

**MATH MODELING CAN**

**MAKE YOU FILTHY RICH**

**ROBERT KAPLINSKY**

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[robertkaplinsky.com](http://robertkaplinsky.com)

[@robertkaplinsky](https://www.instagram.com/robertkaplinsky)





## Real-World Link



Common Core  
State Standards

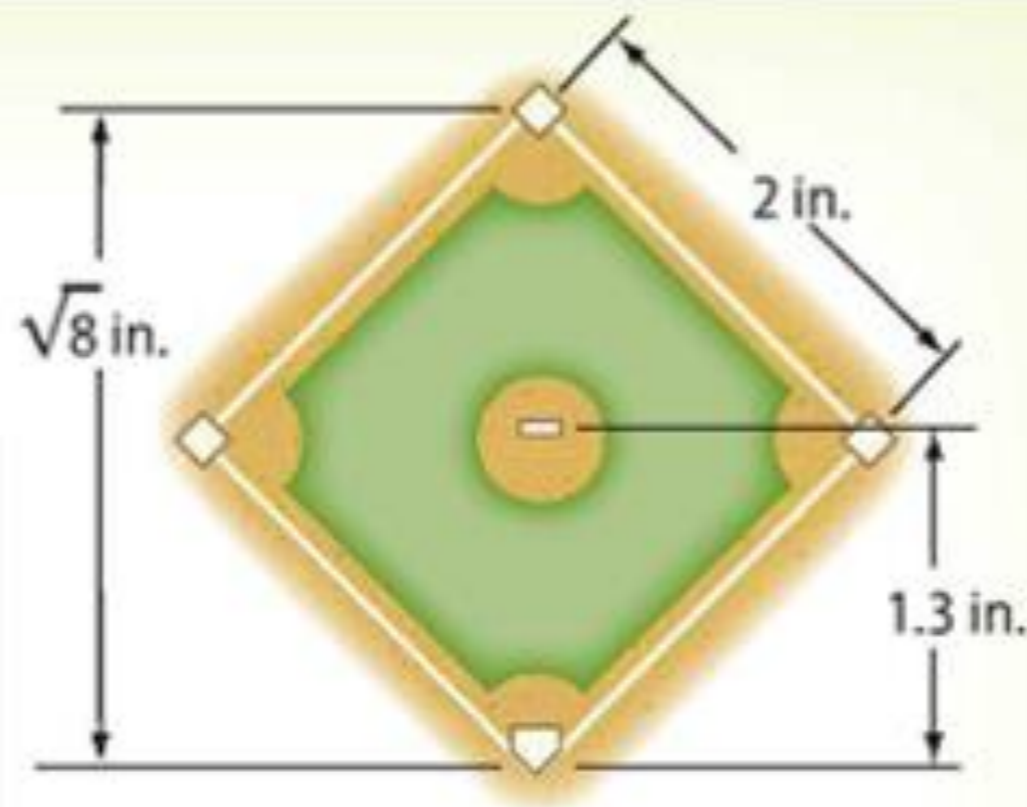
### Content Standards

8.NS.1, 8.NS.2, 8.EE.2

### Mathematical Practices

1, 3, 4, 6

**Sports** Major League baseball has rules for the dimensions of the baseball diamond. A model of the diamond is shown.



1. On the model, the distance from the pitching mound to home plate is 1.3 inches. Is 1.3 a rational number? Explain.

---

2. On the model, the distance from first base to second base is 2 inches. Is 2 a rational number? Explain.

---

3. The distance from home plate to second base is  $\sqrt{8}$  inches. Using a calculator, find  $\sqrt{8}$ . Does it appear to terminate or repeat?





