## WHAT DO WE KNOW

## ABOUT EDUCATION?

## ROBERT KAPLINSKY

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## 

## paradigm shift

## GOALS

## OWHATIS INTELLIGENCE?

## OWHY DONTT STUDENTS REMEMBER?

## IWHAT MATHEMATICS IS IMPORTANT?







## Yes... no... uh... yes... maybe? MANY STUDENTS

## TURING TEST



## CHINESE ROOM



见体配字然的常套


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- What does intelligence even mean?
- How do we ask questions that measure intelligence?
- Will the tasks that work now always be Chinese room and horse proof?


## GOALS <br> ©WHATIS INTELLIGENCE?

## OWHY DONTT STUDENTS REMEMBER?

## IWHAT MATHEMATICS IS IMPORTANT?



Search Facebook

February $28 \cdot \mathrm{e}$
February 28 . 0


If a theif forces you to take money out of an ATM, do not argue or resist. What you do is punch in your pin\# backwards. FX: if its 1234 vou'll type 4321. When you do that, the money will come out but will be stuc $x$ in the slot. The machine will imme diately alert the local police without the robbers knowledge \& begin taking photos of the suspect. Every ATM has the feature. Stay safe.


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Français (France) Deutsch
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1f Like $\rightarrow$ Share
(1) 19

## Snopes

．What＇s New
$\bigcirc$ Hot 50
（6）Fact Check
E News
（1） video
－ Archive
［1 About

## Will Entering Your PIN in Reverse at an ATM Summon the Police？

Entering your PIN in reverse at any ATM will not automatically send an alarm to local police－－the idea is nothing more than an old and unimplemented suggestion．

## clalm

Entering your PIN in reverse at any ATM will automatically summon the police． See Example（s）

RATING


ORIGIN

Messages offering a seemingly helpful heads－up about how to deal with a situation in which one is forced to hand over money withdrawn from an ATM under duress began circulating on the Internet in September 2006：


If a theif forces you to take money
out of an ATM，do not arque or resist．


## Tell them what you're going to tell them. Tell it to them. Then tell them what you told them.


$\qquad$
Lesson 12 sk
Objective: Write PIN Backwards
$W_{\text {rite }}$ backwards.

1. 0461

1640
7. 6842
2. 3625 5263
8. 7532
3. 9572
4. 8713
9. 1549

## Presentation

-Tell them what you're going to tell them.

- Tell it to them.
- Then tell them what you told them.


## Lesson

-State the lesson objectives.

- Teach the lesson.
- Review the lesson objectives.


# The definition of insanity is doing the same thing over and over again but expecting different results. 

Why Some Ideas Survive and Others Die...


## - Understood

## - Remembered

## - Lasting impact

# STICKY ATTRIBUTES 

## $\square$ SIMPLE

- UNEXPECTED
- CONCRETE
- CREDIBLE
- EMOTIONAL
- STORIES

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## Simplify.

$\left(x^{2}+3\right)\left(2 x^{3}-7 x+4\right)$


Fig. 1.
(2)+
$\rightarrow 2 \rightarrow+5$
Fig. 3.

Fig. 5. .


Fig.14.

Fig. 13.


Fig. 6.
Fig. 9.'

Fig. 10.

Eig:12.

