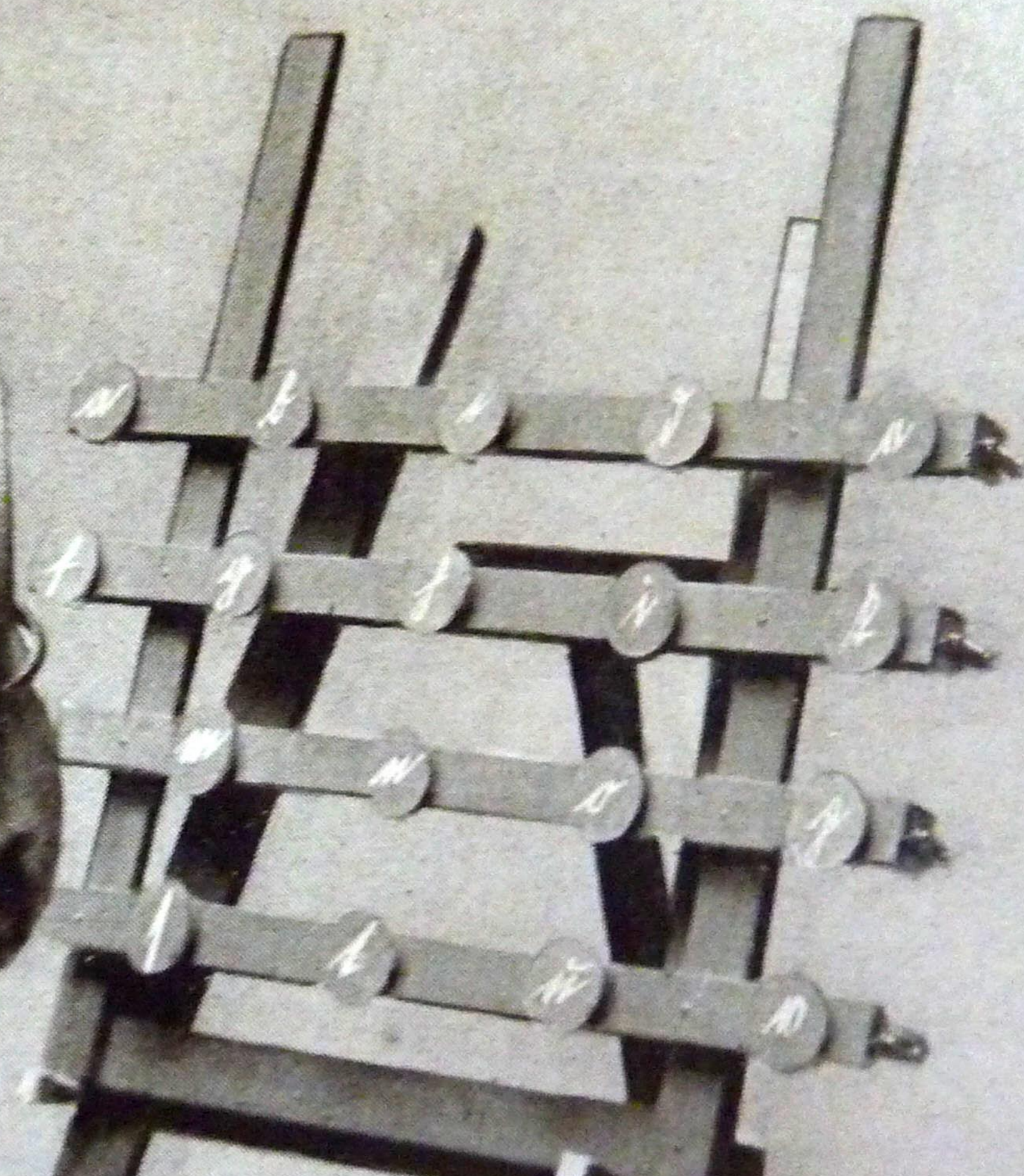
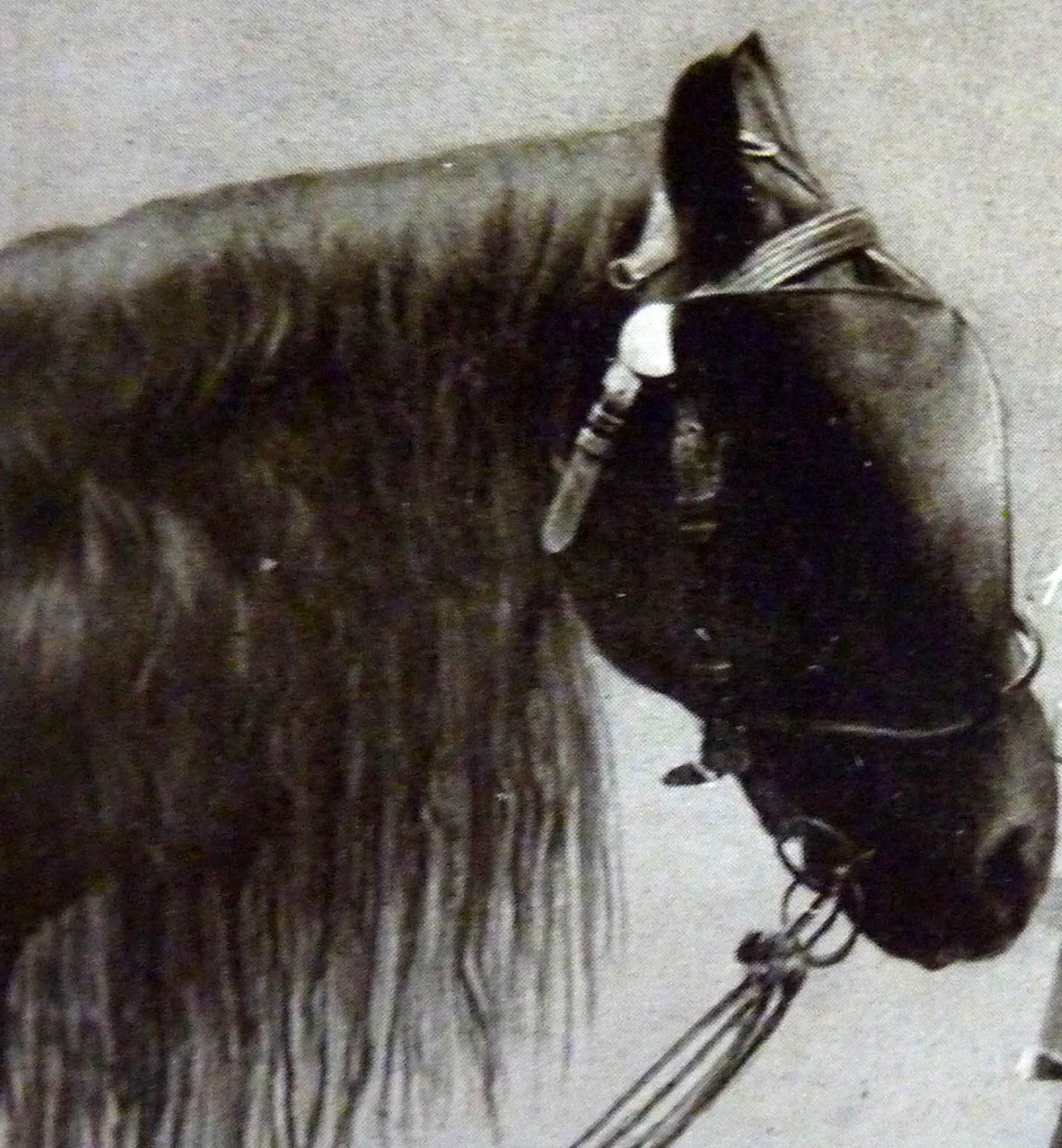
64 o 65 a 66 a 67 g

$$\frac{2}{3} + \frac{3}{4} =$$

$$26743 : 8 =$$

$$712986 \times 3 =$$

Handwritten text on the white saddle cloth, possibly a name or number, which is partially obscured and difficult to read.





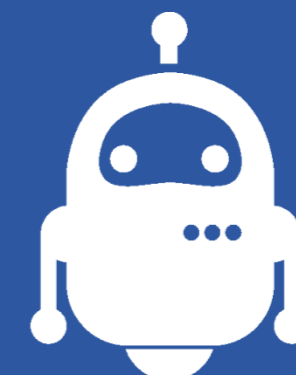


Yes... no... uh...

yes... maybe?

MANY STUDENTS

TURING TEST



CHINESE ROOM



见体配字母的常套



见体配字母的常套

DISCUSSION QUESTIONS

- What does intelligence even mean?
- How do we ask questions that measure intelligence?
- Will the tasks that work now always be Chinese room and horse proof?

GOALS

WHAT IS INTELLIGENCE?

WHY DON'T STUDENTS REMEMBER?

WHAT MATHEMATICS IS IMPORTANT?

WHAT MIGHT IT LOOK LIKE?

WHAT ABOUT WHAT WE USED TO DO?



February 28 · [Profile Picture]



If a thief forces you to take money out of an ATM, do not argue or resist. What you do is punch in your pin # backwards. EX: if its 1234, you'll type 4321. When you do that, the money will come out but will be stuck in the slot. The machine will immediately alert the local police without the robbers knowledge & begin taking photos of the suspect. Every ATM has the feature. Stay safe.

Like Share

19

1,782 shares

3 Comments

Friend Requests See All

[Profile Picture] [Name] Confirm Friend

People You May Know See All

[Profile Picture] [Name] Add Friend

English (US) · Español · Português (Brasil) · Français (France) · Deutsch +

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Will Entering Your PIN in Reverse at an ATM Summon the Police?

Entering your PIN in reverse at any ATM will not automatically send an alarm to local police -- the idea is nothing more than an old and unimplemented suggestion.

CLAIM

Entering your PIN in reverse at any ATM will automatically summon the police.

[See Example\(s\)](#)

RATING

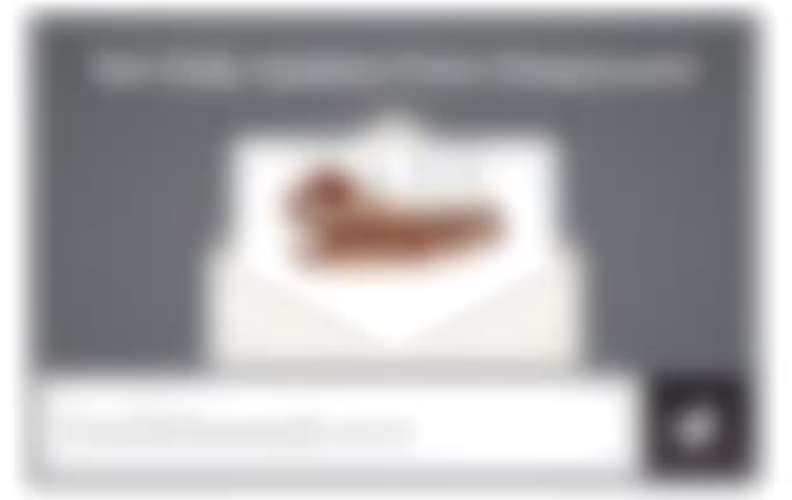


ORIGIN

Messages offering a seemingly helpful heads-up about how to deal with a situation in which one is forced to hand over money withdrawn from an ATM under duress began circulating on the Internet in September 2006:



If a thief forces you to take money out of an ATM, do not argue or resist.





Tell them what you're going
to tell them. Tell it to them.

Then tell them what you told
them.

UNKNOWN

NAME: _____

DATE: _____

Lesson 12 Skills Practice

Objective: Write PIN Backwards

Write backwards.

1. 0461

1640

7. 6842

2486

2. 3625

5263

8. 7532

2357

3. 9572

2759

9. 1549

9415

4. 8713

3178

13.

14.

8109

Presentation

- Tell them what you're going to tell them.
- Tell it to them.
- Then tell them what you told them.

Lesson

- State the lesson objectives.
- Teach the lesson.
- Review the lesson objectives.

The definition of insanity is doing the same thing over and over again but expecting different results.

UNKNOWN

Why Some Ideas Survive and Others Die...

MADE

to

STICK

Chip Heath & Dan Heath

- **Understood**
- **Remembered**
- **Lasting impact**

STICKY ATTRIBUTES

SIMPLE

UNEXPECTED

CONCRETE

CREDIBLE

EMOTIONAL

STORIES

Simplify.

$$(x^2 + 3)(2x^3 - 7x + 4)$$



Fig. 1.

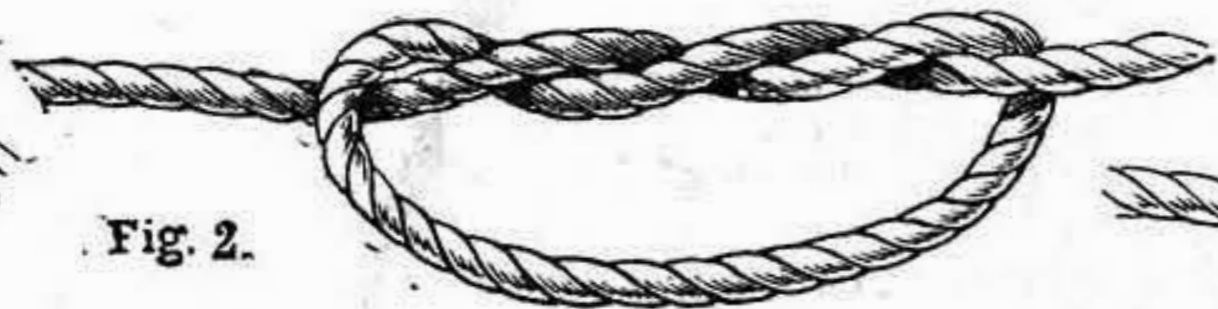


Fig. 2.



Fig. 2a.



Fig. 3.



Fig. 5.



Fig. 4.

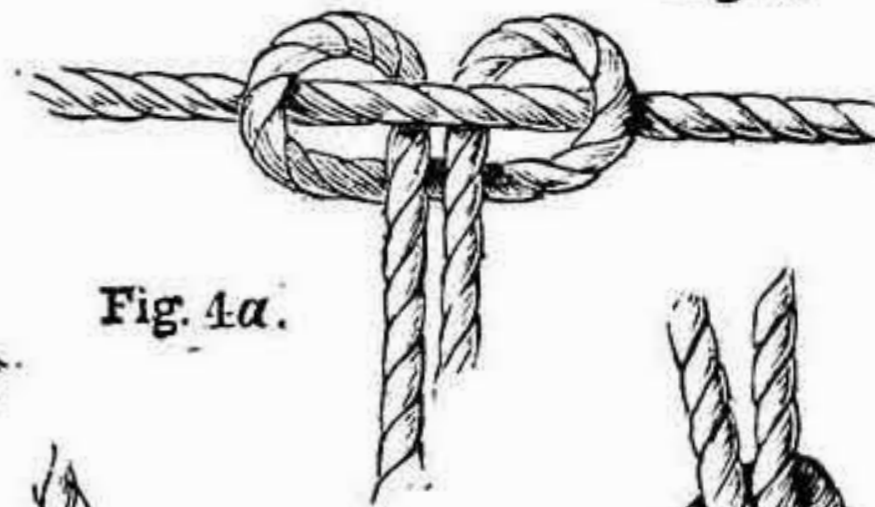


Fig. 4a.



Fig. 14.

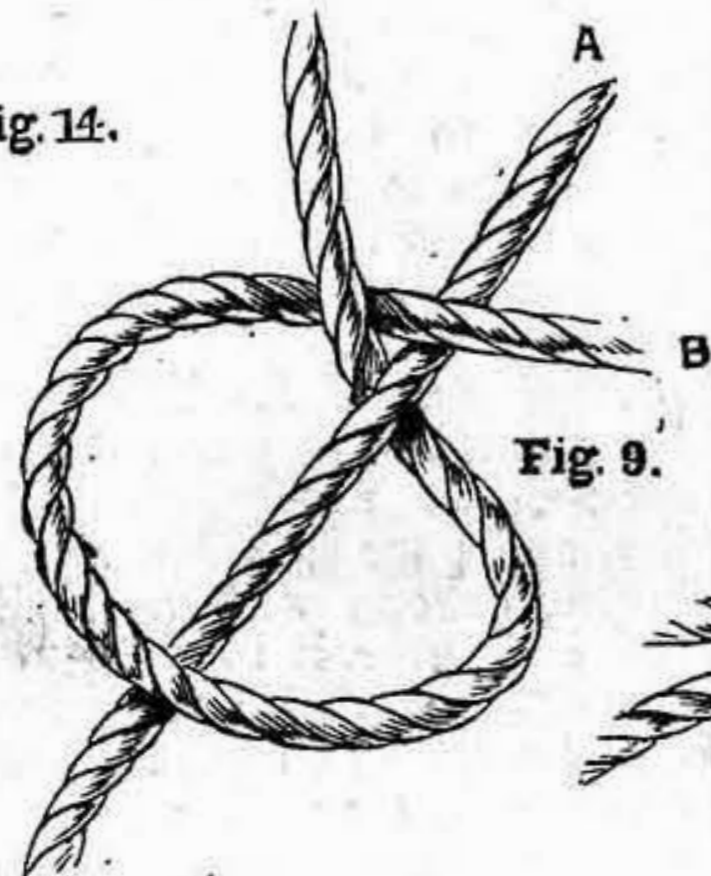


Fig. 9.



Fig. 6.

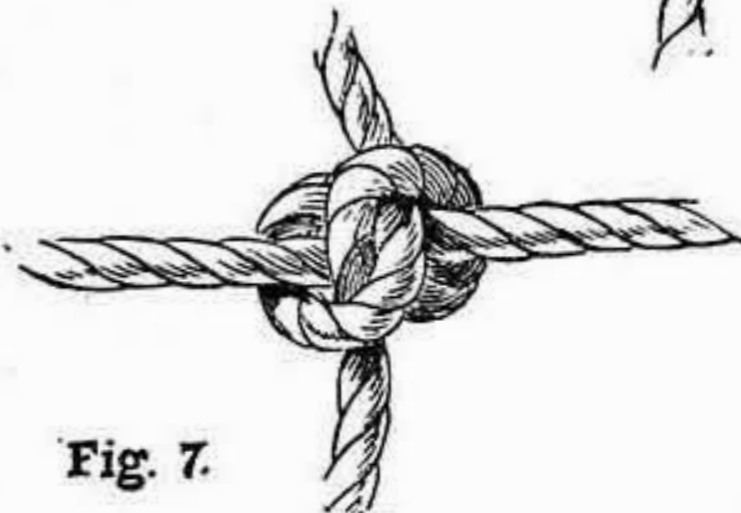


Fig. 7.



Fig. 8.



Fig. 10.



Fig. 11.



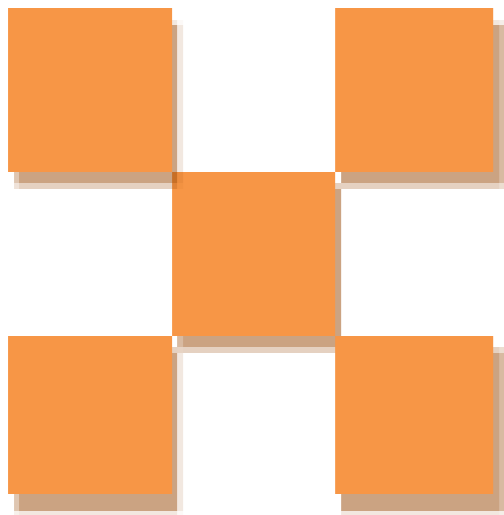
Fig. 13.



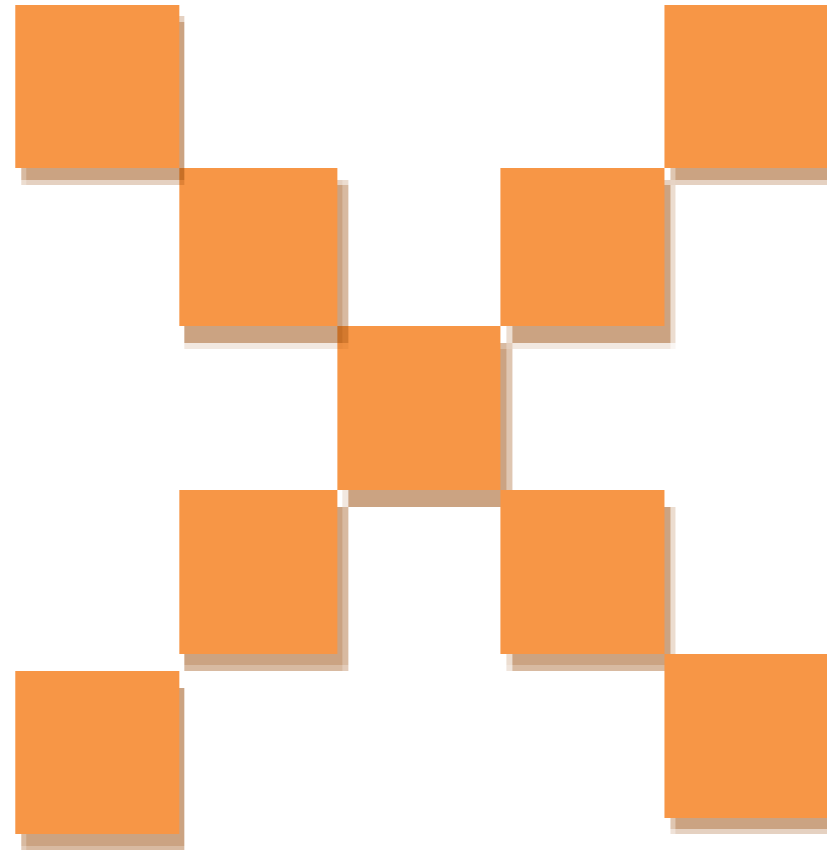
Fig. 12.

If math is the aspirin,
then how do you
create the headache?

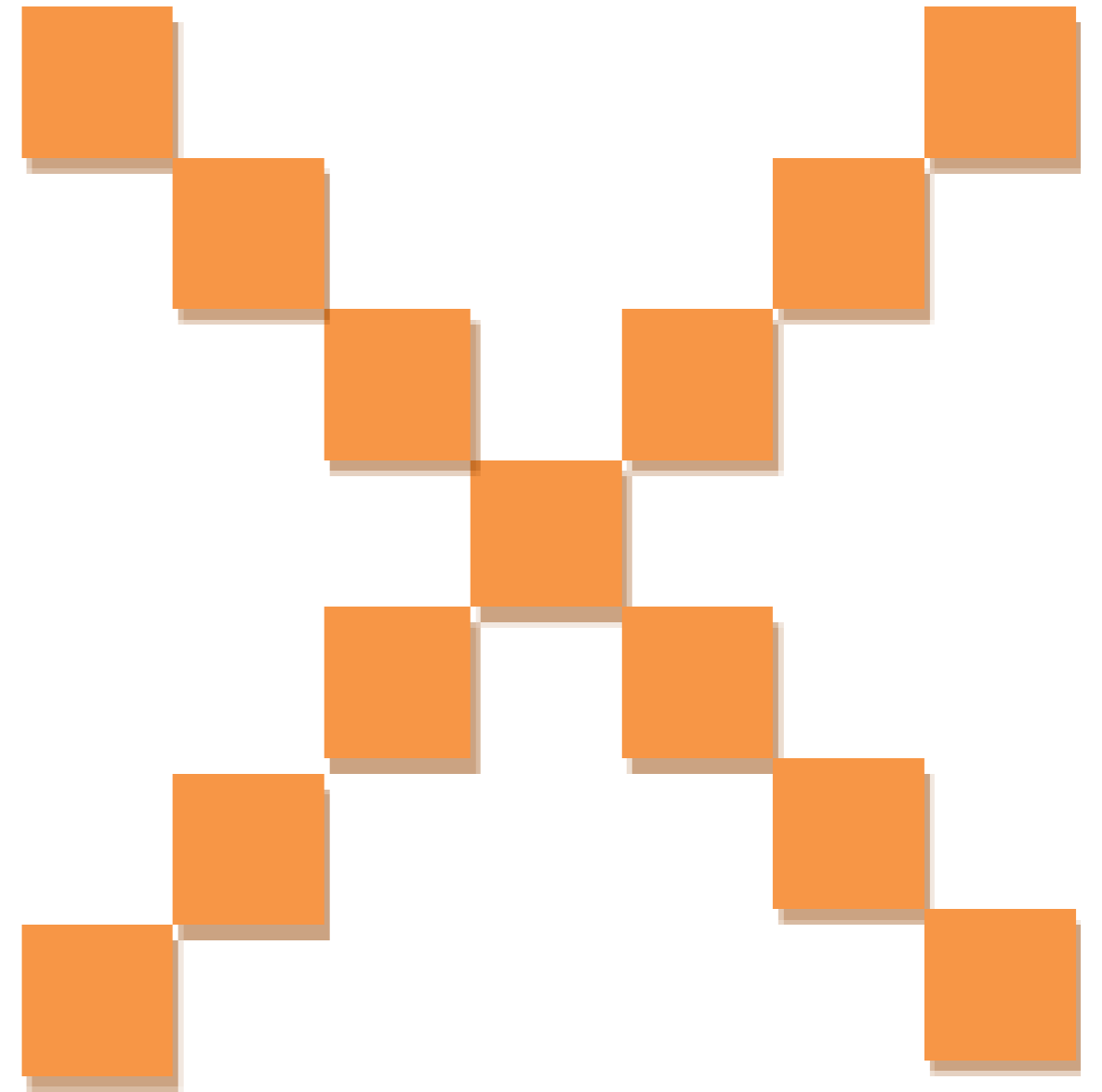
DAN MEYER



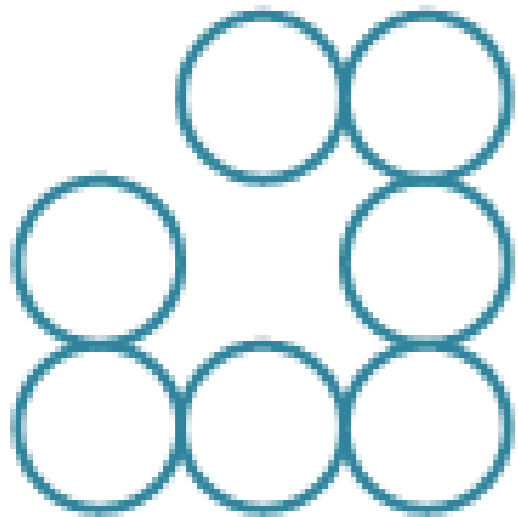
Step 1



Step 2



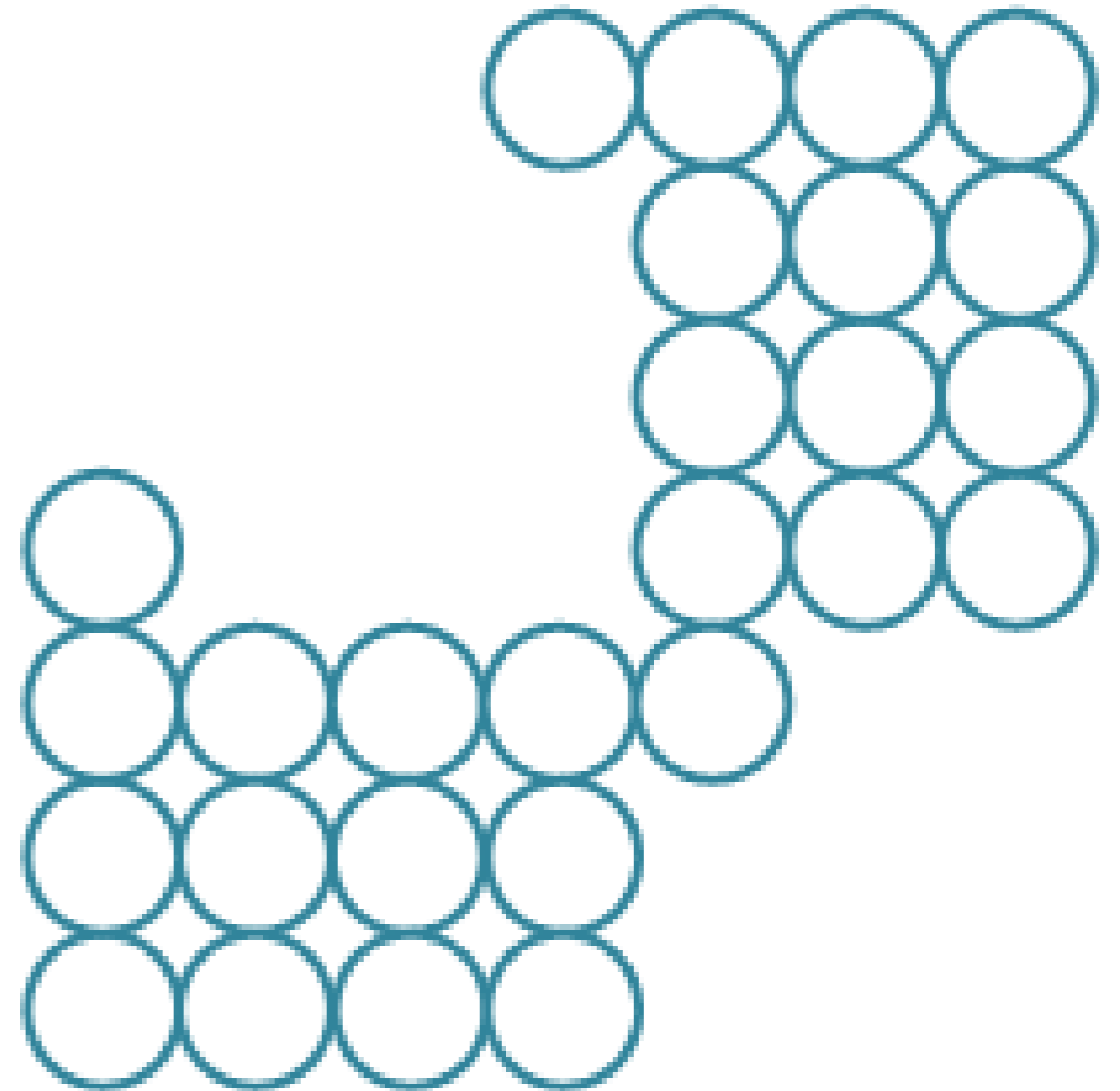
Step 3



Step 1



Step 2



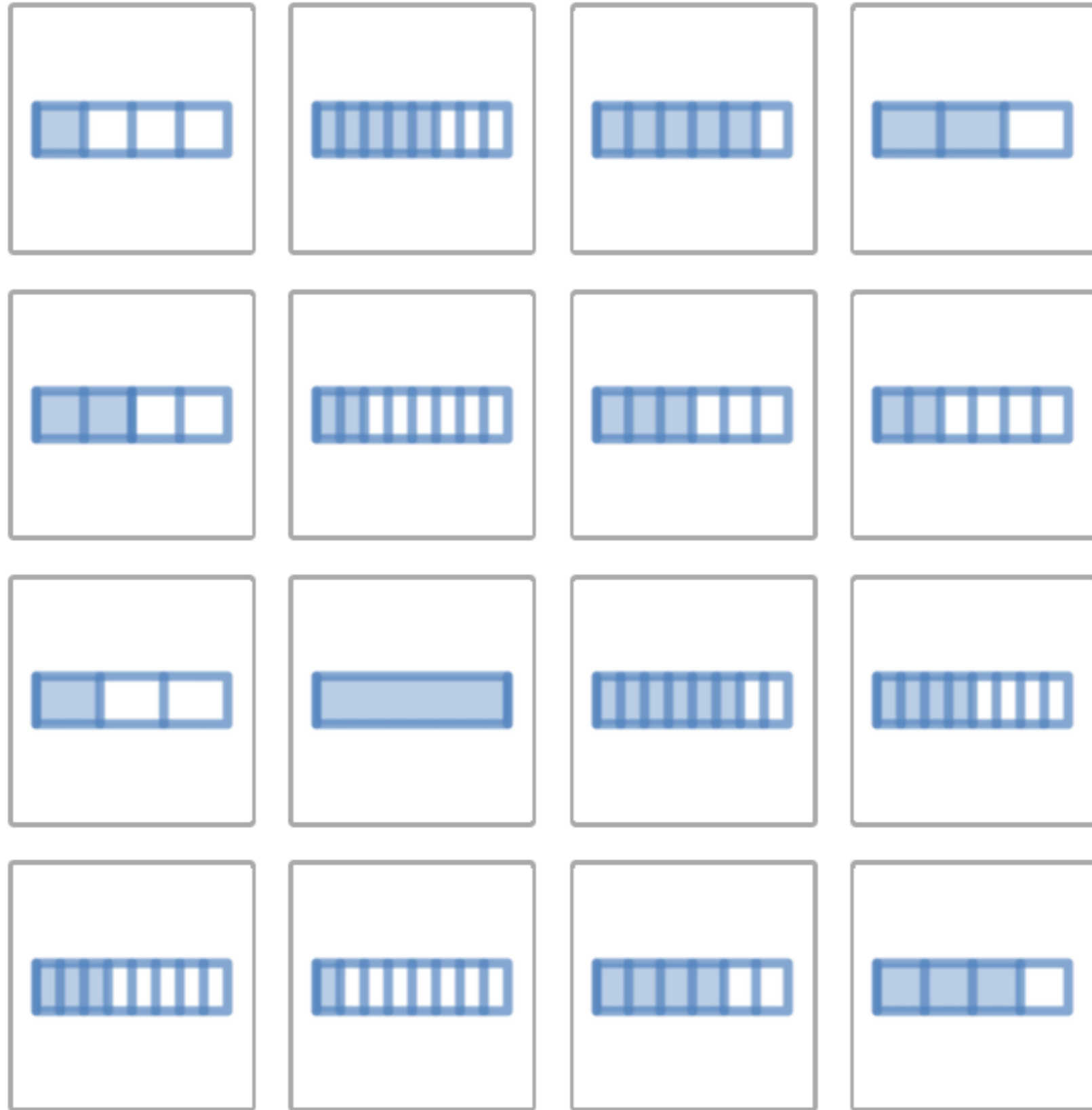
Step 3

Select a person that's special to you for any reason.

Next

Skip the practice round.





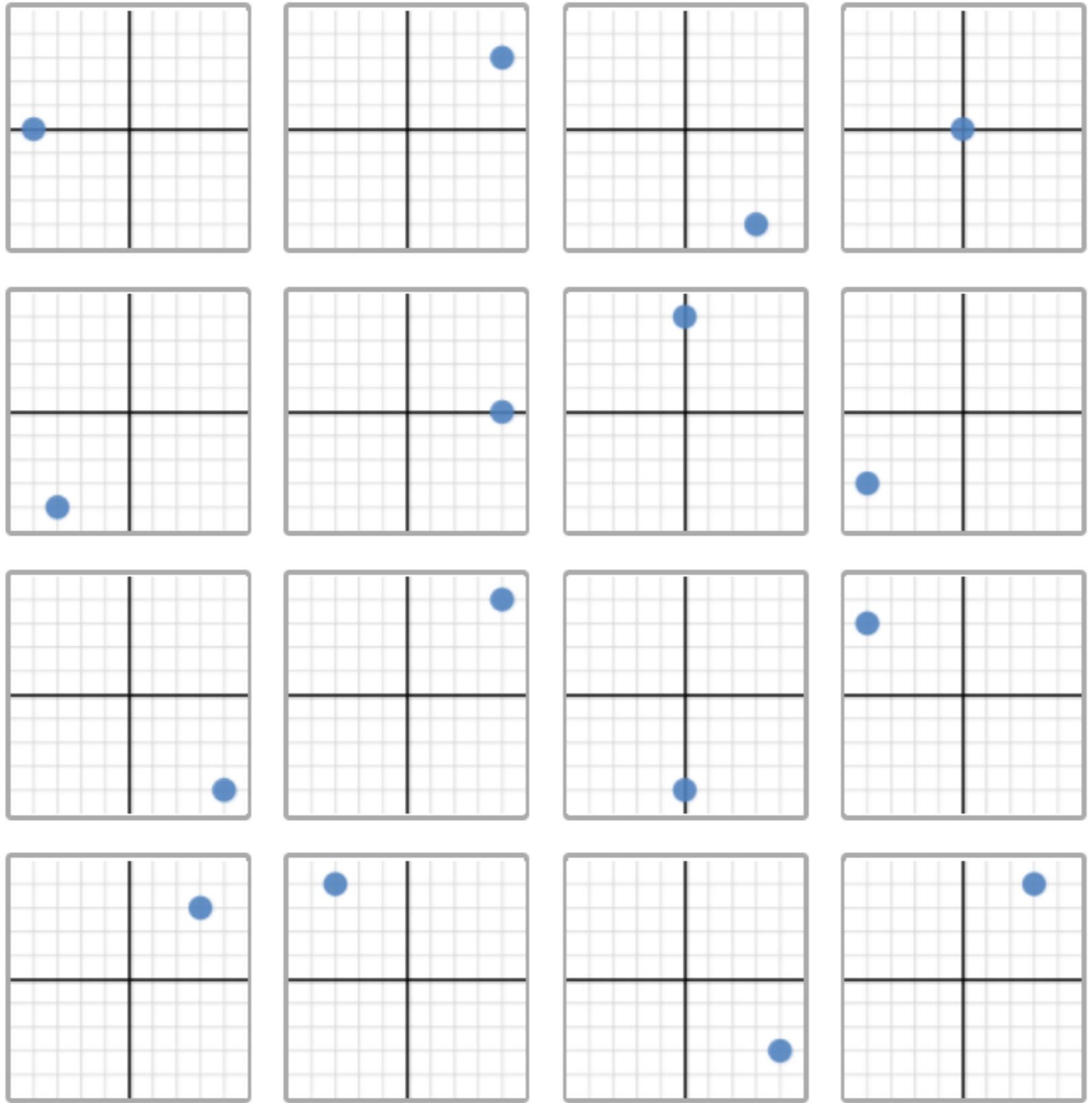
Questions Asked: 0

Your Partner: fghfgh

Your challenge: figure out which graph your partner picked. Ask a "yes" or "no" question about the graph.



Send



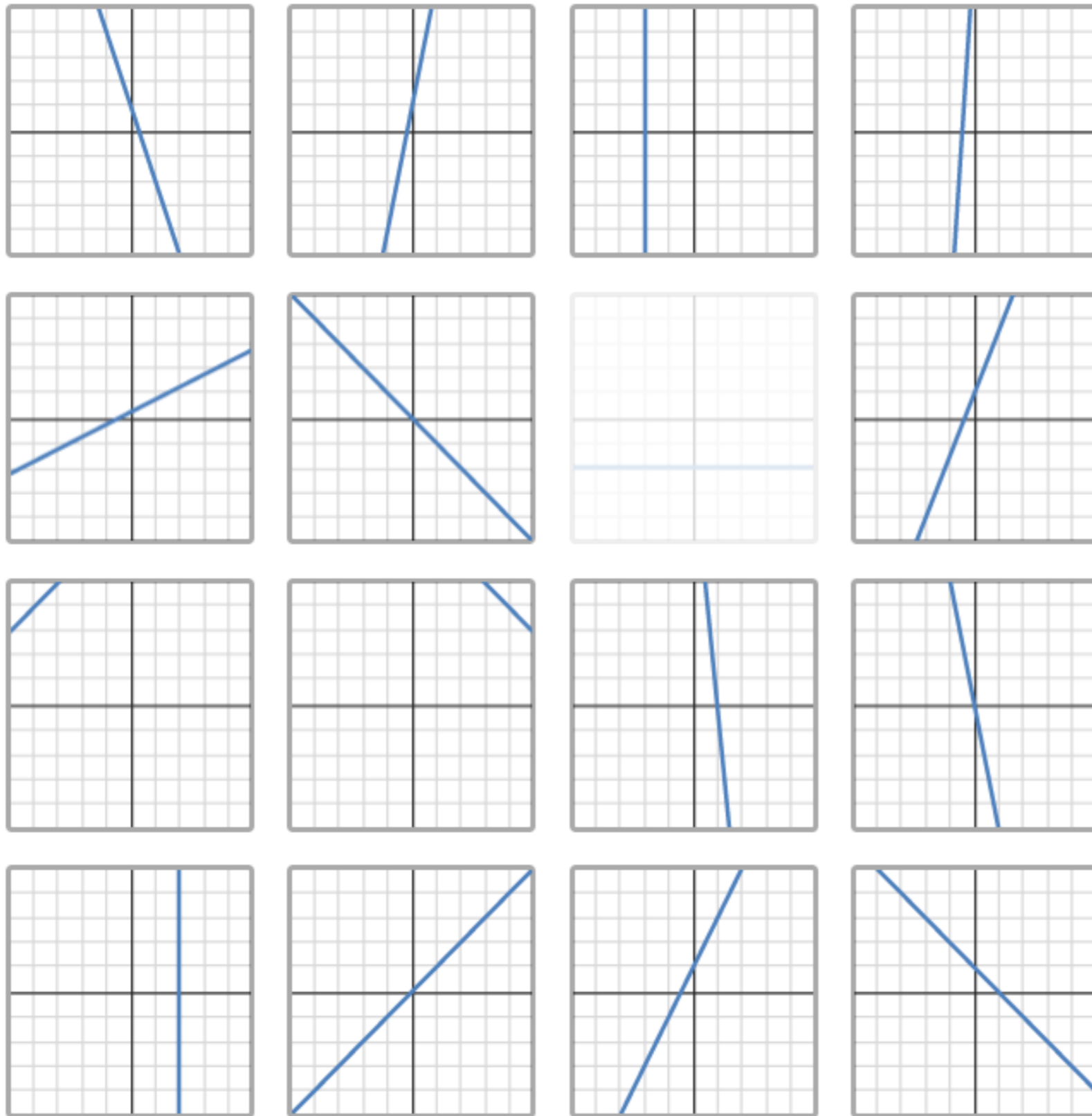
Questions Asked: 0

Your Partner: ghjhgj

Your challenge: figure out which graph your partner picked. Ask a "yes" or "no" question about the graph.



Send



Questions Asked: 2

Your Partner: Lupita

YOU ASKED

Does your line go up and down?

YOUR PARTNER CHOSE

Yes

YOUR PARTNER ELIMINATED



YOU ASKED

Is your line slanted?

YOUR PARTNER CHOSE

I Don't Know

Select lines to eliminate based on your partner's answer. Then press the button below.



Go on without Eliminating



Questions Asked: 0

Your Partner: Robert Kaplinsky

Your challenge: figure out which graph your partner picked. Ask a "yes" or "no" question about the graph.