## Real-World Link



## Common Core State Standards

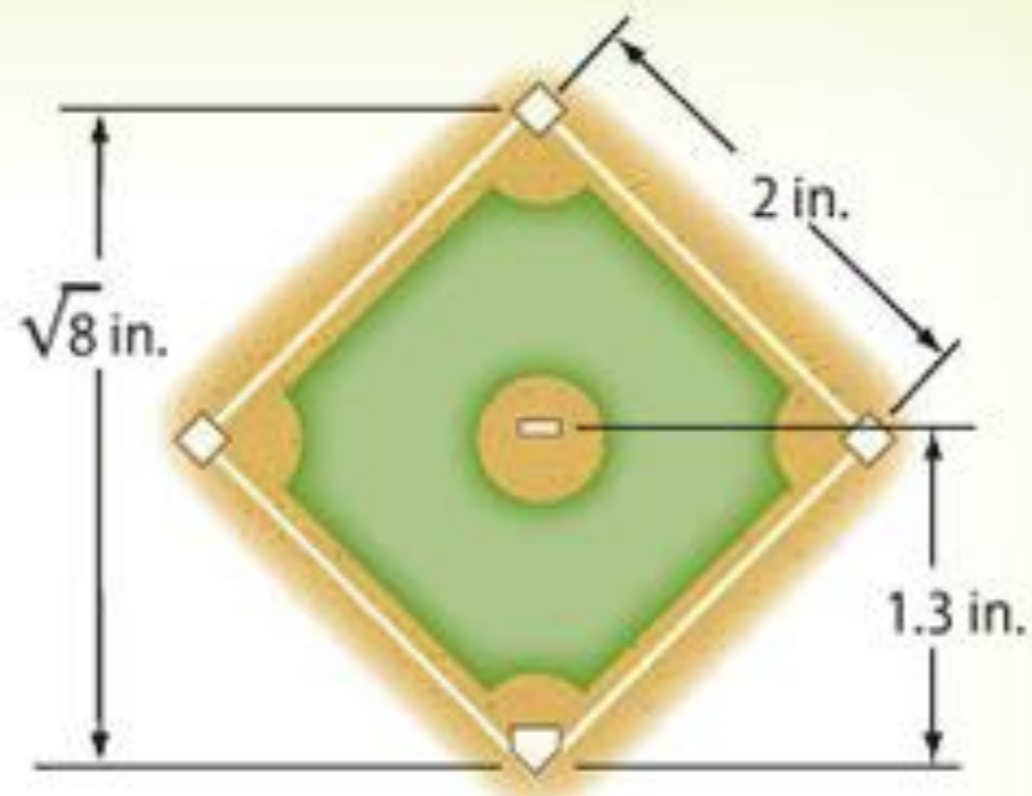
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# Doritos® & Cheetos® Mix **20** Singles

DORITOS® Nacho Cheese Flavored Tortilla Chips 1 OZ. EA. DORITOS® COOL RANCH® Flavored Tortilla Chips 1 OZ. EA. CHEETOS® Puffs Cheese Flavored Snacks 7/8 OZ. EA. CHEETOS® Crunchy Cheese Flavored Snacks 1 OZ. EA.

20 INDIVIDUAL BAGS: 7/8 OZ. EACH, 1 OZ. EACH, TOTAL NET WT. 19 5/8 OZ. (1 LB. 3 5/8 OZ.) 556.3 g ⚠ WARNING: PREVENT ENTANGLEMENT AND STRANGULATION. KEEP THIS BAG AWAY FROM YOUNG CHILDREN. IT IS NOT A TOY.

# THINKING TIME

- Why did many of you expect there to be five of each?
- Why was it not five of each?
- How might they decide on this combination?



# Classic Mix

**20**  
Singles

LAY'S® Classic Potato Chips. DORITOS® Nacho Cheese Flavored Tortilla Chips. DORITOS® COOL RANCH® Flavored Tortilla Chips. CHEETOS® Crunchy Cheese Flavored Snacks. SUNCHIPS® Original Multigrain Snacks. FRITOS® Original Corn Chips (All 1 OZ. Each)

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# GOALS

HOW DO WE MAKE SENSE OF MATH MODELING?

IS IT JUST ANSWERING QUESTIONS?

HOW DO YOU PROFIT FROM MATH MODELING?

