## MATH MODELING CAN

## MAKE YOU FILTHY RICH

## ROBERT KAPLINSKY

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## 

Sports Major League baseball has rules for the dimensions of the baseball diamond. A model of the diamond is shown.

1. On the model, the distance from the pitching mound to home plate is 1.3 inches. Is 1.3 a rational number? Explain.


## Content Standards

8.NS.1, 8.NS.2, 8.EE. 2

Mathematical Practices
1, 3, 4, 6
2. On the model, the distance from first base to second base is 2 inches. Is 2 a rational number? Explain.
3. The distance from home plate to second base is $\sqrt{8}$ inches. Using a calculator, find $\sqrt{8}$. Does it appear to terminate or repeat?


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Common Core State Standards

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20 INOVIUUAL BABS: $\quad 1 / 802$.EACH, $\quad 102$. EACH, TOTAL NET WT. $195 / 8 \mathrm{ZZ}$ ( $1 \mathrm{LB} .35 / 8 \mathrm{OZ}$ ) 556.3 g

- Why did many of you expect there to be five of each?
- Why was it not five of each?
- How might they decide on this combination?


20 INDINIUUAL BAGS: $10 Z$. EACH, TOTAL NET WT. 2002 ( 1 LB. $40 Z$ OZ) 567 g

## GOALS

## ם HOW DO WE MAKE SENSE OF MATH MODELING?

## - IS IT JUST ANSWERING QUESTIONS?

## - HOW DO YOU PROFIT FROM MATH MODELING?

- HOW DO WE HELP OUR STUDENTS IMPROVE?
- WHERE CAN WE FIND MORE RESOURCES?

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##  <br> Spies <br> Analysts <br>  <br> Model






















##  <br> Spies <br> Analysts <br>  <br> Model

# All models are wrong, but some are useful. GEORGE E. P. BOX 

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##  <br> Spies <br> Analysts <br>  <br> Model



## Robert Kaplinsky

@robertkaplinsky
Hey \#MTBoS, can you do me a favor and complete this 3 question anonymous survey about your favorite chips? I need data for a presentation. Please RT. goo.gl/forms/etPtujll... \#iteachmath

notued form
Favorite Chips
Please complete this anonymous survey. I'll be using this data in a presentation.

8:05 PM - 4 Feb 2018

63 Retweets 45 Likes (6) 3

Favorite Chips (Responses)
File Edit View Insert Format Data Tools Form Add-ons Help

## $f_{X}$ Timestamp

|  | A | B | c | D | E | F | G | H |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Timestamp | Lays (Classic) | Doritos (Nacho Cheese) | Doritos (Cool Ranch) | Cheetos (Crunchy) | Sun Chips (Original) | Fritos (Original) | Time Zone |
| 2 | 2/4/2018 20:06:53 | 6 | 5 | 4 | 2 | 3 | 1 | Central Time Zone |
| 3 | 2/4/2018 20:06:55 | 1 | 5 | 6 | 3 | 2 | 4 | Eastern Time Zone |
| 4 | 2/4/2018 20:06:56 | 5 | 2 | 1 | 3 | 6 | 4 | Central Time Zone |
| 5 | 2/4/2018 20:06:57 | 2 | 1 | 6 | 3 | 5 | 4 | Pacific Time Zone |
| 6 | 2/4/2018 20:07:36 | 4 | 1 | 2 | 3 | 5 | 6 | Pacific Time Zone |
| 7 | 2/4/2018 20:08:02 | 5 | 1 | 6 | 4 | 2 | 3 | Pacific Time Zone |
| 8 | 2/4/2018 20:08:05 | 6 | 2 | 4 | 3 | 5 | 1 | Pacific Time Zone |
| 9 | 2/4/2018 20:08:07 | 4 | 2 | 1 | 5 | 3 | 6 | Pacific Time Zone |
| 10 | 2/4/2018 20:08:29 | 5 | 3 | 4 | 1 | 6 | 2 | Central Time Zone |
| 11 | 2/4/2018 20:08:56 | 4 | 5 | 6 | 1 | 2 | 3 | Central Time Zone |
| 12 | 2/4/2018 20:09:54 | 5 | 6 | 5 | 6 | 5 | 4 | Pacific Time Zone |
| 13 | 2/4/2018 20:10:01 | 4 | 2 | 3 | 1 | 5 | 6 | Pacific Time Zone |
| 14 | 2/4/2018 20:10:04 | 6 | 2 | 3 | 1 | 5 | 4 | Central Time Zone |
| 15 | 2/4/2018 20:10:04 | 3 | 5 | 6 | 1 | 4 | 2 | Central Time Zone |
| 16 | 2/4/2018 20:10:05 | 4 | 2 | 6 | 1 | 3 | 5 | Eastern Time Zone |
| 17 | 2/4/2018 20:10:06 | 3 | 2 | 6 | 5 | 1 | 2 | Pacific Time Zone |
| 18 | 2/4/2018 20:10:10 | 4 | 2 | 6 | 3 | 5 | 1 | Mountain Time Zone |
| 19 | 2/4/2018 20:10:12 | 3 | 1 | 5 | 6 | 2 | 4 | Eastern Time Zone |
| 20 | 2/4/2018 20:10:26 | 5 | 3 | 6 | 2 | 4 | 1 | Pacific Time Zone |