Send



Source: robertkaplinsky.com/lessons

100,000,000,000,000,000
400,000,000,000,000,000



Source: robertkaplinsky.com/lessons

STICKY ATTRIBUTES

- SIMPLE
- UNEXPECTED
- CONCRETE
- CREDIBLE
- EMOTIONAL
- STORIES



5% Charged

9:02

Friday, July 11

9:06

10% Charged

9:10

14% Charged

9:14

19% Charged

9:18

24% Charged

9:22

28% Charged

9:26

33% Charged

9:30

38% Charged

9:34

42% Charged

THINKING TIME

9:38

47% Charged

9:42

52% Charged

9:46

56% Charged

9:50

61% Charged

9:54

65% Charged

9:58

70% Charged

10:02

74% Charged

10:06

78% Charged

10:10

82% Charged

10:14

84% Charged

10:18

87% Charged

10:22

89% Charged

10:26

90% Charged

10:30

92% Charged

10:34

93% Charged

10:38

94% Charged

10:42

95% Charged

10:46

96% Charged

10:50

97% Charged

10:54

97% Charged

10:58

98% Charged

11:02

98% Charged

11:06

98% Charged

11:10

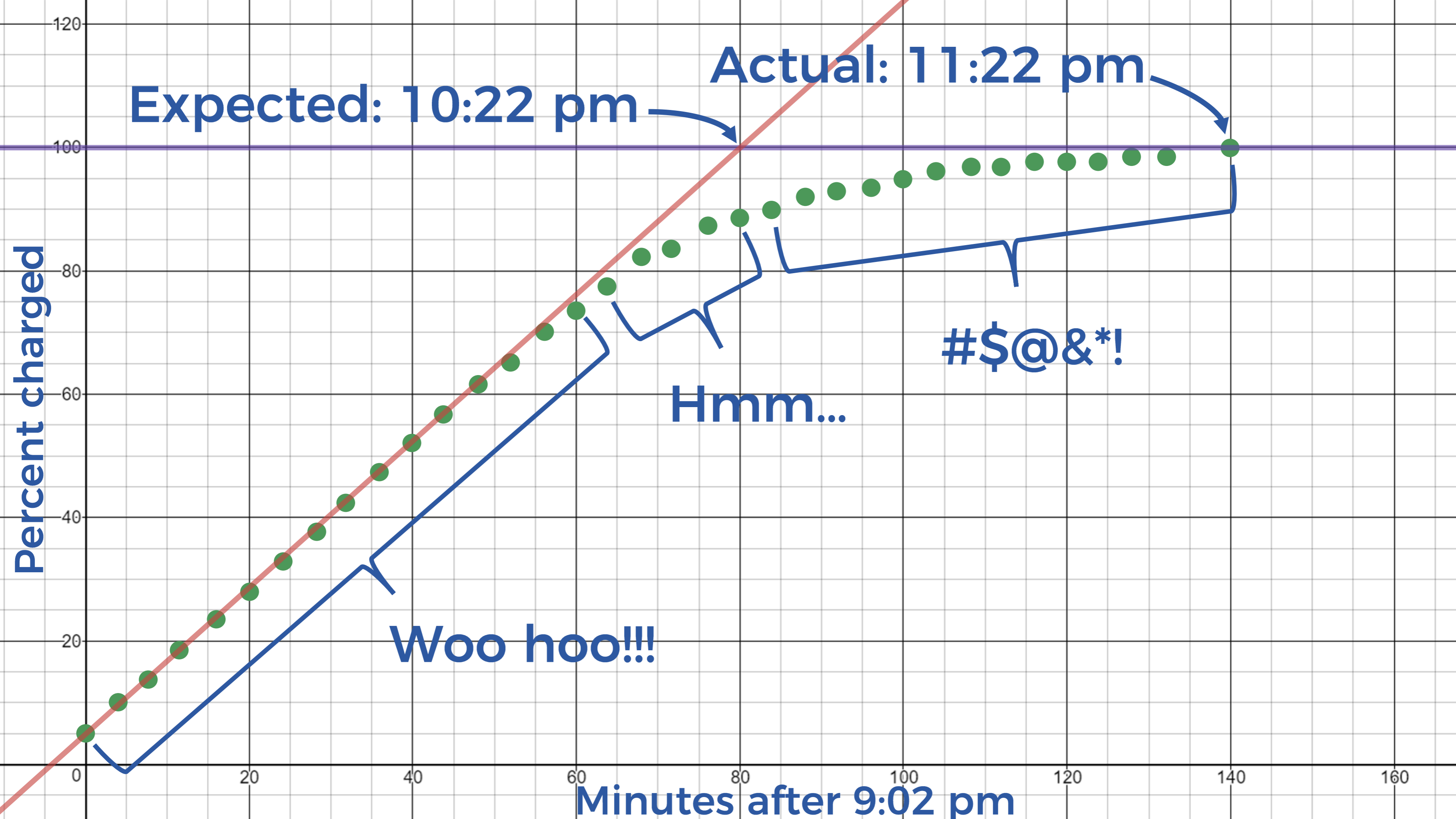
99% Charged

11:14

99% Charged

11:22

100% Charged



Expected: 10:22 pm

Actual: 11:22 pm

Percent charged

Hmm...

#\$@&*!

Woo hoo!!!

Minutes after 9:02 pm

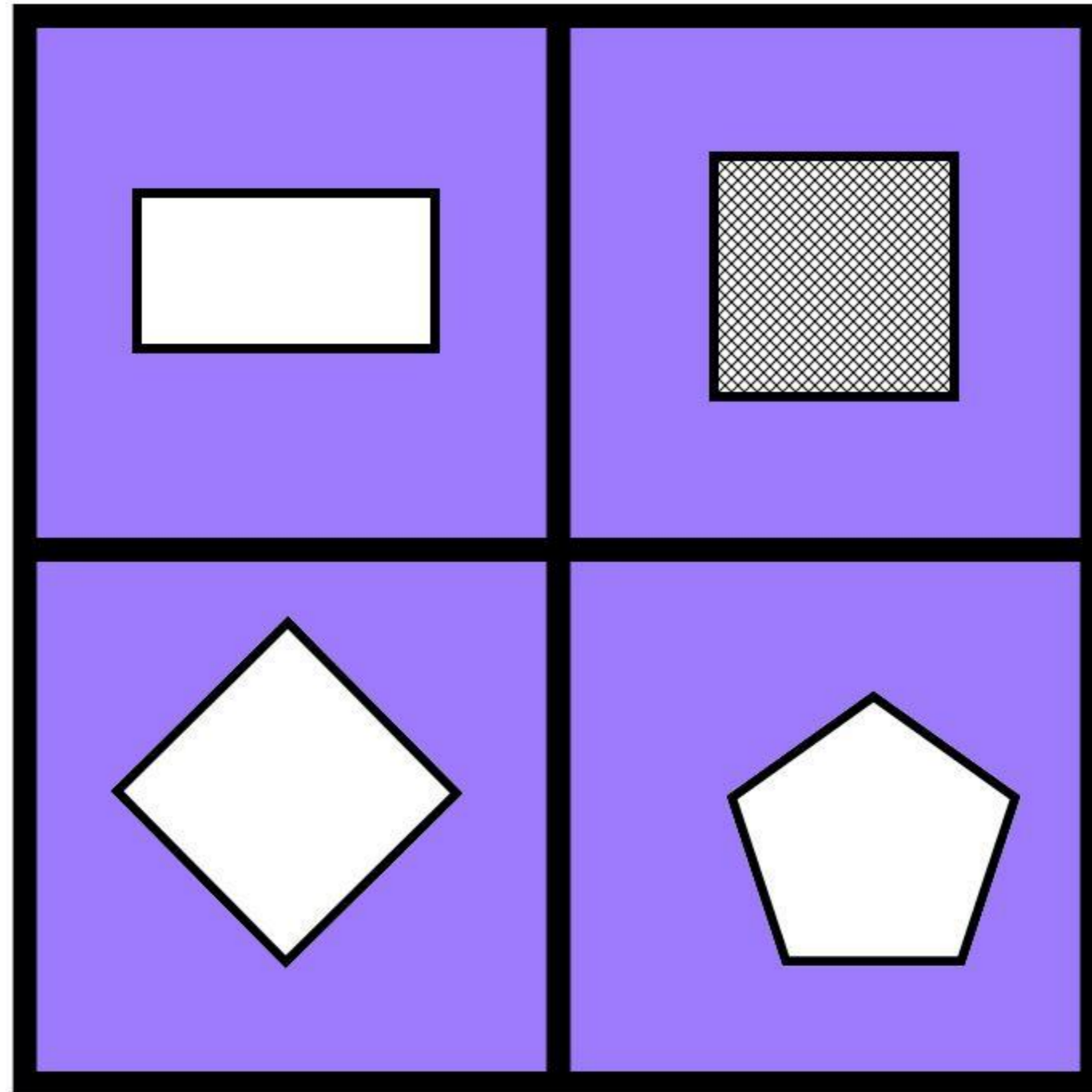
UNEXPECTED

❑ PATTERN BREAKING

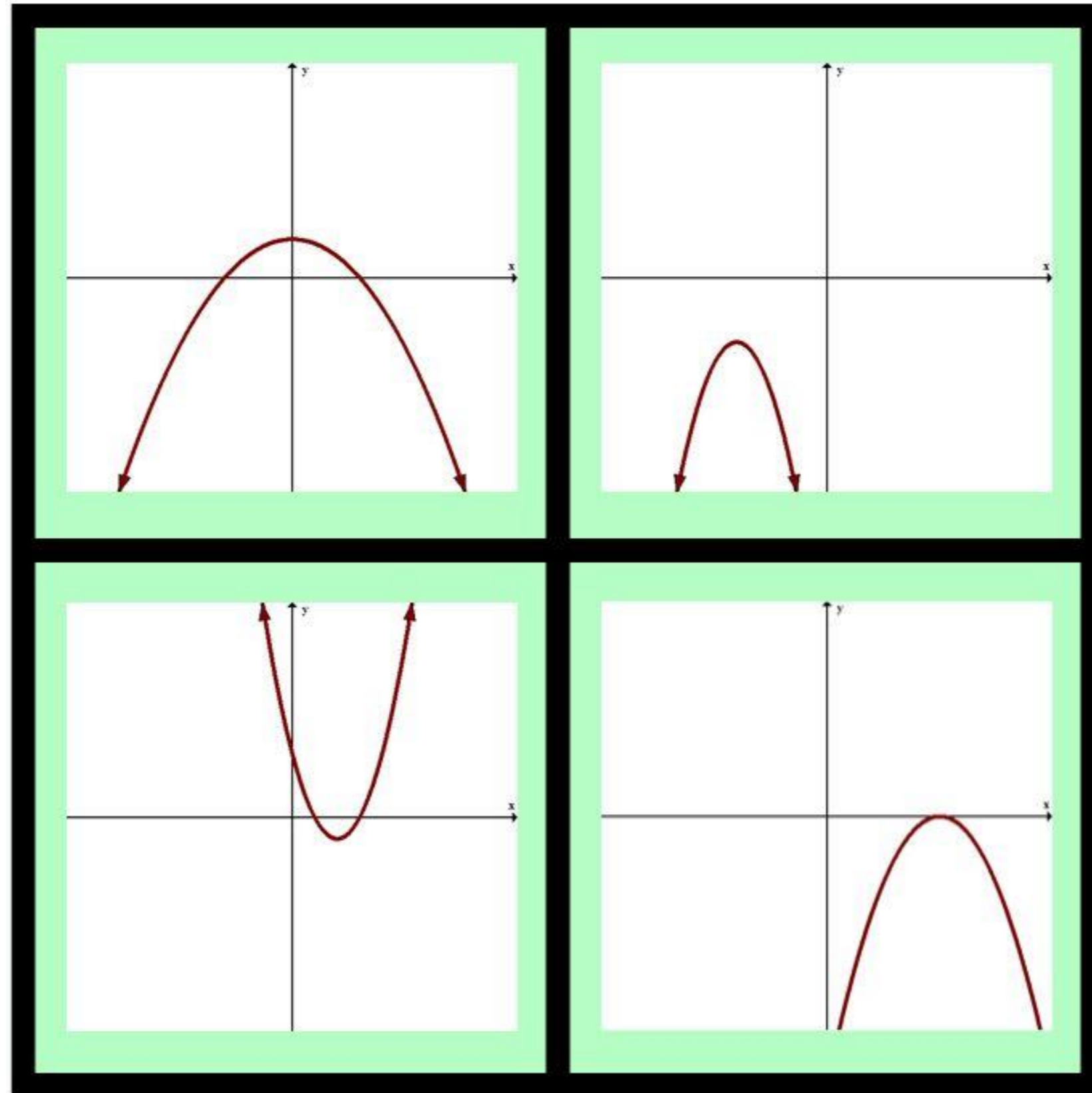
❑ COUNTERINTUITIVE

❑ KNOWLEDGE GAPS

❑ OPEN MIDDLE







UNEXPECTED


PATTERN BREAKING

COUNTERINTUITIVE

KNOWLEDGE GAPS

OPEN MIDDLE

*SURFACE AREA OF A
SPHERE FORMULA
DEMONSTRATION*


$$\frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \frac{1}{16} + \frac{1}{32} + \dots$$

$$= 1$$

$$\frac{1}{2}$$

$$\frac{1}{16}$$

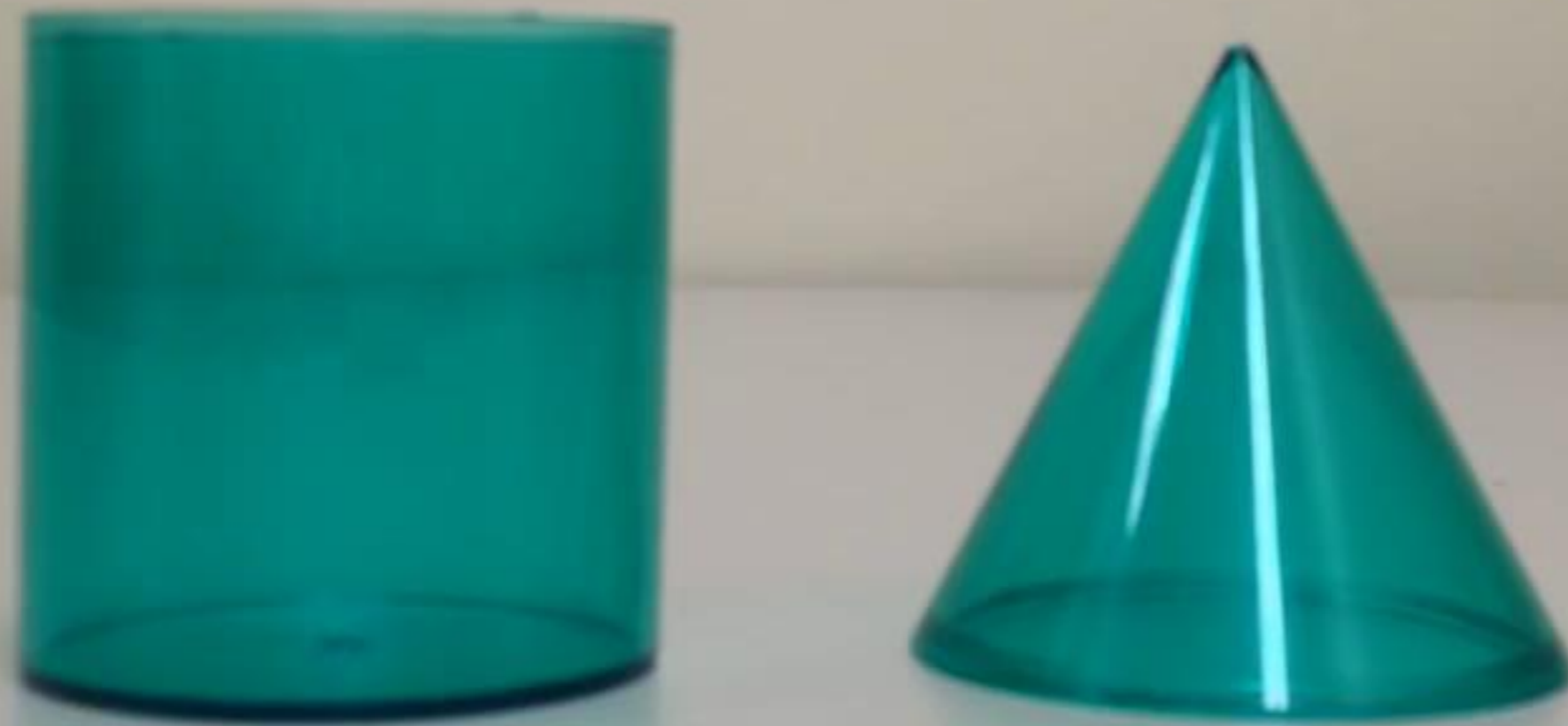
$$\frac{1}{8}$$

$$\frac{1}{32}$$

$$\frac{1}{128}$$

$$\frac{1}{64}$$

$$\frac{1}{4}$$



Source: Kyle Pearce - [youtube.com/watch?v=Yr53Ji4SZDg](https://www.youtube.com/watch?v=Yr53Ji4SZDg)

UNEXPECTED

PATTERN BREAKING

COUNTERINTUITIVE

KNOWLEDGE GAPS

OPEN MIDDLE

Curiosity... arises from the perception of a gap in knowledge or understanding.

GEORGE LOEWENSTEIN





Source: robertkaplinsky.com/lessons



Source: robertkaplinsky.com/lessons



Source: robertkaplinsky.com/lessons



Source: robertkaplinsky.com/lessons

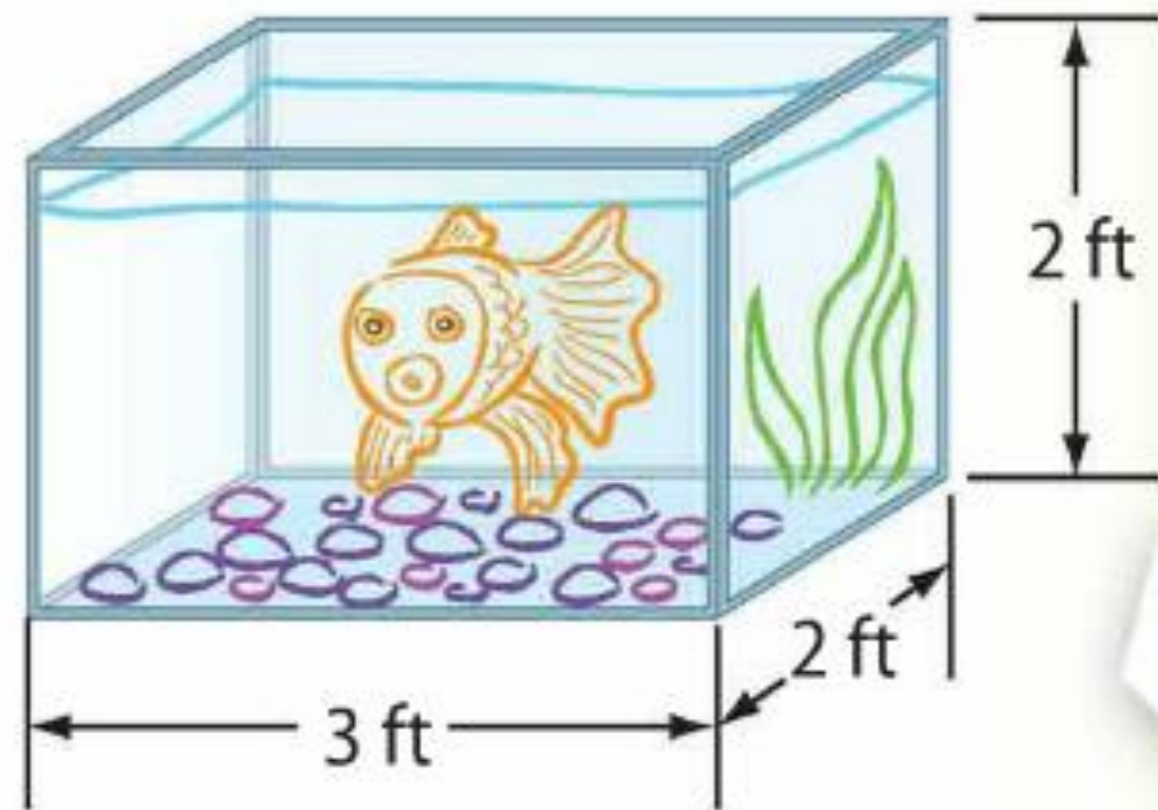


Real-World Link



Aquarium The dimensions of an aquarium are shown.

1. What is the area of the base of the aquarium? _____



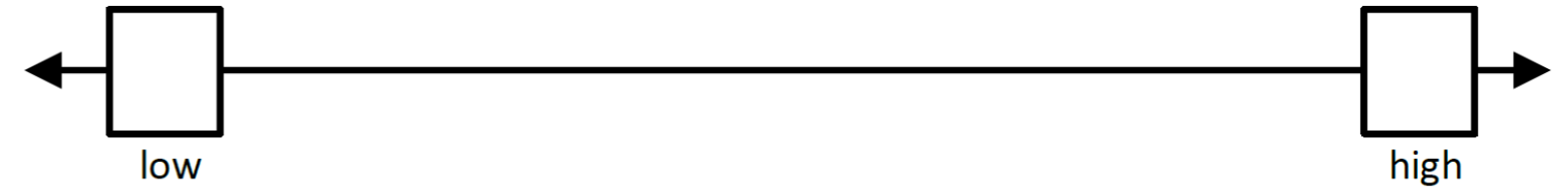
2. What is the height of the aquarium? _____

3. Fill in the blanks to find the volume.

$$\underline{\hspace{2cm}} \times \underline{\hspace{2cm}} \times \underline{\hspace{2cm}} = 12 \text{ ft}^3$$

What problem are you trying to figure out?

What estimates do you have?



Place your estimate on the number line.

What info do you already know about the problem?

What info do you need about the problem?

What is your conclusion? How did you reach that conclusion?

UNEXPECTED

PATTERN BREAKING

COUNTERINTUITIVE

KNOWLEDGE GAPS

OPEN MIDDLE





Map data ©2017 Google

500 mi 

My Village

Treasure Map

Google Maps

Beginning

Closed

Closed

Middle

Open

Closed

End

Closed

Closed



Using the digits 1-9, at most one time each, fill in the boxes to create a fraction that is as close to one as possible.

<hr/>	

Source: Peter Morris on openmiddle.com

	Open Middle	Closed Middle
Beginning	Closed	Closed
Middle	Open	Closed
End	Closed	Closed

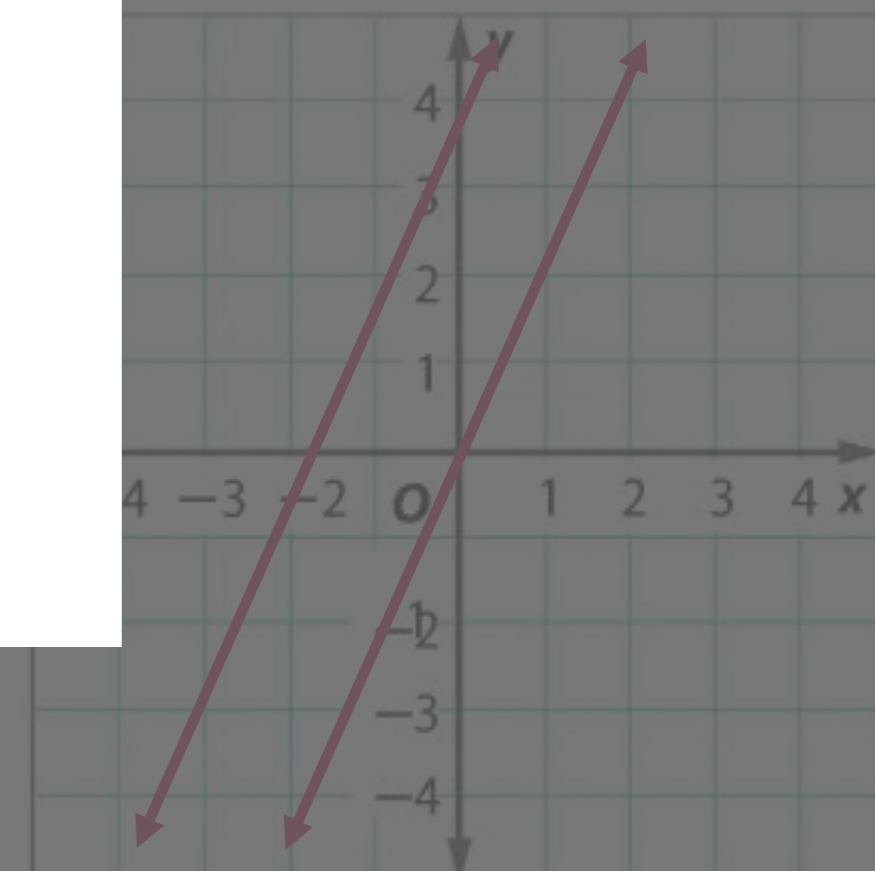
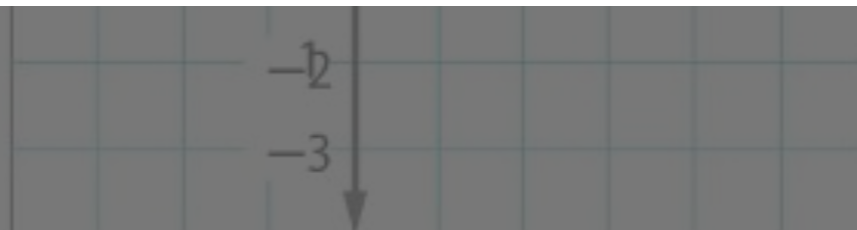
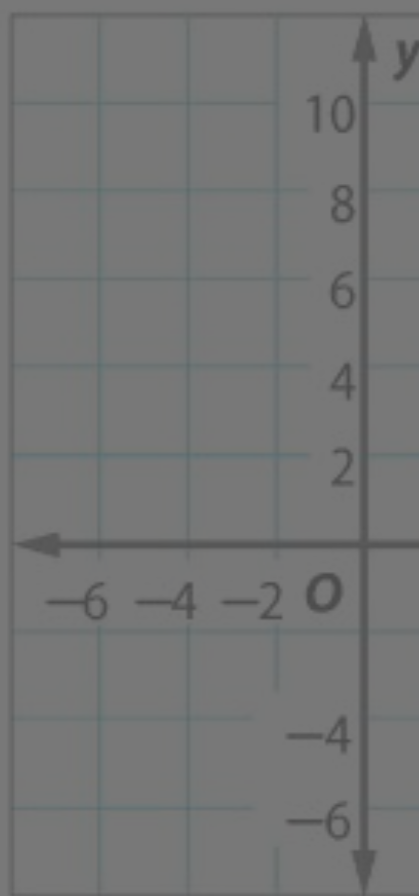
Independent Practice

Solve each system

1. $y = x$

$y = 2x - 4$

Show your work.



$$0 \neq 4$$

$$y = 2x$$

$$y - 2x = 4$$

$$y = 2x$$

THIS UNIT NOT LABELED FOR INDIVIDUAL RETAIL SALE

Ralphs

grade AA
butter

NET WT. 4 OZ. (113g)

THIS UNIT NOT LABELED FOR INDIVIDUAL RETAIL SALE.

Ingredients: Pasteurized Cream, Salt.

DISTRIBUTED BY: RALPHS GROCERY CO. LOS ANGELES, CALIF. 90054

1 Tbsp.	2 Tbsp.	3 Tbsp.	4 Tbsp.	5 Tbsp.	6 Tbsp.	7 Tbsp.	8 Tbsp.
1/4 cup							

1 FIRST QUALITY 1

grade AA

Grade AA
butter
Ralphs

THIS UNIT NOT LABELED FOR INDIVIDUAL RETAIL SALE.

Ingredients: Pasteurized Cream, Salt.

DISTRIBUTED BY: RALPHS GROCERY CO. LOS ANGELES, CALIF. 90054

1 Tbsp.	2 Tbsp.	3 Tbsp.	4 Tbsp.	5 Tbsp.	6 Tbsp.	7 Tbsp.	8 Tbsp.
			1/4 cup		1/3 cup		1/2 cup

1 FIRST QUALITY 1

Grade AA
butter
Ralphs

THIS UNIT NOT LABELED FOR INDIVIDUAL RETAIL SALE.

Ingredients: Pasteurized Cream, Salt.

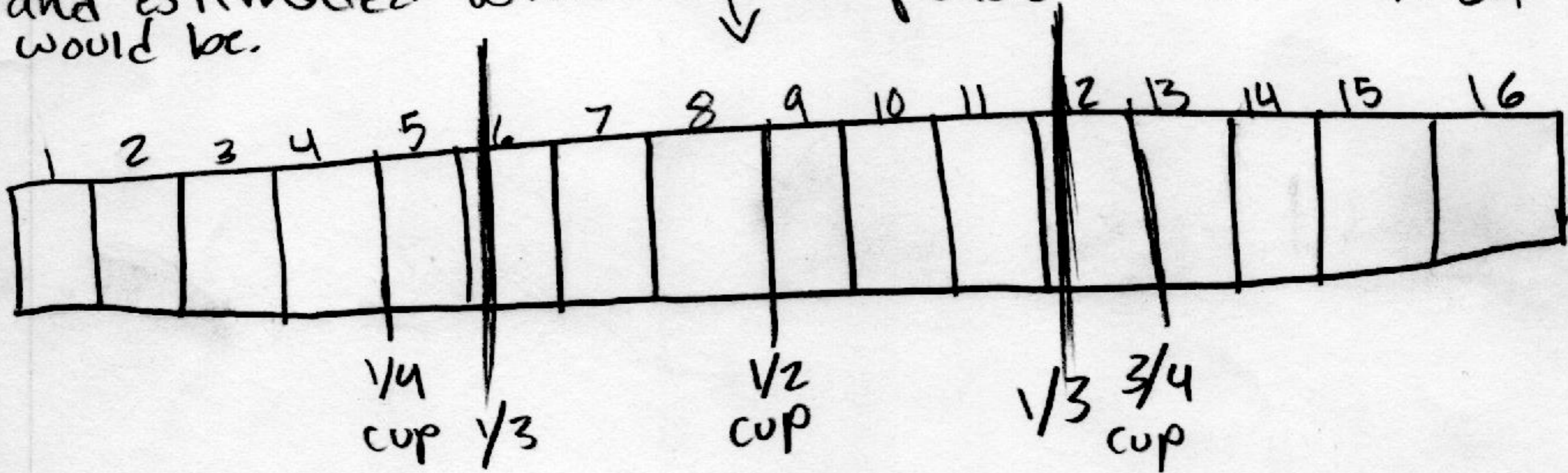
DISTRIBUTED BY: RALPHS GROCERY CO. LOS ANGELES, CALIF. 90054

1 Tbsp.	2 Tbsp.	3 Tbsp.	4 Tbsp.	5 Tbsp.	6 Tbsp.	7 Tbsp.	8 Tbsp.
			1/4 cup		1/3 cup		1/2 cup

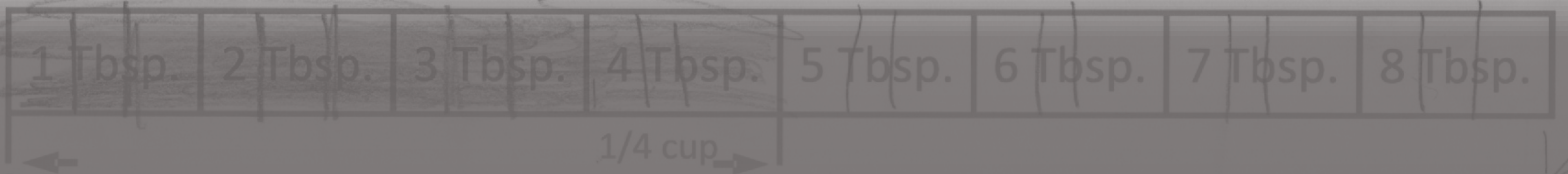
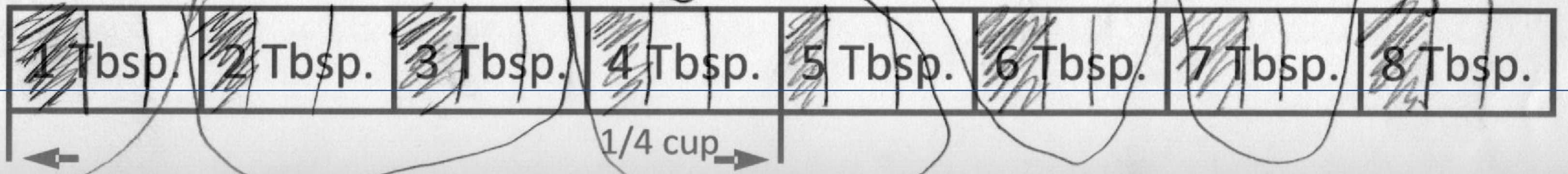
1 FIRST QUALITY 1

What is your conclusion? How did you reach that conclusion?

I reached my answer by drawing a picture of 16 flbsp and estimated where on the picture would the $\frac{1}{3}$ cup would be.



I also divided 16 by 3. $\rightarrow 3 \overline{)16} \begin{array}{r} 5 \\ \underline{15} \\ 1 \end{array}$



What is your conclusion? How did you reach that conclusion?

First, I got the total amount of tablespoons that equal a cup, which is 16 tbsp. After that, I divided 16 by 3 to find $\frac{1}{3}$ of a cup. My quotient was 5 with a remainder of 1. So I divided the remainder to all three equal groups. My answer was that $\frac{1}{3}$ of a cup of butter is 5.33 or $5\frac{1}{3}$ cups.

To check, I multiplied 5.33 by 3 and my answer was 15.99. If you round that, you get 16.00 as the answer.

UNEXPECTED

PATTERN BREAKING

COUNTERINTUITIVE

KNOWLEDGE GAPS

OPEN MIDDLE

STICKY ATTRIBUTES

SIMPLE

UNEXPECTED

CONCRETE

CREDIBLE

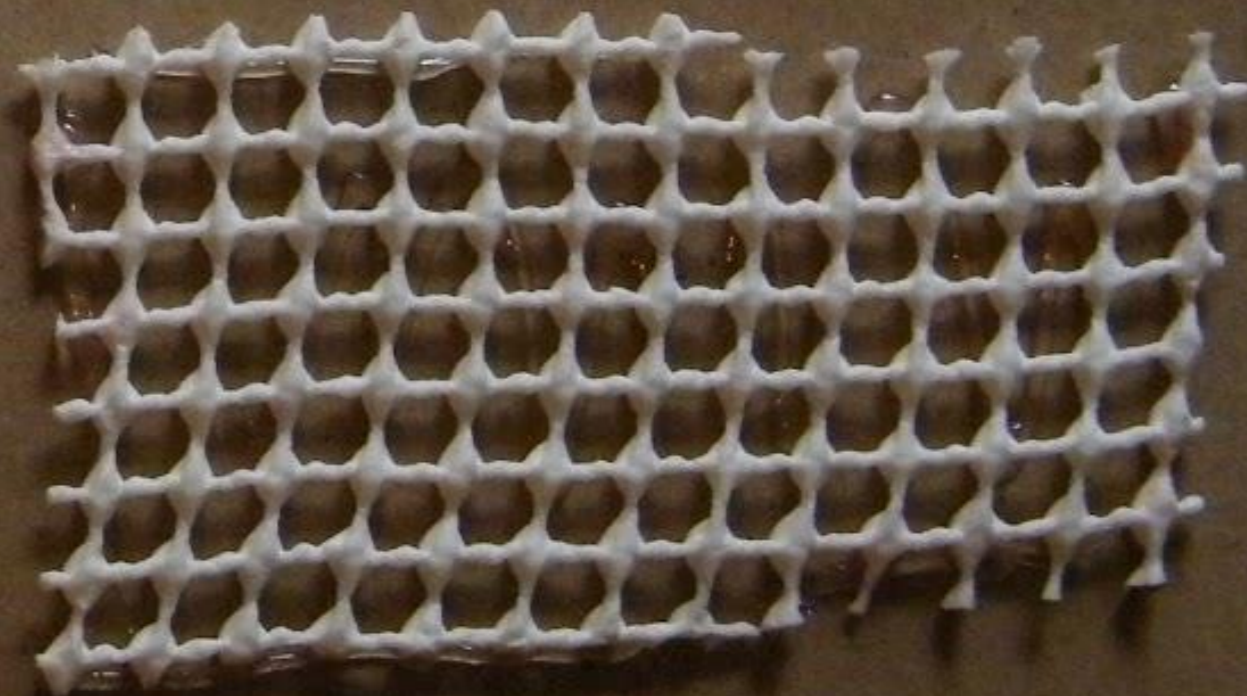
EMOTIONAL

STORIES

Soft



bumpy





Yellow the
stinky socks,

Yellow
the fragrant
flowers,

Source: Color Dog
Scratch





HunterDouglas

HunterDouglas

WINDOW FASHIONS

Window fashions that express your style

FOOD & PAPER

COMPOST

15553
PRESIDENT'S
MINI BRIE
19.6 OUNCES

5.99

4988
VALLEY SUN
SUN-DRIED TOMATOES
JULIENNE CUT 32 OUNCE

UNIT PRICE PER OUNCE
234

SELL PRICE
7.49

VICTORIA

NAME: _____

DATE: _____

PERIOD: _____

Lesson 7 Skills Practice

Objective: Divide Decimals by Decimals

Divide.

1. $4.86 \div 0.2$

7. $2.25 \div 0.15$

13. $7.52 \div 0.74$

2. $628.2 \div 34.9$

8. $421.6 \div 0.4$

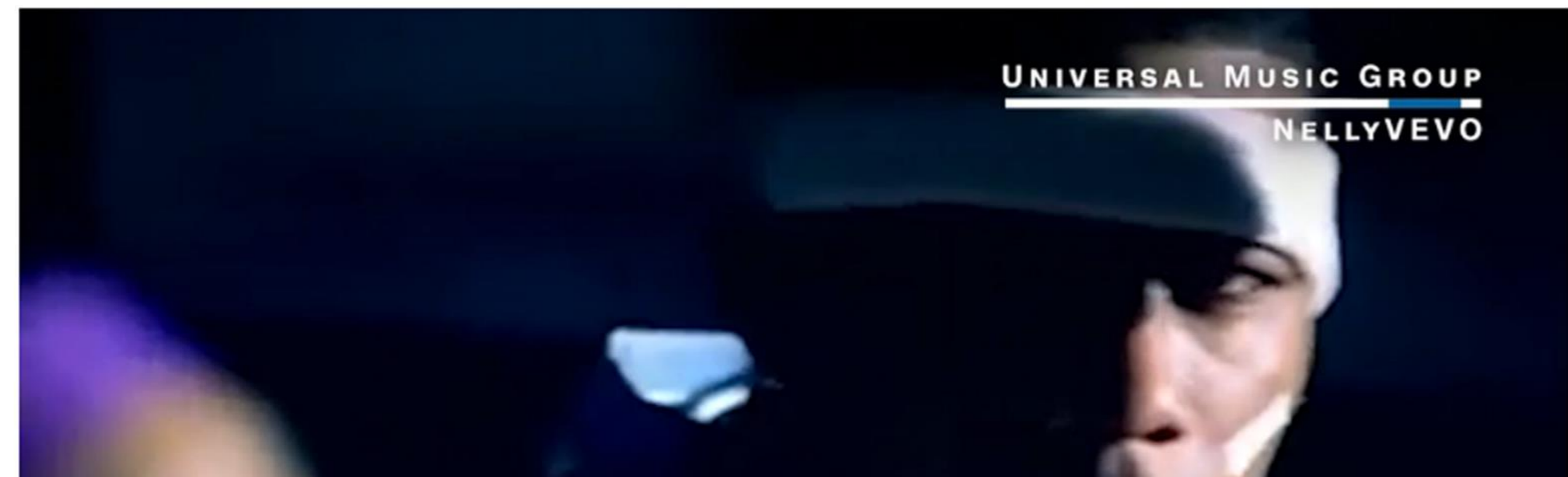
14. $0.105 \div 0.6$



Fans stream Nelly to help him pay off \$2.4 million debt

by [Lisa Respers France](#) @CNNMoney

🕒 September 13, 2016: 2:47 PM ET



- How many \$0.006 are there in \$2,400,000?
- How many 6 are there in 24?

9. Canzonett

In moderate time - with sparkle (Key of G minor)

B.M.

V

mf

pizz.

Stretching, Compressing, and Reflecting Sine and Cosine Graphs

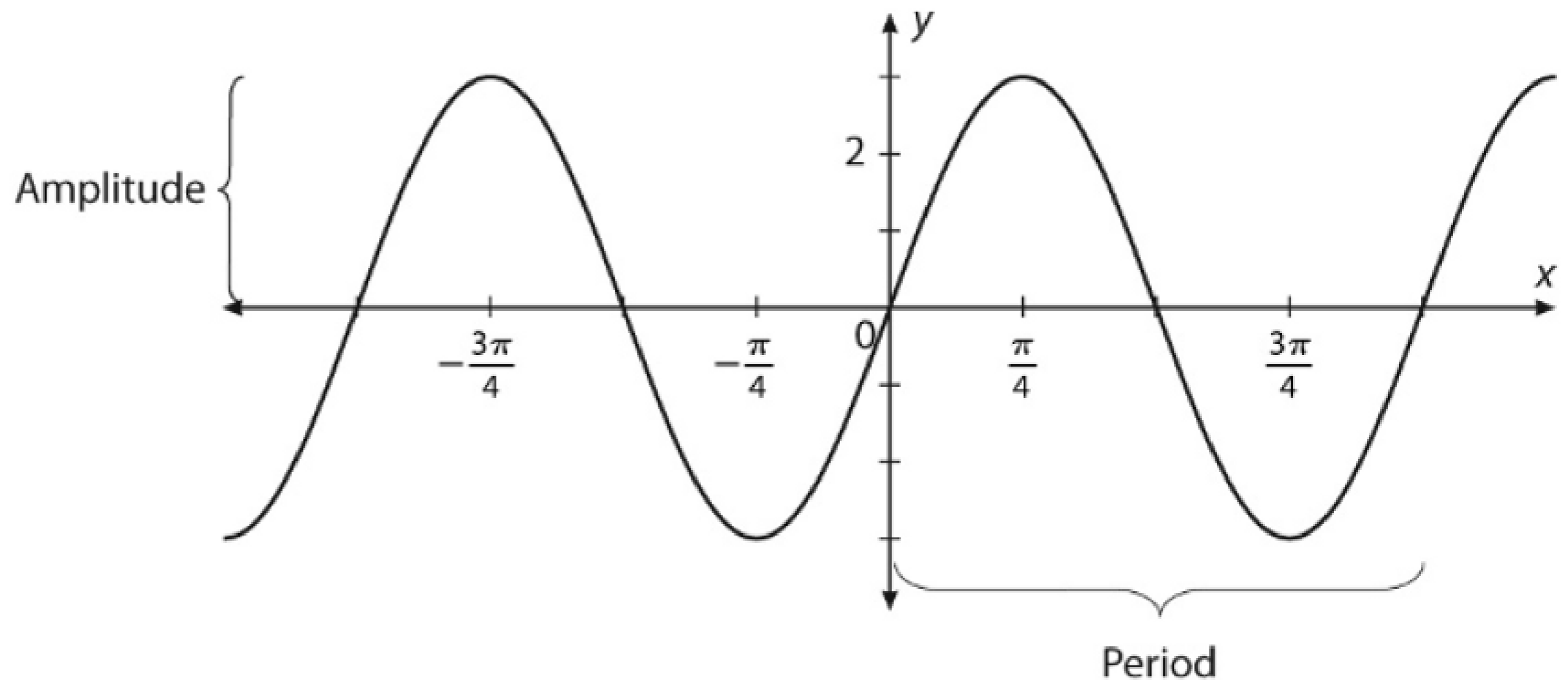
Reteach

For a sine function, $y = a \sin\left(\frac{1}{b}x\right)$.


$$\text{Amplitude} = |a|$$

$$\text{Period} = 2\pi \cdot b$$

If $a < 0$, the graph is reflected across the x -axis.