HOW DO WE HELP OUR STUDENTS IMPROVE?

WHERE CAN WE FIND MORE RESOURCES?









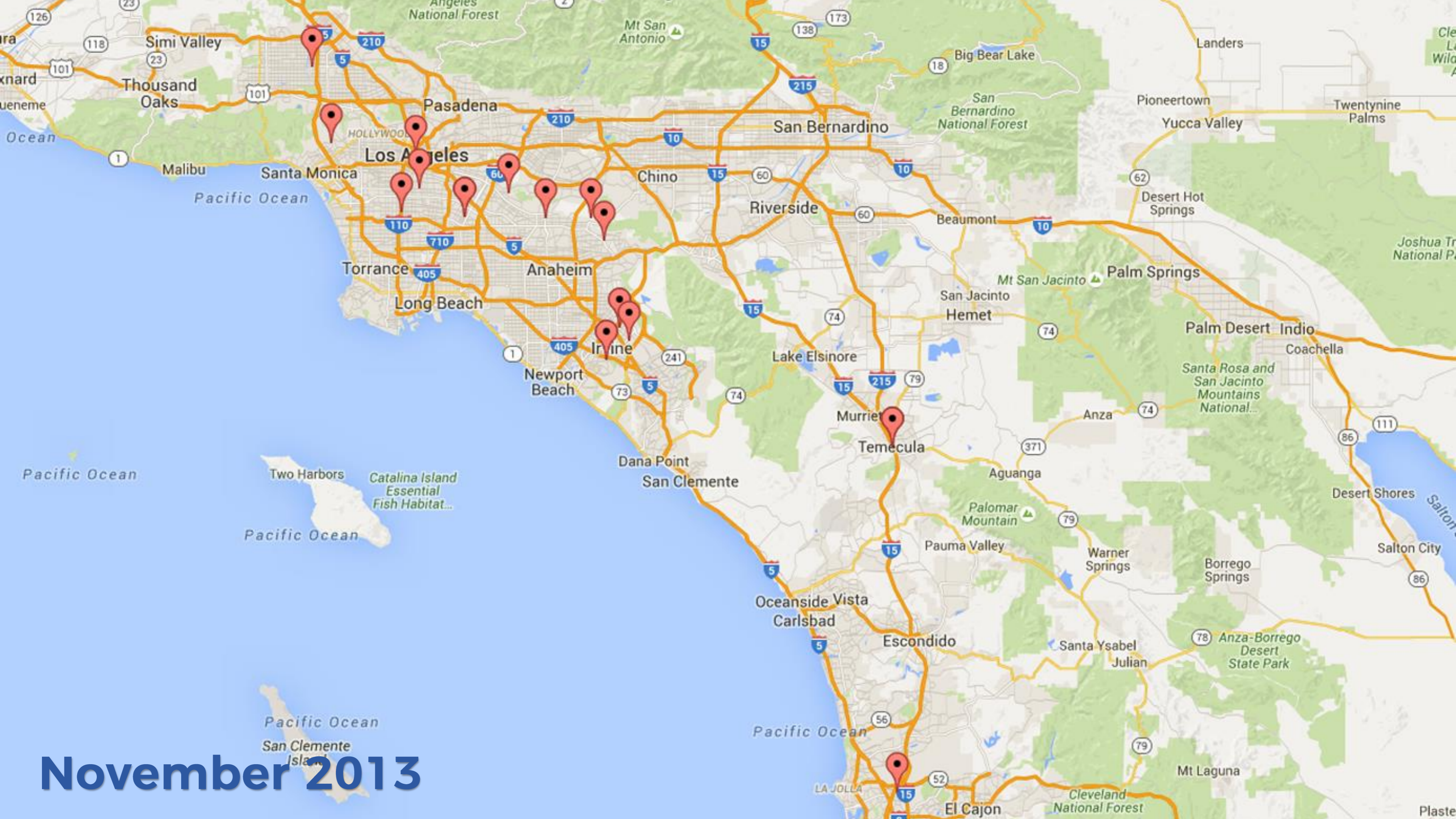




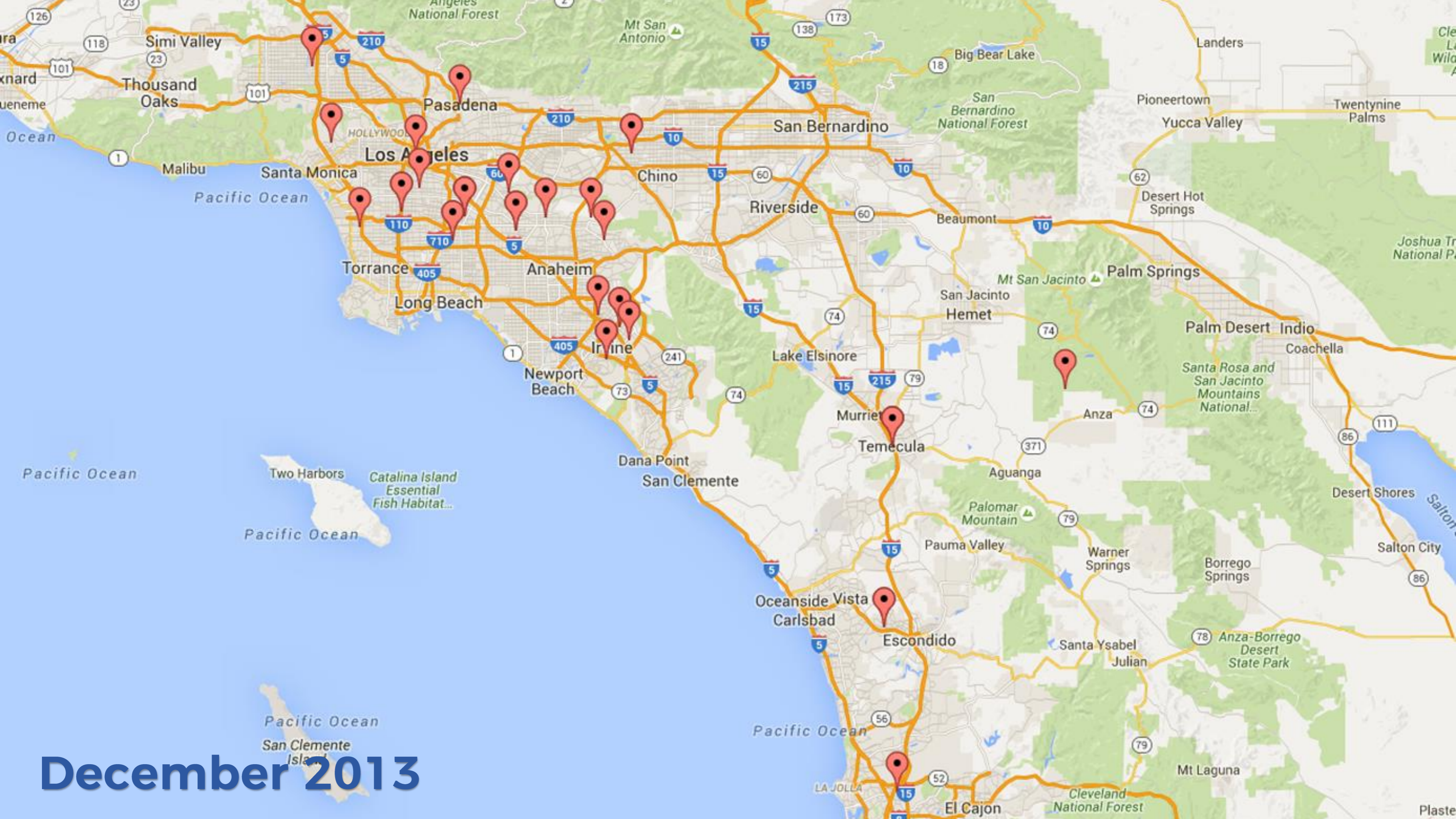