$\square$


## ANALYSTS' JOB FOR THE TOP 1

1. Count all the first place votes for each chip type.
2. Divide the total first place votes for each chip type by the total number of votes.
3. Multiply that fraction by 20 to find how many bags there would be in a twenty pack, rounding as necessary.

## ANALYSTS' EXAMPLE



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## ANALYSTS' JOB FOR THE TOP 4

1. Count all the first, second, third, and fourth place votes for each chip type.
2. Multiply the first place votes by four, the second place votes by three, the third place votes by two, and the fourth place votes by one.
3. Add the weighted votes for each chip type and divide by the total number of weighted votes.
4. Divide the weighted votes for each chip type by the total number of votes.
5. Multiply that fraction by 20 to find how many bags there would be in a twenty pack, rounding as necessary.

## ANALYSTS' EXAMPLE



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## CHIP BAG RESULTS



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- How do we protect our planes?
- Which parts of the planc are boing
hit by the mest buHlete?
- Which parts of the plane are the most critical to protect?

- How do we find the fastest route for cach customer?
- How do we find the fastest route for each customer without impacting our other customers?


20 INDNIDUAL BAGS: 1 OZ. EACH, TOTAL NEE WT. 20 0Z. ( 1 LB. $40 Z$ OZ. 567 g
- How many of cach flavor should we put in a package?
- How many of each flavor should we put in a package for each region?
- How can we determine if the extra cost of creating different packages will make us more money?


# Mathematically proficient students who can apply what they know are comfortable making assumptions and approximations to simplify a complicated situation, realizing that these may need revision later. 

CCSS MATH PRACTICE 4

They routinely interpret their mathematical results in the context of the situation and reflect on whether the results make sense, possibly improving the model if it has not served its purpose.
CCSS MATH PRACTICE 4

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## They used 25 products for a pregnancy prediction' score including: <br> - unscented lotion <br> - mineral supplements <br> - cotton balls

Source: New York Times
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## ANALYSTS' EXAMPLE

1. Add the number of bottles of unscented lotion, jars of mineral supplements, and bags of cotton balls.
2. Multiply that times the day of the week.
3. Click your heels twice.
4. Repeat the phrase "There's no place like home!"


##  <br> Spies <br> Analysts <br>  <br> Model

# Priority is determined by: 

- passenger's fare class
- itinerary
- frequent flyer program membership
- check-in time

Source: United Airlines

- News Feed
- Messenger
$\square$ Watch

4. Mark Marklace

## Explore

E Pages
(25) Events
(127) Groups

24 Friend Lists
(2) On This Day
ce Insights
2: Games
(-) Fundraisers
6) Live Video
(-) Pokes

- See More.

Create
Ad Page Group Event Fundraiser


What's on your mind, Robert?Photo/Video
Feeling/Activity

 $0 \pm 4$



## 

## Trending



- Het*
 nincimen
an Hationtis \#nor


$\rightarrow$ tivn
 ancentinn man
Haita

Watchlist: Latest Episodes (1)


See All

Sponsored


##  <br> Spies <br> Analysts <br>  <br> Model

## The stories that show in your News

 Feed are influenced by:- friends you interact with the most
- the number of comments and likes a post receives
- what kind of story it is (ex: photo, video, status update)
Source: Facebook



## Introducing

## echoplus $\$ 149^{99}$

Now shipping. With built-in smart home hub.