Fig: $4 \alpha$


# If math is the aspirin, then how do you create the headache? 



Step 1


Step 2


Step 3


Step 1


Step 2


Step 3

Skip the practice round




# STICKY ATTRIBUTES 

## $\square$ SIMPLE

## - UNEXPECTED

$\square$ CONCRETE
$\square$ CREDIBLE

- EMOTIONAL
- STORIES

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## 5\% Charged

Source: reasonandwonder.com




Friday, July 11

Sóurce: reasonandwonder.com
9:06


## 14\% Charged

Sóurce: reasonandwonder.com

## 19\% Charged

Source: reasonandwonder.com

$$
9: 18
$$

$$
9: 22
$$

$$
9: 26
$$



38\% Charged

Source: reasonandwonder.com
9:34

9:38

$$
9: 42
$$

$$
9: 46
$$

9:50

$$
9: 54
$$

$$
9: 58
$$

$$
10: 02
$$

10:06


Source: reasonandwonder.com

## 84\% Charged

Sóurce: reasonandwonder.com


Source: reasonandwonder.com


## 89\% Charged

Sóurce: reasonandwonder.com


## 90\% Charged

Sóurce: reasonandwonder.com


## 92\% Charged

Sóurce: reasonandwonder.com


## 93\% Charged

Sóurce: reasonandwonder.com


## 94\% Charged

Sóurce: reasonandwonder.com


## 95\% Charged

Sóurce: reasonandwonder.com

$$
10: 46
$$



## 97\% Charged

Sóurce: reasonandwonder.com


## 97\% Charged

Sóurce: reasonandwonder.com
10:58


Source: reasonandwonder.com


Source: reasonandwonder.com

## 99\% Charged

Source: reasonandwonder.com

## 99\% Charged

Source: reasonandwonder.com

$$
11: 22
$$







## $\begin{array}{lllll}1 & 1 & 1 & 1 & 1\end{array}$ $\frac{1}{2}+\frac{1}{4}+\frac{1}{8}+\frac{1}{16}+\frac{1}{32}+\cdots$

1


RobertKaplinsky.com


Source: Kyle Pearce - youtube.com/watch?v=Yr53Ji4SZDg

# Curiosity... arises from the perception of a gap in knowledge or understanding. 

GEORGE LOEWENSTEIN



Source: robertkaplinsky.com/lessons


$\square$

## Real-World Link

Aquarium The dimensions of an aquarium are shown.

1. What is the area of the base of the aquarium? $\qquad$

2. What is the height of the aquarium?
3. Fill in the blanks to find the volume.

$$
x \quad x \quad=12 \mathrm{ft}^{3}
$$

What estimates do you have?


What info do you already know about the problem?
What info do you need about the problem?

What is your conclusion? How did you reach that conclusion?


Google Maps


My Village

|  | Treasure Map | Google Maps |
| :--- | :--- | :--- |
| Beginning | Closed | Closed |
| Middle | Open | Closed |
| End | Closed | Closed |

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Using the digits 1-9, at most one time each, fill in the boxes to create a fraction that is as close to one as possible.


Extension:<br>How many<br>ways can you prove that you are correct?

Source: Peter Morris on openmiddle.com

|  | Open Middle | Closed Middle |
| :--- | :--- | :--- |
| Beginning | Closed | Closed |
| Middle | Open | Closed |
| End | Closed | Closed |

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## Independent practice



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- STORIES

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$\qquad$
$\qquad$
$\qquad$

## Lesson 7 Skills Practice

Objective: Divide Decimals by Decimals

Divide.

1. $4.86 \div 0.2 \quad$ 7. $2.25 \div 0.15$
2. $7.52 \div 0.74$
3. $628.2 \div 34.9$
4. $421.6 \div 0.4$
5. $0.105 \div 0.6$


## Fans stream Nelly to help him pay off $\$ 2.4$ million debt

by Lisa Respers France @CNNMoney
(L) September 13, 2016: 2:47 PM ET

# - How many \$0.006 are there in \$2,400,000? 

- How many 6 are there in 24?


## LESSON <br> 19-1 <br> Stretching, Compressing, and Reflecting Sine and Cosine Graphs

## Reteach

For a sine function, $y=a \sin \left(\frac{1}{b} x\right)$

Amplitude $=|a|$

Period $=2 \pi \cdot b$

If $a<0$, the graph is reflected across the $x$-axis.


Example Write the function shown in the graph above.


Source: graphingstories.com




The progression of
multiplication

Source: gifletchy.com/progression-videos


## Concrete



## Representational



## Abstract

Source: gfletchy.com

## MY OLD METHODS

$$
\begin{array}{ll}
4(x+3) & (x+3)(x-1) \\
& \text { F } x(x) \\
4(x)+4(3) & 0 \quad x(-1) \\
& \text { I } 3(x) \\
& \text { L } 3(-1) \\
& =x^{2}-x+3 x-3 \\
& =x^{2}+2 x-3
\end{array}
$$

## DISTRIBUTIVE PROPERTY

$4(x+3)$

Concrete


Representational


Abstract

$$
\begin{aligned}
& 4(x+3) \\
& =4(x)+4(3) \\
& =4 x+12
\end{aligned}
$$

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## BINOMIAL MULTIPLICATION

$(x+3)(x-1)$

Concrete


Representational

|  | $x+3$ |  |
| :---: | :---: | :---: |
| $x$ | $x^{2}$ | 3 x |
| 1 | - $x$ | -3 |
| $x^{2}-x+3 x-3$ |  |  |
| $x^{2}+2 x-3$ |  |  |