Example Write the function shown in the graph above.



distance from camera

adam poetzel

Source: graphingstories.com

$$P = 2L + 2R$$


$$A = \pi r^2$$

$$A = \frac{1}{2}bh$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

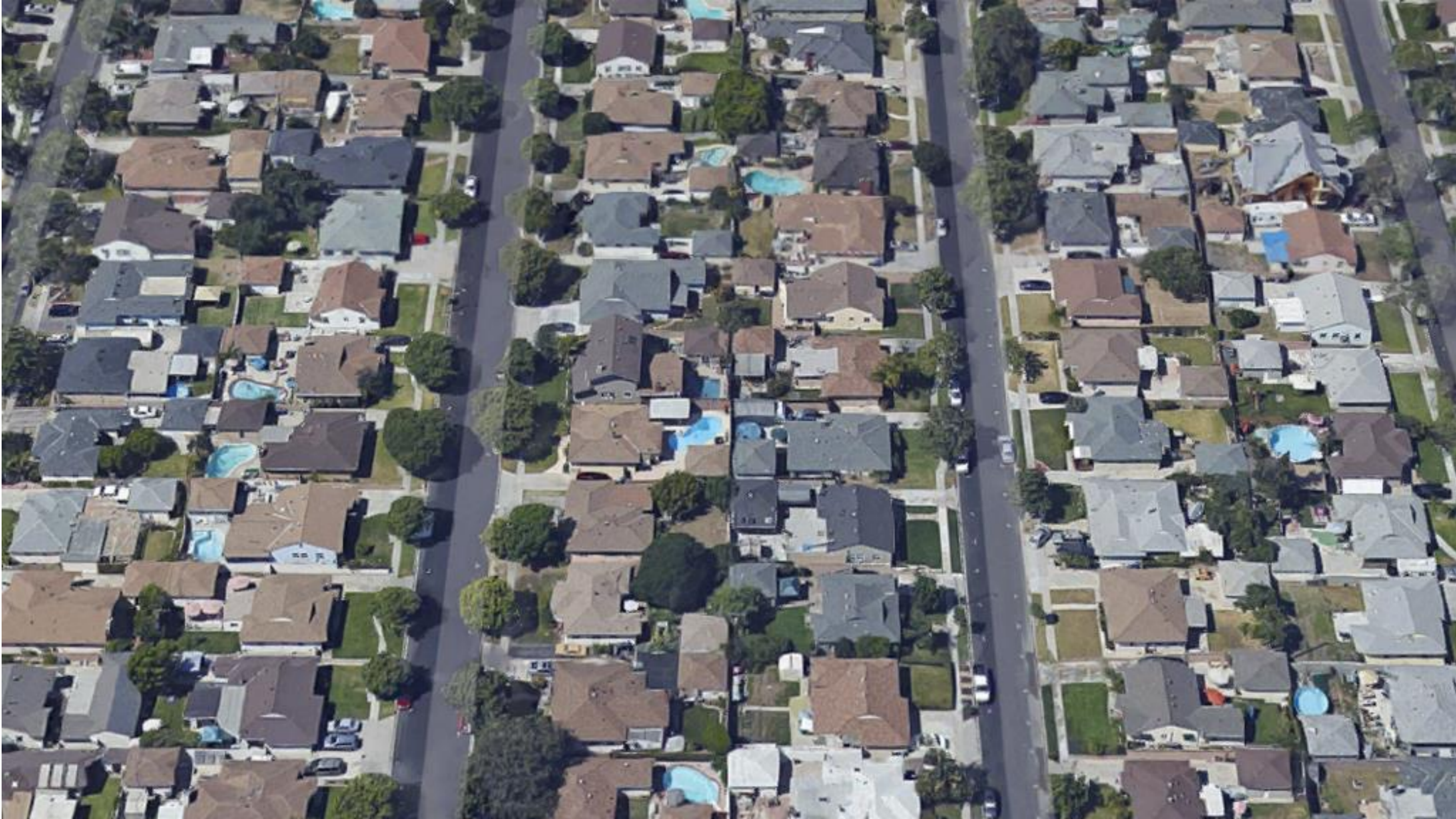
$$\log_b(x^y) = y \cdot \log_b(x)$$

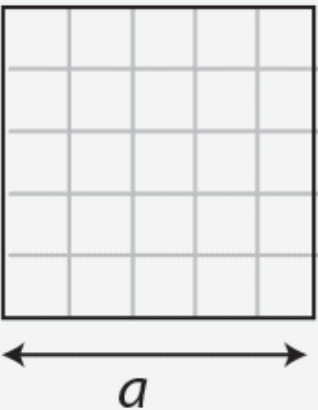
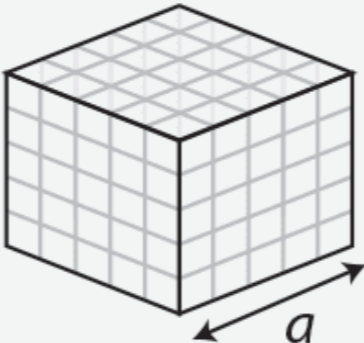
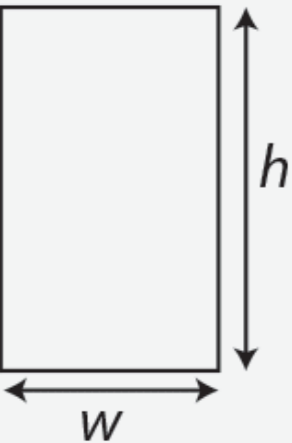
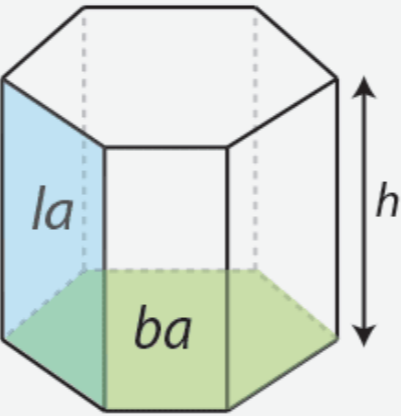
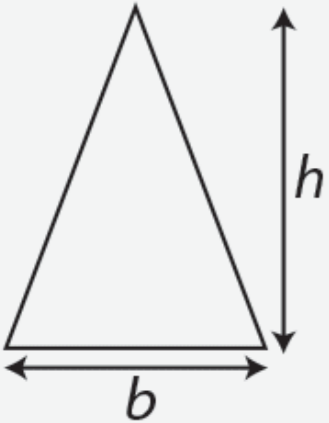
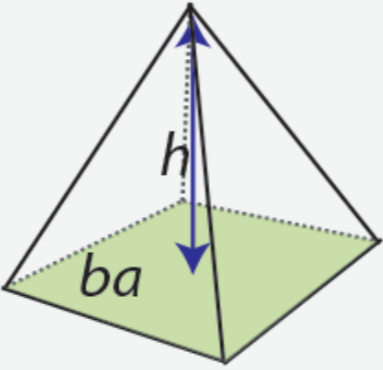

$$e^{i\pi} + 1 = 0$$


$$a^2 + b^2 = c^2$$

“Wait, was it a negative plus a negative or a negative times a negative that equals a positive.”

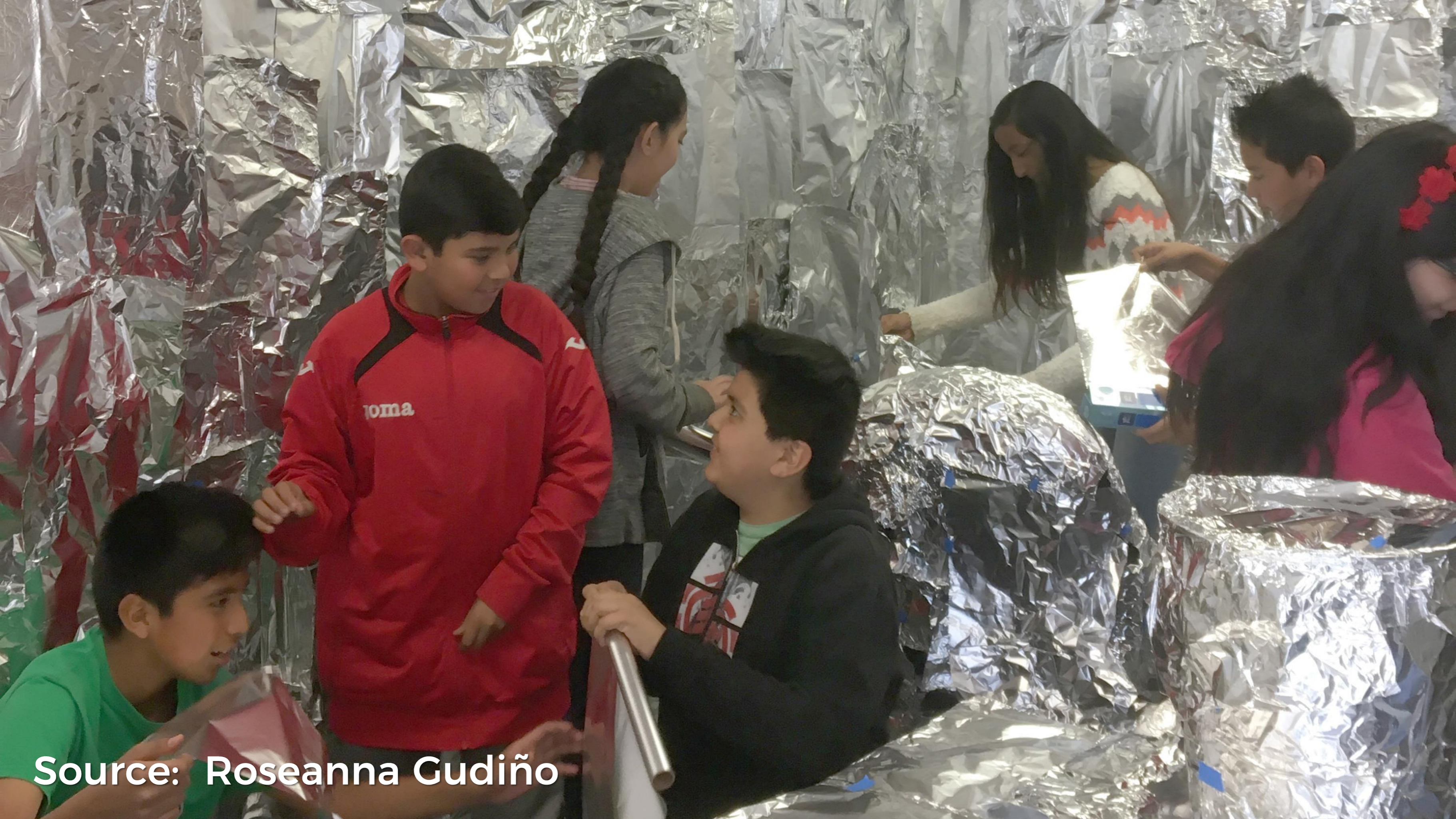
TOO MANY STUDENTS



Two-dimensional plane shapes	Area <i>The measure of how many squares will fit into a shape.</i> Units²	Three-dimensional solid shapes	Surface Area <i>The measure of the area of all outward facing sides.</i> Units²	Volume <i>The measure of how many cubes will fit into a shape.</i> Units³
Square 	Area = a^2 or $a \times a$ Example: $a = 5\text{cm}$ $\text{Area} = 5^2 = 25\text{cm}^2$	Cube 	Surface Area = $6 \times a^2$ Example: $a = 5\text{cm}$ $\text{Surface Area} = 150\text{cm}^2$	Volume = a^3 or $a \times a \times a$ Example: $a = 5\text{cm}$. $\text{Volume} = 125\text{cm}^3$
Rectangle 	Area = $w \times h$ Example: $w = \text{width} = 10\text{cm}$ $\text{height} = 20\text{cm}$ $\text{Area} = 10 \times 20 = 200\text{cm}^2$	Prism 	Surface Area = $2 \times ba + la$ Example: $ba = \text{base area} = 20\text{cm}^2$ $la = \text{lateral area (all sides)} = 60\text{cm}^2$ $\text{Surface area} = 2 \times 20 + 60 = 100\text{cm}^2$	Volume = $ba \times h$ Example: $ba = \text{base area} = 20\text{cm}^2$ $h = \text{height} = 5\text{cm}$ $\text{Volume} = 20 \times 5 = 100\text{cm}^3$
Triangle 	Area = $b \times h \times 0.5$ Example: $b = \text{base} = 20\text{cm}$ $h = \text{vertical height} = 15\text{cm}$ $\text{Area} = 20 \times 15 \times 0.5 = 150\text{cm}^2$	Pyramid 	Surface Area = $ba + la$ Example: $ba = \text{base area} = 16\text{cm}^2$ $la = \text{lateral area (all sides)} = 60\text{cm}^2$ $\text{Surface area} = 16 + 60 = 76\text{cm}^2$	Volume = $ba \times h \times 1/3$ Example: $ba = \text{base area} = 16\text{cm}^2$ $h = \text{height} = 9\text{cm}$ $\text{Volume} = 16 \times 9 \times 1/3 = 48\text{cm}^3$
n 	Area = $n \times s \times a \times 0.5$	n	Surface Area = $fa \times s$	



Source: robertkaplinsky.com/lessons

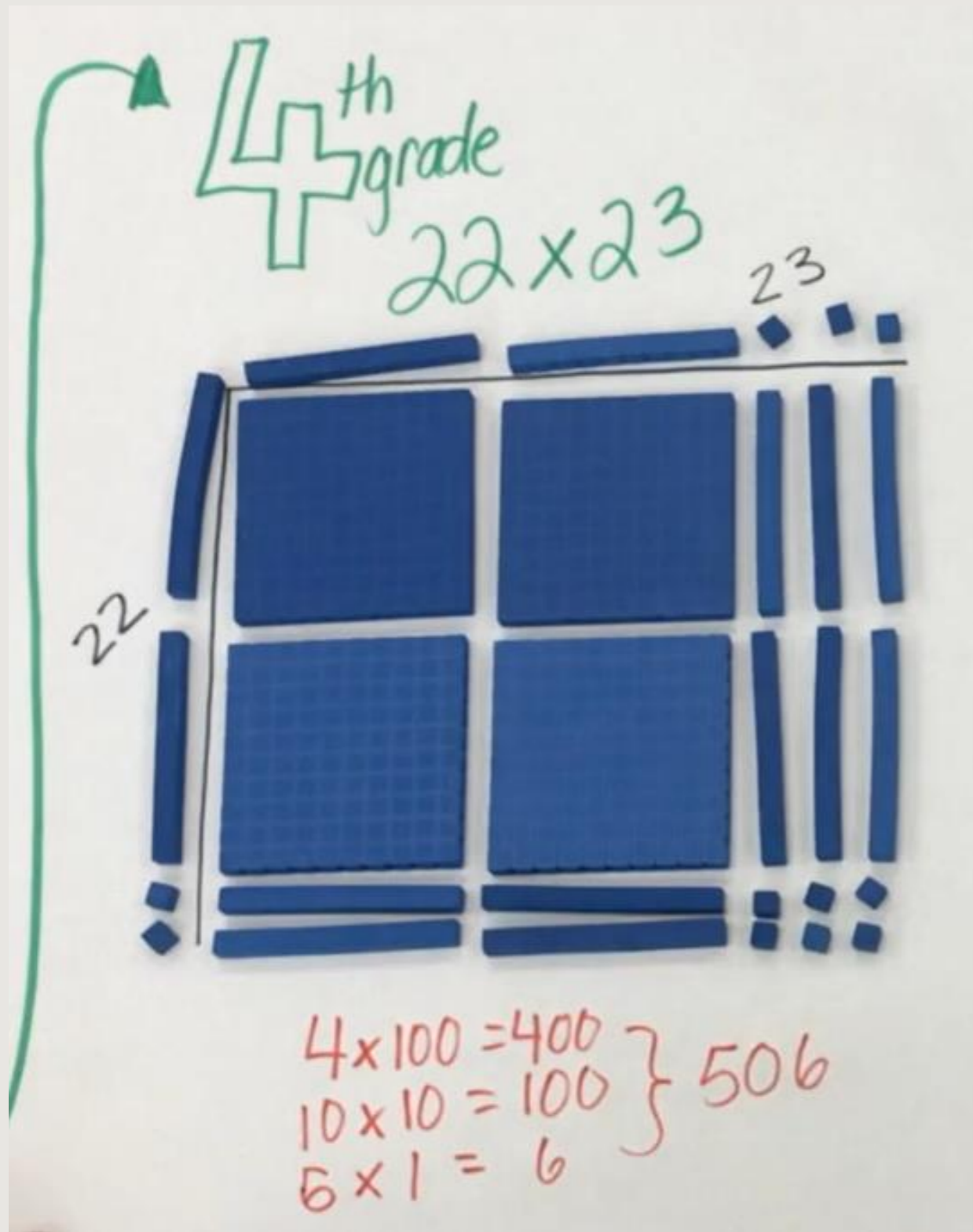


Source: Roseanna Gudiño



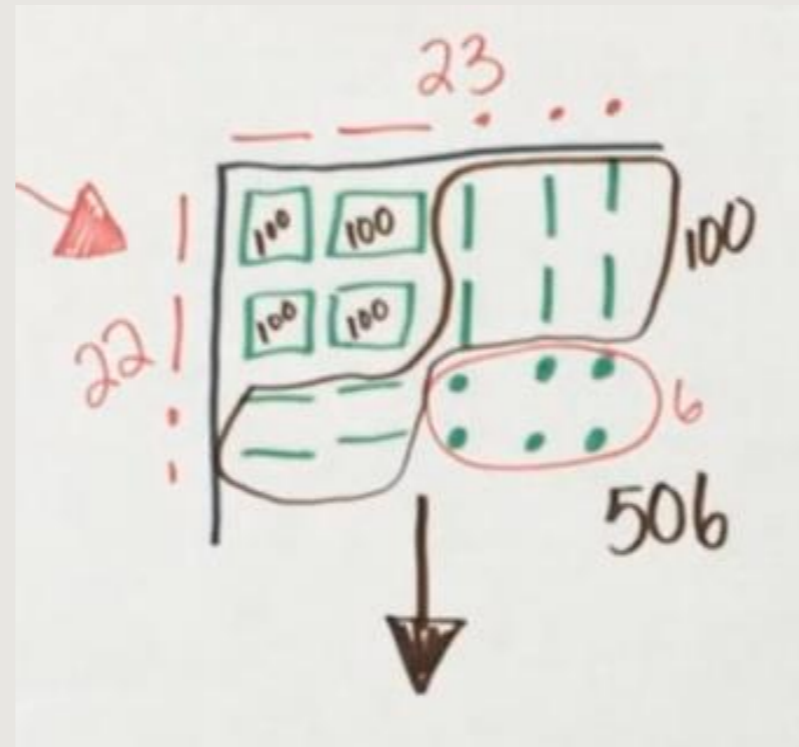
The progression of
multiplication



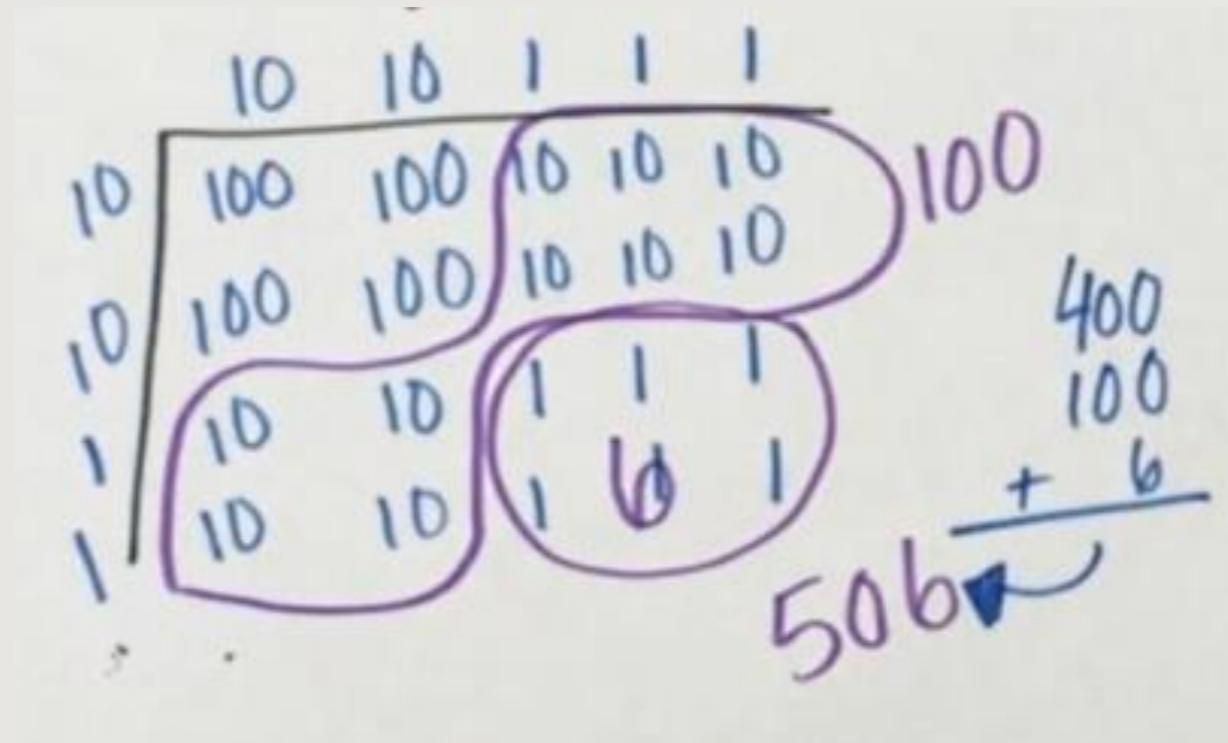


Concrete

Source: gfletchy.com




Representational



Abstract

MY OLD METHODS

$$4(x + 3)$$


$$4(x) + 4(3)$$

$$(x + 3)(x - 1)$$

F $x(x)$

O $x(-1)$

I $3(x)$

L $3(-1)$

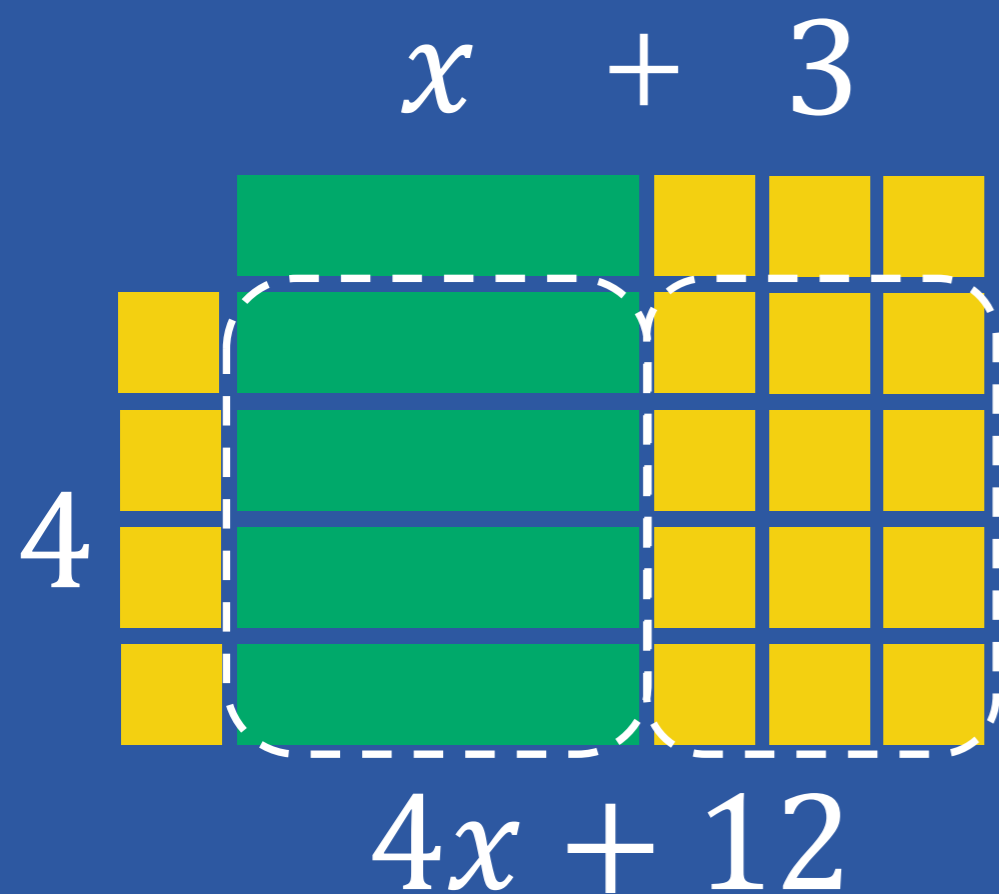
$$= x^2 - x + 3x - 3$$

$$= x^2 + 2x - 3$$

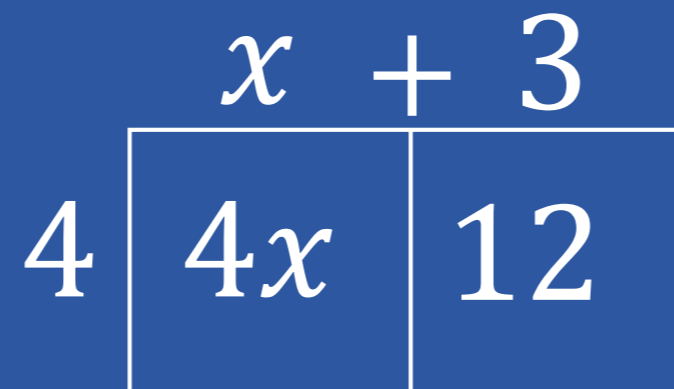
DISTRIBUTIVE PROPERTY

$$4(x + 3)$$

Concrete



Representational



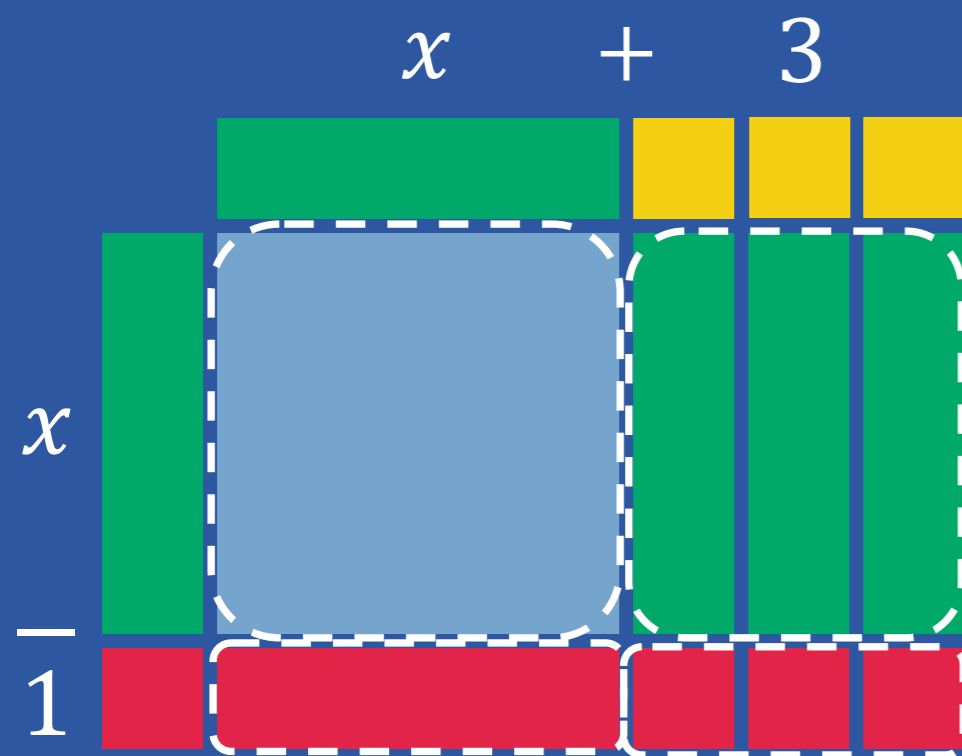
Abstract

$$\begin{aligned} &4(x + 3) \\ &= 4(x) + 4(3) \\ &= 4x + 12 \end{aligned}$$

BINOMIAL MULTIPLICATION

$$(x + 3)(x - 1)$$

Concrete



$$x^2 - x + 3x - 3$$

$$x^2 + 2x - 3$$

Representational

$$x + 3$$

x	x^2	$3x$
-1	$-x$	-3

$$x^2 - x + 3x - 3$$

$$x^2 + 2x - 3$$

Abstract

$$\begin{aligned} &(x + 3)(x - 1) \\ &= x^2 - x + 3x - 3 \\ &= x^2 + 2x - 3 \end{aligned}$$

STICKY ATTRIBUTES

SIMPLE

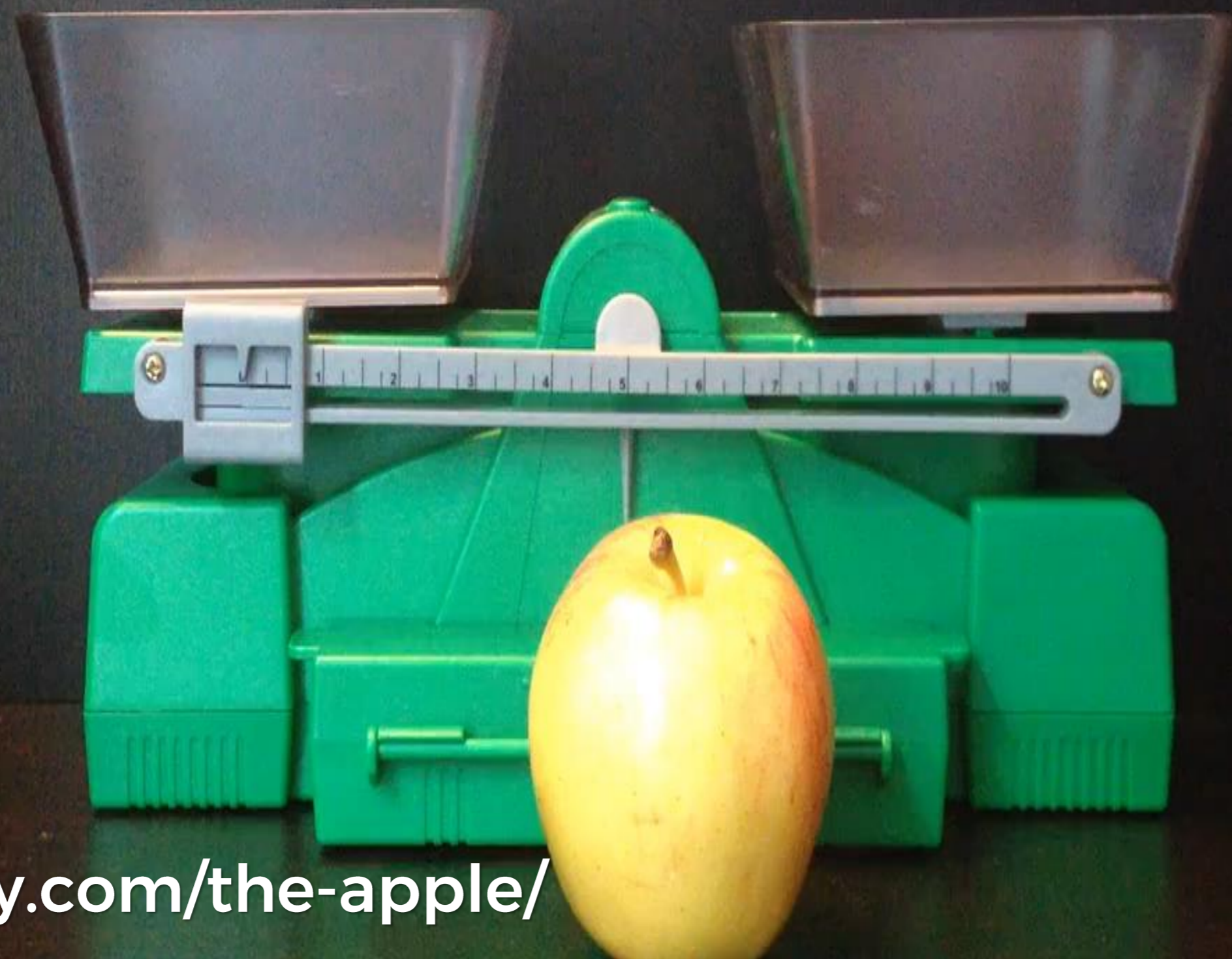
UNEXPECTED

CONCRETE

CREDIBLE

EMOTIONAL

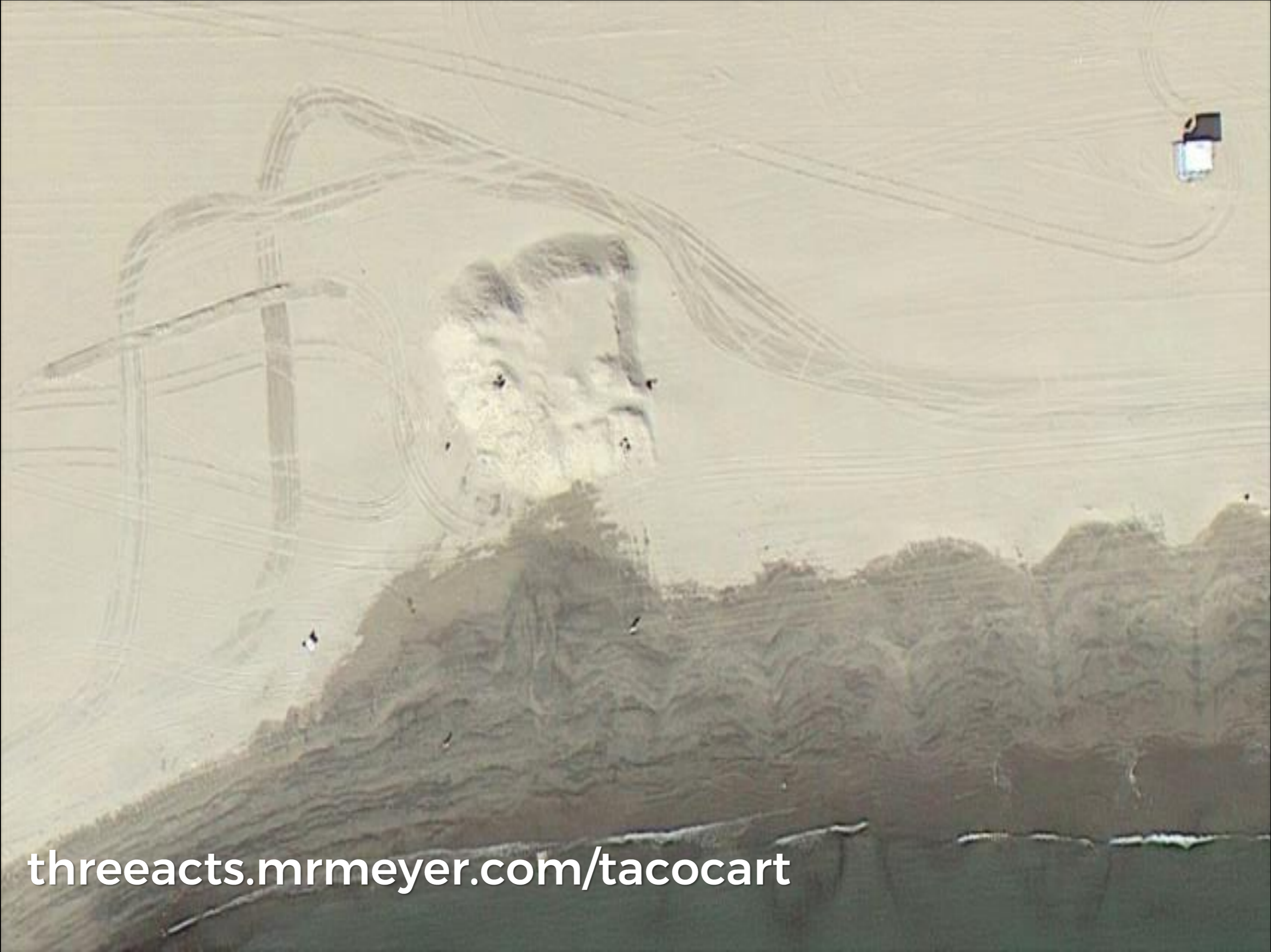
STORIES



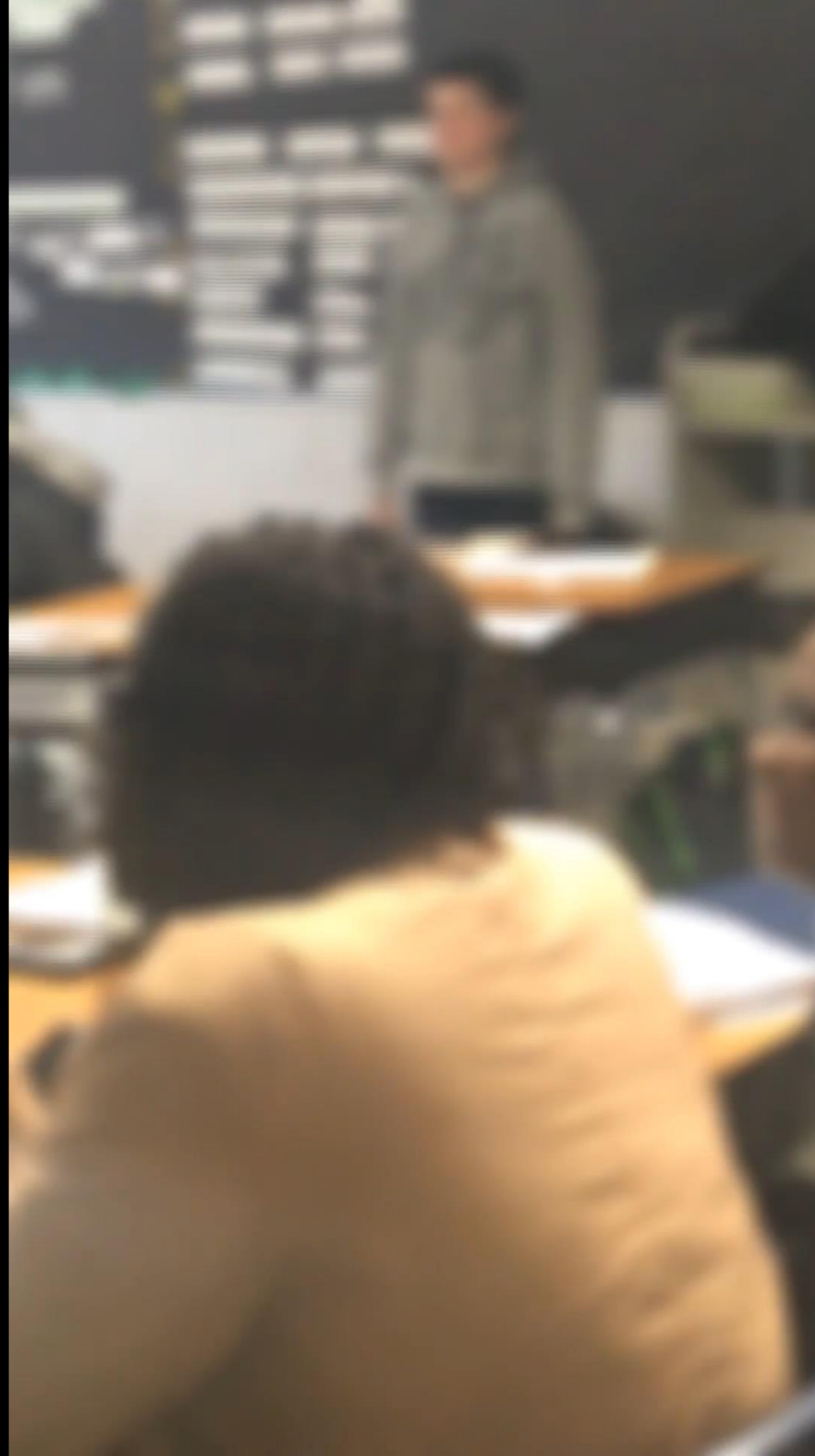
Source: gfletchy.com/the-apple/



Source: JJ Martinez



Source: threeacts.mrmeyer.com/tacocart



**Source:
Jenise Sexton**



Source: Tom Ward



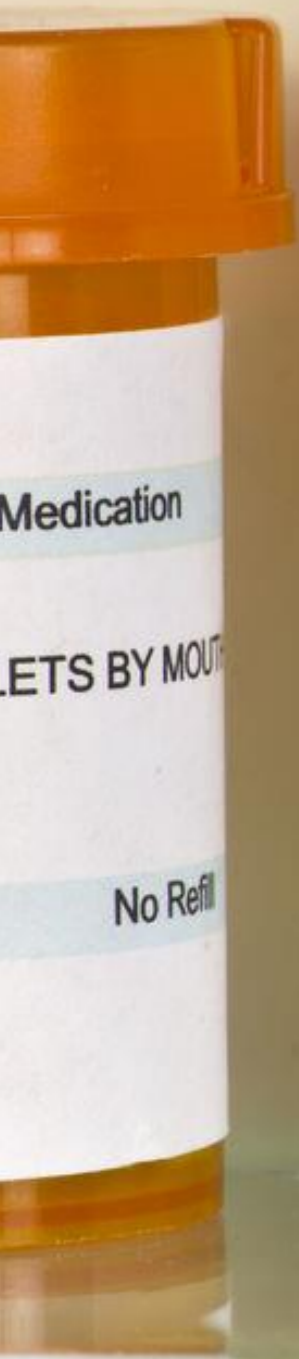
Source: Tom Ward



Source: fawnnguyen.com/barbie-bungee



**Source:
Fawn Nguyen**



Medication
TAKEN BY MOUTH
No Refill



Division

Pain Relief Fever Reduction

NSAID

200 Tablets 200 mg



Functions

Pain Reliever/ Fever Reducer
Caffeine-Free

200 tablets
325 mg each

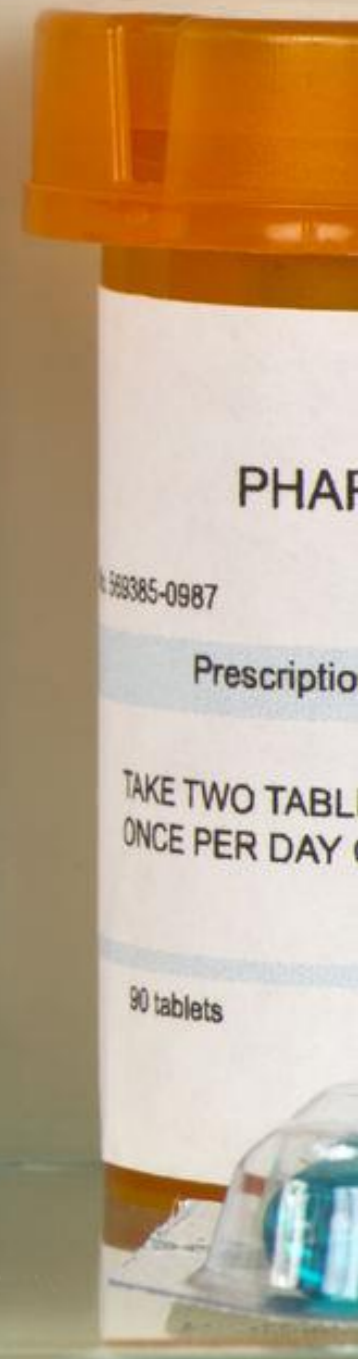


Extra Strength

Perimeter

Pain Reliever/ Fever Reducer

200 Capsules 500 mg. each





PHAR
360385-0987
Prescription
TAKE TWO TABLETS
ONCE PER DAY
90 tablets

Act 1 Engaging Opener

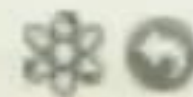
Act 2 Get Info. Solve Problem.