Related to items you've viewed See more


Verizon
Prepaid.
Save up to

##  <br> Spies <br> Analysts <br>  <br> Model

## Amazon's recommendation system is based on:

- what a user has bought in the past
- which items they have in their shopping cart
- items they've rated and liked
- what other customers have viewed and purchased

Source: Fortune


Guarantee EMobile

##  <br> Spies <br> Analysts <br>  <br> Model

## The four main components of

 the equations are:- what you say
- what you do
- what people like you do
- historical data

Source: Mashable

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##  <br> Spies <br> Analysts <br>  <br> Model



## The index has three levels:

- Green: full menu - restaurant has power and damage is limited.
- Yellow: limited menu - no power or only power from a generator, or food supplies may be low. : the restaurant is closed - indicating severe damage.

Source: Wikipedia

## MORE EXAMPLES

- How does US News and World Reports rank colleges?
- How does Google know which results to show?
- How do sports teams know who to draft?
- How does SpaceX make boosters land standing up?
- How does Zillow estimate home prices?
- How does Pandora know what music to play?
- How did the BCS rank college football teams?
- How do they figure out who should speak at a conference?


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$\qquad$
$\qquad$
$\qquad$

| What problem are you trying to figure out? | What estimates do you have? |
| :---: | :---: |
|  | Place your estimate on the number line. |
| What info do you already know about the problem? | What info do you need y ou the problem? |
| TOP SECRET! |  |
| What is your conclusion? How did you reach that conclusion? |  |

Your work
[DANGER

# MODELING EXAMPLES 



## - ELEMENTARY SCHOOL

## ■ MIDDLESCHOOL



##  <br> Spies <br> Analysts <br>  <br> Model



Name: $\qquad$ Period: $\qquad$ Date: $\qquad$


## COUNT ALL



## COUNT GROUPS



[^0]
## INVENTED STRATEGY




The main attraction for a busload of Dover fifth-graders was supposed to be the Museum of Fine Arts, but that all changed when they stopped by Kelly's Roast Beef and got a glimpse of their soda-drinking future.

At the entrance of Kelly's sat a sleek Coca-Cola Freestyle fountain crafted to resemble an old-fashioned vending machine, but with a twist: a touchscreen computer embedded in the machine gives customers the option of 125 flavors. You can quench your thirst with a Coke or a Sprite, or try something more exotic - Sprite with Grape or a Hi-C Orange Vanilla.

# MODELING EXAMPLES 

 emmememmemmemmemmemmememmemment
## © ELEMENTARY SCHOOL

## 

## ■ MIDDLESCHOOL




##  <br> Spies <br> Analysts <br>  <br> Model


$\qquad$
$\qquad$ Date: $\qquad$


What is your conclusion? How did you reach that conclusion?
$\qquad$ Period: $\qquad$ Date: $\qquad$




Your work


Total bundles: 3,740 rot 10 s at at 8 ss $=3,961$ bundles

$2=10 x$

## $w$

## $2+$

# MODELING EXAMPLES 

emmegmmmemmmemmemmemmemmemmen

## © ELEMENTARY SCHOOL



## © MIDDLE SCHOOL




##  <br> Spies <br> Analysts <br>  <br> Model



Name: $\qquad$ Period: $\qquad$ Date: $\qquad$



Your work


Non-staggered pipes
Staggered pipes


1 pipe $=h \mathrm{~cm}$
1 pipe $=h \mathrm{~cm}$
$\partial$ pipes = $\partial h \mathrm{~cm}$
3 pipes $=3 h \mathrm{~cm}$
$\partial$ pipes $=33 \mathrm{~cm}$

$$
\because \cdot{ }_{:}^{\prime}
$$

20 pipes $=20 h \mathrm{~cm}$
20 pipes $=33 \mathrm{~cm}$

# MODELING EXAMPLES 

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## © ELEMENTARY SCHOOL



## M MIDDLE SCHOOL

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## PBL RESOURCES

- Problem-based lesson search engine: robertkaplinsky.com/prbl-search-engine
- My lessons (Elementary, Middle, and High School) robertkaplinsky.com/lessons
- Dan Meyer (Middle and High School) threeacts.mrmeyer.com
- Andrew Stadel (Elementary and Middle School) www.estimation180.com/lessons.html
- Graham Fletcher (Elementary and Middle School) gfletchy.com/3-act-lessons

Home


How I Can Help You

Real World Problems
My workshops help teachers implement problem-based lessons by helping them experience them from both student and teacher perspective, leading to increase students' success with performance tasks and the Common Core State Standards.