## Abstract

$$
\begin{aligned}
& (x+3)(x-1) \\
& =x^{2}-x+3 x-3 \\
& =x^{2}+2 x-3
\end{aligned}
$$

# STICKY ATTRIBUTES 

$\square$ SIMPLE
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$\square$ CONCRETE
$\square$ CREDIBLE
$\square$ EMOTIONAL

- STORIES

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## Source:

Jenise Sexton




## Source:

Fawn Nguyen



# STICKY ATTRIBUTES 

$\square$ SIMPLE
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C CONCRETE
© CREDIBLE
$\square$ EMOTIONAL

- STORIES

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Things I never thought I'd say: "So you're saying that Thor has less party than Justin Bieber, but more than Obama?"


RETWEETS LIKES
4

# STICKY ATTRIBUTES 

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CONCRETE
© CREDIBLE
EMOTIONAL

## - STORIES

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# Patrick Peterson Hasn't 'Gotten Around' to Cashing \$15 Million Bonus Check <br> KYLENEWPORT <br> AUGUST 25, 2014 

Source: robertkaplinsky.com/lessons
20. Sports Cornerback Patrick Peterson did not deposit a $\$ 15,361,000$ signing bonus check for 27 days. Assuming a 2\% interest rate, how much money did he lose by not cashing the check immediately?



## IMPORTANCE OF CONTEXT

- Play four songs
- Tapped out
- Write down song names
- Share answers with neighbors
- Listen again with song names


## SONG \#1



## SONG \#3

## SONG \#4

## SONG \#1

## Itsy Bitsy Spider

## SONG \#2

## Wheels On The Bus

## SONG \#3

## Row Row Row Your Boat

## SONG \#4

## Take Me Out To The Ballgame

# Random favor: please listen to me tapping out 4 songs and try to guess the name. Should take < 2 min. It's not easy! 

```
ecognizing Tapped Songs
```



## Recognizing Tapped Songs

Please listen to each of the four songs, type in the name of the song, and the click submit. You may have no clue about what the song is called. If that happens, just write something like, "I don't...
docs.google.com

2:47 PM - 13 Jun 2017

## TAKEAWAYS (PART ONE)

- Of 192 people surveyed:
- Itsy Bitsy Spider: ~41\%
- Wheels on the Bus: ~29\%
- Row Your Boat: ~25\%
- Take Me Out to the Ballgame: ~3\%


# TAKEAWAYS (PART TWO) 

- Many said, "I'm sorry. I don't know."
- Many said, "I'm not good at this."
- Many said, "I don’t like this."


## CURSE OF KNOWLEDGE



Abstract

# STICKY ATTRIBUTES 

$\square$ SIMPLE
© UNEXPECTED
CONCRETE
© CREDIBLE
E EMOTIONAL
$\square$ STORIES

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UNEXPECTED CONCRETE

- CREDIBLE

EMOTIONAL
$\square$ STORIES

- SIMPLE
- UNEXPECTED
- CONCRETE
- CREDIBLE
$\square$ EMOTIONAL
- STORIES
- Which of the attributes (simple, unexpected, concrete, credible, emotional, and stories) resonates most with you and why?
- How can we apply these attributes to how we teach mathematics?


## GOALS

WWHATIS INTELLIGENCE?
©WHY DONTT STUDENTS REMEMBER?

## IWHAT MATHEMATICS IS IMPORTANT?

Sports Major League baseball has rules for the dimensions of the baseball diamond. A model of the diamond is shown.

1. On the model, the distance from the pitching mound to home plate is 1.3 inches. Is 1.3 a rational number? Explain.


## Content Standards

8.NS.1, 8.NS.2, 8.EE. 2

Mathematical Practices
1, 3, 4, 6
2. On the model, the distance from first base to second base is 2 inches. Is 2 a rational number? Explain.
3. The distance from home plate to second base is $\sqrt{8}$ inches. Using a calculator, find $\sqrt{8}$. Does it appear to terminate or repeat?