Act 3 Big Reveal

▶ 0:21 **We Will Rock You**
Queen — Greatest Hits I  



We Will Rock You
Queen — Greatest Hits I



0:00



Source: estimation180.com

ESTIMATION180.COM

STICKY ATTRIBUTES

SIMPLE

UNEXPECTED

CONCRETE

CREDIBLE

EMOTIONAL

STORIES







Source: mrvaudrey.com

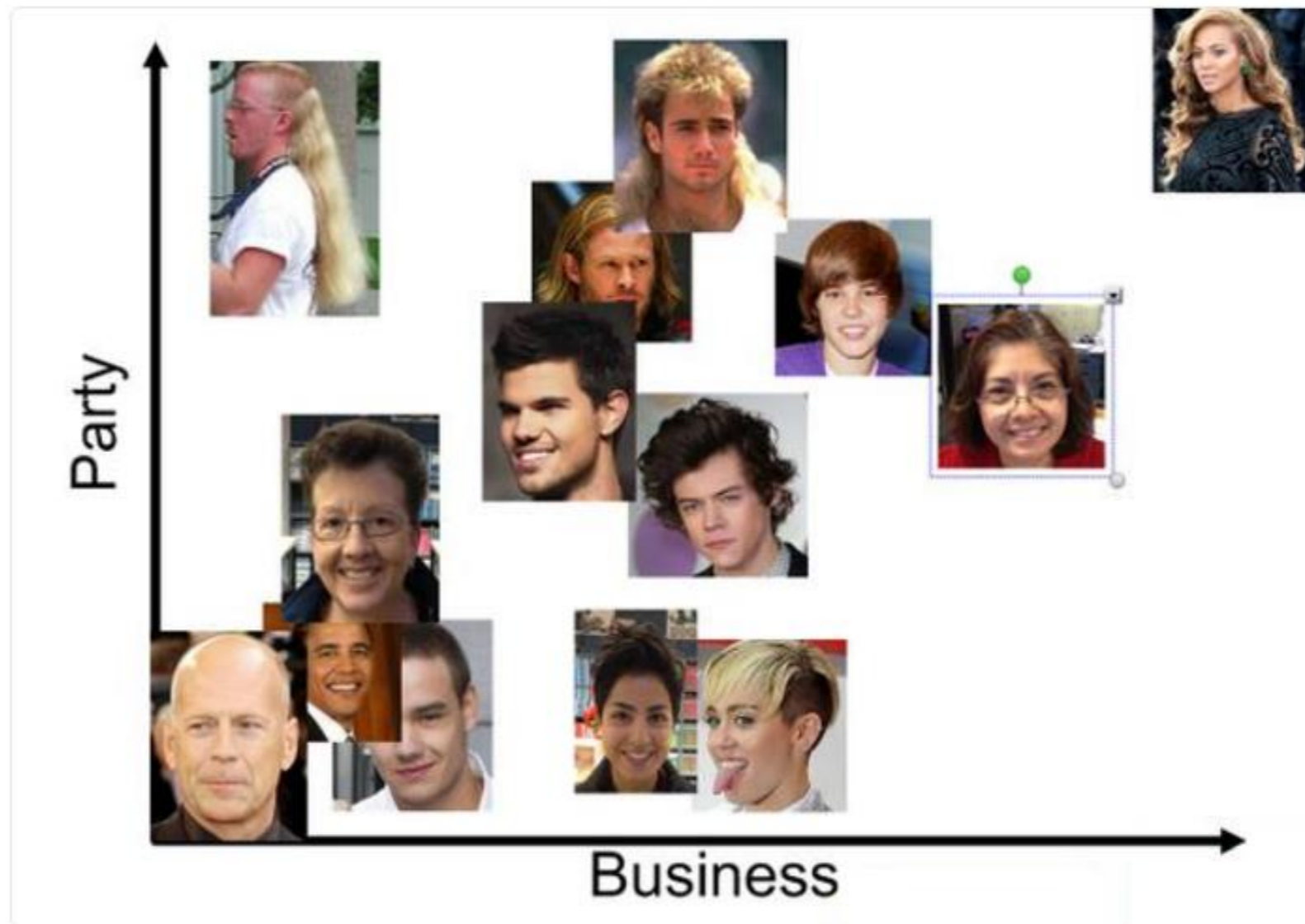


Matt Vaudrey
@MrVaudrey

Following



Things I never thought I'd say: "So you're saying that Thor has less party than Justin Bieber, but more than Obama?"



RETWEETS
4

LIKES
7



GREEN BAY

ARIZONA

	7	6	3	2	1	9	8	5	4	0
2	Vila	ROB S	SHEP	ROB S	SHEP CO.	PAPA	K+R	Vila	ROB S	DB
7	DB	DB	DB	K+R	ROB S	BILL	SHEP CO.	SHEP	SHEP CO.	DB.
8	K+R	ROB S	KB	CHRIS C	PAPA	RICK	ROB S	SHEP CO.	ROB S	KB
3	ROB S	SHEP	ROB S	DB	BILL	CHRIS C	SCHWEITZ LOCK	Vila	SHEP	SHEP CO.
4	SHEP CO.	DB	SHEP	RICK	ROB S	BILL	THE SCHWEITZ	THE SCHWEITZ	THE SCHWEITZ	THE SCHWEITZ
9	PAPA	ROB S	CHRIS C	CHRIS C	CHRIS C	KB	THE SCHWEITZ	DB	BILL	SHEP
0	DB	SHEP CO.	K+R	RICK	DB	ROB S	DB	Vila	RICK	Vila
5	BILL	DB	ROB S	ROB S	Vila	Vila	ROB S	KB	ROB S	K+R
1		ROB S		Vila	ROB S			KB	Vila	SHEP

• PAYOUTS •

1ST QUARTER \$25

HALFTIME \$50

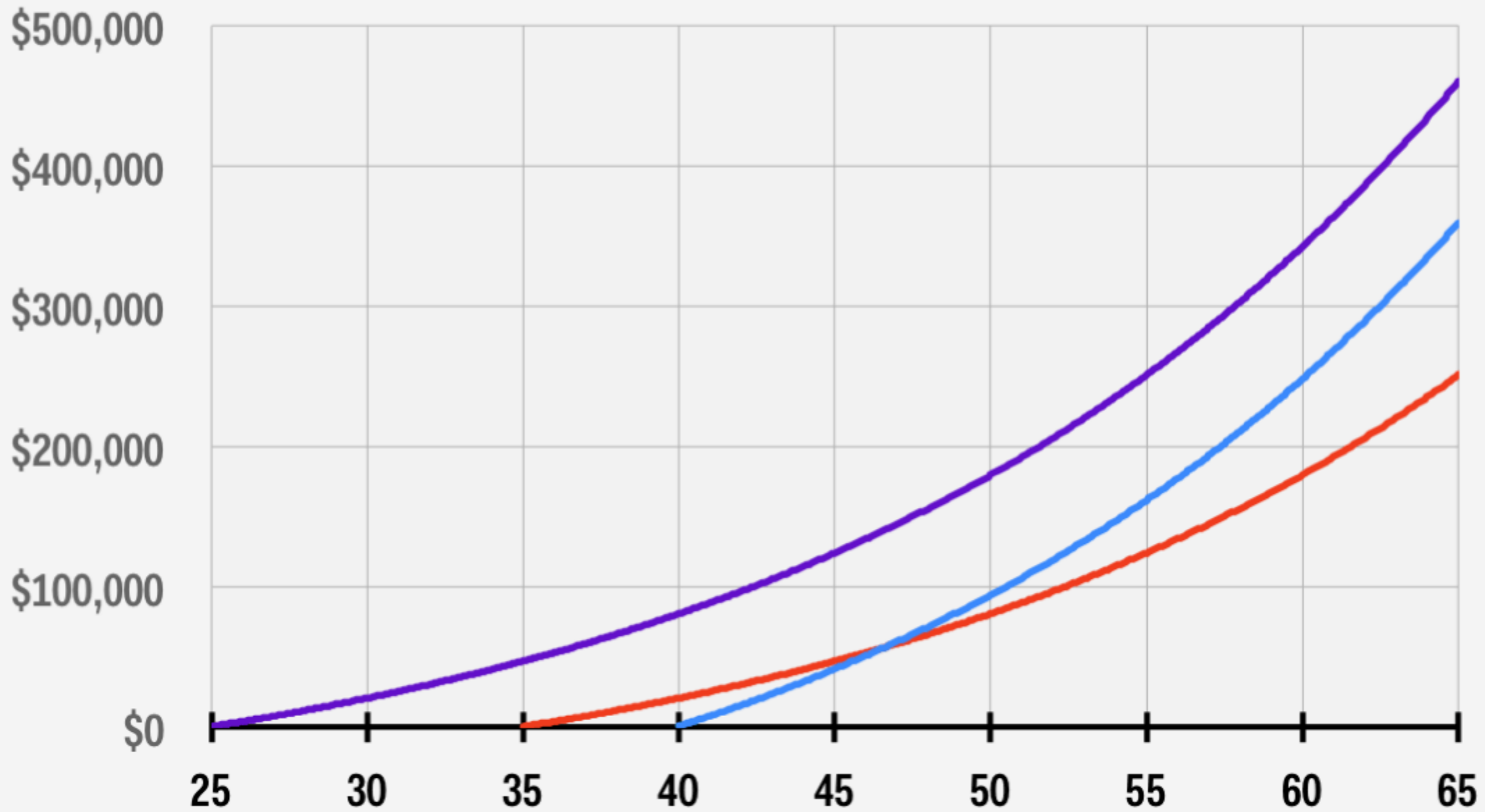
3RD QUARTER \$25

FINAL \$100

\$2 SQUARES

Start saving in your 20s

— Start at 25 — Start at 35 — Start at 40, double savings





Source: robertkaplinsky.com/lessons

tangible > magnitude

STICKY ATTRIBUTES

SIMPLE

UNEXPECTED

CONCRETE

CREDIBLE

EMOTIONAL

STORIES



Source: robertkaplinsky.com/lessons

Patrick Peterson Hasn't 'Gotten Around' to Cashing \$15 Million Bonus Check

KYLE NEWPORT 

AUGUST 25, 2014



Source: robertkaplinsky.com/lessons

20. Sports Cornerback Patrick Peterson did not deposit a \$15,361,000 signing bonus check for 27 days. Assuming a 2% interest rate, how much money did he lose by not cashing the check immediately?



11:35 34°
abc 7
abc7.com

Source: robertkaplinsky.com/lessons

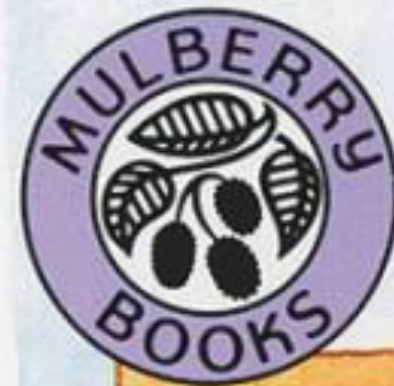
If you were as strong as an **ANT**...



Source: If You Hopped Like A Frog by David M. Schwartz

The Doorbell Rang

by Pat Hutchins



IMPORTANCE OF CONTEXT

- Play four songs
- Tapped out
- Write down song names
- Share answers with neighbors
- Listen again with song names

SONG #1



SONG #2

SONG #3



SONG #4

SONG #1

Itsy Bitsy Spider

SONG #2

Wheels On The Bus

SONG #3

**Row Row Row
Your Boat**

SONG #4

Take Me Out To The Ballgame




Robert Kaplinsky

@robertkaplinsky



Random favor: please listen to me tapping out 4 songs and try to guess the name. Should take < 2 min. It's not easy!

	<p>Recognizing Tapped Songs</p> <p>Please listen to each of the four songs, type in the name of the song, and the click submit. You may have no clue about what the song is called. If that happens, just write something like, "I don't..."</p> <p>docs.google.com</p>
---	--

RETWEET

1



2:47 PM - 13 Jun 2017

TAKEAWAYS (PART ONE)

- Of 192 people surveyed:
 - Itsy Bitsy Spider: ~41%
 - Wheels on the Bus: ~29%
 - Row Your Boat: ~25%
 - Take Me Out to the Ballgame: ~3%

TAKEAWAYS (PART TWO)

- Many said, “I’m sorry. I don’t know.”
- Many said, “I’m not good at this.”
- Many said, “I don’t like this.”

COURSE OF KNOWLEDGE

Context



Dissertation

Executive Summary

Formulas

Abstract

STICKY ATTRIBUTES

SIMPLE

UNEXPECTED

CONCRETE

CREDIBLE

EMOTIONAL

STORIES

SIMPLE

UNEXPECTED

CONCRETE

CREDIBLE

EMOTIONAL

STORIES



SIMPLE

UNEXPECTED

CONCRETE

CREDIBLE

EMOTIONAL

STORIES

NAME: _____

DATE: _____

Lesson 12 Skills Practice

Objective: Write PIN Backwards

Write backwards.

1. 0461
1640

2. 3625
5263

3. 9572
2759

4. 8713
3178

7. 6842
2486

8. 7532
2357

9. 1549
9415

13.

14

8109

DISCUSSION QUESTIONS

- Which of the attributes (simple, unexpected, concrete, credible, emotional, and stories) resonates most with you and why?
- How can we apply these attributes to how we teach mathematics?

GOALS

WHAT IS INTELLIGENCE?

WHY DON'T STUDENTS REMEMBER?

WHAT MATHEMATICS IS IMPORTANT?

WHAT MIGHT IT LOOK LIKE?

WHAT ABOUT WHAT WE USED TO DO?



Doritos® & Cheetos® Mix **20** Singles

6 DORITOS® Nacho Cheese Flavored Tortilla Chips 1 OZ. EA. 6 DORITOS® COOL RANCH® Flavored Tortilla Chips 1 OZ. EA. 3 CHEETOS® Puffs Cheese Flavored Snacks 7/8 OZ. EA. 5 CHEETOS® Crunchy Cheese Flavored Snacks 1 OZ. EA.

20 INDIVIDUAL BAGS: 3-7/8 OZ. EACH, 17-1 OZ. EACH, TOTAL NET WT. 19 5/8 OZ. (1 LB. 3 5/8 OZ.) 556.3 g ⚠ WARNING: PREVENT ENTANGLEMENT AND STRANGULATION. KEEP THIS BAG AWAY FROM YOUNG CHILDREN. IT IS NOT A TOY.

THINKING TIME

- Why did you expect there to be five of each?
- Why was it not five of each?
- How did they decide on this combination?



Classic Mix

20
Singles

4 LAY'S® Classic Potato Chips, 4 DORITOS® Nacho Cheese Flavored Tortilla Chips, 2 DORITOS® COOL RANCH® Flavored Tortilla Chips, 4 CHEETOS® Crunchy Cheese Flavored Snacks, 2 SUNCHIPS® Original Multigrain Snacks, 4 FRITOS® Original Corn Chips (All 1 OZ. Each)

20 INDIVIDUAL BAGS: 1 OZ. EACH, TOTAL NET WT. 20 OZ. (1 LB. 4 OZ.) 567 g

⚠ WARNING: PREVENT ENTANGLEMENT AND STRANGULATION. KEEP THIS BAG AWAY FROM YOUNG CHILDREN. IT IS NOT A TOY.

WHAT MATH IS IMPORTANT?

- WHAT CAN MATH MODELING FEEL LIKE?
- HOW IS MATH MODELING USED?
- IS IT JUST CREATING THE MODEL?
- WHAT IS NOT MATH MODELING?
- WHAT MIGHT IT LOOK LIKE?
- HOW DO YOU COMPARE PROBLEMS?