## Depth of Knowledge

Problems at higher depth of knowledge levels have the potential to challenge your most talented student yet remain accessible to everyone. I can help teachers develop best practices for implementing them so that students persevere longer towards finding the solution.

## Search

Type and hit enter

## Subscribe for

 UpdatesDo you like the ideas you're reading? If so, you'll love having the best ones sent to you via email!

Enter your information below and I'll send you a short email each Tuesday about an idea you can use with your students right away.

If you live in the United States, enter your zip code and I'll use it to let you know about events near you.

First Name

## Lessons



Robert Kaplinsky's Problem-Based Lessons
File Edit View Insert Format Data Tools Add-ons Help All changes saved in Drive


| $f x$ |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | A | B | c | D | E | F | G | H |  |
| 1 | Lesson | Concept / Skill | Standard $1$ | Standard $2$ | Standard $3$ | Standard <br> 4 | Standard $5$ | Standard $6$ | Stan $7$ |
| 2 | How Much Money Were Those Pennies? | Money, Multiply ing Decimals, Proportions | 4.MD. 2 | 5.NBT. 5 | 5.NBT. 7 | 7.RP. 3 |  |  |  |
| 3 | How Can We \#SaveNelly? | Dividing Decimals | 6.NS. 3 |  |  |  |  |  |  |
| 4 | How Many Chip Bags Will There Be? | Ratio and Proportions, Population Sampling | 6. RP. 3 | 6. RP.3C | 7.RP. 2 | 7.RP. 3 | 7.SP. 1 | 7.SP. 2 |  |
| 5 | How Can We Make Stronger Passwords? | Permutations, Combinations, Probability, Exponents, Exponential Growth | 7.SP. 8 | 8.EE. 1 | S-MD. 7 | S-CP. 5 | S-CP. 9 |  |  |
| 6 | How Many Hot Dogs And Buns Should He Buy? | Least Common Multiple (LCM) | 6.NS. 4 |  |  |  |  |  |  |
| 7 | What Does 2000 Calories Look Like? | Unit Rates, Ratios, Solving Equations, and Solving Inequalities | 6.EE. 3 | 6.EE. 4 | 6.EE. 5 | 6.EE. 6 | 6.EE. 7 | 6.EE. 8 | 6. RP. |
| 8 | How Much Money Are The Coins Worth? | Decimal Operations and Coin Counting | 2.MD. 8 | 5.NBT. 7 | 6.NS. 3 |  |  |  |  |
| 9 | How Many Times Will A Case of Paper Jam? | Interpreting Percentages | 6. RP.3c | 7.RP. 3 |  |  |  |  |  |
| 10 | How Many Soda Combinations Are There On A Coke Freestyle? | Counting, Composing, and Decomposing Numbers | K.CC. 5 | K.CC. 6 | K.OA. 1 | K.OA. 2 | K. OA. 3 | K.OA. 4 | K.NB |
| 11 | What Should The Freeway Sign Show? | Fractions on Number Lines, Converting Units, Decimal and Fraction Operations | 3.NF. 1 | 3.NF. 2 | 3.NF.2a | 3.NF.2b | 3.NF. 3 | 3.NF.3a | 4. MD |
| 12 | How Fast Was The Fastest Motorcycle Speeding Ticket Ever? | Converting Units and Unit Rates | 5.MD. 1 | 6.RP.3d | 7.RP. 1 | N.Q. 1 |  |  |  |
| 13 | How Much Did Patrick Peterson Lose By Not Cashing His Check? | Compound and/or Simple Interest | 7.RP. 3 | N-RN. 2 | A-SSE. 1 | A-SSE.3C | A-SSE. 4 | A-REI. 11 | F-IF |