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Common Core State Standards

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20 INOVIUUAL BABS: $\quad 1 / 802$.EACH, $\quad 102$. EACH, TOTAL NET WT. $195 / 8 \mathrm{ZZ}$ ( $1 \mathrm{LB} .35 / 8 \mathrm{OZ}$ ) 556.3 g

## THINKING TIME

- Why did many of you expect there to be five of each?
- Why was it not five of each?
- How might they decide on this combination?


20 INDIIIDUAL BAGS: 1 OZ. EACH, TOTAL NE WT. 20 OZ. ( 1 LB. $40 Z$ OZ.) 567 g

## MATH MODELING

## ■ HOW DO WE MAKE SENSE OF MATH MODELING?

## ■ IS IT JUST ANSWERING QUESTIONS?

## ■ HOW DO YOU PROFIT FROM MATH MODELING?

## ■ HOW DO WE HELP OUR STUDENTS IMPROVE?






##  <br> Spies <br> Analysts <br>  <br> Model






















##  <br> Spies <br> Analysts <br>  <br> Model

# All models are wrong, but some are useful. GEORGE E. P. BOX 



20 INDINIUUAL BAGS: $10 Z$. EACH, TOTAL NET WT. 2002 ( 1 LB. $40 Z$ OZ) 567 g

##  <br> Spies <br> Analysts <br>  <br> Model

## THINKING TIME



20 INOVIDUAL BAGS: $10 Z$. EACH, TOTAL NEE WT. 200 OZ ( 1 LB. 40 OZ ) 567 g

## Robert Kaplinsky

@robertkaplinsky
Hey \#MTBoS, can you do me a favor and complete this 3 question anonymous survey about your favorite chips? I need data for a presentation. Please RT. goo.gl/forms/etPtuill... \#iteachmath


Favorite Chips
Please complete this anonymous survey. I'll be using this data in a presentation.

8:05 PM - 4 Feb 2018

63 Retweets 45 Likes (3) 0

Favorite Chips (Responses)
File Edit View Insert Format Data Tools Form Add-ons Help
$f_{X} \mid$ Timestamp

|  | A | B | C | D | E | F | G | H |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Timestamp | Lays (Classic) | Doritos (Nacho Cheese) | Doritos (Cool Ranch) | Cheetos (Crunchy) | Sun Chips (Original) | Fritos (Original) | Time Zone |
| 2 | 2/4/2018 20:06:53 | 6 | 5 | 4 | 2 | 3 | 1 | Central Time Zone |
| 3 | 2/4/2018 20:06:55 | 1 | 5 | 6 | 3 | 2 | 4 | Eastern Time Zone |
| 4 | 2/4/2018 20:06:56 | 5 | 2 | 1 | 3 | 6 | 4 | Central Time Zone |
| 5 | 2/4/2018 20:06:57 | 2 | 1 | 6 | 3 | 5 | 4 | Pacific Time Zone |
| 6 | 2/4/2018 20:07:36 | 4 | 1 | 2 | 3 | 5 | 6 | Pacific Time Zone |
| 7 | 2/4/2018 20:08:02 | 5 | 1 | 6 | 4 | 2 | 3 | Pacific Time Zone |
| 8 | 2/4/2018 20:08:05 | 6 | 2 | 4 | 3 | 5 | 1 | Pacific Time Zone |
| 9 | 2/4/2018 20:08:07 | 4 | 2 | 1 | 5 | 3 | 6 | Pacific Time Zone |
| 10 | 2/4/2018 20:08:29 | 5 | 3 | 4 | 1 | 6 | 2 | Central Time Zone |
| 11 | 2/4/2018 20:08:56 | 4 | 5 | 6 | 1 | 2 | 3 | Central Time Zone |
| 12 | 2/4/2018 20:09:54 | 5 | 6 | 5 | 6 | 5 | 4 | Pacific Time Zone |
| 13 | 2/4/2018 20:10:01 | 4 | 2 | 3 | 1 | 5 | 6 | Pacific Time Zone |
| 14 | 2/4/2018 20:10:04 | 6 | 2 | 3 | 1 | 5 | 4 | Central Time Zone |
| 15 | 2/4/2018 20:10:04 | 3 | 5 | 6 | 1 | 4 | 2 | Central Time Zone |
| 16 | 2/4/2018 20:10:05 | 4 | 2 | 6 | 1 | 3 | 5 | Eastern Time Zone |
| 17 | 2/4/2018 20:10:06 | 3 | 2 | 6 | 5 | 1 | 2 | Pacific Time Zone |
| 18 | 2/4/2018 20:10:10 | 4 | 2 | 6 | 3 | 5 | 1 | Mountain Time Zone |
| 19 | 2/4/2018 20:10:12 | 3 | 1 | 5 | 6 | 2 | 4 | Eastern Time Zone |
| 20 | 2/4/2018 20:10:26 | 5 | 3 | 6 | 2 | 4 | 1 | Pacific Time Zone |