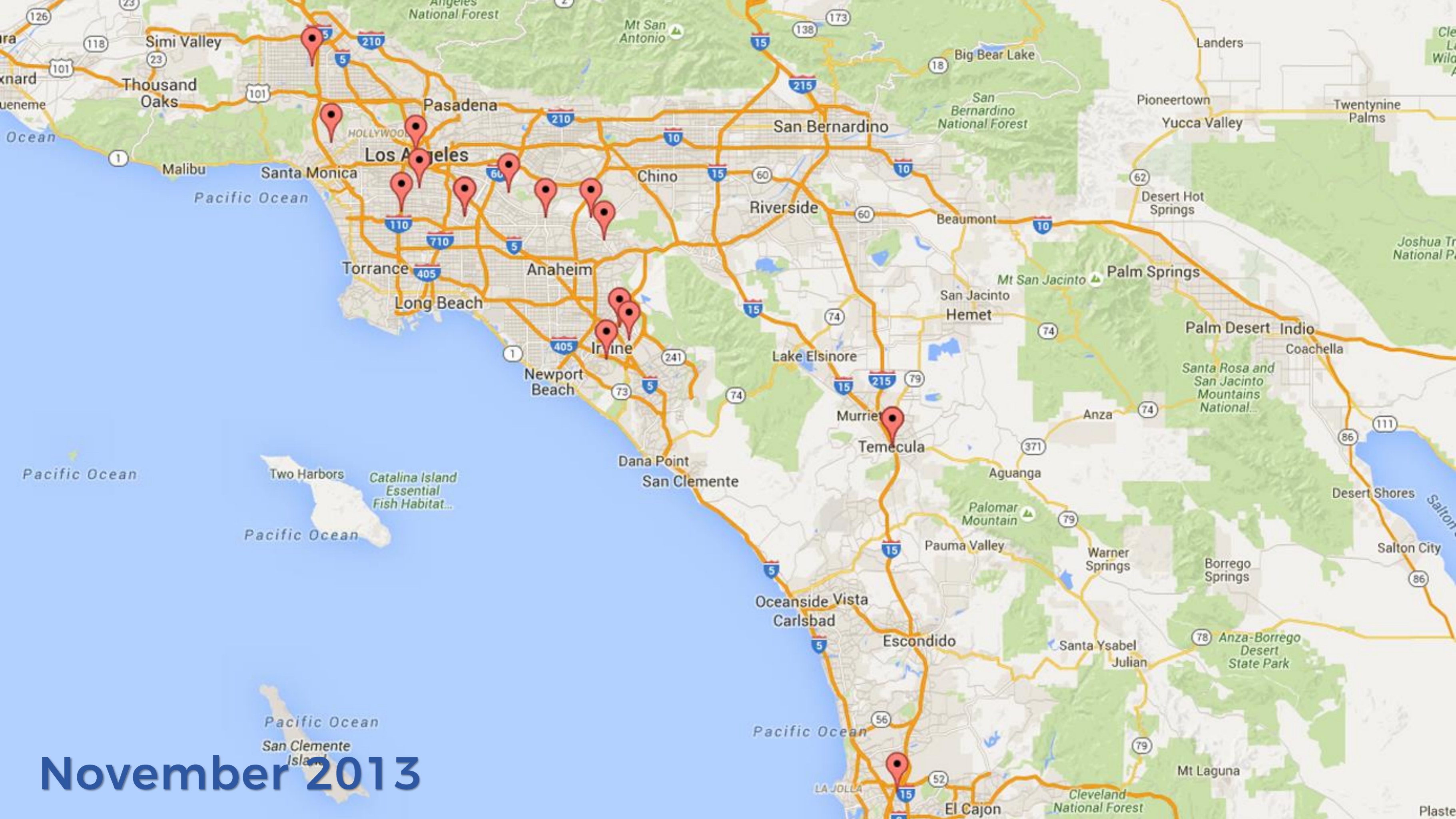




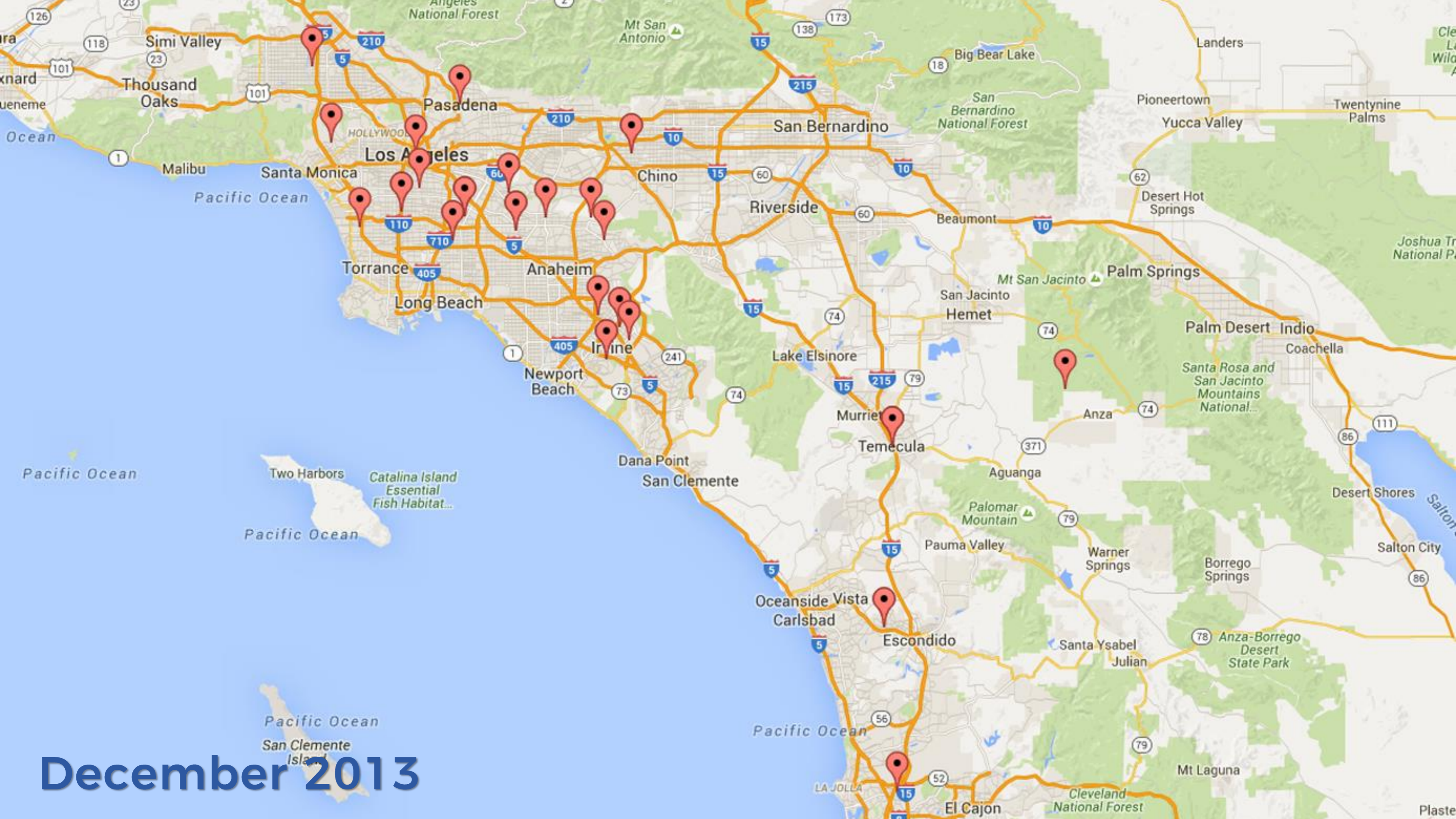
Spies

Analysts

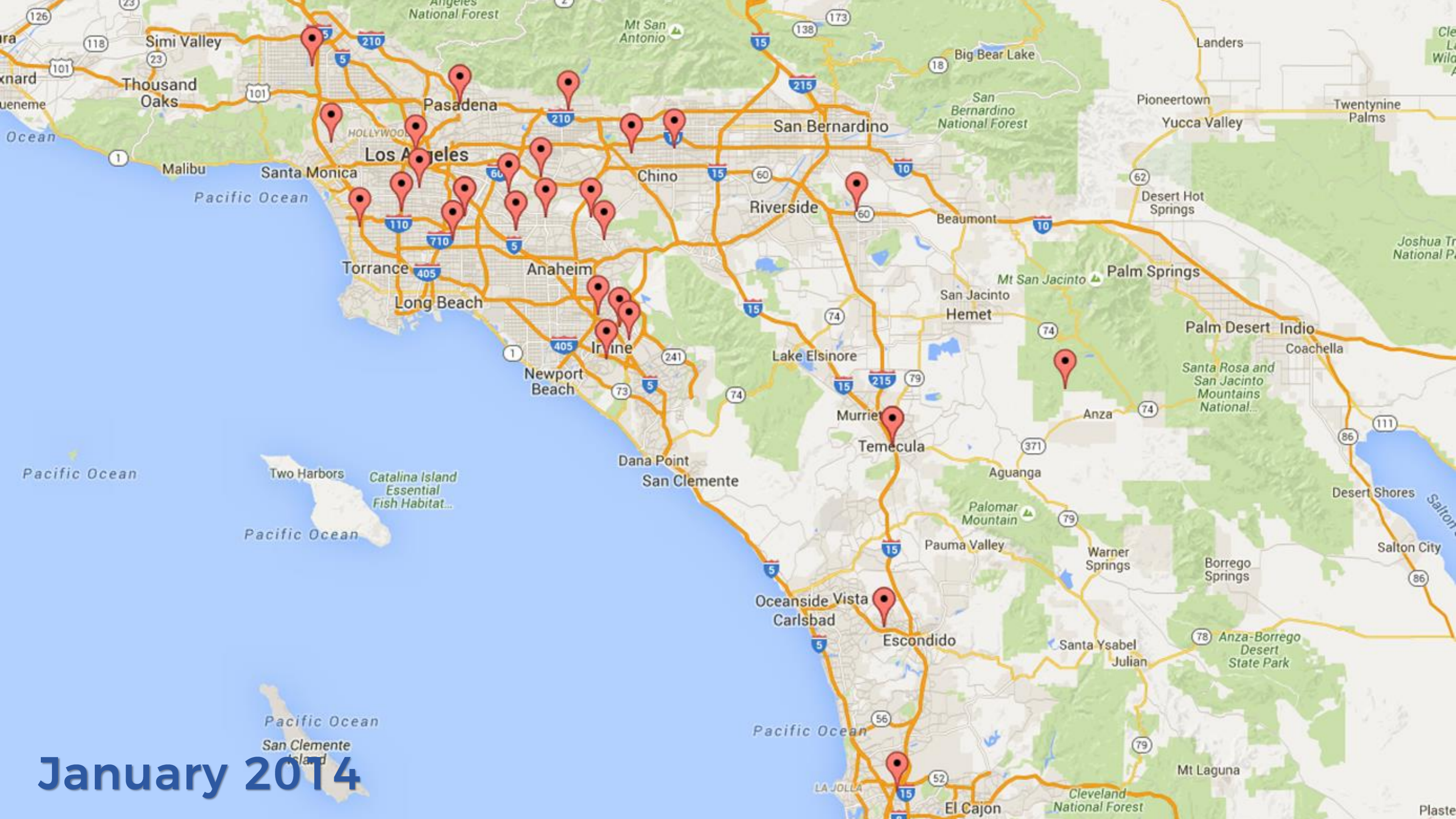
Model



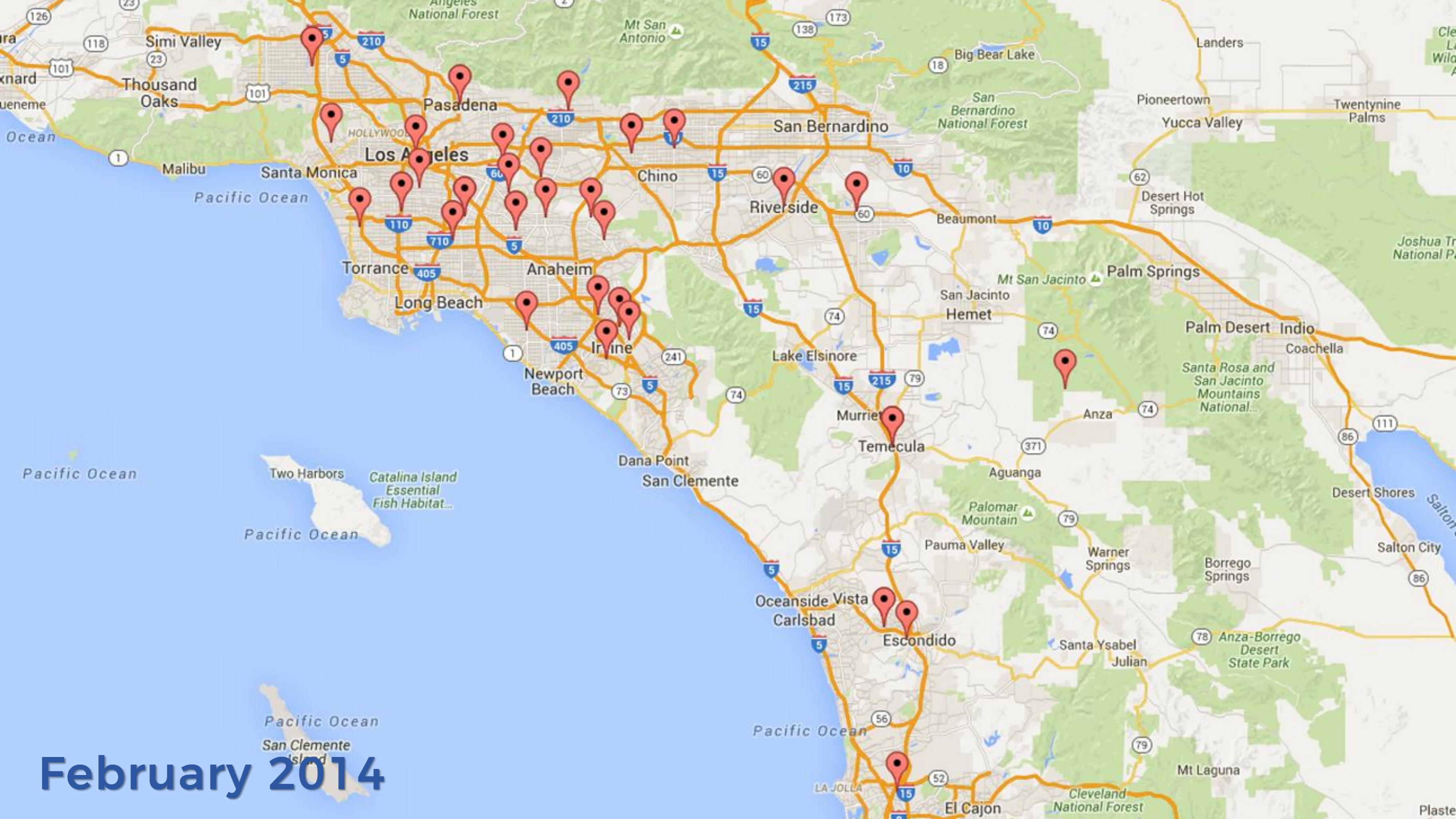
November 2013



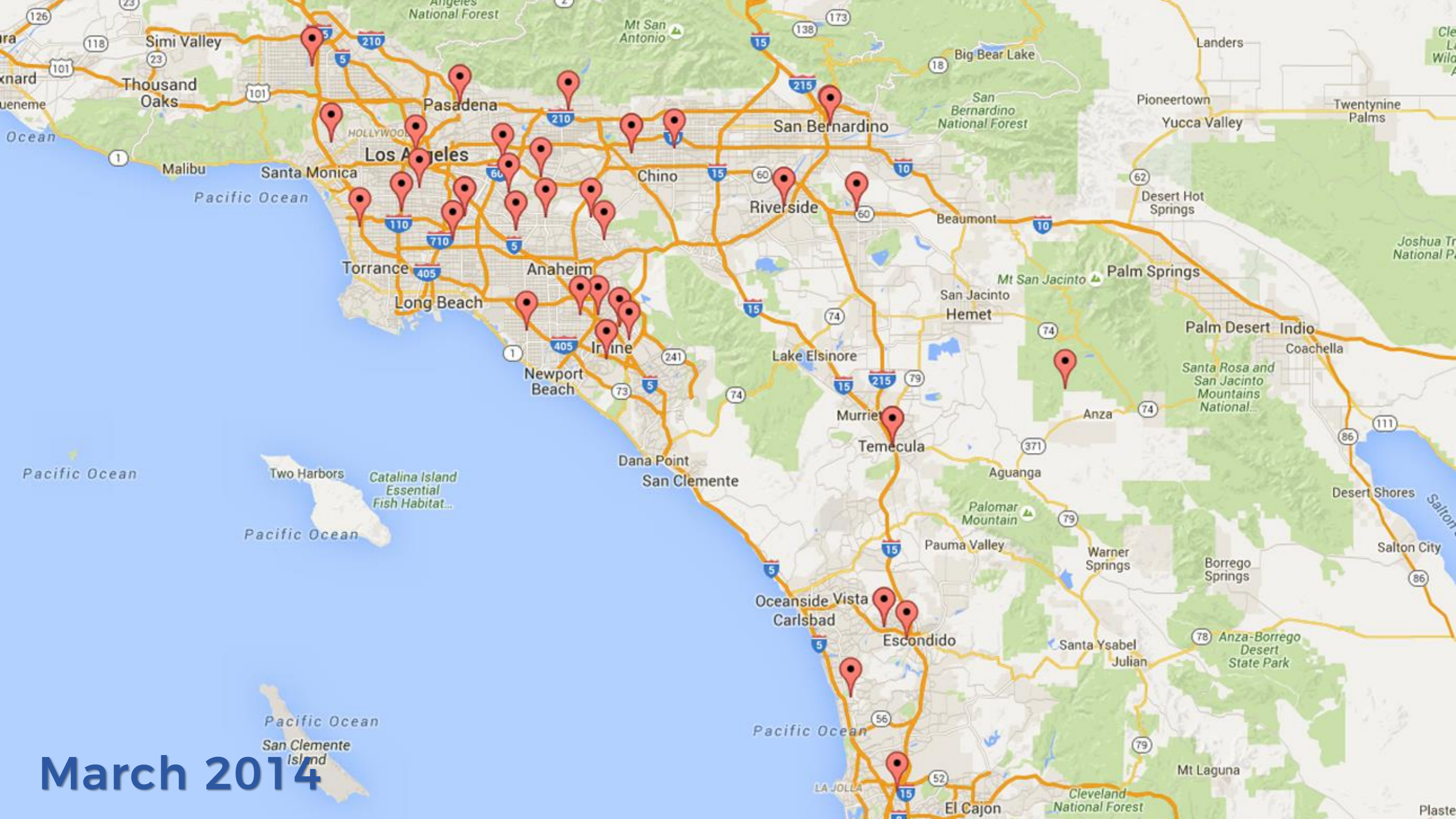
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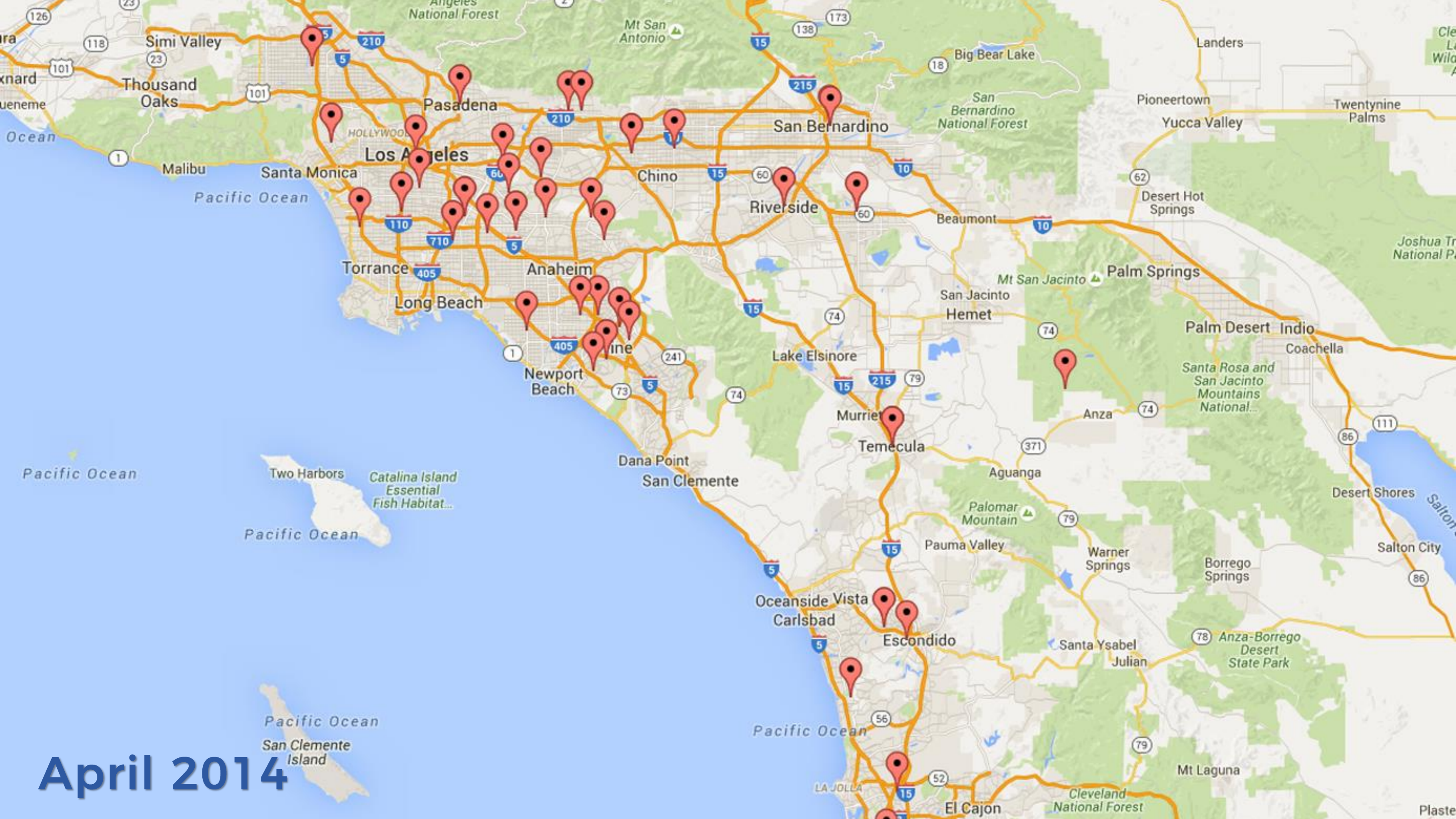
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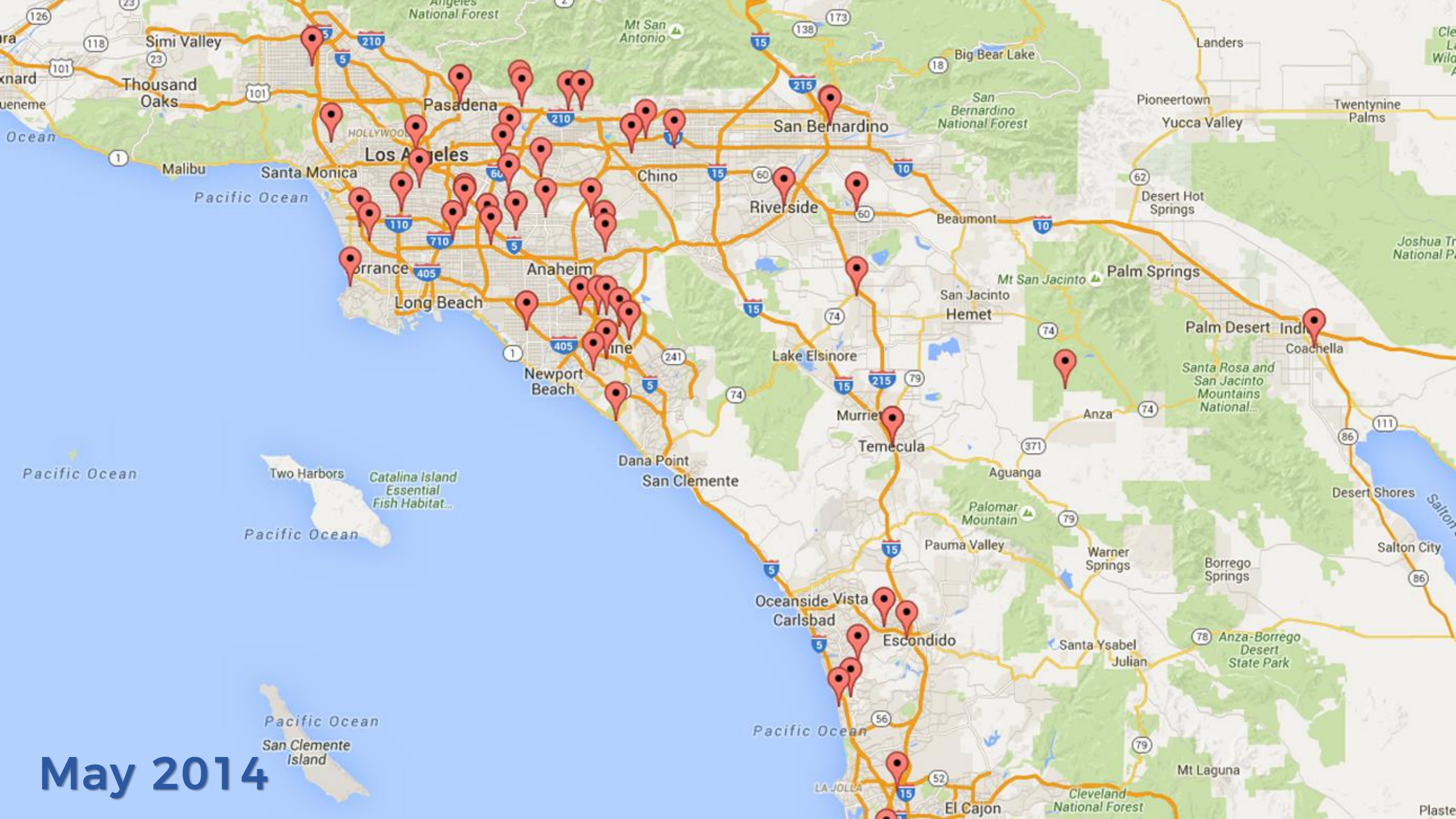
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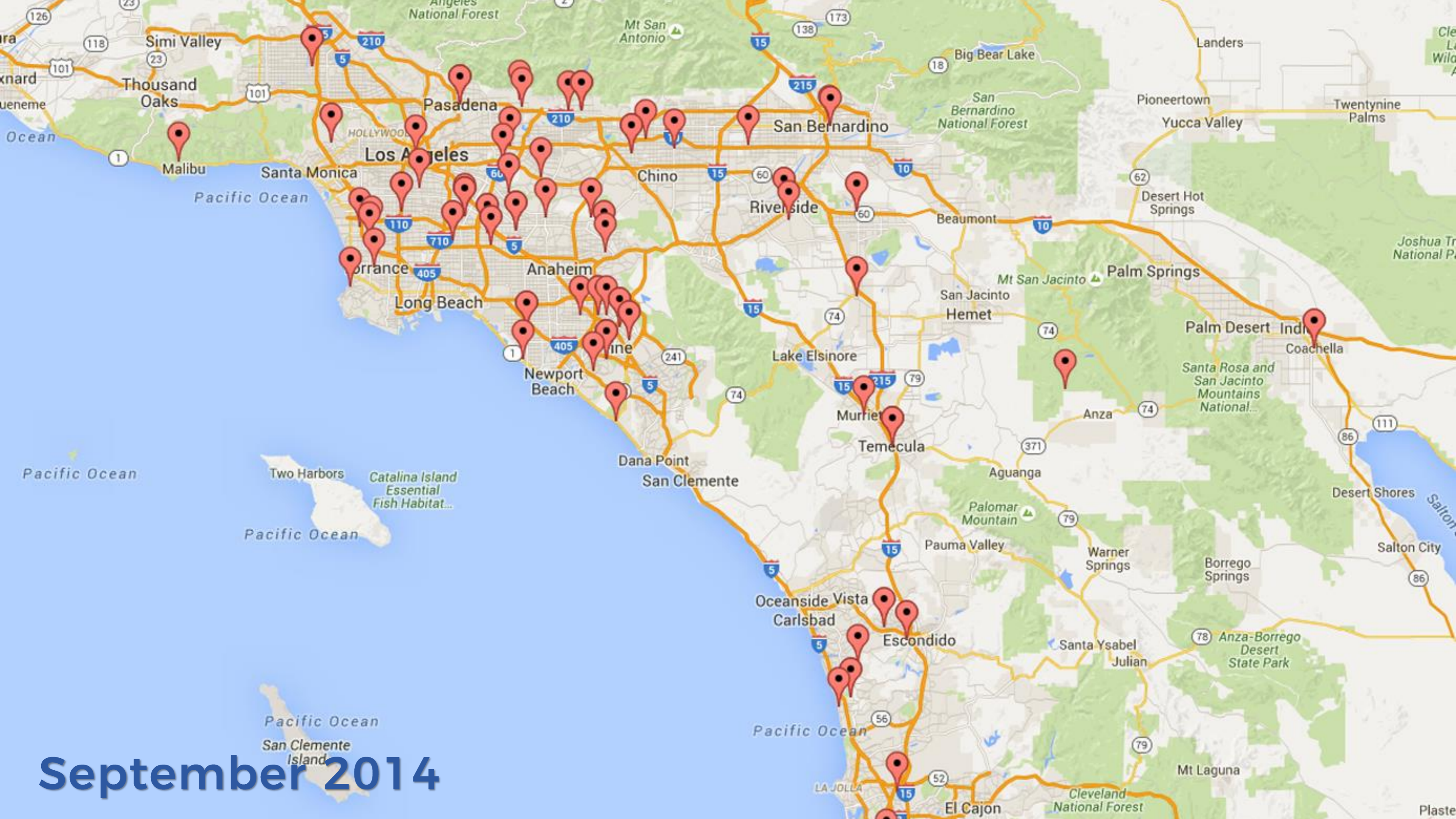
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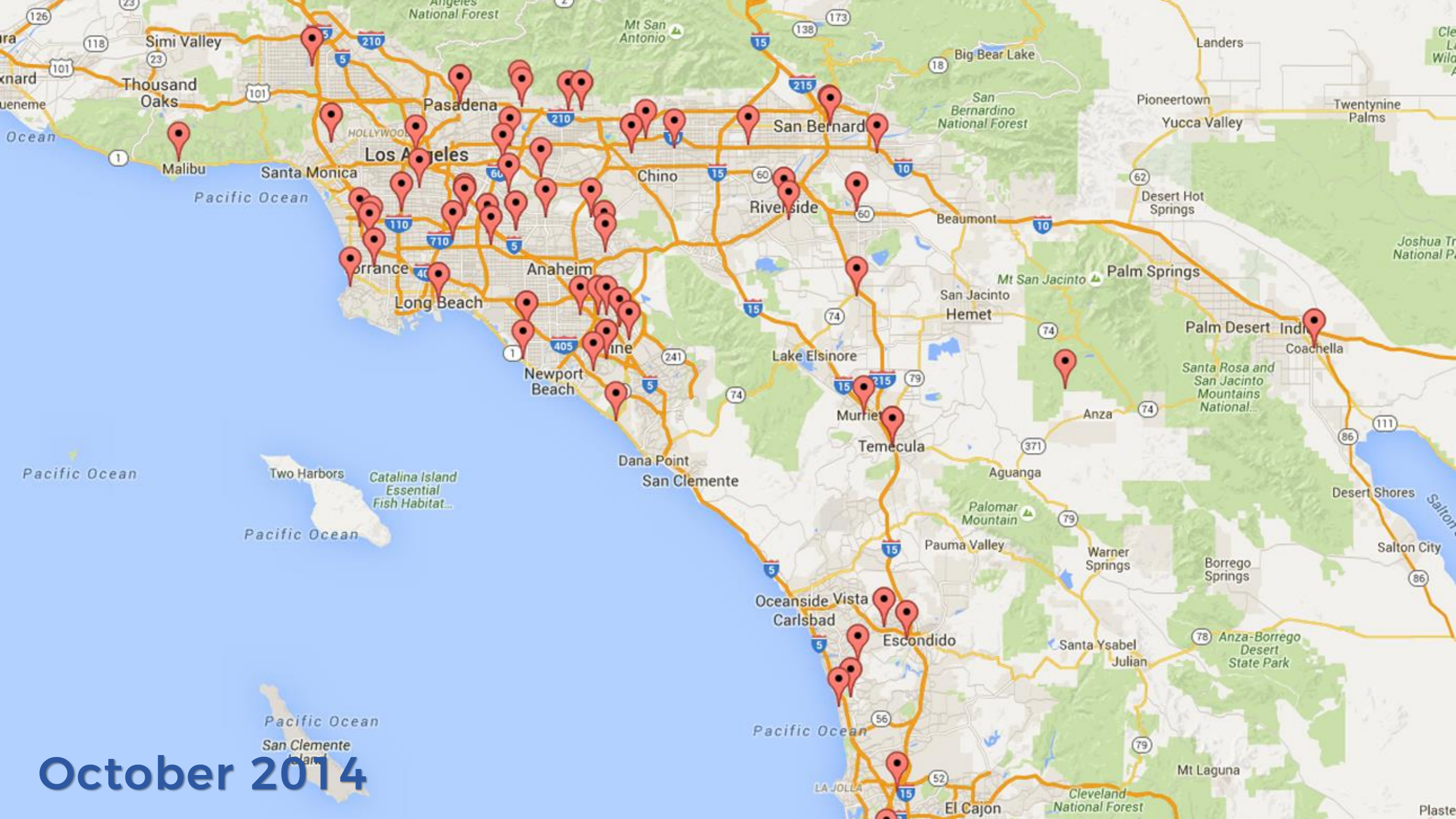
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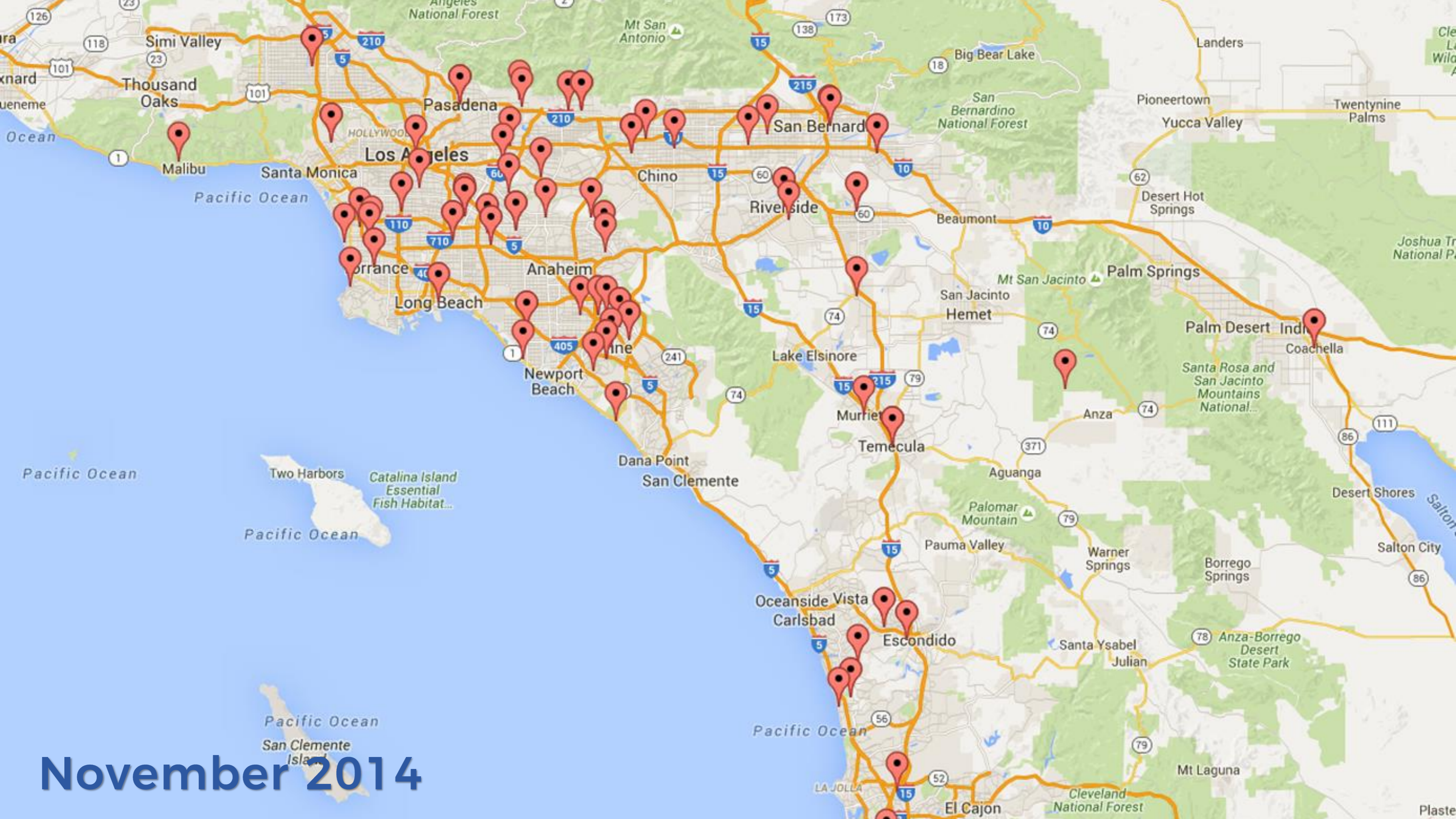
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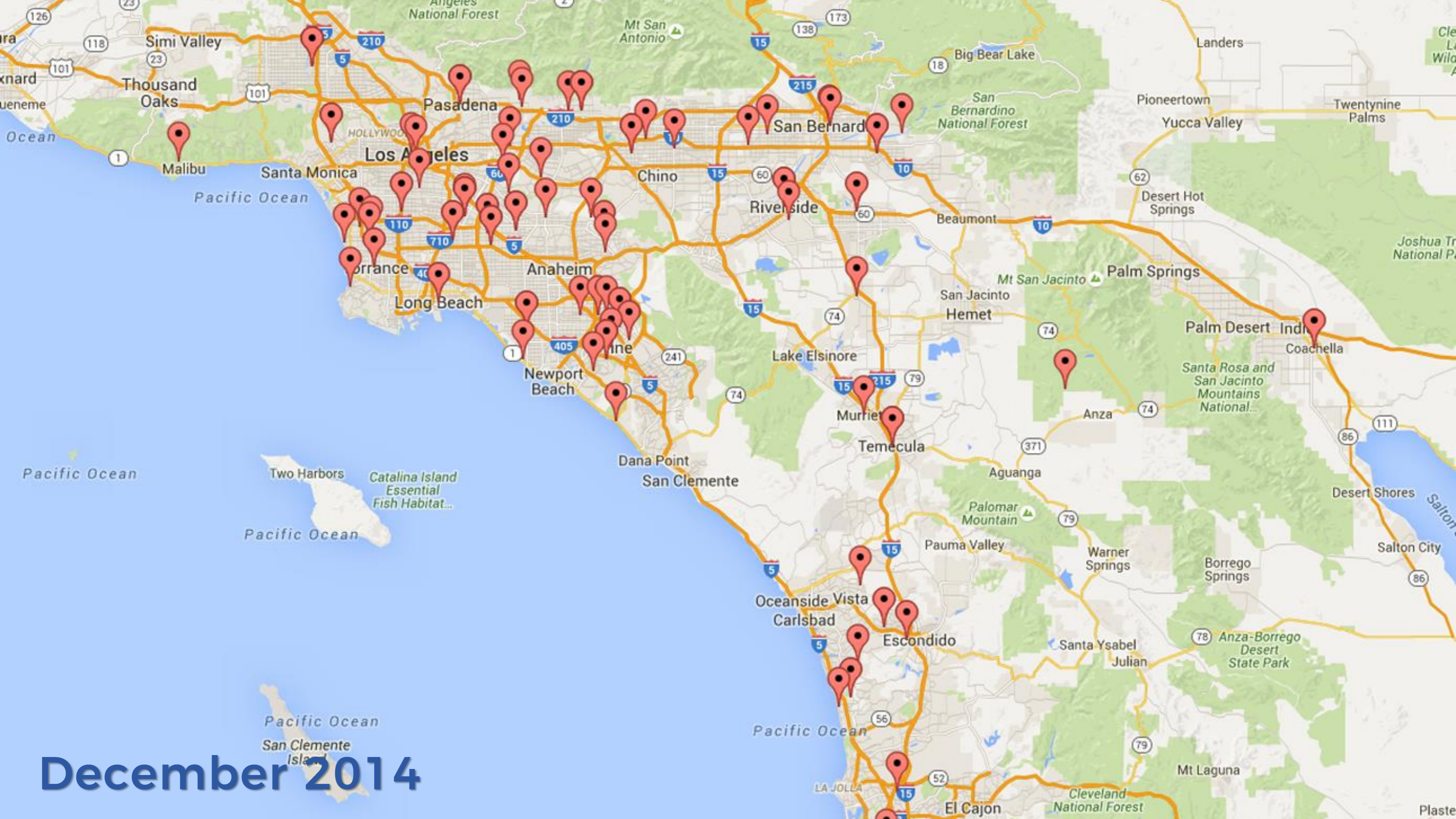
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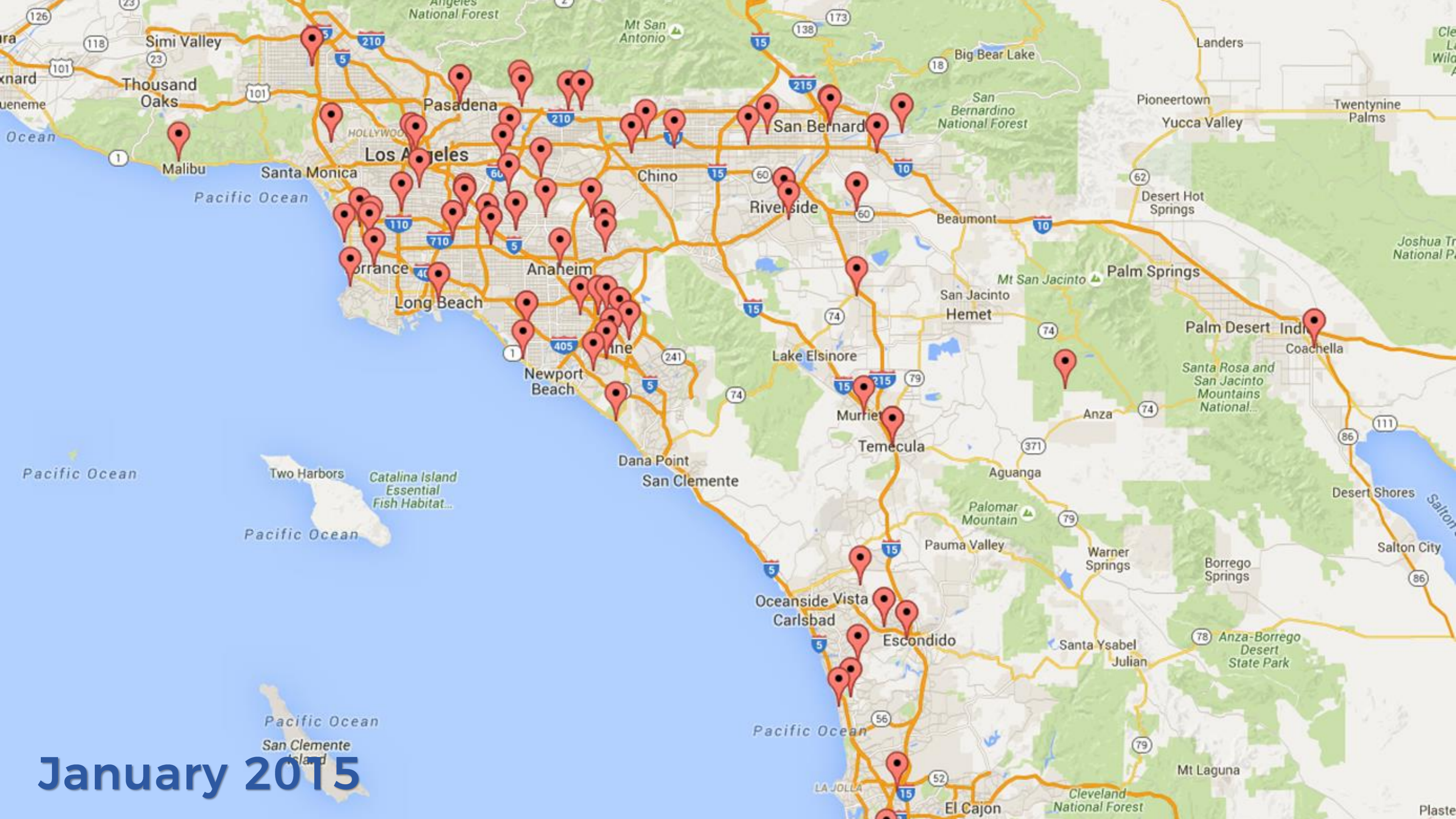
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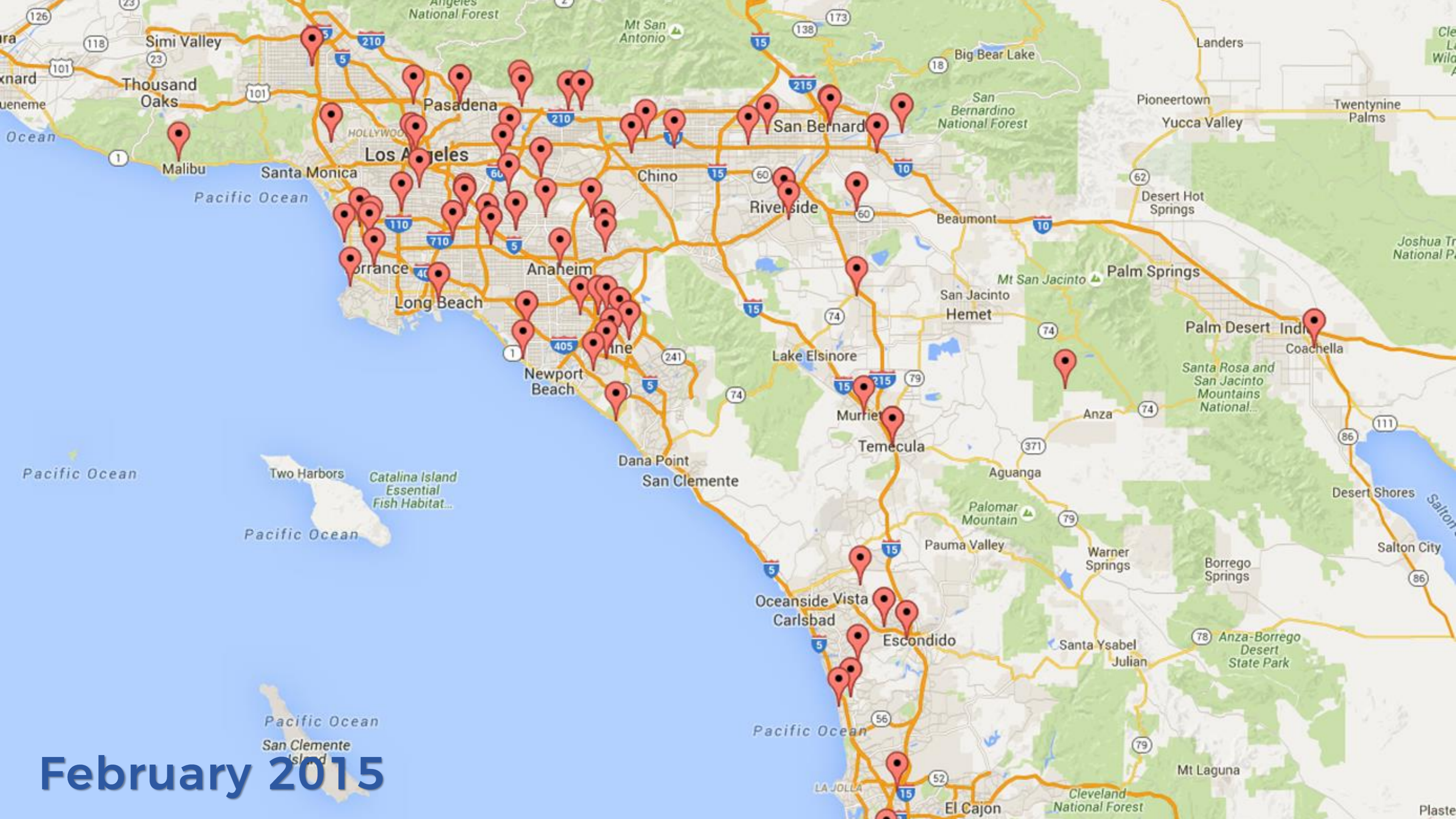
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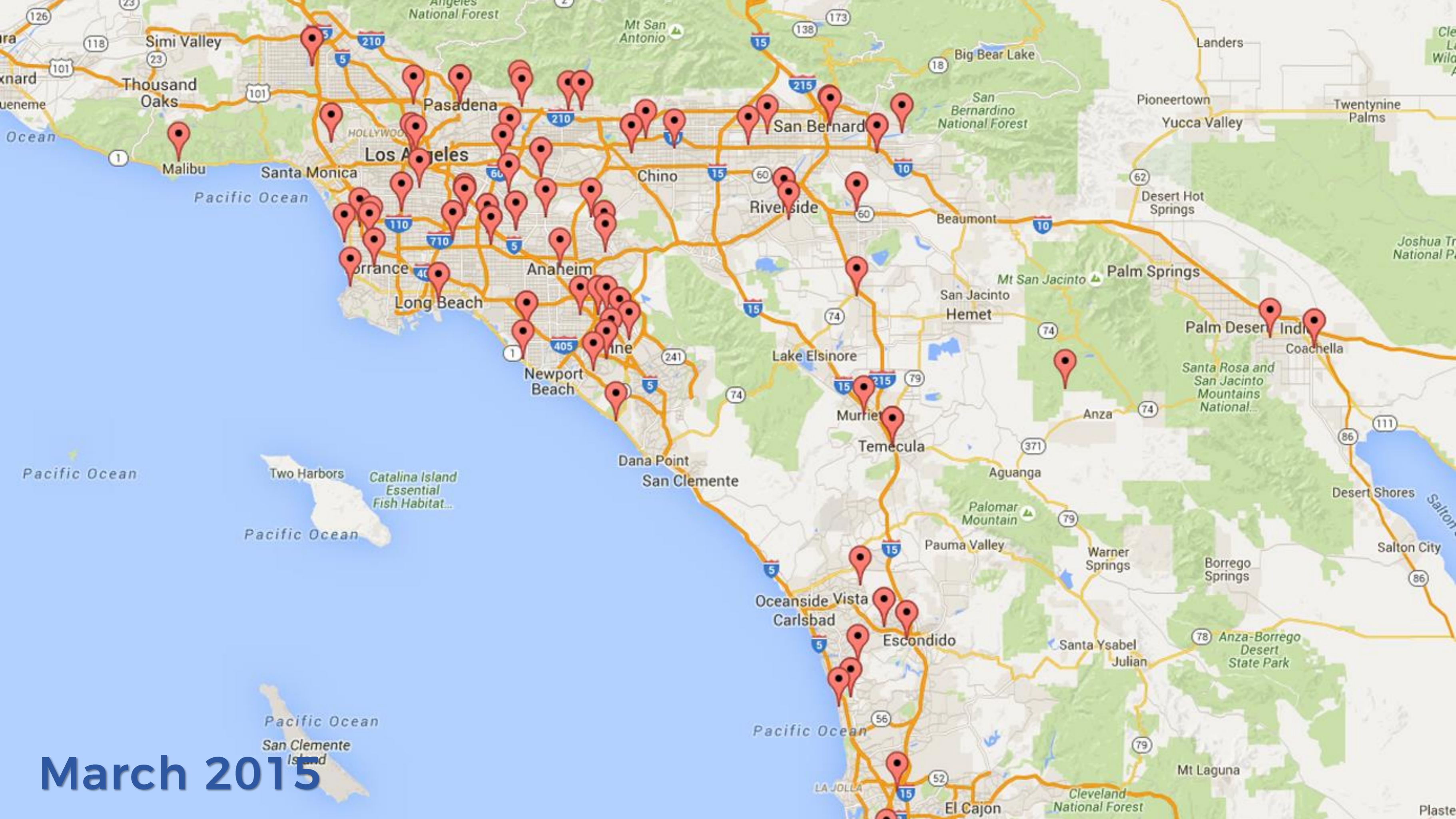
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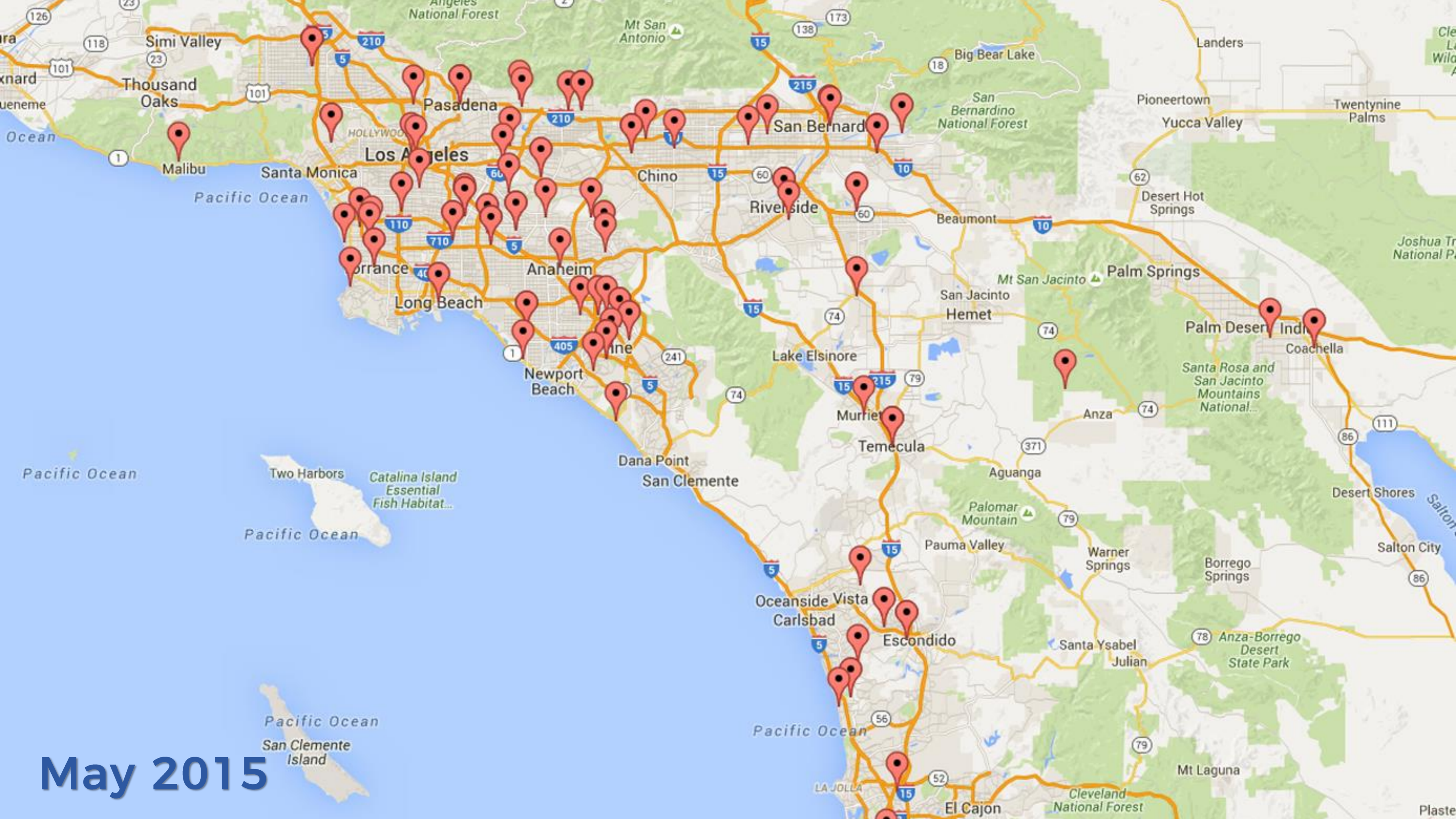
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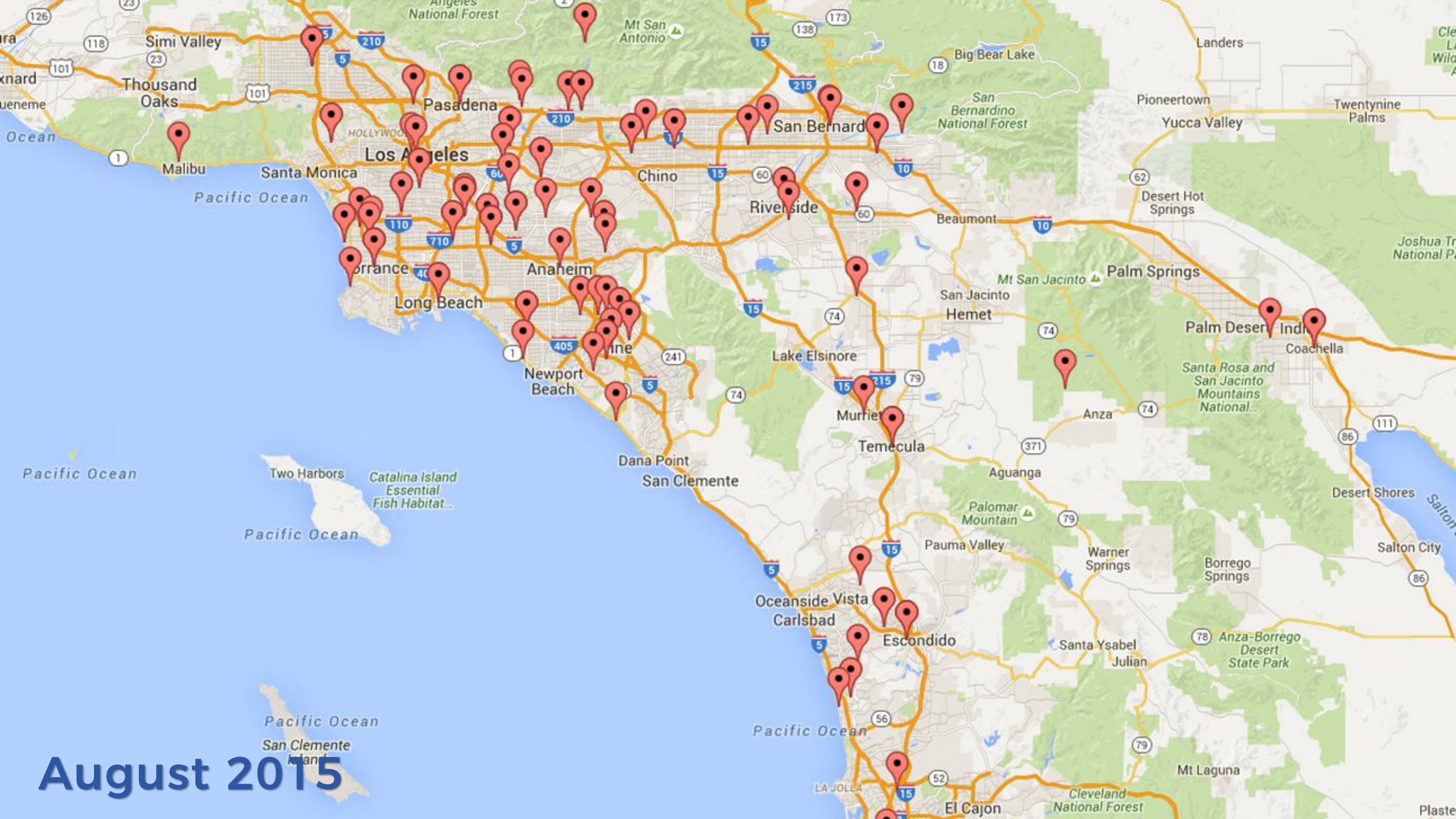
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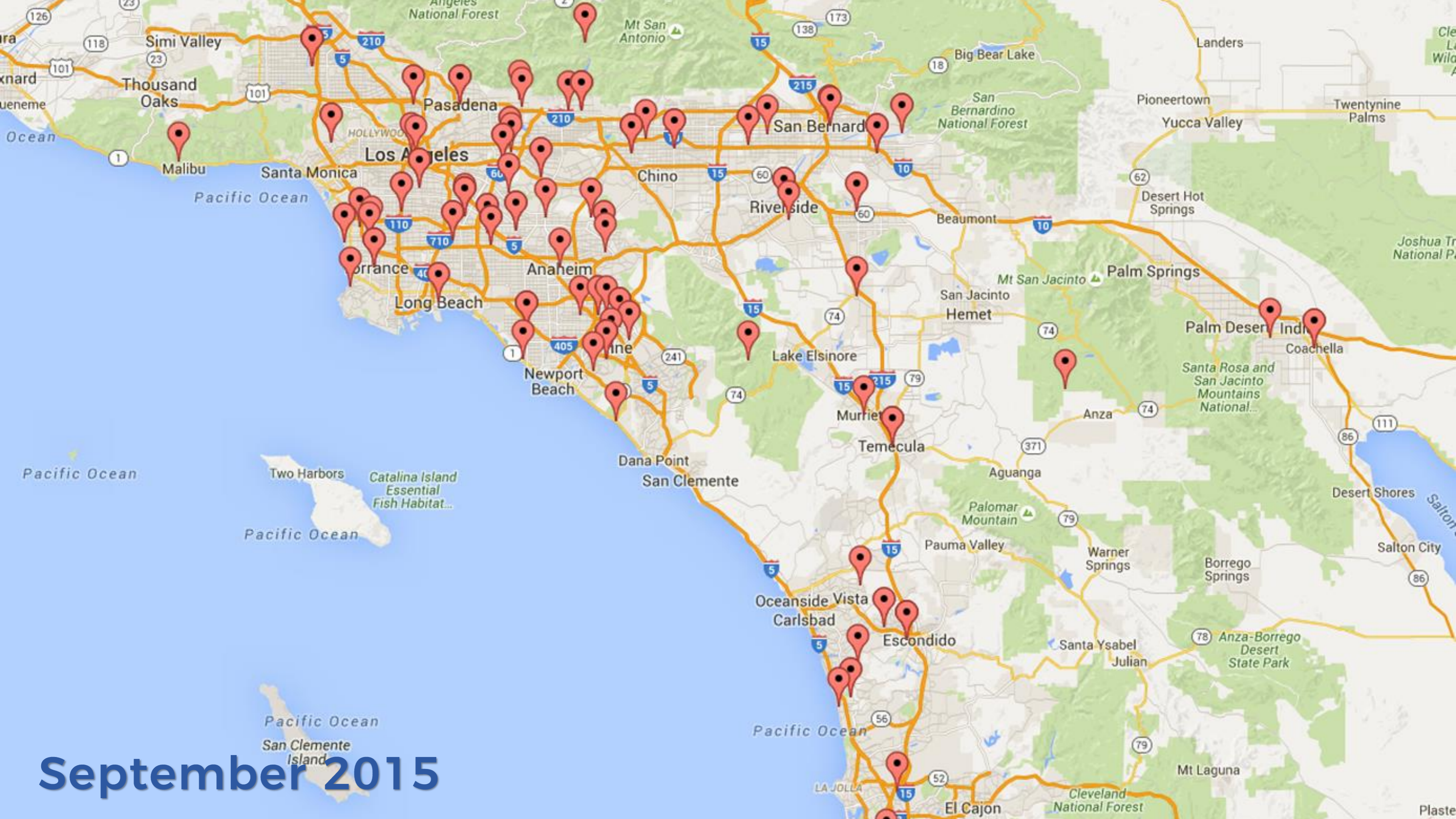
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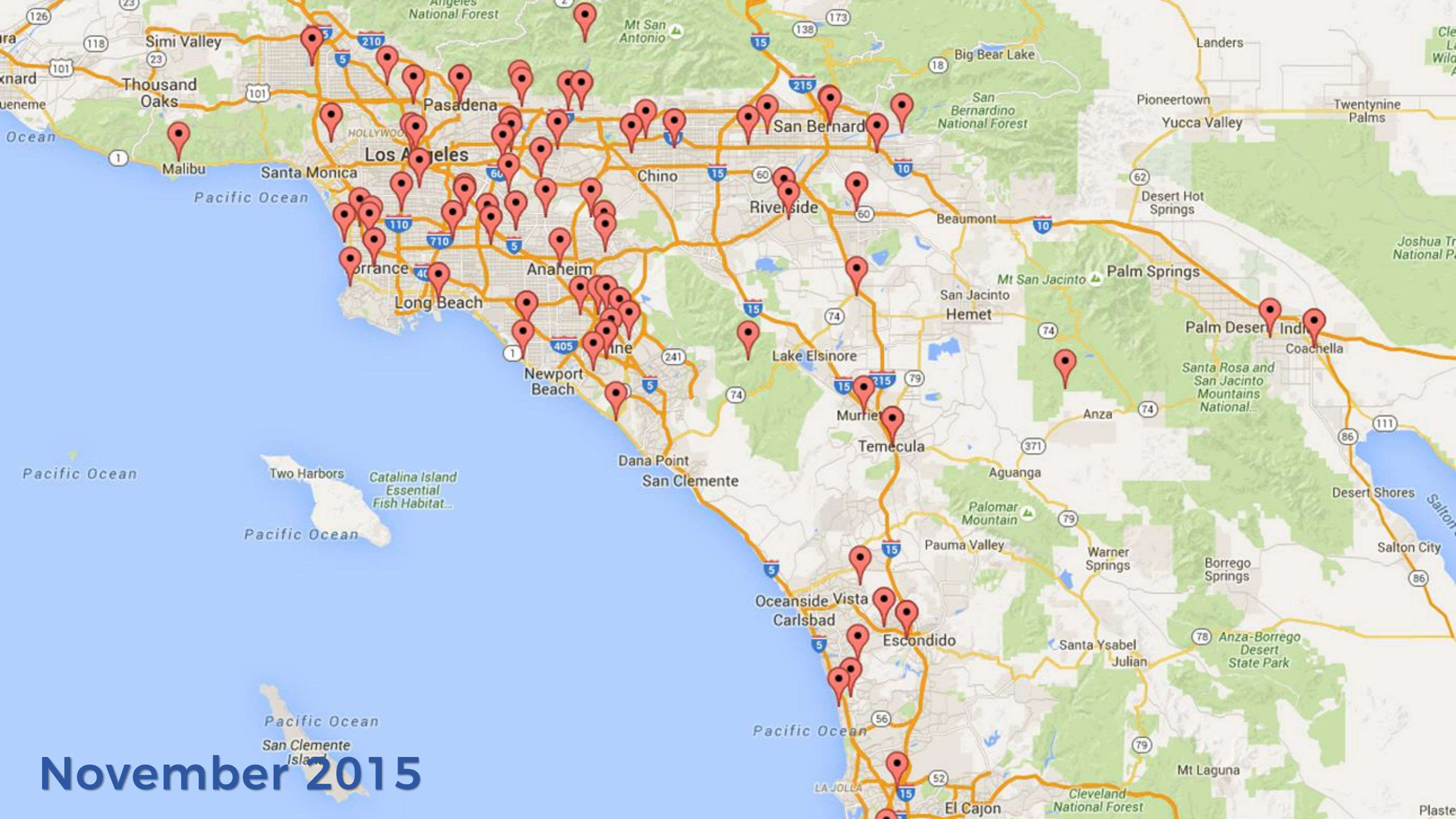
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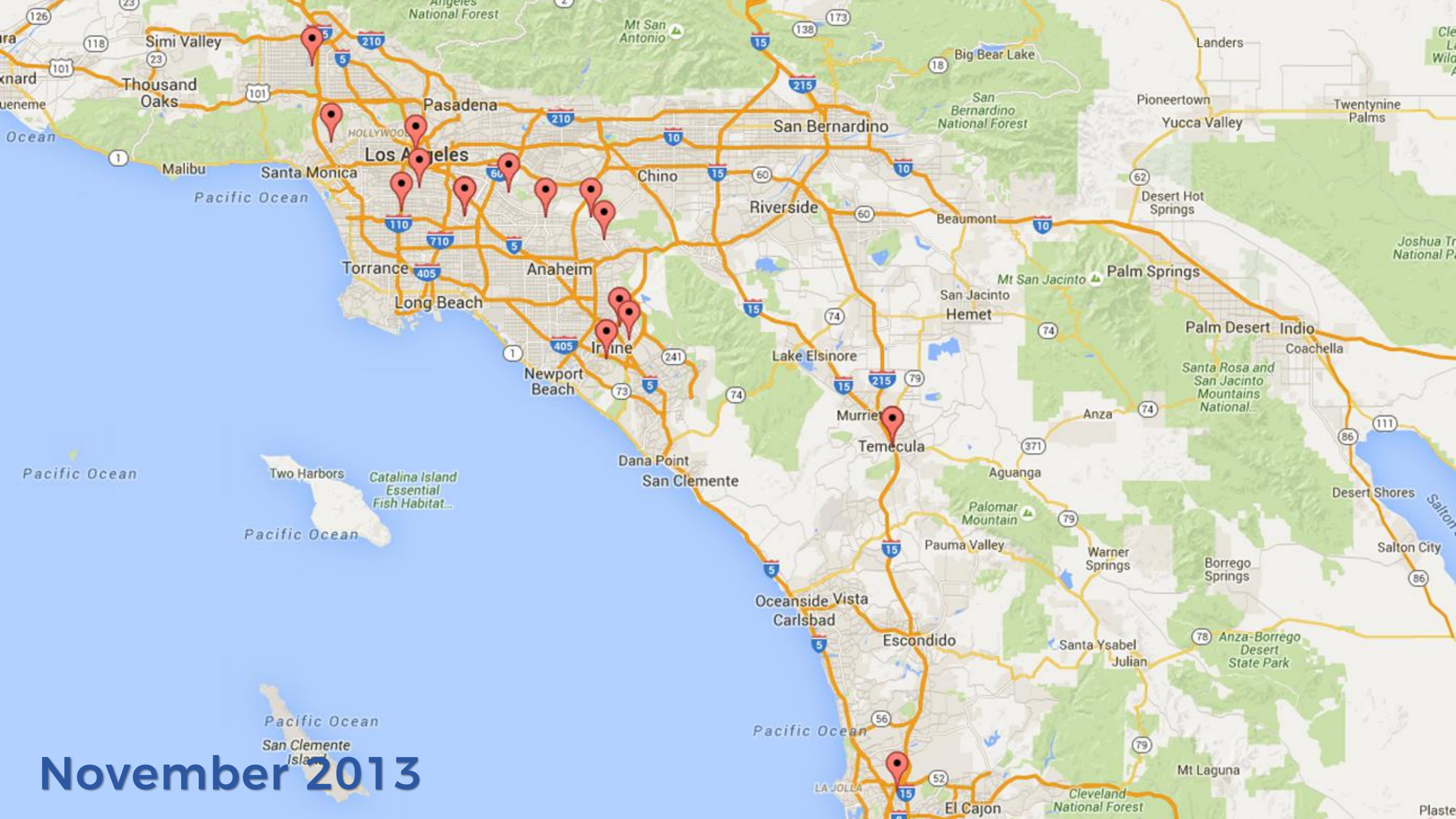
August 2015