| 14 | How Many Biscuits Can You Make? | Dividing Fractions and Mixed Numbers | 5.NF. 7 | 5.NF.7a | 5.NF.7b | 5.NF.7c | 6.NS. 1 |  |  |
| 15 | How Much Bigger Should They Make Zoolander's School? | Scale and Proportions | 5.NF.5A | 7.RP. 2 | 7.G. 1 |  |  |  |  |
| 16 | Where Is The Freeway Sign Located? | Identify ing Fractions on a Number Line | 3.NF. 1 | 3.NF. 2 | 3.NF.2a | 3.NF.2b | 3.NF. 3 | 3.NF.3a | 3.NF. |
| 17 | How Far Apart Are Exits On A Ring Road? | Arc length measures | G-C. 5 |  |  |  |  |  |  |
| 18 | How Much Is One Third Of A Cup Of Butter? | Identify ing Fractions on a Number Line | 3.NF. 1 | 3.NF. 2 | 3.NF.2a | 3.NF.2b | 3.NF. 3 | 3.NF.3a | 3.NF. |
| 19 | How Do Skytypers Write Messages? | Transformations (Rotations, Reflections, Dilations, and Translations) | 8. G. 1 | 8. G. 2 | 8.G. 3 | 8. G. 4 | G-CO. 2 | G-CO. 3 | G-C |
| 20 | How Big Is The Bermuda Triangle? | Coordinate Geometry: Area of Triangle | G-GPE. 7 |  |  |  |  |  |  |
| 21 | What Fraction Of Children Are In The Right Car Seat? | Representing and Comparing Fractions | 3.NF. 1 | 3.NF. 2 | 3.NF. 3 | 4.NF. 1 | 4.NF. 2 |  |  |
| 22 | How Much Did The Temperature Drop? | Absolute Value | 6.NS.7c | 7.NS.1c |  |  |  |  |  |
| 23 | How Much Shorter Are Staggered Pipe Stacks? | Circles, Pythagorean Theorem, trigonometric ratios, and linear functions | 8. G. 7 | A-CED. 1 | A-CED. 3 | A-CED. 4 | A-SSE.1a | A-SSE.1b | A-SS |
| 24 | How Do You Write A Check To Pay For Something? | Expanded Form | 2.NBT. 3 | 4.NBT. 2 | 5.NBT.3a |  |  |  |  |
| 25 | How Can We Correct The Scarecrow? | Pythagorean Theorem | 8. G. 6 | G-SRT. 4 |  |  |  |  |  |
| 26 | How Much Does A 100×100 In-N-Out Cheeseburger Cost? | Building and Interpretting Linear Functions | 8.F. 1 | 8.F. 3 | 8.F. 4 | 8.F. 5 | F-IF. 4 | F-IF. 5 | F-IF |
| 27 | How Can We Water All Of The Grass? | Circles, Pythagorean Theorem, trigonometric ratios | 7.G. 4 | 8.G. 7 | G-SRT. 8 | G-MG. 1 | G-MG. 3 |  |  |
| 28 | How Much Money IS That?! | Volume of rectangular prism | 5.MD. 3 | 5.MD. 4 | 5.MD. 5 | 5.MD.5b | 5.MD.5c | 6.G. 2 | 7.G. 6 |
| 29 | How Much Money Should Dr. Evil Demand? | Exponential Growth | N-RN. 2 | A-SSE. 1 | A-SSE.3C | A-SSE. 4 | A-REI. 11 | F-IF. 4 | F-IF. |
| 30 | How Tall Is Mini-Me? | Scale and Dividing Decimals | 5.NF. 5 | 5.NF.5a | 5.NF.5b | 6.NS. 3 |  |  |  |
| 31 | How Did They Make Ms. Pac-Man? | Transformations (Rotations, Reflections, and Translations) | 8.G. 1 | 8.G. 2 | 8.G. 3 | 8.G. 4 | G-SRT. 2 | G-CO. 4 | G-CO |
| 32 | Which Ticket Option Is The Best Deal? | Unit Rates and Ratios | 6. RP. 2 | 6. RP. 3 | 6.RP.3a | 6.RP.3b |  |  |  |
| 33 | How Far Apart Are The Freeway Exits? | Fractions on a Number Line and Subtracting Fractions | 3.NF. 2 | 3.NF.2b | 4.NF. 2 | 4.NF.3a | 4.NF.3C | 4.NF.3d | 5.NF. |
| 34 | Do We Have Enough Paint? | Area | 3.MD. 5 | 3.MD. 6 | 3.MD. 7 |  |  |  |  |

$+\equiv$ Sheet1 -

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