$\square$

- The available data includes:
- Lays, Nacho Cheese Doritos, Cool Ranch Doritos, Cheetos, Sun Chips, and Fritos ranked from 1 to 6
- Geographic region: West, Central, or Eastern


## ANALYSTS' JOB FOR THE TOP 1

1. Count all the first place votes for each chip type.
2. Divide the total first place votes for each chip type by the total number of votes.
3. Multiply that fraction by 20 to find how many bags there would be in a twenty pack, rounding as necessary.

## ANALYSTS' EXAMPLE



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## ANALYSTS' JOB FOR THE TOP 4

1. Count all the first, second, third, and fourth place votes for each chip type.
2. Multiply the first place votes by four, the second place votes by three, the third place votes by two, and the fourth place votes by one.
3. Add the weighted votes for each chip type and divide by the total number of weighted votes.
4. Divide the weighted votes for each chip type by the total number of votes.
5. Multiply that fraction by 20 to find how many bags there would be in a twenty pack, rounding as necessary.

## ANALYSTS' EXAMPLE



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## CHIP BAG RESULTS



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## MATH MODELING

 ■ HOW DO WE MAKE SENSE OF MATH MODELING?\author{

- IS IT JUST ANSWERING QUESTIONS?
}


## - HOW DO YOU PROFIT FROM MATH MODELING?

- HOW DO WE HELP OUR STUDENTS IMPROVE?

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- How do we protect our planes?
- Which parts of the planc are boing hit by the mest buHlete?
- Which parts of the plane are the most critical to protect?

- How do we find the fastest route for each custemer?
- How do we find the fastest route for each customer without impacting our other customers?


20 INDNIDUAL BAGS: 1 OZ. EACH, TOTAL NEE WT. 20 0Z. ( 1 LB. $40 Z$ OZ. 567 g
- How many of each flaver should we put in a packase?
- Hew many of each flawor should we put in a packuge for such region?
- How can we determine if the extra cost of creating different packages will make us more money?


# Mathematically proficient students who can apply what they know are comfortable making assumptions and approximations to simplify a complicated situation, realizing that these may need revision later. 

CCsS


PRACTICE 4

They routinely interpret their mathematical results in the context of the situation and reflect on whether the results make sense, possibly improving the model if it has not served its purpose.
Ccss


4

## MATH MODELING

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##  <br> Spies <br> Analysts <br>  <br> Model



## They used 25 products for a pregnancy prediction' score including: <br> - unscented lotion <br> - mineral supplements <br> - cotton balls

Source: New York Times
RobertKaplinsky.com

## ANALYSTS' EXAMPLE

1. Add the number of bottles of unscented lotion, jars of mineral supplements, and bags of cotton balls.
2. Multiply that times the day of the week.
3. Click your heels twice.
4. Repeat the phrase "There's no place like home!"


##  <br> Spies <br> Analysts <br>  <br> Model



# Priority is determined by: 

- passenger's fare class
- itinerary
- frequent flyer program membership
- check-in time

Source: United Airlines

- News Feed
- Messenger
$\square$ Watch

4. Mark Marklace

## Explore

E Pages
(25) Events
(127) Groups

24 Friend Lists
(2) On This Day
ce Insights
2: Games
(-) Fundraisers
6) Live Video
(-) Pokes

- See More.

Create
Ad Page Group Event Fundraiser


What's on your mind, Robert?Photo/Video
Feeling/Activity

 $0 \pm 4$



## 

## Trending



- Het*
 nincimen
an Hationtis \#nor


$\rightarrow$ tivn
 ancentinn man
Haita

Watchlist: Latest Episodes (1)


See All

Sponsored


##  <br> Spies <br> Analysts <br>  <br> Model



## The stories that show in your News

 Feed are influenced by:- friends you interact with the most
- the number of comments and likes a post receives
- what kind of story it is (ex: photo, video, status update)
Source: Facebook
RobertKaplinsky.com



## Introducing

## echoplus $\$ 149^{99}$

Now shipping. With built-in smart home hub.