September 2015



November 2015



November 2013

Spies

Analysts

Model





Classic Mix

20
Singles

4 LAY'S® Classic Potato Chips, 4 DORITOS® Nacho Cheese Flavored Tortilla Chips, 2 DORITOS® COOL RANCH® Flavored Tortilla Chips, 4 CHEETOS® Crunchy Cheese Flavored Snacks, 2 SUNCHIPS® Original Multigrain Snacks, 4 FRITOS® Original Corn Chips (All 1 OZ. Each)

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Spies

Analysts

Model



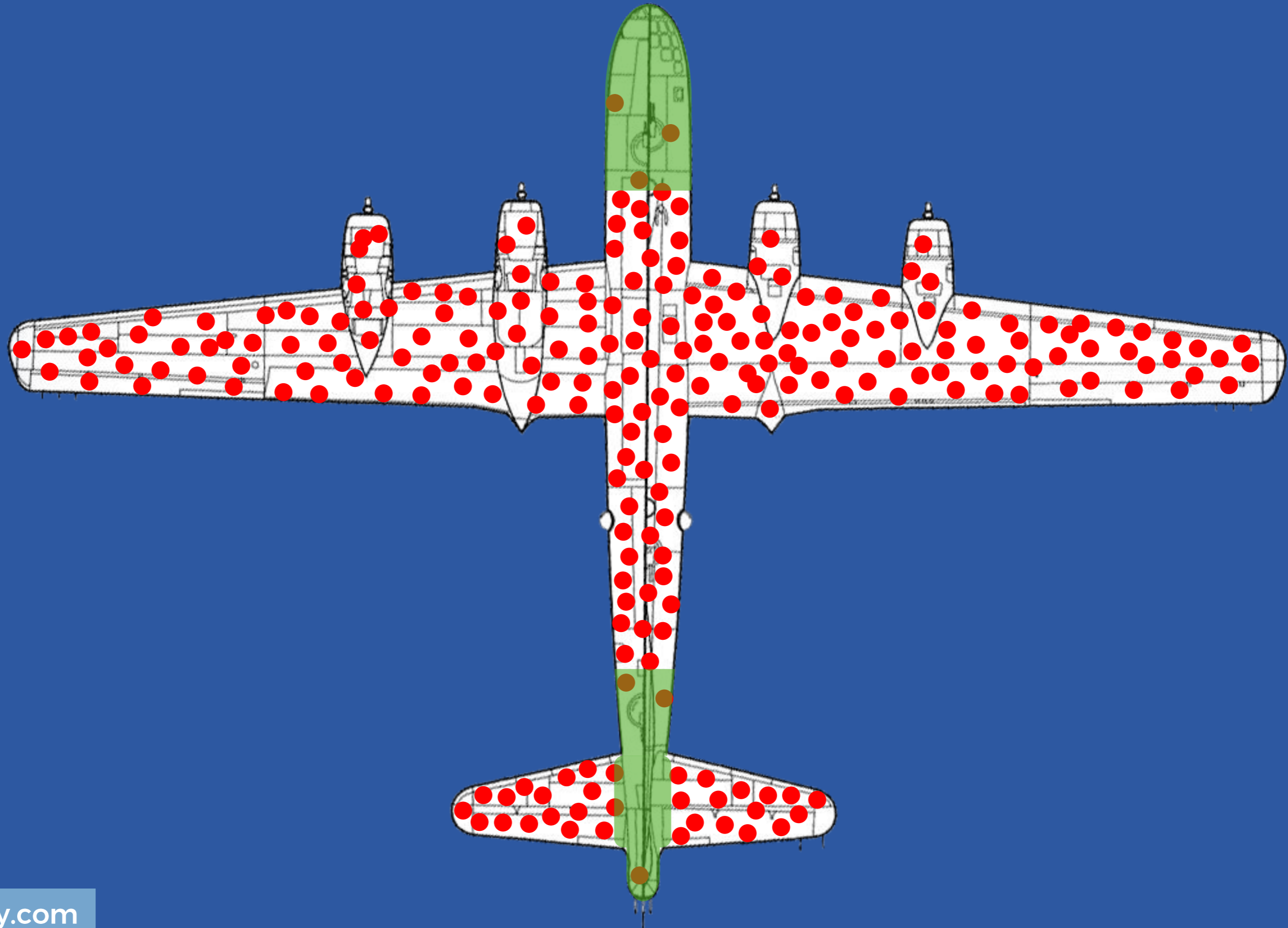
THINKING TIME

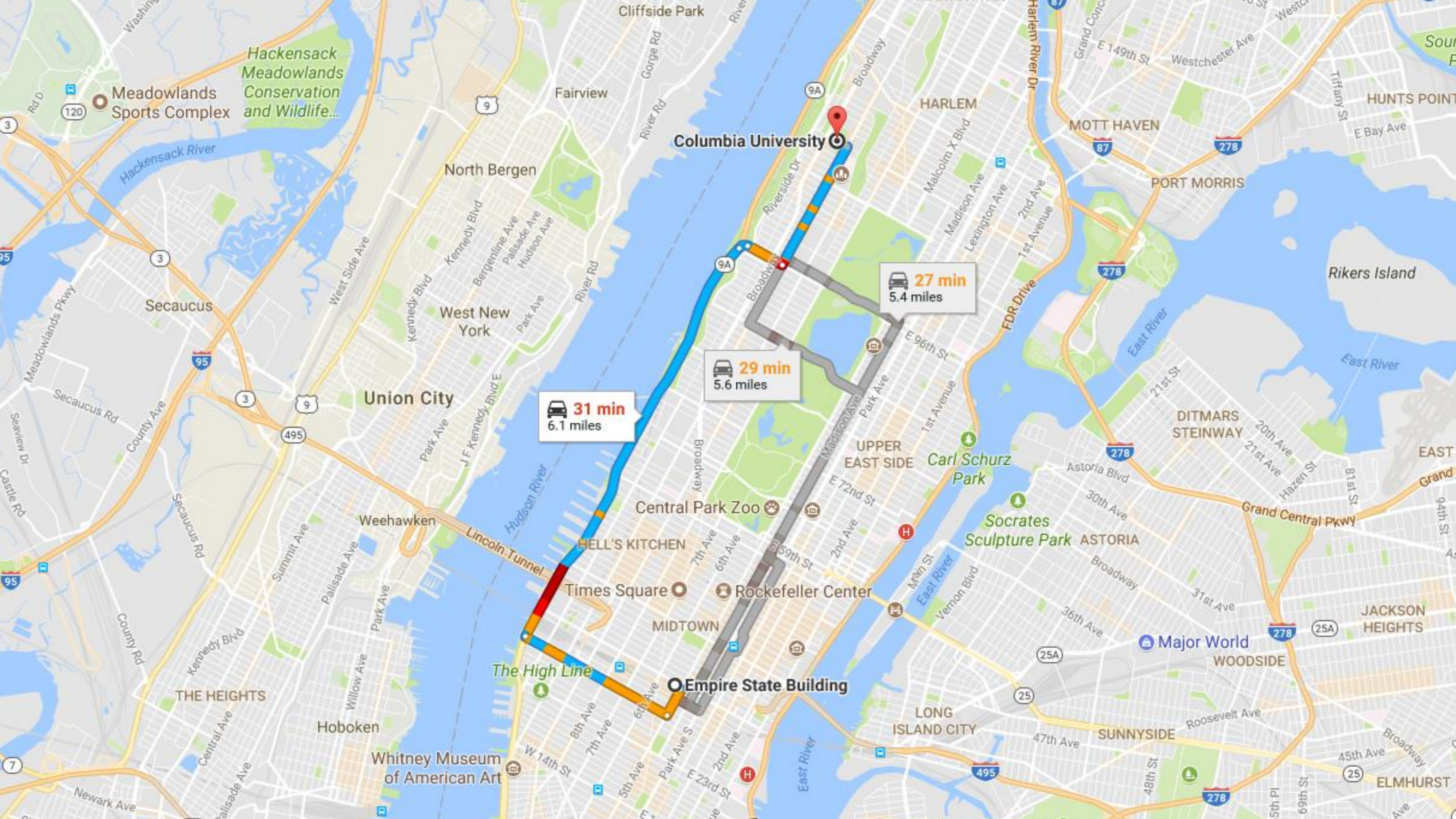


All models are
wrong, but some
are useful.

GEORGE E. P. BOX







Columbia University

Empire State Building

31 min
6.1 miles

29 min
5.6 miles

27 min
5.4 miles

Hackensack Meadowlands Conservation and Wildlife...

Meadowlands Sports Complex

Union City

Whitney Museum of American Art

Rockefeller Center

Times Square

Carl Schurz Park

Socrates Sculpture Park

Central Park Zoo

HELL'S KITCHEN

UPPER EAST SIDE

ASTORIA

LONG ISLAND CITY

SUNNYSIDE

Major World

JACKSON HEIGHTS

ELMHURST

Rikers Island

HUNTS POINT

MOTT HAVEN

PORT MORRIS

ASTORIA

DITMARS STEINWAY

Grand Central Pkwy

Roosevelt Ave

FDR Drive

Carl Schurz Park

Socrates Sculpture Park

UPPER EAST SIDE

UPPER EAST SIDE

59th St

59th St

59th St

59th St

59th St

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UPPER EAST SIDE

UPPER EAST SIDE

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UPPER EAST SIDE

UPPER EAST SIDE

Fairview

Fairview

Fairview

Fairview

Fairview

Fairview

Fairview

Fairview

Fairview

Fairview

Fairview

Fairview

Fairview

Fairview

Fairview

Fairview

Fairview

Fairview

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Fairview

Fairview

Fairview

Fairview

Fairview

Fairview

Fairview

Fairview

Fairview

North Bergen

West New York

Weehawken

Hoboken

THE HEIGHTS

Secaucus

Meadowlands Sports Complex

Hackensack Meadowlands Conservation and Wildlife...

Rikers Island

HUNTS POINT

MOTT HAVEN

PORT MORRIS

ASTORIA

DITMARS STEINWAY

Grand Central Pkwy

Roosevelt Ave

FDR Drive

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LONG ISLAND CITY

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ELMHURST

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PORT MORRIS

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UPPER EAST SIDE

ASTORIA

LONG ISLAND CITY

SUNNYSIDE

Major World

JACKSON HEIGHTS

ELMHURST

Rikers Island

HUNTS POINT

MOTT HAVEN

PORT MORRIS

ASTORIA

DITMARS STEINWAY

Grand Central Pkwy

Roosevelt Ave

FDR Drive

Carl Schurz Park

Socrates Sculpture Park

UPPER EAST SIDE

ASTORIA

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Socrates Sculpture Park

UPPER EAST SIDE

ASTORIA



Apply mathematics to
problems arising in
everyday life, society,
and the workplace.

TEKS PROCESS STANDARDS

Use a problem-solving model that incorporates analyzing given information, formulating a plan or strategy, determining a solution, justifying the solution, and evaluating the problem-solving process and the reasonableness of the solution.

TEKS PROCESS STANDARDS

WHAT MATH IS IMPORTANT?

WHAT CAN MATH MODELING FEEL LIKE?

HOW IS MATH MODELING USED?

IS IT JUST CREATING THE MODEL?

WHAT IS NOT MATH MODELING?

WHAT MIGHT IT LOOK LIKE?

HOW DO YOU COMPARE PROBLEMS?



TARGET PARKING




```
graph TD; Spies --> Analysts; Analysts --> Model; Model --> Spies; Analysts --> Model;
```

Spies

Analysts

Model

THINKING TIME



They used 25 products for a pregnancy prediction' score including:

- **unscented lotion**
- **mineral supplements**
- **cotton balls**

Source: New York Times



UNITED



4047



A319
4047

B→

←G

B G→

Spies

Analysts

Model



THINKING TIME

Priority is determined by:

- passenger's fare class
- itinerary
- frequent flyer program membership
- check-in time

Source: United Airlines



Search



Robert

Home



Robert Kaplinsky

News Feed

Messenger

Watch

Marketplace

Explore

Pages

Events

Groups

Friend Lists

On This Day 3

Insights

Games 7

Fundraisers

Live Video

Pokes

See More...

Create

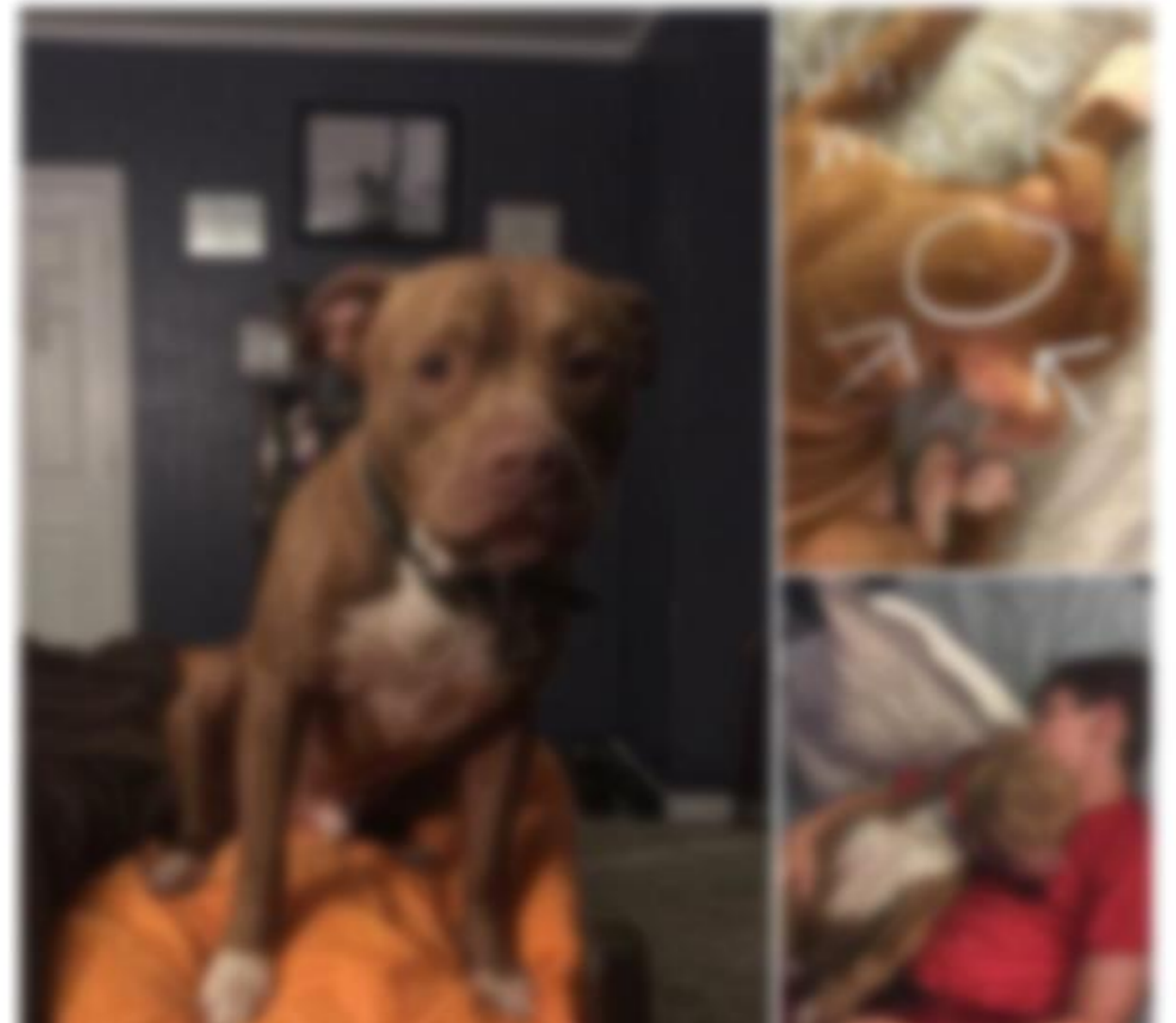
Ad · Page · Group · Event · Fundraiser

Make Post | Photo/Video Album | Live Video

What's on your mind, Robert?

Photo/Video | Feeling/Activity

Hopeing this boy gets back to his family



News better than...

Trending
- Janet Mock
- Fredericksburg, Virginia
- Anthony Weiner

Watchlist: Latest Episodes
- The Mindy Project
- The Mindy Project

Sponsored Create Ad

Spies

Analysts

Model

THINKING TIME

The stories that show in your News Feed are influenced by:

- friends you interact with the most
- the number of comments and likes a post receives
- what kind of story it is (ex: photo, video, status update)

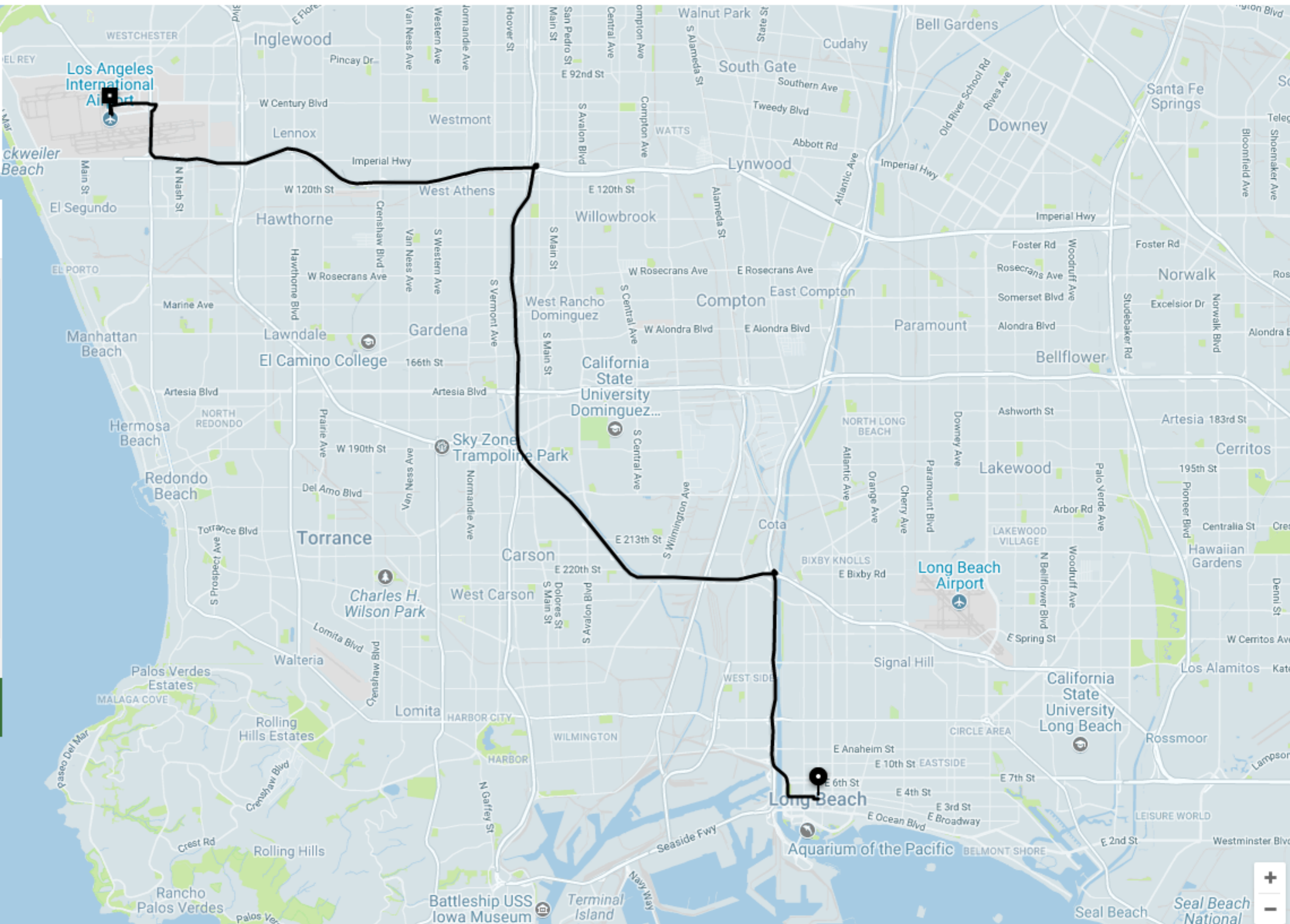
Source: Facebook



● Long Beach, CA

● Los Angeles International Airport, W... →

- Your Options:
- UberBLACK \$95-125 ?
 - UberSUV \$119-155 ?
 - uberX \$30-39 ?
 - UberSELECT \$73-94 ?
 - uberXL \$49-64 ?
 - UberLUX \$141-182 ?
 - POOL \$30-31 ?
- SIGN UP TO RIDE** →



Spies

Analysts

Model



THINKING TIME

This fare includes (but is not limited to):

- **A base rate**
- **Rates for estimated time and distance of the route**
- **The current demand for rides in the area**
- **Booking fee**
- **Any applicable surcharges, fees, and tolls**

Source: Uber



NEW & INTERESTING FINDS ON AMAZON

EXPLORE



All ▾



black friday deals week

Departments ▾

Your Pickup Location Browsing History ▾ Robert's Amazon.com Black Friday Deals Week Gift Cards & Registry Sell Help

EN

Hello, Robert Account & Lists ▾

Orders

Prime ▾



Introducing

echo plus \$149⁹⁹

Now shipping. With built-in smart home hub.

PRIME

Prime members save on deals at Whole Foods



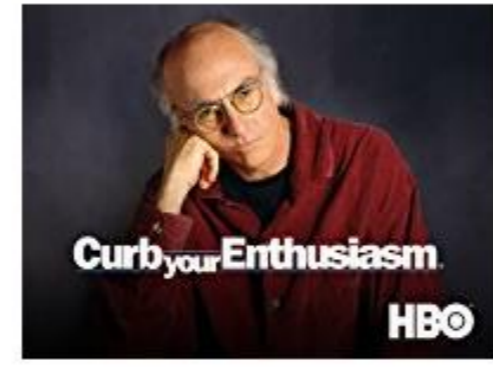
FRESH

NOW AVAILABLE Try our selection



VIDEO

Recommended for you: Curb Your Enthusiasm Season...



MUSIC

Recommended for you: The Hamilton Mixtape [Expli...



MEET ALEXA

Voice control your world with Echo & Alexa devices



RECENT VIEWS

View your browsing history



Related to items you've viewed [See more](#)



Verizon Prepaid.
Save up to \$80/mo

Spies

Analysts

Model



THINKING TIME

Amazon's recommendation system is based on:

- what a user has bought in the past
- which items they have in their shopping cart
- items they've rated and liked
- what other customers have viewed and purchased

Source: Fortune



#1 in dates, relationships and marriages

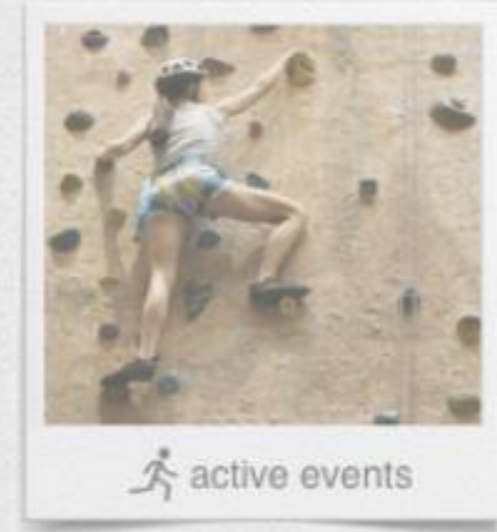


I am a: Seeking a:

Between ages: and

Near ZIP/Postal code:

[View Photos »](#)



active events



happy hours

Do fun stuff, meet cool people
matchevents



cooking classes



game nights

Spies

Analysts

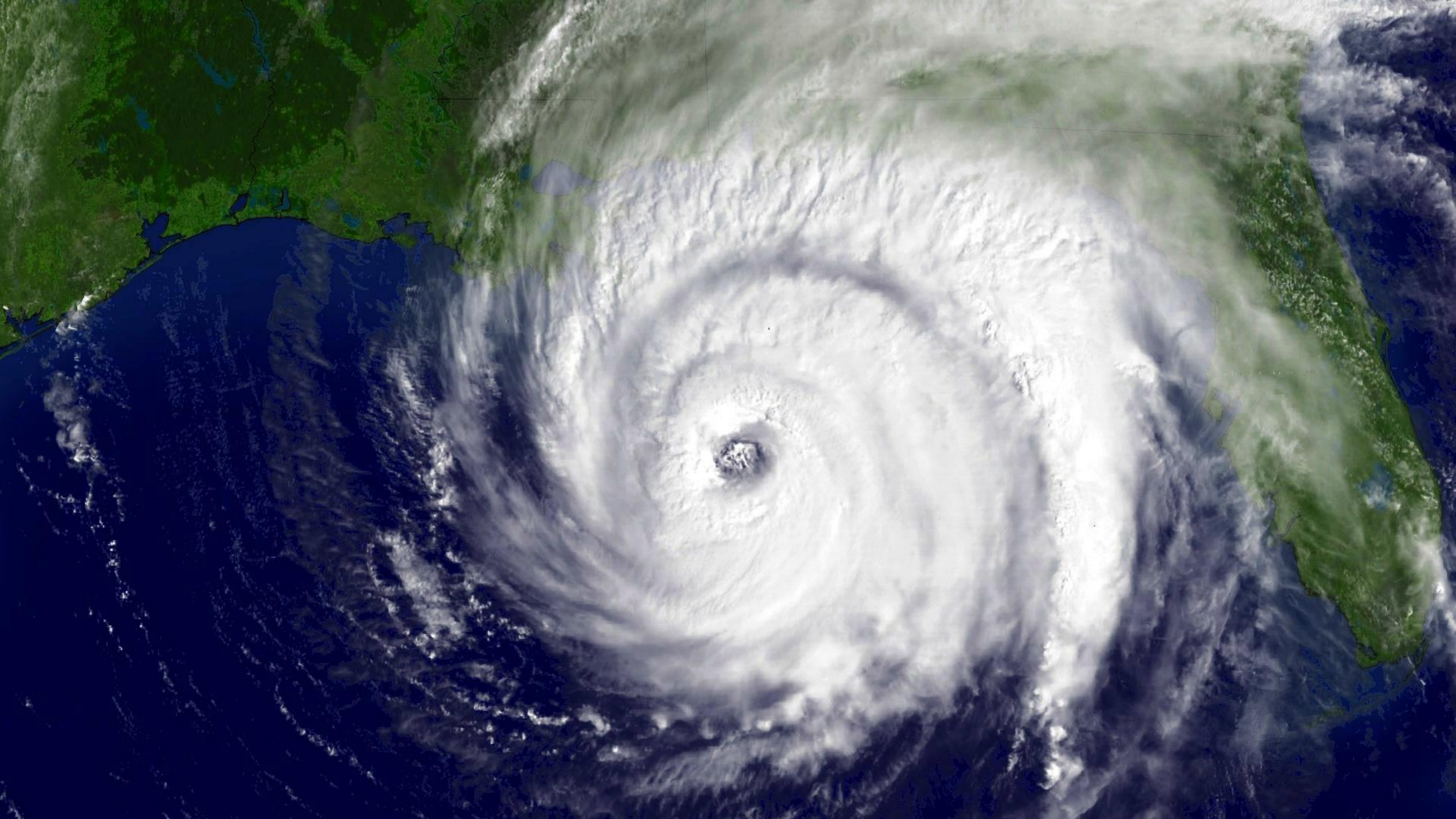
Model

THINKING TIME

The four main components of the equations are:

- what you say
- what you do
- what people like you do
- historical data

Source: Mashable



Spies

Analysts

Model

THINKING TIME



WAFFLE HOUSE

WAFFLE HOUSE

The index has three levels:

- **Green**: full menu - restaurant has power and damage is limited.
- **Yellow**: limited menu - no power or only power from a generator, or food supplies may be low.
- **Red**: the restaurant is closed - indicating severe damage.

Source: Wikipedia

MORE EXAMPLES

- How does US News and World Reports rank colleges?
- How does Google know which results to show?
- How do sports teams know who to draft?
- How does NASA make their trajectories?
- How does Zillow estimate home prices?
- How does Pandora know what music to play?
- How did the BCS rank college football teams?
- How do they figure out who should speak at a conference?

WHAT MATH IS IMPORTANT?

WHAT CAN MATH MODELING FEEL LIKE?

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IS IT JUST CREATING THE MODEL?

WHAT IS NOT MATH MODELING?

WHAT MIGHT IT LOOK LIKE?

HOW DO YOU COMPARE PROBLEMS?

NOT MATH MODELING

WHAT DO TEXTBOOKS USE?

WHAT DID OLD TEXTBOOKS USE?

WHAT DID ASSESSMENTS USE?

WHERE DID THIS COME FROM?

WHY IS THIS A PROBLEM?

WHAT HAPPENS IF WE DO NOTHING?



Real-World Link



Common Core
State Standards

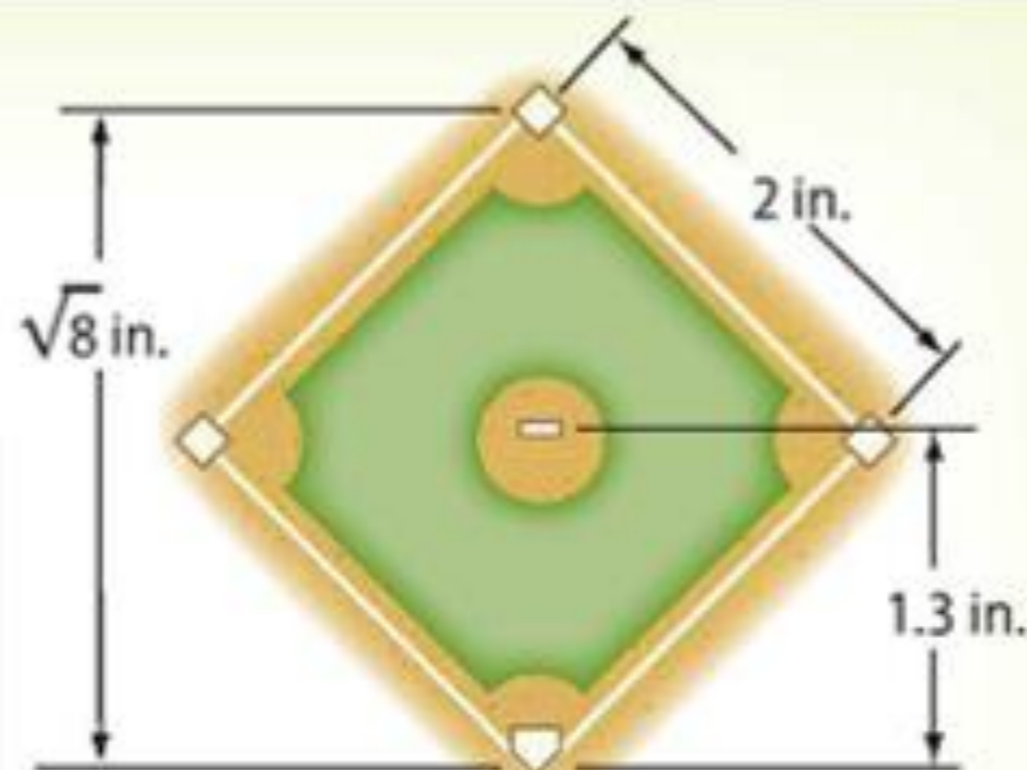
Content Standards

8.NS.1, 8.NS.2, 8.EE.2

Mathematical Practices

1, 3, 4, 6

Sports Major League baseball has rules for the dimensions of the baseball diamond. A model of the diamond is shown.



1. On the model, the distance from the pitching mound to home plate is 1.3 inches. Is 1.3 a rational number? Explain.

2. On the model, the distance from first base to second base is 2 inches. Is 2 a rational number? Explain.

3. The distance from home plate to second base is $\sqrt{8}$ inches. Using a calculator, find $\sqrt{8}$. Does it appear to terminate or repeat?





Real-World Link



Common Core State Standards

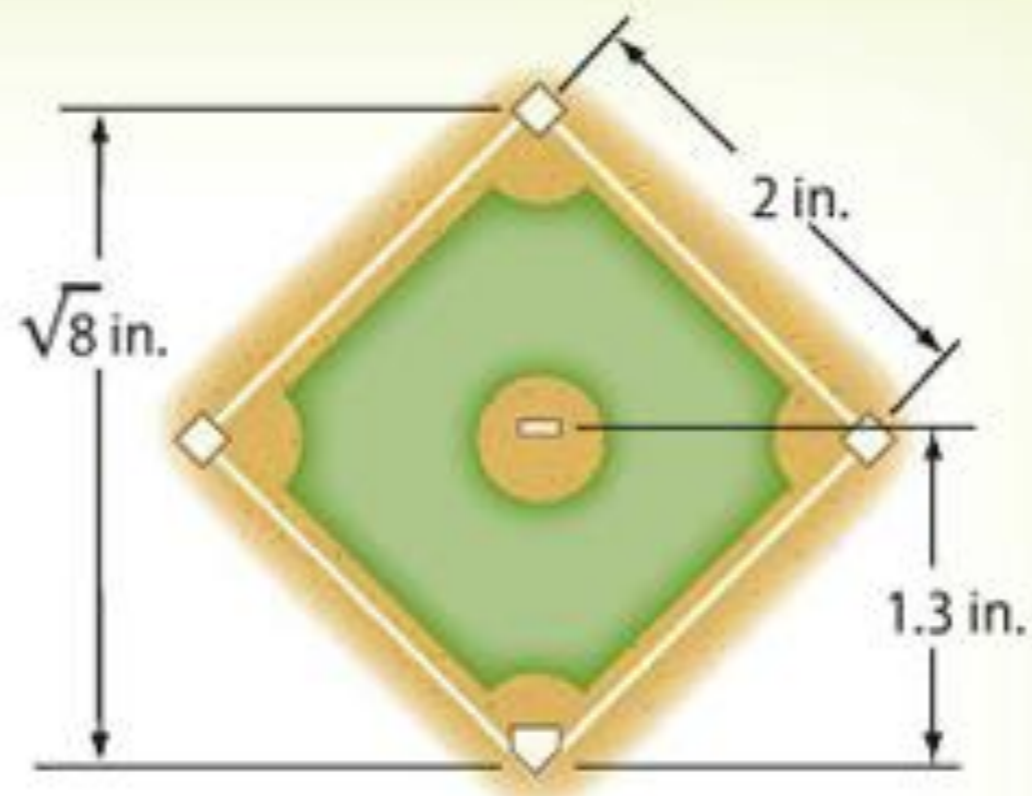
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Mathematical Practices

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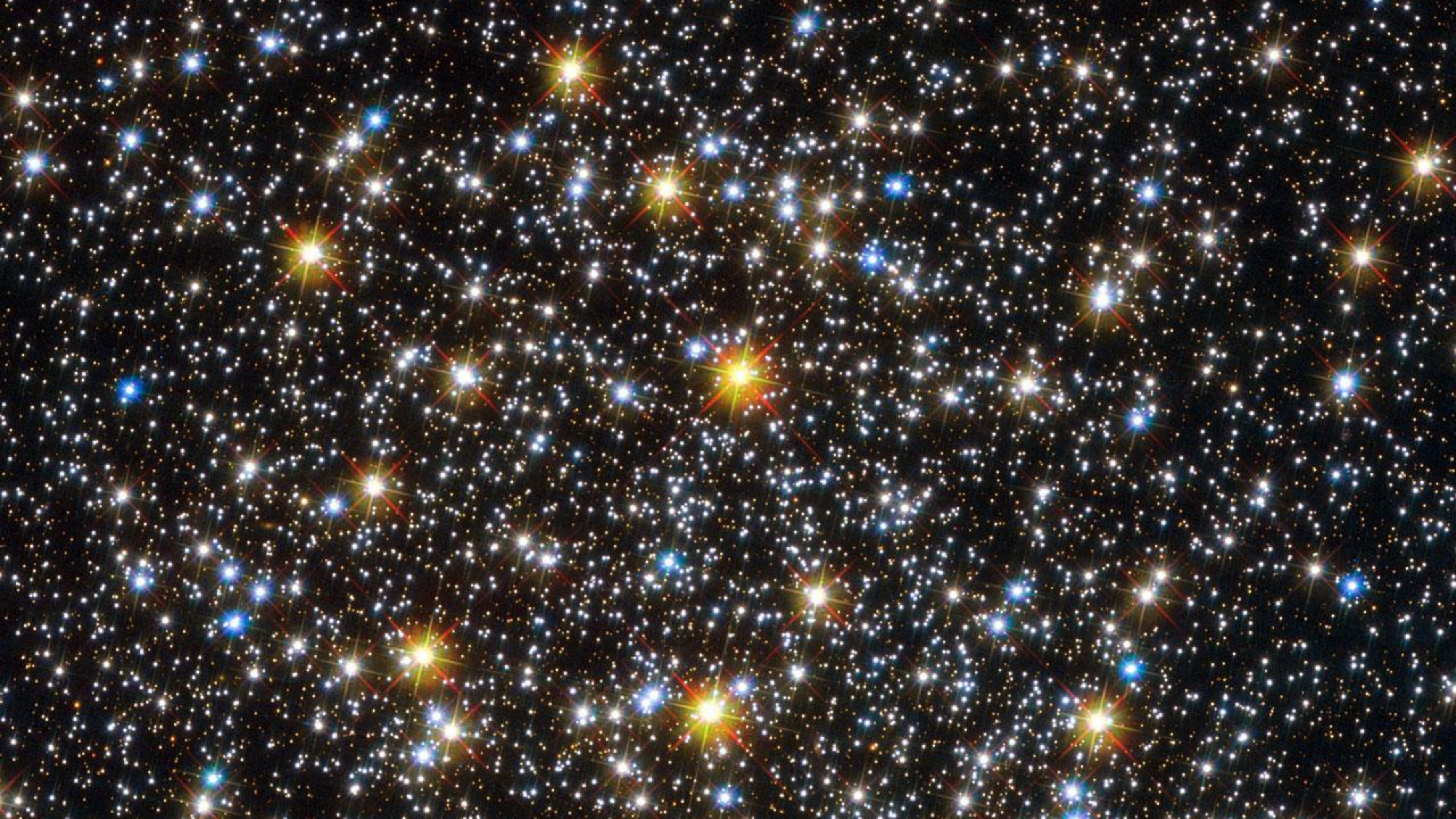