Related to items you've viewed See more


Verizon
Prepaid.
Save up to

##  <br> Spies <br> Analysts <br>  <br> Model



## Amazon's recommendation system is based on:

- what a user has bought in the past
- which items they have in their shopping cart
- items they've rated and liked
- what other customers have viewed and purchased

Source: Fortune


Guarantee EMobile


##  <br> Spies <br> Analysts <br>  <br> Model

## The four main components of

 the equations are:- what you say
- what you do
- what people like you do
- historical data

Source: Mashable
RobertKaplinsky.com



##  <br> Spies <br> Analysts <br>  <br> Model



## The index has three levels:

- Green: full menu - restaurant has power and damage is limited.
- Yellow: limited menu - no power or only power from a generator, or food supplies may be low. : the restaurant is closed - indicating severe damage.

Source: Wikipedia

## MORE EXAMPLES

- How does US News and World Reports rank colleges?
- How does Google know which results to show?
- How do sports teams know who to draft?
- How does SpaceX make boosters land standing up?
- How does Zillow estimate home prices?
- How does Pandora know what music to play?
- How did the BCS rank college football teams?
- How do they figure out who should speak at a conference?


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$\qquad$
$\qquad$
$\qquad$

| What problem are you trying to figure out? | What estimates do you have? |
| :---: | :---: |
|  | Place your estimate on the number line. |
| What info do you already know about the problem? | What info do you need y ou the problem? |
| TOP SECRET! |  |
| What is your conclusion? How did you reach that conclusion? |  |

Your work


# MODELNG EXAMPLES 

 mmmmmmmmmmmmem - MIDDLESCHOOL|>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>1

## - HIGH SCHOOL



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##  <br> Spies <br> Analysts <br>  <br> Model


$\qquad$
$\qquad$ Date: $\qquad$


What is your conclusion? How did you reach that conclusion?
$\qquad$ Period: $\qquad$ Date: $\qquad$




Your work


Total bundles: 3,740 rot 10 sa act 8 ss $=3,961$ bundles

$2=10 x$

## $w$

## $2+$

# MODELING EXAMPLES 

## emmenmmmmmemmemmmmmem

## ■ MIDDLESCHOOL

|>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>0

## - HICH SCHOOL





##  <br> Spies <br> Analysts <br>  <br> Model



Name: $\qquad$ Period: $\qquad$ Date: $\qquad$


What is your conclusion? How did you reach that conclusion?




Your work


Staggered pipes g


1 pipe $=h \mathrm{~cm}$
1 pipe $=h \mathrm{~cm}$
a pipes = ah cm
3 pipes $=3 \mathrm{hcm}$
a pipes $=33 \mathrm{~cm}$

$$
: ' \quad-\quad
$$

20 pipes $=20 h \mathrm{~cm}$
20 pipes $=33 \mathrm{~cm}$

## STAGGERED PIPES



# MODELING EXAMPLES 

## emmenmmmmmemmemmmmmem

## ■ MIDDLESCHOOL

## 

## ■ HIGH SCHOOL



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Common Core State Standards

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8.NS.1, 8.NS.2, 8.EE. 2

Mathematical Practices
1, 3, 4, 6
2. On the model, the distance from first base to second base is 2 inches. Is 2 a rational number? Explain.
3. The distance from home plate to second base is $\sqrt{8}$ inches. Using a calculator, find $\sqrt{8}$. Does it appear to terminate or repeat?


- What previous understandings of mathematical modeling were confirmed?
- How has your understanding of mathematical modeling shifted?
- What would you recommend math teachers do differently?


## GOALS <br> ©WHAT IS INTELLIGENCE? <br> ©WHY DON'T STUDENTS REMEMBER? UWHAT MATHEMATICS IS IMPORTANT?

## PBL RESOURCES

- Problem-based lesson search engine: robertkaplinsky.com/prbl-search-engine
- My lessons (Middle, and High School) robertkaplinsky.com/lessons
- Dan Meyer (Middle and High School) threeacts.mrmeyer.com
- Andrew Stadel (Middle School) www.estimation180.com/lessons.html


## R Robert Kaplinsky

Home


## How I Can Help You

Real World Problems
My workshops help teachers implement problem-based lessons by helping them experience them from both student and teacher perspective, leading to increase students' success with performance tasks and the Common Core State Standards.


## Depth of Knowledge

Problems at higher depth of knowledge levels have the potential to challenge your most talented student yet remain accessible to everyone. I can help teachers develop best practices for implementing them so that students persevere longer towards finding the solution.

Search
Type and hit enter

## Subscribe for

 UpdatesDo you like the ideas you're reading? If so, you'll love having the best ones sent to you via email!

Enter your information below and I'll send you a short email each Tuesday about an idea you can use with your students right away.

If you live in the United States, enter your zip code and I'll use it to let you know about events near you.

First Name

## Lessons



Robert Kaplinsky's Problem-Based Lessons
File Edit View Insert Format Data Tools Add-ons Help All changes saved in Drive


| $f x$ |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | A | B | c | D | E | F | G | H |  |
| 1 | Lesson | Concept / Skill | Standard $1$ | Standard $2$ | Standard $3$ | Standard $4$ | Standard $5$ | Standard $6$ | Stan $7$ |
| 2 | How Much Money Were Those Pennies? | Money, Multiply ing Decimals, Proportions | 4.MD. 2 | 5.NBT. 5 | 5.NBT. 7 | 7.RP. 3 |  |  |  |
| 3 | How Can We \#SaveNelly? | Dividing Decimals | 6.NS. 3 |  |  |  |  |  |  |
| 4 | How Many Chip Bags Will There Be? | Ratio and Proportions, Population Sampling | 6.RP. 3 | 6. RP.3C | 7.RP. 2 | 7.RP. 3 | 7.SP. 1 | 7.SP. 2 |  |
| 5 | How Can We Make Stronger Passwords? | Permutations, Combinations, Probability, Exponents, Exponential Growth | 7.SP. 8 | 8.EE. 1 | S-MD. 7 | S-CP. 5 | S-CP. 9 |  |  |
| 6 | How Many Hot Dogs And Buns Should He Buy? | Least Common Multiple (LCM) | 6.NS. 4 |  |  |  |  |  |  |
| 7 | What Does 2000 Calories Look Like? | Unit Rates, Ratios, Solving Equations, and Solving Inequalities | 6.EE. 3 | 6.EE. 4 | 6.EE. 5 | 6.EE. 6 | 6.EE. 7 | 6.EE. 8 | 6. RP |
| 8 | How Much Money Are The Coins Worth? | Decimal Operations and Coin Counting | 2.MD. 8 | 5.NBT. 7 | 6.NS. 3 |  |  |  |  |
| 9 | How Many Times Will A Case of Paper Jam? | Interpreting Percentages | 6. RP.3C | 7.RP. 3 |  |  |  |  |  |
| 10 | How Many Soda Combinations Are There On A Coke Freestyle? | Counting, Composing, and Decomposing Numbers | K.CC. 5 | K.CC. 6 | K.OA. 1 | K.OA. 2 | K. OA. 3 | K.OA. 4 | K.NB |
| 11 | What Should The Freeway Sign Show? | Fractions on Number Lines, Converting Units, Decimal and Fraction Operations | 3.NF. 1 | 3.NF. 2 | 3.NF.2a | 3.NF.2b | 3.NF. 3 | 3.NF.3a | 4. MD |
| 12 | How Fast Was The Fastest Motorcycle Speeding Ticket Ever? | Converting Units and Unit Rates | 5.MD. 1 | 6.RP.3d | 7.RP. 1 | N.Q. 1 |  |  |  |
| 13 | How Much Did Patrick Peterson Lose By Not Cashing His Check? | Compound and/or Simple Interest | 7.RP. 3 | N-RN. 2 | A-SSE. 1 | A-SSE.3C | A-SSE. 4 | A-REI. 11 | F-IF |
| 14 | How Many Biscuits Can You Make? | Dividing Fractions and Mixed Numbers | 5.NF. 7 | 5.NF.7a | 5.NF.7b | 5.NF.7c | 6.NS. 1 |  |  |