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```
graph TD; Spies --> Analysts; Analysts --> Model; Model --> Spies;
```

Spies

Analysts

Model

THINKING TIME



100,000,000,000,000,000
400,000,000,000,000,000

000,000,000,000,000,000,
000,000,000,000,000,000,





Model with Mathematics

Write two numbers in scientific notation with values between 100 and 1,000. Then write an inequality that shows the relationship between your two numbers.

NOT MATH MODELING

WHAT DO TEXTBOOKS USE?

WHAT DID OLD TEXTBOOKS USE?

WHAT DID ASSESSMENTS USE?

WHERE DID THIS COME FROM?

WHY IS THIS A PROBLEM?

WHAT HAPPENS IF WE DO NOTHING?

MILNE'S
INDUCTIVE ALGEBRA

Milne's Inductive Algebra © 1881

183. DIRECTIONS FOR SOLVING.—*Represent one of the unknown quantities by x , and from the conditions of the problem find an expression for each of the other quantities given.*

Find from the problem two expressions that are equal, and express them as an equation.

Solve the equation.

51. When the half of a certain number is added to the number, the sum is as much more than 60 as the number is less than 65. What is the number? *50 ans*

52. The difference between two numbers is 8, and the quotient arising from dividing the greater by the less is 3. What are the numbers?

53. A man left one-half of his property to his wife, one-sixth to his children, a twelfth to his brother, and the rest, which was \$600, to charitable purposes. How much property had he?

NOT MATH MODELING

WHAT DO TEXTBOOKS USE?

WHAT DID OLD TEXTBOOKS USE?

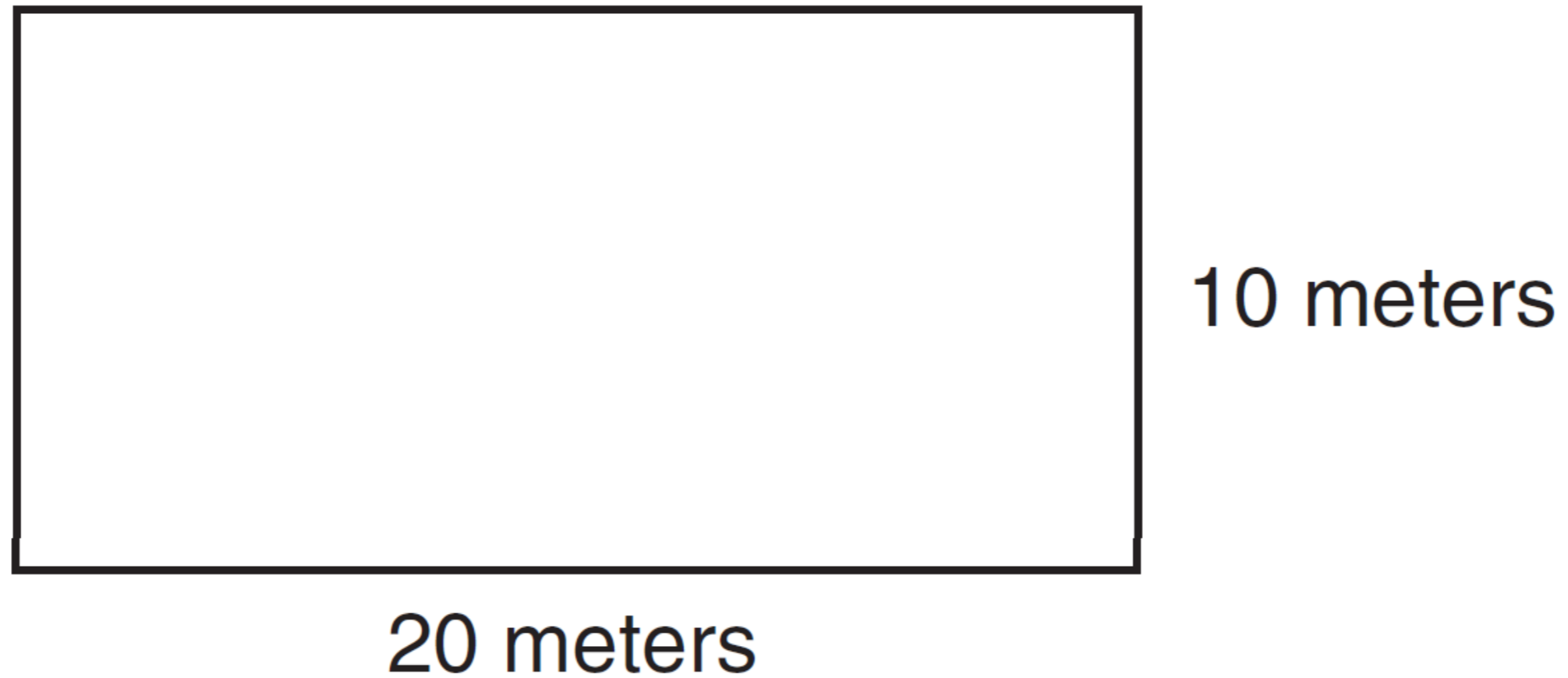
WHAT DID ASSESSMENTS USE?

WHERE DID THIS COME FROM?

WHY IS THIS A PROBLEM?

WHAT HAPPENS IF WE DO NOTHING?

71



**What is the perimeter in meters
?**

NOT MATH MODELING

WHAT DO TEXTBOOKS USE?

WHAT DID OLD TEXTBOOKS USE?

WHAT DID ASSESSMENTS USE?

WHERE DID THIS COME FROM?

WHY IS THIS A PROBLEM?

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NOT MATH MODELING

WHAT DO TEXTBOOKS USE?

WHAT DID OLD TEXTBOOKS USE?

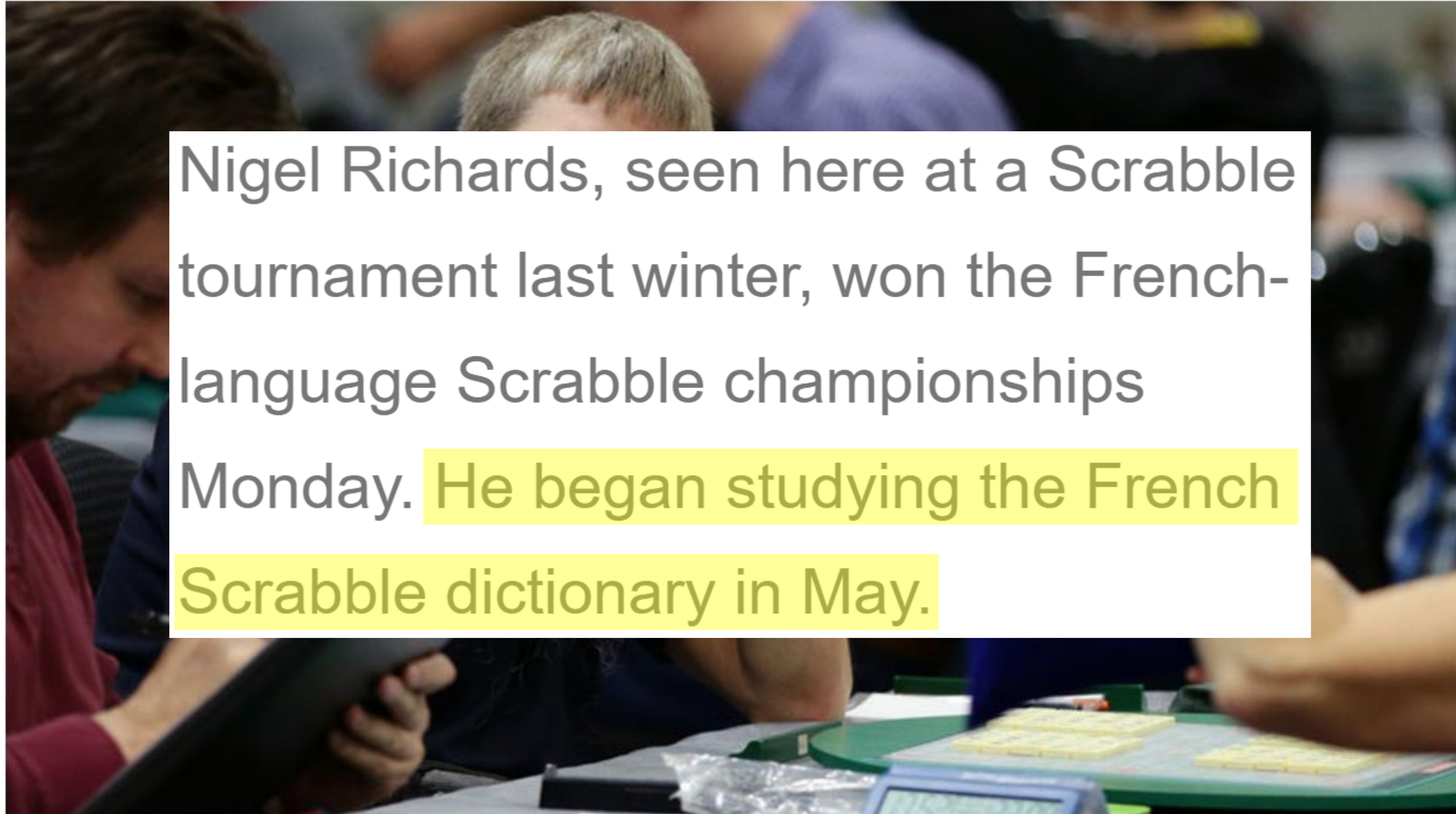
WHAT DID ASSESSMENTS USE?

WHERE DID THIS COME FROM?

WHY IS THIS A PROBLEM?

WHAT HAPPENS IF WE DO NOTHING?

Winner Of French Scrabble Title



Nigel Richards, seen here at a Scrabble tournament last winter, won the French-language Scrabble championships Monday. He began studying the French Scrabble dictionary in May.

NOT MATH MODELING

WHAT DO TEXTBOOKS USE?

WHAT DID OLD TEXTBOOKS USE?

WHAT DID ASSESSMENTS USE?

WHERE DID THIS COME FROM?

WHY IS THIS A PROBLEM?

WHAT HAPPENS IF WE DO NOTHING?

THIS UNIT NOT LABELED FOR INDIVIDUAL RETAIL SALE

Ralphs

grade AA

butter

NET WT. 4 OZ. (113g)

NET WT. 4 OZ. (113g)

DISTRIBUTED BY: RALPHS GROCERY CO. LOS ANGELES, CALIF. 90054

1 Tbsp.	2 Tbsp.	3 Tbsp.	4 Tbsp.	5 Tbsp.	6 Tbsp.	7 Tbsp.	8 Tbsp.
			1/4 cup				

1 FIRST QUALITY 1

Ralphs

grade AA
butter

TOP 10 SEARCHES

1. $\frac{1}{3}$ cup butter
2. robert kaplinsky
3. how many tablespoons in $\frac{1}{3}$ cup butter
4. #observeme
5. how many tablespoons is $\frac{1}{3}$ cup of butter
6. $\frac{1}{3}$ cup butter in tablespoons
7. how many tablespoons in $\frac{1}{3}$ cup of butter
8. how much is $\frac{1}{3}$ cup of butter
9. observe me
10. $\frac{1}{3}$ cup butter to tbsp



How much is one third of a cup of butter?



All

News

Shopping

Maps

Images

More ▼

Search tools

NOT MATH MODELING

WHAT DO TEXTBOOKS USE?

WHAT DID OLD TEXTBOOKS USE?

WHAT DID ASSESSMENTS USE?

WHERE DID THIS COME FROM?

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WHAT MATH IS IMPORTANT?

WHAT CAN MATH MODELING FEEL LIKE?

HOW IS MATH MODELING USED?

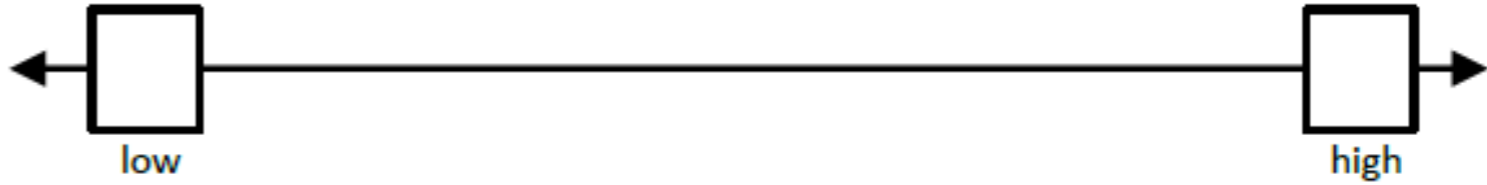
IS IT JUST CREATING THE MODEL?

WHAT IS NOT MATH MODELING?

WHAT MIGHT IT LOOK LIKE?

HOW DO YOU COMPARE PROBLEMS?

Name: _____ Period: _____ Date: _____

What problem are you trying to figure out?	What estimates do you have?
	 <p data-bbox="2059 714 2768 752">Place your estimate on the number line.</p>
What info do you already know about the problem?	What info do you need about the problem?
<p data-bbox="736 1001 1685 1365">TOP SECRET!</p>	<p data-bbox="1725 767 2558 1103">SPIES ONLY</p>
What is your conclusion? How did you reach that conclusion?	

Your work

DANGER

**ANALYSTS
AT WORK**



THINKING TIME

COUNT ALL



1 Coca-Cola 8 Sprite 16 Fanta Orange 24 Pibb Xtra 27 YALT 32 W!C Orange 40 Minute Maid LEMONADE 46 POWERADE Orange

2 Coca-Cola Cherry 5 Coca-Cola Raspberry 9 Sprite Strawberry 13 Sprite Cherry 17 Fanta Fruit Punch 21 Fanta Strawberry 25 Banq's 28 YALT Red Berry 30 YALT Grape 33 Fanta Fruit Punch 37 Minute Maid Strawberry 44 Minute Maid Cherry 47 Fanta Fruit Punch 51 Fanta Strawberry

3 Coca-Cola Orange 6 Coca-Cola Vanilla 10 Sprite Grape 14 Sprite Peach 18 Fanta Raspberry 22 Fanta Cherry 29 YALT Orange 31 YALT Peach 34 Fanta Raspberry 38 Minute Maid Orange 45 Minute Maid Raspberry 48 Minute Maid Raspberry 52 Minute Maid Cherry

4 Coca-Cola Lime 7 Coca-Cola Cherry Vanilla 11 Sprite Raspberry 15 Sprite Orange 19 Fanta Lime 23 Fanta Grape 35 Fanta Grape 39 Minute Maid Fruit Punch 49 Fanta Lime 53 Fanta Grape

12 NEW Sprite Vanilla 20 Fanta Peach 26 NEW YALT

no caffeine no caffeine no caffeine no caffeine no caffeine no caffeine no caffeine no caffeine

low/no calories

54 Coca-Cola zero. 62 Diet Coke 69 Diet Coke 76 Sprite zero. 84 Fanta zero Orange 92 Pibb zero 95 DAŠANI Lemon 103 DAŠANI sensations Lemon 111 Minute Maid Light LEMONADE 117 POWERADE ZERO Orange 125 Seagram's LEMON LIME Seltzer

55 NEW Coca-Cola Cherry 59 NEW Coca-Cola Raspberry 63 NEW Coca-Cola Cherry 66 70 NEW Coca-Cola Raspberry 73 77 NEW Coca-Cola Cherry 81 85 NEW Fanta Fruit Punch 89 NEW Fanta Strawberry 93 Banq's 96 DAŠANI Orange 100 104 DAŠANI Strawberry 108 112 DAŠANI sensations Orange 115 118 Minute Maid Strawberry 122 Minute Maid Cherry

56 NEW Fanta Orange 60 64 NEW Coca-Cola Orange 67 71 NEW Coca-Cola Vanilla 74 78 NEW Fanta Grape 82 86 NEW Fanta Peach 90 NEW Fanta Raspberry 97 DAŠANI Raspberry 101 105 DAŠANI Cherry 109 113 DAŠANI sensations Raspberry 116 119 Minute Maid Orange 123 Minute Maid Raspberry

57 NEW Fanta Lime 61 65 NEW Coca-Cola Lime 68 72 NEW Coca-Cola Cherry Vanilla 75 79 NEW Fanta Raspberry 83 87 NEW Fanta Lime 91 NEW Fanta Grape 98 DAŠANI Lime 102 106 DAŠANI sensations Lime 110 114 Minute Maid Fruit Punch 120 Minute Maid Lime 124 Minute Maid Grape

58 NEW Fanta Lemon 80 NEW Sprite Vanilla 88 NEW Fanta Peach 94 NEW Banq's 99 DAŠANI Peach 107 DAŠANI sensations Peach 121 Minute Maid Lemon

no caffeine no caffeine no caffeine no caffeine no caffeine no caffeine no caffeine no caffeine no caffeine no caffeine

COUNT GROUPS



7

Cherry
Raspberry
Orange
Vanilla
Lime
Cherry Vanilla

8

no caffeine

Strawberry
Cherry
Grape
Peach
Raspberry
Orange
Vanilla

8

no caffeine

Fruit Punch
Strawberry
Raspberry
Cherry
Lime
Grape
Peach

1

2

no caffeine

5

Red Berry
Grape
Orange
Peach

8

no caffeine

Fruit Punch
Strawberry
Raspberry
Cherry
Grape
Raspberry Lime
Orange Vanilla

6

no caffeine

Strawberry
Cherry
Orange
Raspberry
Fruit Punch

8

no caffeine

Fruit Punch
Strawberry
Raspberry
Cherry
Lime
Grape
Lemon

low/no calories

Cherry
Raspberry
Orange
Vanilla
Lime
Cherry Vanilla
Lemon

8

Cherry
Raspberry
Orange
Vanilla
Lime
Cherry Vanilla

7

no caffeine

Cherry
Raspberry
Orange
Vanilla
Lime
Cherry Vanilla

7

no caffeine

Strawberry
Cherry
Grape
Peach
Raspberry
Orange
Vanilla

8

no caffeine

Fruit Punch
Strawberry
Raspberry
Cherry
Lime
Grape
Peach

8

1

2

no caffeine

no caffeine

Orange
Strawberry
Raspberry
Cherry
Lime
Grape
Peach

8

no caffeine

Orange
Strawberry
Raspberry
Cherry
Lime
Grape
Peach

8

no caffeine

Strawberry
Cherry
Orange
Raspberry
Fruit Punch

6

no caffeine

Fruit Punch
Strawberry
Raspberry
Cherry
Lime
Grape
Lemon

8

no caffeine

1

INVENTED STRATEGY



8 8 8 7 7 7 8

Coca-Cola Sprite Fanta Orange Pibb VULT W!C Orange Minute Maid LEMONADE POWERADE Orange

no caffeine no caffeine no caffeine no caffeine no caffeine no caffeine no caffeine

Cherry, Raspberry, Orange, Vanilla, Lime, Cherry Vanilla, Strawberry, Cherry, Grape, Peach, Raspberry, Orange, NEW Sprite Vanilla, Fruit Punch, Strawberry, Raspberry, Cherry, Lime, Grape, Peach, NEW Pibb, VULT Red Berry, Grape, Orange, Peach, Fruit Punch, Strawberry, Raspberry, Cherry, Grape, Raspberry, Lime, NEW W!C Orange Punch, Strawberry, Fruit Punch, NEW Minute Maid Strawberry, Cherry, Orange, Raspberry, NEW Minute Maid Fruit Punch, Fruit Punch, Strawberry, Raspberry, Cherry, Lime, Grape, Lemon

low/no calories

Coca-Cola zero. Diet Coke Diet Coke Sprite zero. Fanta zero Orange Pibb zero DAsANI Lemon DAsANI sensations Lemon Minute Maid Light LEMONADE POWERADE ZERO Orange Seagram's LEMON LIME Soften

no caffeine no caffeine no caffeine no caffeine no caffeine no caffeine no caffeine no caffeine no caffeine no caffeine

Cherry, Raspberry, Orange, Vanilla, Lime, Cherry Vanilla, Strawberry, Cherry, Grape, Peach, Raspberry, Orange, NEW Sprite Vanilla, Fruit Punch, Strawberry, Raspberry, Cherry, Lime, Grape, Peach, NEW Pibb, DAsANI Orange, Strawberry, Raspberry, Cherry, Lime, Grape, Peach, DAsANI sensations Orange, Strawberry, Raspberry, Cherry, Lime, Grape, Peach, NEW Minute Maid Strawberry, Cherry, Orange, Raspberry, NEW Minute Maid Fruit Punch, Fruit Punch, Strawberry, Raspberry, Cherry, Lime, Grape, Lemon

8 8 8 8 8 8 8 8 8 8

Spies

Analysts

Model



LIVE



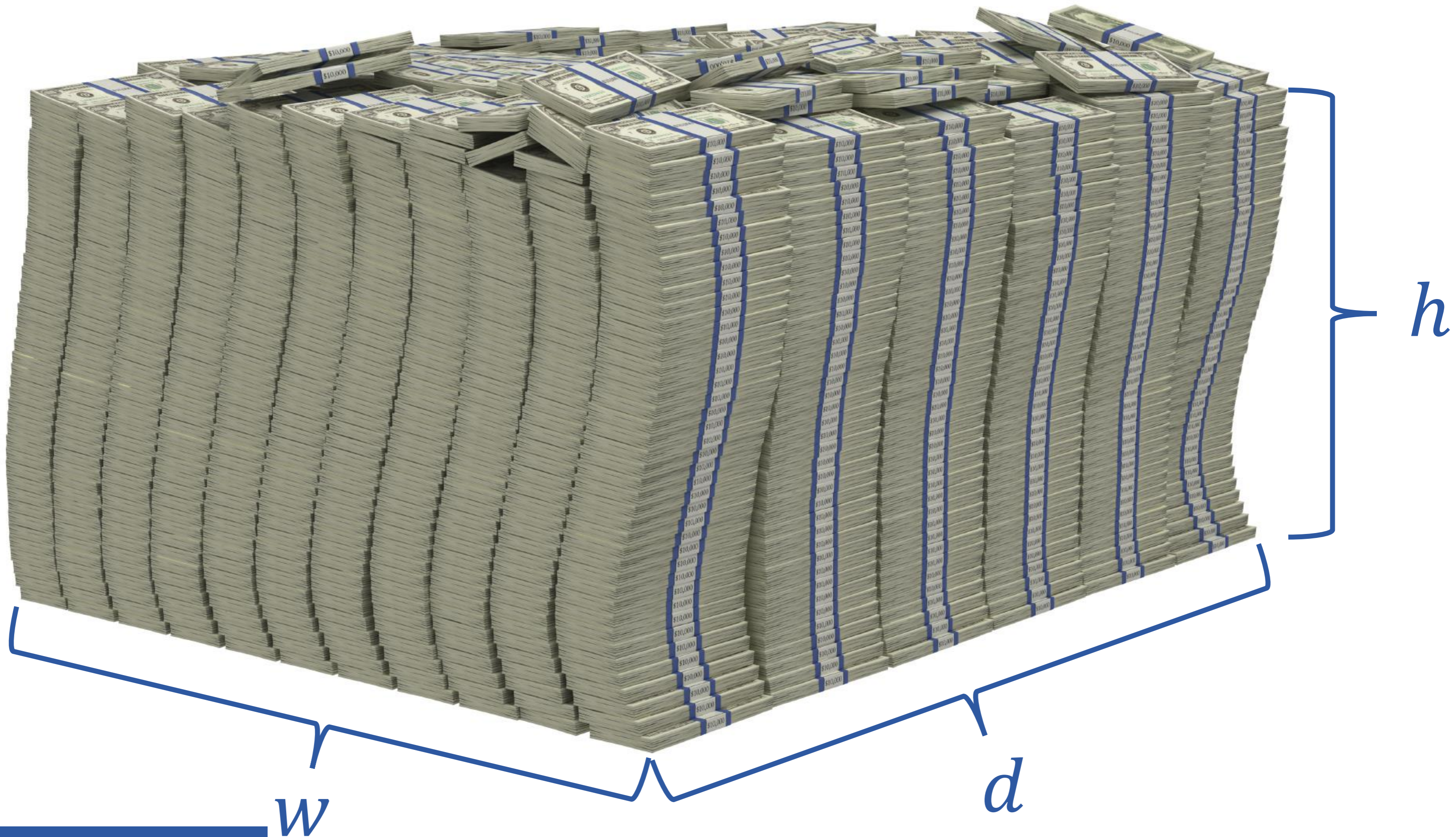
FOX NEWS

Junction

THINKING TIME







Spies

Analysts

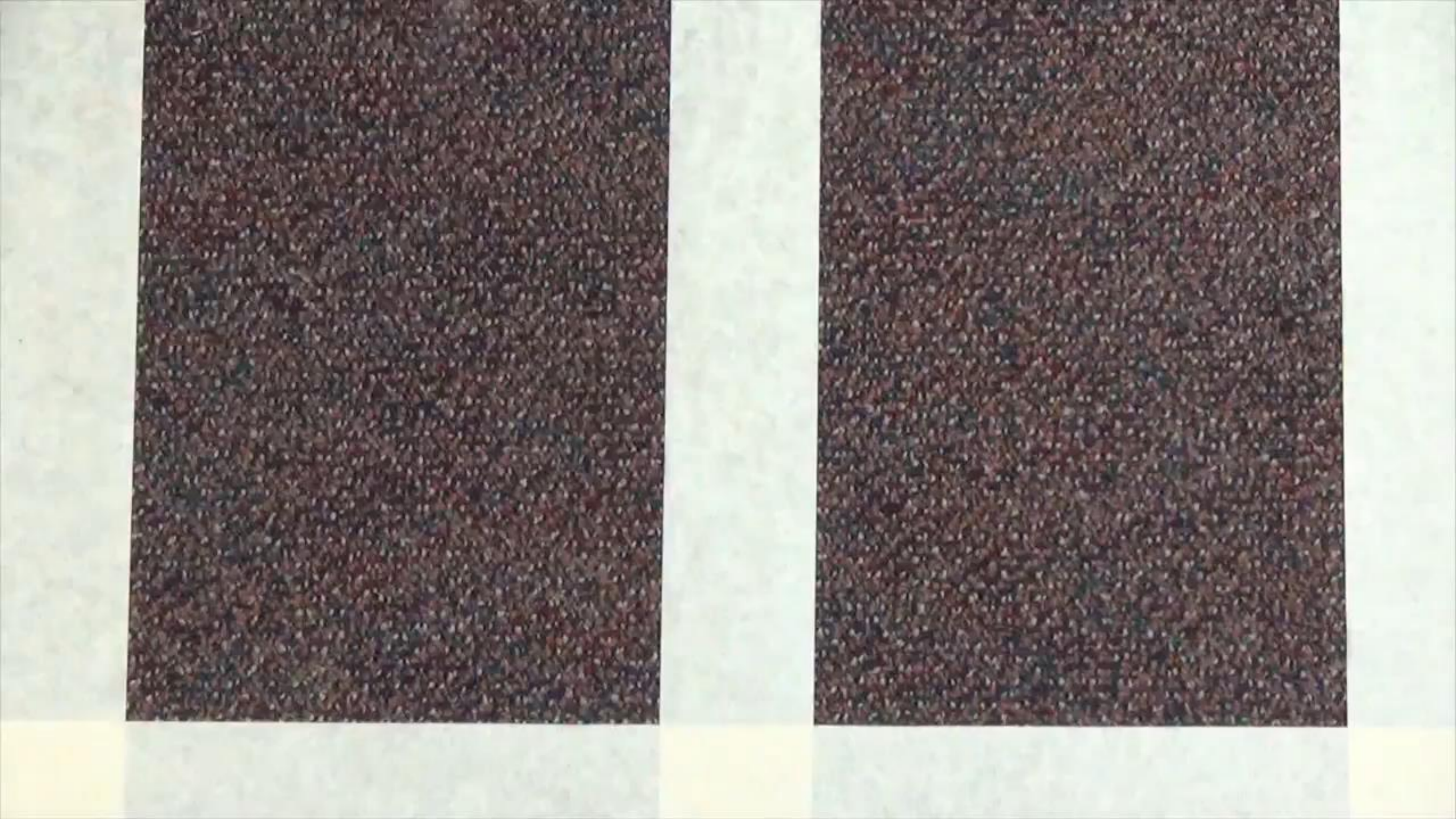
Model





NON-STAGGERED

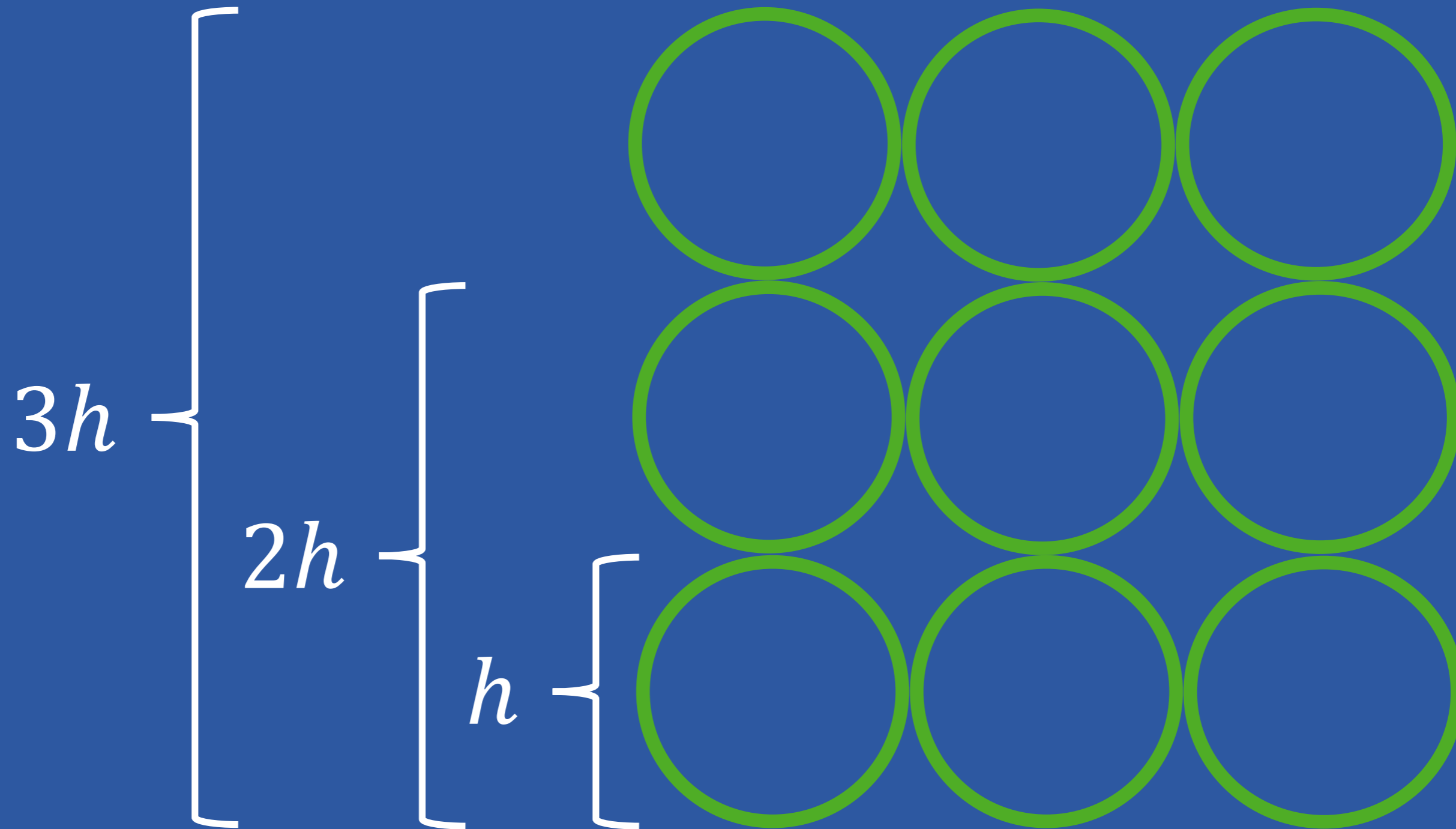
STAGGERED



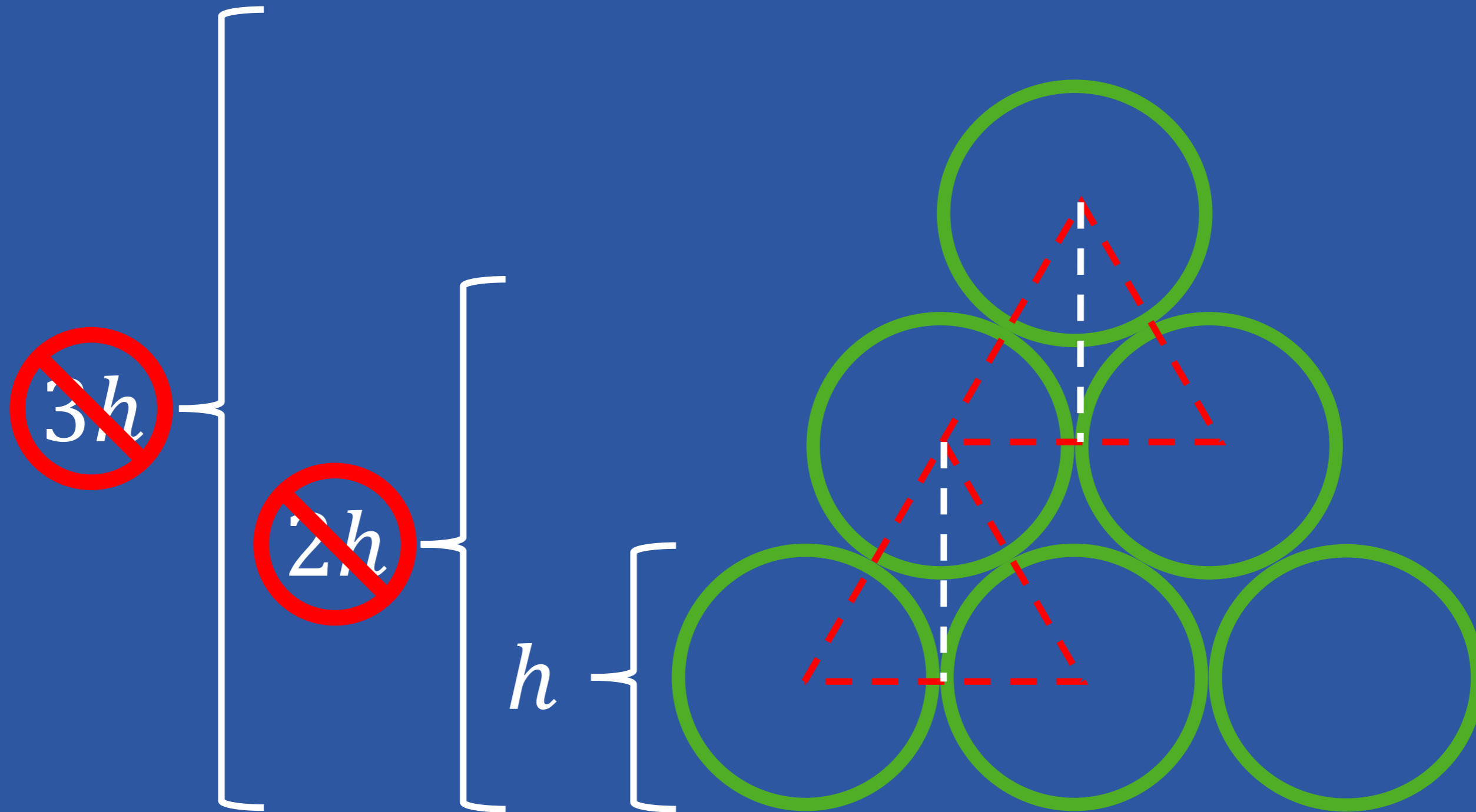
THINKING TIME



NON-STAGGERED PIPES



STAGGERED PIPES