| 15 | How Much Bigger Should They Make Zoolander's School? | Scale and Proportions | 5.NF.5A | 7.RP. 2 | 7.G. 1 |  |  |  |  |
| 16 | Where Is The Freeway Sign Located? | Identify ing Fractions on a Number Line | 3.NF. 1 | 3.NF. 2 | 3.NF.2a | 3.NF.2b | 3.NF. 3 | 3.NF.3a | 3.NF. |
| 17 | How Far Apart Are Exits On A Ring Road? | Arc length measures | G-C. 5 |  |  |  |  |  |  |
| 18 | How Much Is One Third Of A Cup Of Butter? | Identify ing Fractions on a Number Line | 3.NF. 1 | 3.NF. 2 | 3.NF.2a | 3.NF.2b | 3.NF. 3 | 3.NF.3a | 3.NF |
| 19 | How Do Skytypers Write Messages? | Transformations (Rotations, Reflections, Dilations, and Translations) | 8.G. 1 | 8. G. 2 | 8. G. 3 | 8.G. 4 | G-CO. 2 | G-CO. 3 | G-CO |
| 20 | How Big Is The Bermuda Triangle? | Coordinate Geometry: Area of Triangle | G-GPE. 7 |  |  |  |  |  |  |
| 21 | What Fraction Of Children Are In The Right Car Seat? | Representing and Comparing Fractions | 3.NF. 1 | 3.NF. 2 | 3.NF. 3 | 4.NF. 1 | 4.NF. 2 |  |  |
| 22 | How Much Did The Temperature Drop? | Absolute Value | 6.NS.7c | 7.NS.1c |  |  |  |  |  |
| 23 | How Much Shorter Are Staggered Pipe Stacks? | Circles, Pythagorean Theorem, trigonometric ratios, and linear functions | 8. G. 7 | A-CED. 1 | A-CED. 3 | A-CED. 4 | A-SSE.1a | A-SSE.1b | A-SS |
| 24 | How Do You Write A Check To Pay For Something? | Expanded Form | 2.NBT. 3 | 4.NBT. 2 | 5.NBT.3a |  |  |  |  |
| 25 | How Can We Correct The Scarecrow? | Pythagorean Theorem | 8.G. 6 | G-SRT. 4 |  |  |  |  |  |
| 26 | How Much Does A 100×100 In-N-Out Cheeseburger Cost? | Building and Interpretting Linear Functions | 8.F. 1 | 8.F. 3 | 8. F. 4 | 8.F. 5 | F-IF. 4 | F-IF. 5 | F-IF |
| 27 | How Can We Water All Of The Grass? | Circles, Pythagorean Theorem, trigonometric ratios | 7. G. 4 | 8. G. 7 | G-SRT. 8 | G-MG. 1 | G-MG. 3 |  |  |
| 28 | How Much Money IS That?! | Volume of rectangular prism | 5.MD. 3 | 5.MD. 4 | 5.MD. 5 | 5.MD.5b | 5.MD.5c | 6. G. 2 | 7. G. 6 |
| 29 | How Much Money Should Dr. Evil Demand? | Exponential Growth | N-RN. 2 | A-SSE. 1 | A-SSE.3C | A-SSE. 4 | A-REI. 11 | F-IF. 4 | F-IF |
| 30 | How Tall Is Mini-Me? | Scale and Dividing Decimals | 5.NF. 5 | 5.NF.5a | 5.NF.5b | 6.NS. 3 |  |  |  |
| 31 | How Did They Make Ms. Pac-Man? | Transformations (Rotations, Reflections, and Translations) | $8 . \mathrm{G}$. | 8.G. 2 | $8 . \mathrm{G} .3$ | $8 . \mathrm{G}$. | G-SRT. 2 | G-CO. 4 | G-CO |
| 32 | Which Ticket Option Is The Best Deal? | Unit Rates and Ratios | 6.RP. 2 | 6. RP. 3 | 6. RP.3a | 6. RP.3b |  |  |  |
| 33 | How Far Apart Are The Freeway Exits? | Fractions on a Number Line and Subtracting Fractions | 3.NF. 2 | 3.NF.2b | 4.NF. 2 | 4.NF.3a | 4.NF.3c | 4.NF.3d | 5.NF. |
| 34 | Do We Have Enough Paint? | Area | 3.MD. 5 | 3.MD. 6 | 3.MD. 7 |  |  |  |  |

$+\equiv$ Sheet1 -

## Scary \& Dangerous

## WHAT DO WE KNOW

## ABOUT EDUCATION?

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