```
graph TD; Spies --> Analysts; Analysts --> Model; Model --> Spies; Analysts --> Model;
```

Spies

Analysts

Model

WHAT MATH IS IMPORTANT?

WHAT CAN MATH MODELING FEEL LIKE?

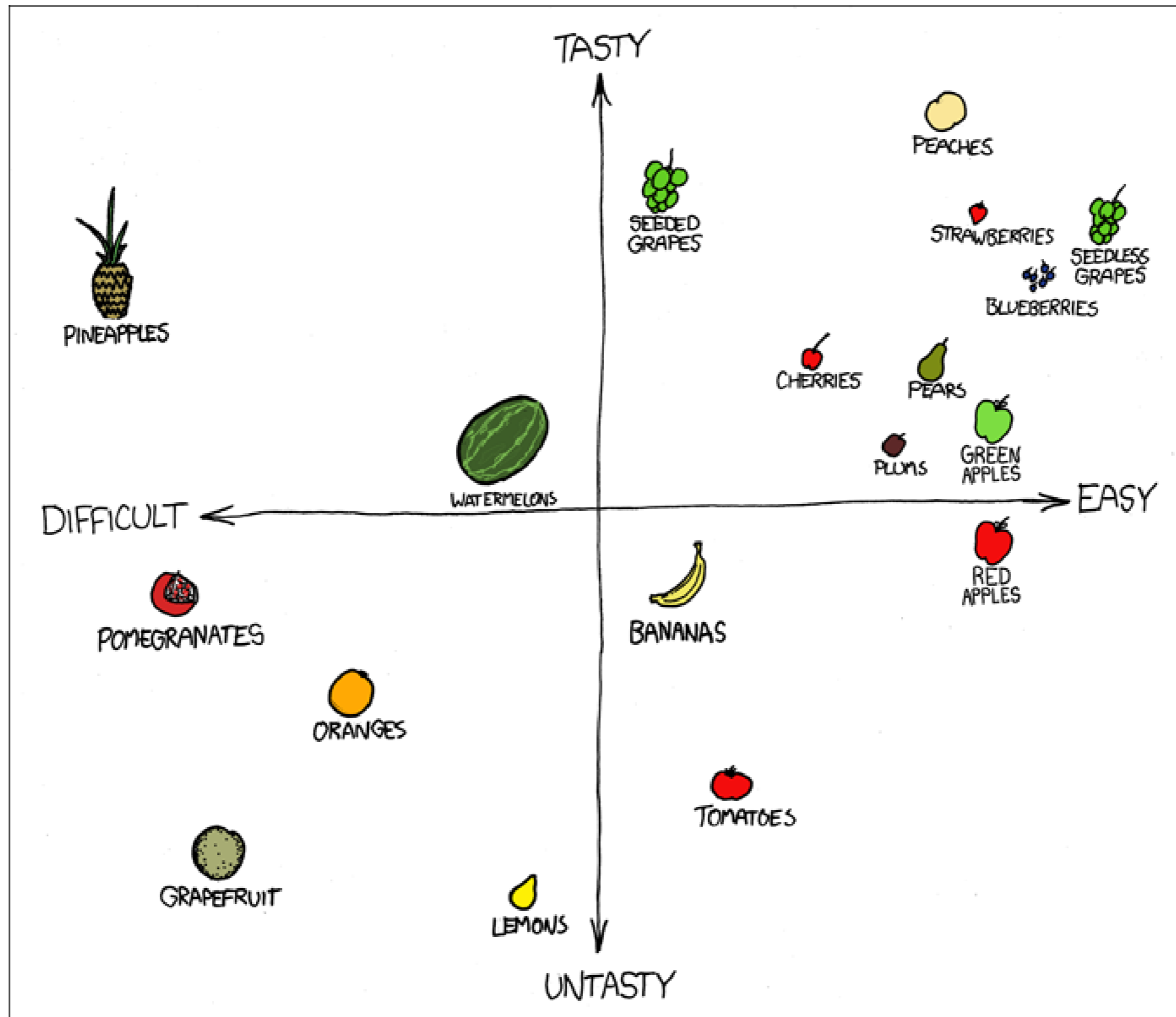
HOW IS MATH MODELING USED?

IS IT JUST CREATING THE MODEL?

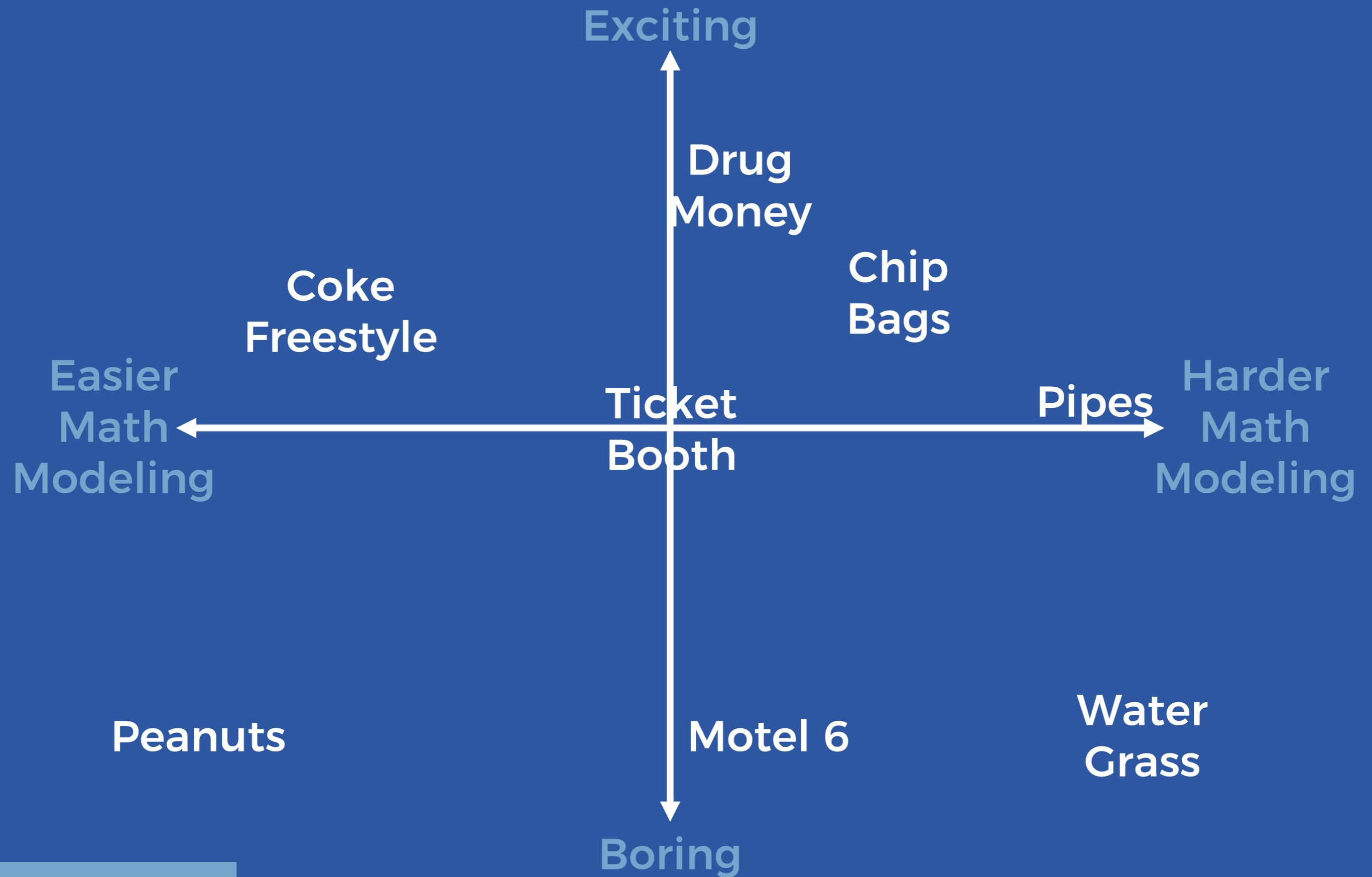
WHAT IS NOT MATH MODELING?

WHAT MIGHT IT LOOK LIKE?

HOW DO YOU COMPARE PROBLEMS?



Source: xkcd.com via Dan Meyer



Spies

Analysts

Model



THINKING TIME

MATH MODEL

- **Spies**

- 3rd Act?
- Checkpoint?
- Open ended?
- Incorrect answer?
- Solutions match answer?

- **Analysts**

- What do I do with this information?!



NETFLIX

2009

DATE: 09-21-09

PAY TO THE ORDER OF: BellKor's Pragmatic Chaos

\$1,000,000⁰⁰

AMOUNT: ONE MILLION

⁰⁰/100

FOR: The Netflix Prize

Reed Hastings

DISCUSSION QUESTIONS

- What previous understandings of mathematical modeling were confirmed?
- How has your understanding of mathematical modeling shifted?
- What would you recommend math teachers do differently?

WHAT MATH IS IMPORTANT?

✓ WHAT CAN MATH MODELING FEEL LIKE?

✓ HOW IS MATH MODELING USED?

✓ IS IT JUST CREATING THE MODEL?

✓ WHAT IS NOT MATH MODELING?

✓ WHAT MIGHT IT LOOK LIKE?

✓ HOW DO YOU COMPARE PROBLEMS?

GOALS

WHAT IS INTELLIGENCE?

WHY DON'T STUDENTS REMEMBER?

WHAT MATHEMATICS IS IMPORTANT?

WHAT MIGHT IT LOOK LIKE?

WHAT ABOUT WHAT WE USED TO DO?









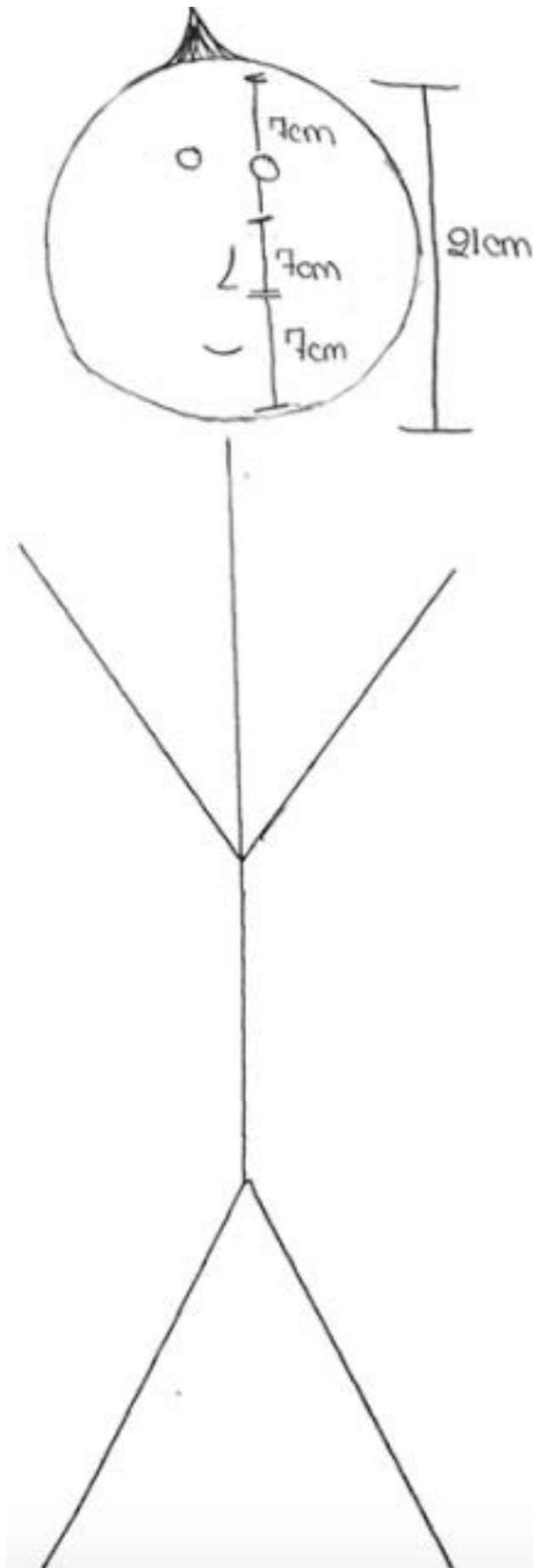


Ben Stiller

Biography

Date of Birth	30 November 1965, New York City, New York, USA
Birth Name	Benjamin Edward Stiller
Height	5' 7" (1.7 m)

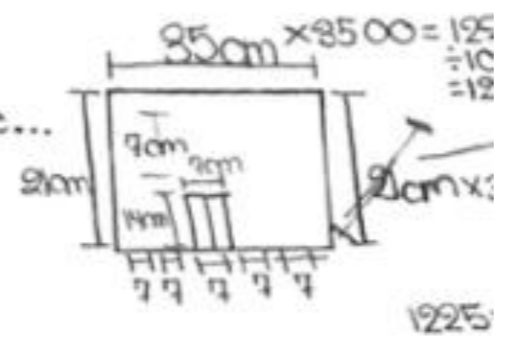




Mesure de la tête } Recherche...
 est environ $\frac{1}{8}$ de la
 Taille de le corps }
 $170\text{cm} \div 8 = 21.25\text{cm}$
 \approx environ $\approx 21\text{cm}$
 Nez est environ 7cm
 donc $\frac{1}{3}$ du visage > Recherche...

La moyenne taille

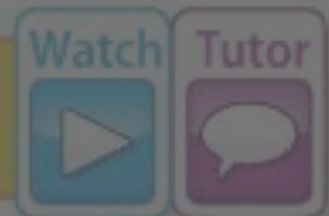
Derek's zoolander height: 170cm



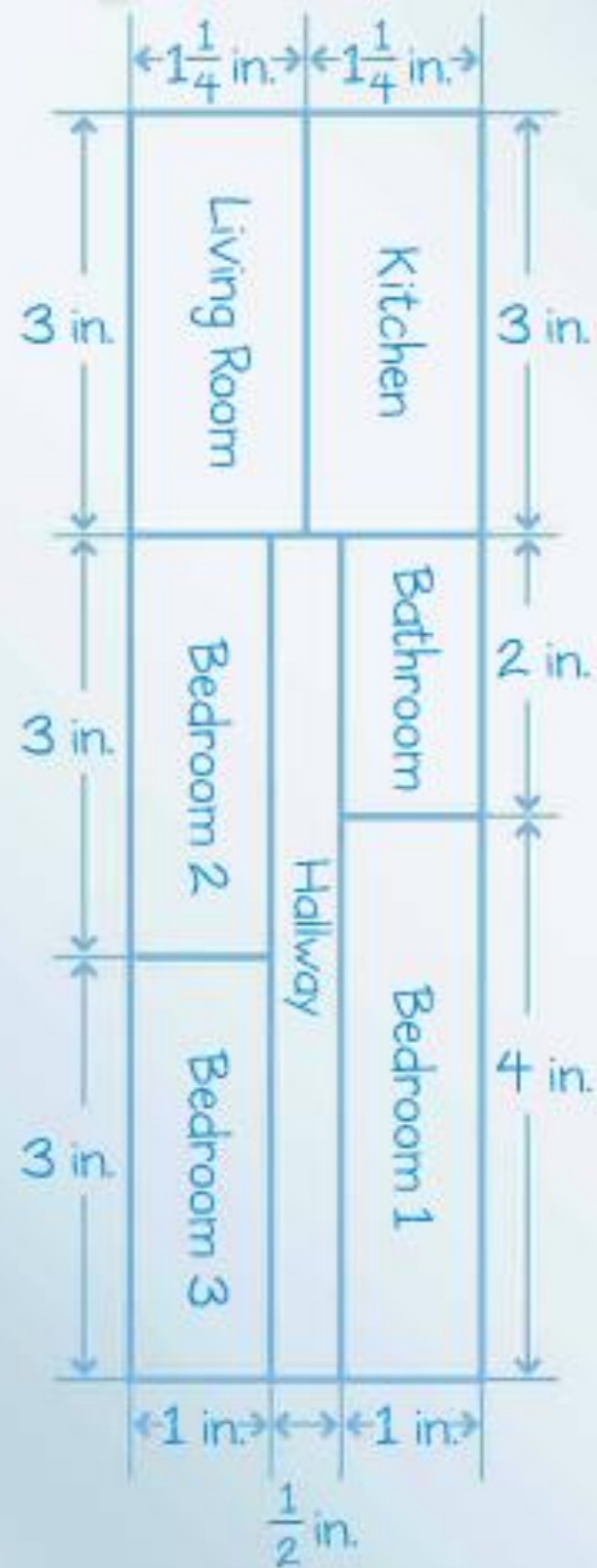
on a multi
 110295937



Example



4. A floor plan for a home is shown at the left where $\frac{1}{2}$ inch represents 3 feet of the actual home. What is the actual area of bedroom 1?



Length of Bedroom 1.

$$\frac{\frac{1}{2} \text{ in.}}{3 \text{ ft}} = \frac{4 \text{ in.}}{w}$$

← floor plan
← actual

$$\frac{1}{2}w = 12$$

Find cross products.

$$w = 24$$

Divide each side by $\frac{1}{2}$.

Width of Bedroom 1.

$$\frac{\frac{1}{2} \text{ in.}}{3 \text{ ft}} = \frac{1 \text{ in.}}{x}$$

← floor plan
← actual

$$\frac{1}{2}x = 3$$

Find cross products.

$$x = 6$$

Divide each side by $\frac{1}{2}$.

So, the area of bedroom 1 is 24×6 or 144 square feet.

Got It? Do this problem to find out.

DISCUSSION QUESTIONS

- How did the spy and analyst components interact when working on this problem?
- How do traditional textbook problems handle the spy and analyst components?

GOALS

WHAT IS INTELLIGENCE?

WHY DON'T STUDENTS REMEMBER?

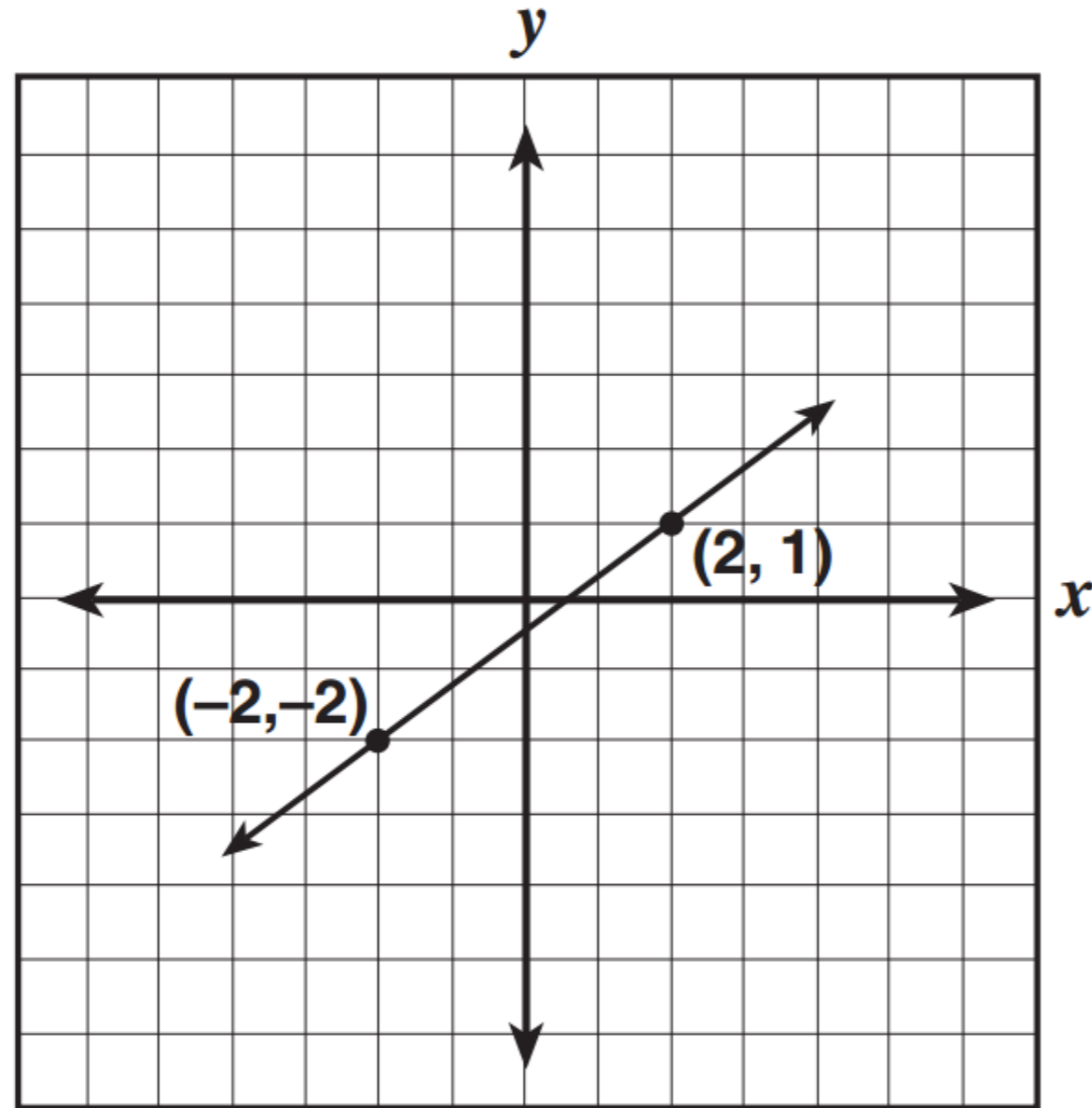
WHAT MATHEMATICS IS IMPORTANT?

WHAT MIGHT IT LOOK LIKE?

WHAT ABOUT WHAT WE USED TO DO?

Student Name	ID Number	Perf. Level	Scaled Score	Mathematics Clusters											
				(Clusters where the percent correct is shown in bold represent proficiency for that cluster.)											
				Rational numbers		Exponents, powers, and roots		Quantitative relationships and evaluating expressions		Multi-step problems, graphing, and functions		Measurement and geometry		Statistics, data analysis, and probability	
Number Correct	Percent Correct	Number Correct	Percent Correct	Number Correct	Percent Correct	Number Correct	Percent Correct	Number Correct	Percent Correct	Number Correct	Percent Correct	Number Correct	Percent Correct		
ALAN, ALAN	11111	ADV	476	13	93%	8	100%	8	80%	14	93%	12	92%	5	100%
ALAN, ALAN	11111	ADV	464	13	93%	7	88%	8	80%	15	100%	11	85%	5	100%
ALAN, ALAN	11111	ADV	453	10	71%	8	100%	10	100%	14	93%	11	85%	5	100%
ALAN, ALAN	11111	ADV	453	13	93%	8	100%	9	90%	12	80%	11	85%	5	100%
ALAN, ALAN	11111	ADV	444	14	100%	7	88%	8	80%	13	87%	10	77%	5	100%
ALAN, ALAN	11111	ADV	444	12	86%	8	100%	8	80%	15	100%	10	77%	4	80%
ALAN, ALAN	11111	ADV	444	13	93%	8	100%	8	80%	14	93%	9	69%	5	100%
ALAN, ALAN	11111	ADV	435	12	86%	6	75%	9	90%	14	93%	10	77%	5	100%
ALAN, ALAN	11111	ADV	435	12	86%	6	75%	8	80%	14	93%	11	85%	5	100%
ALAN, ALAN	11111	ADV	435	13	93%	7	88%	9	90%	12	80%	10	77%	5	100%
ALAN, ALAN	11111	ADV	427	13	93%	6	75%	9	90%	12	80%	10	77%	5	100%
ALAN, ALAN	11111	ADV	427	13	93%	7	88%	6	60%	13	87%	11	85%	5	100%
ALAN, ALAN	11111	ADV	427	14	100%	5	63%	7	70%	14	93%	10	77%	5	100%
ALAN, ALAN	11111	ADV	421	13	93%	6	75%	6	60%	14	93%	10	77%	5	100%
ALAN, ALAN	11111	ADV	421	11	79%	5	63%	9	90%	13	87%	11	85%	5	100%
ALAN, ALAN	11111	ADV	414	12	86%	6	75%	8	80%	11	73%	11	85%	5	100%
ALAN, ALAN	11111	ADV	414	12	86%	8	100%	8	80%	13	87%	8	62%	4	80%
ALAN, ALAN	11111	PRO	408	11	79%	6	75%	9	90%	11	73%	10	77%	5	100%
ALAN, ALAN	11111	PRO	402	12	86%	8	100%	9	90%	8	53%	11	85%	3	60%
ALAN, ALAN	11111	PRO	402	8	57%	7	88%	8	80%	13	87%	10	77%	5	100%
ALAN, ALAN	11111	PRO	402	13	93%	6	75%	7	70%	13	87%	8	62%	4	80%
ALAN, ALAN	11111	PRO	402	11	79%	5	63%	7	70%	11	73%	12	92%	5	100%
ALAN, ALAN	11111	PRO	402	13	93%	7	88%	9	90%	10	67%	7	54%	5	100%
ALAN, ALAN	11111	PRO	402	13	93%	7	88%	7	70%	11	73%	8	62%	5	100%
ALAN, ALAN	11111	PRO	396	10	71%	6	75%	9	90%	14	93%	7	54%	4	80%
ALAN, ALAN	11111	PRO	396	12	86%	8	100%	6	60%	9	60%	11	85%	4	80%

52 What is the slope of this line?



- A $\frac{1}{2}$
- B $\frac{3}{4}$
- C 1
- D $\frac{4}{3}$



Student Name	ID Number	Perf. Level	Scaled Score	Mathematics Clusters											
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Number Correct	Percent Correct	Number Correct	Percent Correct	Number Correct	Percent Correct	Number Correct	Percent Correct	Number Correct	Percent Correct	Number Correct	Percent Correct	Number Correct	Percent Correct		
...	...	ADV	476	13	93%	8	100%	8	80%	14	93%	12	92%	5	100%
...	...	ADV	464	13	93%	7	88%	8	80%	15	100%	11	85%	5	100%
...	...	ADV	453	10	71%	8	100%	10	100%	14	93%	11	85%	5	100%
...	8	100%	11	85%	5	100%
...	10	77%	5	100%
...	10	77%	4	80%
...	9	69%	5	100%
...	12	75%	10	77%	5	100%
...	12	75%	11	85%	5	100%
...	7	88%	10	77%	5	100%
...	6	75%	10	77%	5	100%
...	...	ADV	7	88%	11	85%	5	100%
...	...	ADV	5	63%	10	77%	5	100%
...	...	ADV	421	...	93%	6	75%	6	10	77%	5	100%
...	...	ADV	421	11	79%	5	63%	9	90%	13	87%	11	85%	5	100%
...	...	ADV	414	12	86%	6	75%	8	80%	11	73%	11	85%	5	100%
...	...	ADV	414	12	86%	8	100%	8	80%	13	87%	8	62%	4	80%
...	...	PRO	408	11	79%	6	75%	9	90%	11	73%	10	77%	5	100%
...	...	PRO	402	12	86%	8	100%	9	90%	8	53%	11	85%	3	60%
...	...	PRO	402	8	57%	7	88%	8	80%	13	87%	10	77%	5	100%
...	...	PRO	402	13	93%	6	75%	7	70%	13	87%	8	62%	4	80%
...	...	PRO	402	11	79%	5	63%	7	70%	11	73%	12	92%	5	100%
...	...	PRO	402	13	93%	7	88%	9	90%	10	67%	7	54%	5	100%
...	...	PRO	402	13	93%	7	88%	7	70%	11	73%	8	62%	5	100%
...	...	PRO	396	10	71%	6	75%	9	90%	14	93%	7	54%	4	80%
...	...	PRO	396	12	86%	8	100%	6	60%	9	60%	11	85%	4	80%

X-RAY VISION PROBLEMS

WHY DO WE NEED THEM?

WHY ARE THEY DIFFERENT?

HOW DO YOU IMPLEMENT THEM?

HOW DO YOU CREATE YOUR OWN?

WHERE DO YOU GET OTHERS?

PROBLEM ONE

Solve for x .

$$21 + x = 70$$

PROBLEM TWO

Using the digits 1 to 9, at most one time each, create two equations: one where x has a positive value and one where x has a negative value.

$$\boxed{} + x = \boxed{}$$

PROBLEM THREE

Using the digits 1 to 9, at most one time each, create an equation where x has the greatest possible value.

$$\square\square + x = \square\square$$



Robert Kaplinsky

@robertkaplinsky

MS & HS #MTBoS Ts, please ask your Ss these 3 ?s and put the % who answered correctly here:

[docs.google.com/forms/d/e/1FAI](https://docs.google.com/forms/d/e/1FAI...) Answers at top of form.

PROBLEM ONE
Solve for x.
 $21 + x = 7$

PROBLEM TWO
Using the digits 1 to 9, at most one time each, create two equations: one where x has a positive value and one where x has a negative value.
[][] + x = [][]

PROBLEM THREE
Using the digits 1 to 9, at most one time each, create an equation where x has the greatest possible value.
[][] + x = [][]

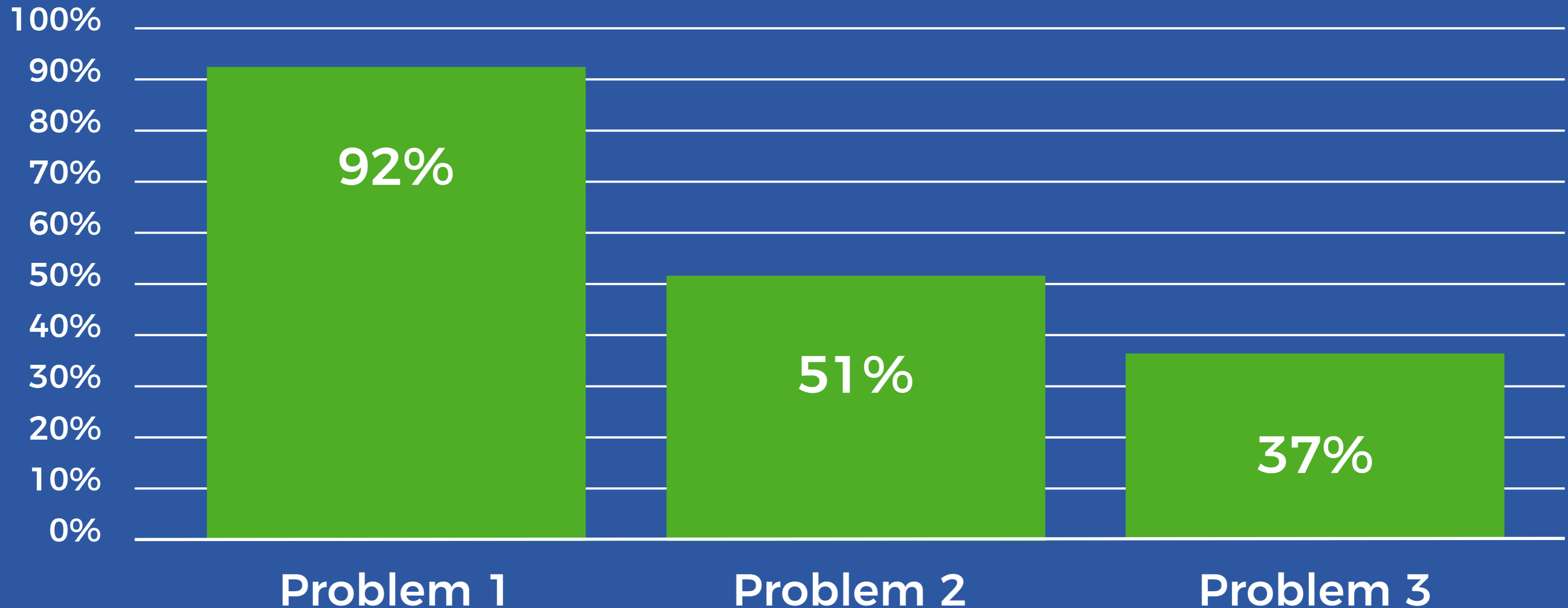
RobertKaplinsky.com

RETWEETS
36

LIKES
54



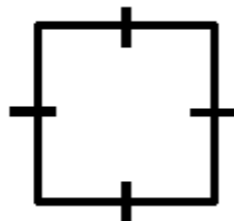
PROBLEM RESULTS



Depth of Knowledge Matrix - Secondary Math

Topic	Dividing Fractions	Solving Two-Step Equations	Exponents	Solving Equations with Variables on Both Sides
CCSS Standard(s)	<ul style="list-style-type: none"> 6.NS.1 	<ul style="list-style-type: none"> 7.EE.4a 	<ul style="list-style-type: none"> 8.EE.1 	<ul style="list-style-type: none"> 8.EE.8 A-REI.3
DOK 1 Example	Evaluate. $\frac{4}{9} \div \frac{2}{5}$	Solve for x. $2x + 3 = 9$	Evaluate. 3^4	Solve for x. $3x + 2 = -2x + 4$
DOK 2 Example	Use the digits 1 to 9, at most one time each, to fill in the boxes to make two different pairs of fractions that have a quotient of $\frac{2}{3}$. $\frac{\square}{\square} \div \frac{\square}{\square} = \frac{2}{3}$	Use the digits 1 to 9, at most one time each, to create two equations: one where x has a positive value and one where x has a negative value. $\square x + \square = \square$	Use the digits 1 to 9, at most one time each, to fill in the boxes to make two true number sentences. $\square^{\square} = 64$	Use the digits 1 to 9, at most <u>two</u> times each, to fill in the boxes to make an equation with no solutions. $\square x + \square = \square x + \square$
DOK 3 Example	Use the digits 1 to 9, at most one time each, to fill in the boxes to make two fractions that have a quotient that is as close to $\frac{4}{11}$ as possible. $\frac{\square}{\square} \div \frac{\square}{\square}$	Use the digits 1 to 9, at most one time each, to create an equation where x has the greatest possible value. $\square x + \square = \square$	Use the digits 1 to 9, at most one time each, to fill in the boxes to make a result that has the greatest value possible. $\square^{\square} = \square\square\square$	Use the digits 1 to 9, at most one time each, to fill in the boxes so that the solution is closest to zero. $\square x + \square = \square x + \square$

Depth of Knowledge Matrix - Secondary Math

Topic	Geometric Proofs	Complex Numbers	Trigonometric Functions	Definite Integral
CCSS Standard(s)	<ul style="list-style-type: none"> G-CO.11 	<ul style="list-style-type: none"> N-CN.2 	<ul style="list-style-type: none"> F-TF.3 	<ul style="list-style-type: none"> N/A
DOK 1 Example	Add one geometric marking to demonstrate the quadrilateral is a square. 	Multiply the binomials. $(3 + 4i)(2 + 3i)$	Evaluate. $\sin \frac{\pi}{3}$	Solve. $\int_2^6 x^3 dx$
DOK 2 Example	Use exactly 5 geometric markings to show that a quadrilateral is a square.	Use the integers -9 to 9, at most one time each, to fill in the boxes twice: once to make a positive real number product and once to make a negative real number product. $(\square + \square i)(\square + \square i)$	Use the digits 1 to 9, at most one time each, to fill in the boxes and make two true number sentences. $\sin \frac{\square \pi}{\square} = 0$	Use the digits 1 to 9, at most one time each, to fill in the boxes and make a positive and a negative solution. $\int_{\square}^{\square} x^{\square} dx$
DOK 3 Example	What is the least number of geometric markings needed to demonstrate that a quadrilateral is a square?	Use the integers -9 to 9, at most one time each, to fill in the boxes and make a real number product with the greatest value. $(\square + \square i)(\square + \square i)$	Use the digits 1 to 9, at most one time each, so that the function has the greatest possible value. $\sin \frac{\square \pi}{\square} = \frac{\sqrt{\square}}{\square}$	Use the digits 1 to 9, at most one time each, to fill in the boxes and make a solution that is as close to 100 as possible. $\int_{\square}^{\square} x^{\square} dx$

DOK ONE

$$6.9 + a = 46$$

DOK TWO

- 11.** Anton walked 8.9 miles of his 13.5-mile goal for this week. Use the equation $m + 8.9 = 13.5$ to find which path Anton should walk so that he meets his goal for the week.

Path Lengths	
Meadow Path	3.2 miles
Circle Path	4.2 miles
Oak Tree Path	4.6 miles

DOK THREE

- 14. Reasoning** Kyle bought a movie ticket for \$8.45 and a drink for \$1.80. He had just enough money remaining to buy a large popcorn. How much money did Kyle start with? Write an equation to show your reasoning. © MP.2

Cost of Popcorn	
Small	\$2.85
Medium	\$3.75
Large	\$4.75
Extra Large	\$4.85

X-RAY VISION PROBLEMS

WHY DO WE NEED THEM?

WHY ARE THEY DIFFERENT?

HOW DO YOU IMPLEMENT THEM?

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WHERE DO YOU GET OTHERS?

IMPLEMENTATION

- Open Middle Worksheet

First attempt:

Points: ____/2 attempt ____/2 explanation

What did you learn from this attempt? How will your strategy change on your next attempt?

Name: _____ Period: _____ Date: _____

First attempt:

Points: ____/2 attempt ____/2 explanation

What did you learn from this attempt? How will your strategy change on your next attempt?

Second attempt:

Points: ____/2 attempt ____/2 explanation

IMPLEMENTATION

- Open Middle Worksheet
- Classwork
 - Single problem for entire class
 - Extensions menu

QUESTION #1

Use the digits 1 to 9, at most one time each, to create an equation where x has the greatest possible value.

$$\square\square + x = \square\square$$

4 points

QUESTION #2

Solve for x .

$$3x + 7 = 19$$

1 point

QUESTION #3

Use the digits 1 to 9, at most one time each, to create two equations: one where x has a positive value and one where x has a negative value.

$$\square\square + x = \square\square$$

2 points

QUESTION #4

Use the digits 1 to 9, at most one time each, to make each equation true.

$$\square + a = \square$$

$$\square - \square = \square$$

SOLVING EQUATIONS EXTENSION MENU

You must earn at least 12 points by doing the problems of your choice. Circle the questions you

QUESTION #5

Use the digits 1 to 9, at most one time each, to create an equation where x has the greatest possible value.

IMPLEMENTATION

- Open Middle Worksheet
- Classwork
 - Single problem for entire class
 - Extensions menu
- Homework
- Assessments

X-RAY VISION PROBLEMS

WHY DO WE NEED THEM?

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STEP ONE

- **Find a One-Operation Problem**
 - Addition
 - Subtraction
 - **Multiplying**
 - Dividing
 - Exponents (including square root)
 - Trigonometric functions

ADDING 2-DIGIT NUMBERS

Solve.

$$41 + 36 =$$

MULTIPLYING FRACTIONS

Solve.

$$\frac{3}{7} \times \frac{2}{9} =$$

THINKING TIME

STEP TWO

- Go from DOK 1 to DOK 2
 - Strategically remove some information from the problem to prevent immediate calculation
 - Increase the quantity of solutions needed to increase the need to look for patterns

ADDING 2-DIGIT NUMBERS

Using the digits 1 to 9, at most one time each, fill in the boxes to make two different pairs of two-digit numbers that have a sum of 71.

$$\boxed{} \boxed{} + \boxed{} \boxed{} = 71$$

MULTIPLYING FRACTIONS

Using the digits 1 to 9, at most one time each, fill in the boxes to make two different pairs of fractions that have a product of $\frac{2}{3}$.

$$\frac{\boxed{}}{\boxed{}} \times \frac{\boxed{}}{\boxed{}} = \frac{2}{3}$$

THINKING TIME

STEP THREE

- Go from DOK 2 to DOK 3
 - Introduce the need to optimize the solution by making the greatest or least product / sum / difference / quotient / answer.
 - Another optimization option is make the answer closest to a specific value.

ADDING 2-DIGIT NUMBERS

Using the digits 1 to 9, at most one time each, fill in the boxes to make the smallest sum.

$$\boxed{} \boxed{} + \boxed{} \boxed{} = \boxed{} \boxed{}$$

MULTIPLYING FRACTIONS

Using the digits 1 to 9, at most one time each, fill in the boxes to make two fractions that have a product that is as close to $\frac{4}{11}$ as possible.

$$\frac{\boxed{}}{\boxed{}} \times \frac{\boxed{}}{\boxed{}}$$

THINKING TIME

3 Steps to Increase Math DOK Levels

Step 1: Find a One-Operation Problem

- Procedural problems with one operation are easiest to modify.
- Other problems may also be modified but may not be as easy.

Adding 2-Digit Numbers

Solve.

$$41 + 36 = \underline{\quad}$$

Multiplying Fractions

Solve.

$$\frac{3}{7} \times \frac{2}{9} = \underline{\quad}$$

Trigonometry

Solve.

$$\sin \frac{\pi}{3} = \underline{\quad}$$

Step 2: Go from DOK 1 to DOK 2

- Strategically remove some information from the problem to prevent immediate calculation
- Increase the quantity of solutions needed to increase the need to look for patterns

Adding 2-Digit Numbers

Using the digits 1 to 9, at most one time each, fill in the boxes

Multiplying Fractions

Using the digits 1 to 9, at most one time each, fill in the boxes

Trigonometry

Using the digits 1 to 9, at most one time each, fill in the boxes

TWO PROBLEMS

Problem One

Find the sum: $37 + 27$

Problem Two

Using the digits 1 to 9, at most one time each, fill in the boxes to make the smallest sum.

$$\boxed{} + \boxed{} = \boxed{}$$

Problem Drives Sense Making

Yes

No

Teacher Drives Sense Making

Yes

Ideal

Valuable

No

Valuable

Not ideal

X-RAY VISION PROBLEMS

WHY DO WE NEED THEM?

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Open Middle

Challenging math problems worth solving

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Kinder ▾

Grade 1 ▾

Grade 2 ▾

Grade 3 ▾

Grade 4 ▾

Grade 5 ▾

Grade 6 ▾

Grade 7 ▾

Grade 8 ▾

High School ▾

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THE TOP 10 MOST POPULAR PROBLEMS OF 2016

1. Two-Step Equations by Robert Kaplinsky, Daniel Mendivil, Daniel Luevanos, and Robert Kaplinsky
2. Order of Operations by Robert Kaplinsky with answer from Michael Fenton and his students
3. Dot Card Counting by Dan Meyer
4. Rational and Irrational Numbers by Bryan Anderson
5. One Solution, No Solutions, Infinite Solutions by Bryan Anderson
6. Multiplying a Two-Digit Number by a Single-Digit Number by Robert Kaplinsky
7. Exponents and Order of Operations by Zack Miller
8. Converting Between Fractions and Decimals by Robert Kaplinsky
9. Interpreting Percentages by Robert Kaplinsky
10. Two-Step Equations 3 by Erick Lee

WHAT ARE PEOPLE SAYING ABOUT OPEN MIDDLE?



Brian Marko



Search



OPEN MIDDLE WORKSHEET

Download the Open Middle Worksheet (Regular):
Version 1.2

Download the Open Middle Worksheet (Large):
Version 1.1

BROWSE BY DEPTH OF KNOWLEDGE LEVEL

DOK 2: Skills and Concepts

DOK 3: Strategic Thinking

BROWSE BY COMMON CORE STATE STANDARDS

Kindergarten (10)

Counting & Cardinality (2)

Geometry (2)

Number & Operations in Base Ten (1)

Operations & Algebraic Thinking (5)

EQUIDISTANT POINTS

Directions: How many points with integer coordinates are 5 units away from $(-2, 3)$?

Hint

Which methods are available to determine the answer to this problem? What shape is defined by *all* of the points that are 5 units away $(-2, 3)$?

Answer

12 points: $(-5, 7)$, $(-7, 3)$, $(-5, -1)$, $(-2, -2)$, $(3, 3)$, $(1, -1)$, $(-2, 8)$, $(1, 7)$, $(2, 6)$, $(-6, -6)$, $(-6, 0)$, and $(2, 0)$

Source: [Dylan Kane](#)



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OPEN MIDDLE WORKSHEET

Download the Open Middle Worksheet (Regular):
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BROWSE BY DEPTH OF KNOWLEDGE LEVEL

DOK 2: Skills and Concepts

DOK 3: Strategic Thinking

BROWSE BY COMMON CORE STATE STANDARDS

Kindergarten (10)

Counting & Cardinality (2)

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Open Middle @openmiddle · Jan 11



Open Middle @openmiddle · Jan 11

Hey @openmiddle fans, we want to hear from you. Why you use our problems



Open Middle

@openmiddle

Hey @openmiddle fans, we want to hear from you. Why do you use our problems with your students? Share your success stories or lessons learned.

RETWEETS

7

LIKES

6



2:10 PM - 11 Jan 2017



8



7



6



1



2



X-RAY VISION PROBLEMS

WHY DO WE NEED THEM?

WHY ARE THEY DIFFERENT?

HOW DO YOU IMPLEMENT THEM?

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DISCUSSION QUESTIONS

- How can x-ray vision problems like the kinds on openmiddle.com spot misconceptions that may often go unnoticed?
- How do Open Middle problems build both procedural skills and conceptual understanding?

CALL TO ACTION

Action	Do Now	Start Planning	Yes & No	Don't Do
Incorporate higher DOK problems on assessments.		✓		
Replace all DOK 1 problems with higher DOK problems.				✓
Share these resources with colleagues to make them aware.	✓			
Find problems I can integrate on Open Middle.	✓			
Use the 3 steps process to strengthen existing problems.			✓	

PBL RESOURCES

- Problem-based lesson search engine:
robertkaplinsky.com/prbl-search-engine
- My lessons (Elementary, Middle, and High School)
robertkaplinsky.com/lessons
- Dan Meyer (Middle and High School)
threeacts.mrmeyer.com
- Andrew Stadel (Elementary and Middle School)
www.esteemation180.com/lessons.html
- Graham Fletcher (Elementary and Middle School)
gfletchy.com/3-act-lessons



Home



How Much Money IS That?!
(Volume of a rectangular prism)

Search

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Do you like the ideas you're reading? If so, you'll love having the best ones sent to you via email!

Enter your information below and I'll send you a short email each Tuesday about an idea you can use with your students right away.

If you live in the United States, enter your zip code and I'll use it to let you know about events near you.

First Name

How I Can Help You



Real World Problems

My workshops help teachers implement problem-based lessons by helping them experience them from both student and teacher perspective, leading to increase students' success with performance tasks and the Common Core State Standards.



Depth of Knowledge

Problems at higher depth of knowledge levels have the potential to challenge your most talented student yet remain accessible to everyone. I can help teachers develop best practices for implementing them so that students persevere longer towards finding the solution.

Lessons

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- [1st](#)
- [2nd](#)
- [3rd](#)
- [4th](#)
- [5th](#)
- [6th](#)
- [7th](#)
- [8th](#)
- [Alg 1](#)
- [Geo](#)
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How Much Money Were Those Pennies?



How Can We #SaveNelly?



How Many Chip Bags Will There Be?



How Can We Make Stronger Passwords?

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First Name

Robert Kaplinsky's Problem-Based Lessons

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	A	B	C	D	E	F	G	H	I
1	Lesson	Concept / Skill	Standard 1	Standard 2	Standard 3	Standard 4	Standard 5	Standard 6	Standard 7
2	How Much Money Were Those Pennies?	Money, Multiplying Decimals, Proportions	4.MD.2	5.NBT.5	5.NBT.7	7.RP.3			
3	How Can We #SaveNelly?	Dividing Decimals	6.NS.3						
4	How Many Chip Bags Will There Be?	Ratio and Proportions, Population Sampling	6.RP.3	6.RP.3c	7.RP.2	7.RP.3	7.SP.1	7.SP.2	
5	How Can We Make Stronger Passwords?	Permutations, Combinations, Probability, Exponents, Exponential Growth	7.SP.8	8.EE.1	S-MD.7	S-CP.5	S-CP.9		
6	How Many Hot Dogs And Buns Should He Buy?	Least Common Multiple (LCM)	6.NS.4						
7	What Does 2000 Calories Look Like?	Unit Rates, Ratios, Solving Equations, and Solving Inequalities	6.EE.3	6.EE.4	6.EE.5	6.EE.6	6.EE.7	6.EE.8	6.RP.2
8	How Much Money Are The Coins Worth?	Decimal Operations and Coin Counting	2.MD.8	5.NBT.7	6.NS.3				
9	How Many Times Will A Case of Paper Jam?	Interpreting Percentages	6.RP.3c	7.RP.3					
10	How Many Soda Combinations Are There On A Coke Freestyle?	Counting, Composing, and Decomposing Numbers	K.CC.5	K.CC.6	K.OA.1	K.OA.2	K.OA.3	K.OA.4	K.NB.1
11	What Should The Freeway Sign Show?	Fractions on Number Lines, Converting Units, Decimal and Fraction Operations	3.NF.1	3.NF.2	3.NF.2a	3.NF.2b	3.NF.3	3.NF.3a	4.MD.1
12	How Fast Was The Fastest Motorcycle Speeding Ticket Ever?	Converting Units and Unit Rates	5.MD.1	6.RP.3d	7.RP.1	N.Q.1			
13	How Much Did Patrick Peterson Lose By Not Cashing His Check?	Compound and/or Simple Interest	7.RP.3	N-RN.2	A-SSE.1	A-SSE.3c	A-SSE.4	A-REI.11	F-IF.4
14	How Many Biscuits Can You Make?	Dividing Fractions and Mixed Numbers	5.NF.7	5.NF.7a	5.NF.7b	5.NF.7c	6.NS.1		
15	How Much Bigger Should They Make Zoolander's School?	Scale and Proportions	5.NF.5A	7.RP.2	7.G.1				
16	Where Is The Freeway Sign Located?	Identifying Fractions on a Number Line	3.NF.1	3.NF.2	3.NF.2a	3.NF.2b	3.NF.3	3.NF.3a	3.NF.3b
17	How Far Apart Are Exits On A Ring Road?	Arc length measures	G-C.5						
18	How Much Is One Third Of A Cup Of Butter?	Identifying Fractions on a Number Line	3.NF.1	3.NF.2	3.NF.2a	3.NF.2b	3.NF.3	3.NF.3a	3.NF.3b
19	How Do Skytypers Write Messages?	Transformations (Rotations, Reflections, Dilations, and Translations)	8.G.1	8.G.2	8.G.3	8.G.4	G-CO.2	G-CO.3	G-CO.4
20	How Big Is The Bermuda Triangle?	Coordinate Geometry: Area of Triangle	G-GPE.7						
21	What Fraction Of Children Are In The Right Car Seat?	Representing and Comparing Fractions	3.NF.1	3.NF.2	3.NF.3	4.NF.1	4.NF.2		
22	How Much Did The Temperature Drop?	Absolute Value	6.NS.7c	7.NS.1c					
23	How Much Shorter Are Staggered Pipe Stacks?	Circles, Pythagorean Theorem, trigonometric ratios, and linear functions	8.G.7	A-CED.1	A-CED.3	A-CED.4	A-SSE.1a	A-SSE.1b	A-SSE.1c
24	How Do You Write A Check To Pay For Something?	Expanded Form	2.NBT.3	4.NBT.2	5.NBT.3a				
25	How Can We Correct The Scarecrow?	Pythagorean Theorem	8.G.6	G-SRT.4					
26	How Much Does A 100x100 In-N-Out Cheeseburger Cost?	Building and Interpreting Linear Functions	8.F.1	8.F.3	8.F.4	8.F.5	F-IF.4	F-IF.5	F-IF.6
27	How Can We Water All Of The Grass?	Circles, Pythagorean Theorem, trigonometric ratios	7.G.4	8.G.7	G-SRT.8	G-MG.1	G-MG.3		
28	How Much Money IS That?!	Volume of rectangular prism	5.MD.3	5.MD.4	5.MD.5	5.MD.5b	5.MD.5c	6.G.2	7.G.6
29	How Much Money Should Dr. Evil Demand?	Exponential Growth	N-RN.2	A-SSE.1	A-SSE.3c	A-SSE.4	A-REI.11	F-IF.4	F-IF.7
30	How Tall Is Mini-Me?	Scale and Dividing Decimals	5.NF.5	5.NF.5a	5.NF.5b	6.NS.3			
31	How Did They Make Ms. Pac-Man?	Transformations (Rotations, Reflections, and Translations)	8.G.1	8.G.2	8.G.3	8.G.4	G-SRT.2	G-CO.4	G-CO.5
32	Which Ticket Option Is The Best Deal?	Unit Rates and Ratios	6.RP.2	6.RP.3	6.RP.3a	6.RP.3b			
33	How Far Apart Are The Freeway Exits?	Fractions on a Number Line and Subtracting Fractions	3.NF.2	3.NF.2b	4.NF.2	4.NF.3a	4.NF.3c	4.NF.3d	5.NF.1
34	Do We Have Enough Paint?	Area	3.MD.5	3.MD.6	3.MD.7				



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WHAT DO WE KNOW ABOUT EDUCATION?

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