**Spies**

**Analysts**

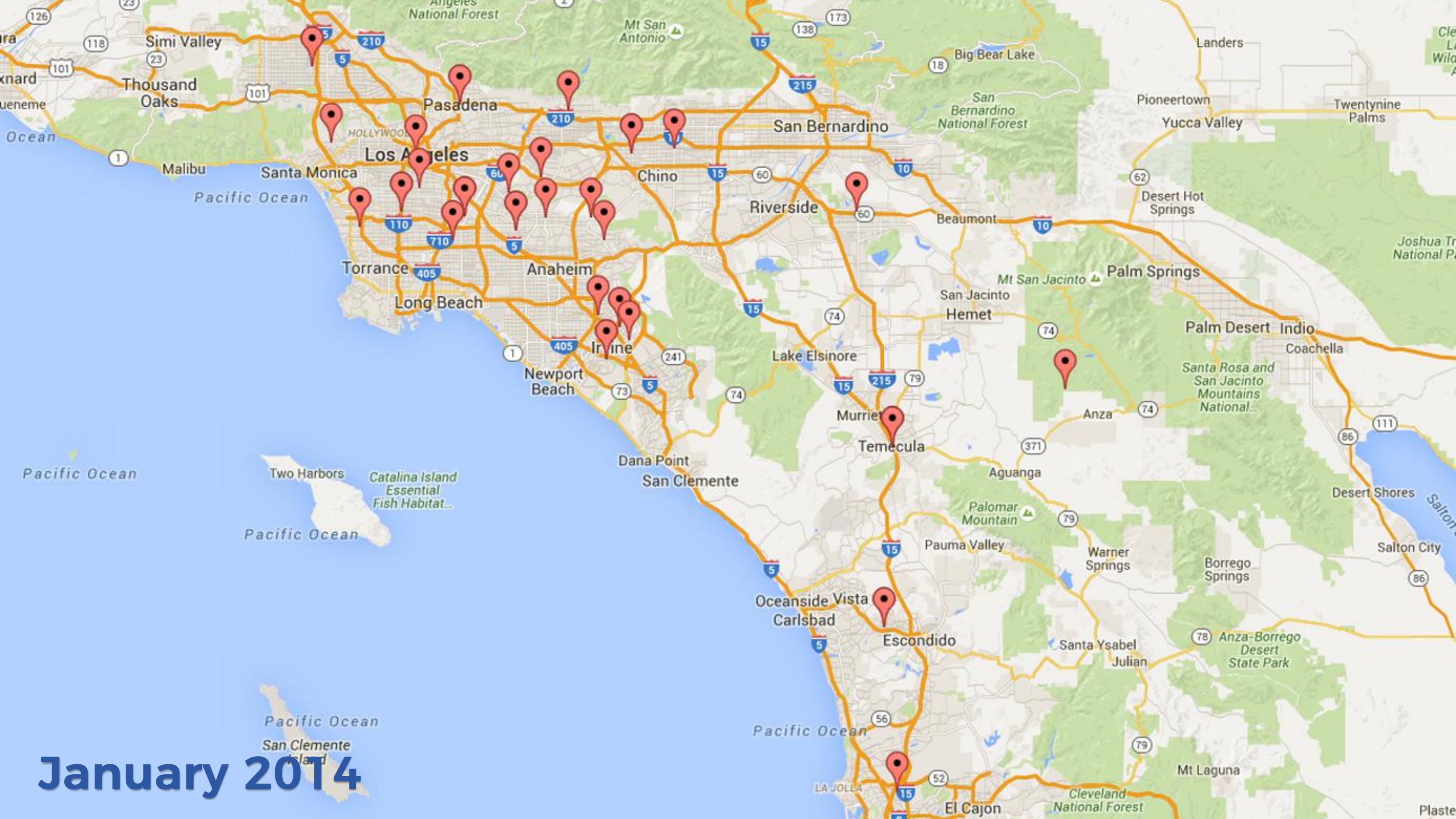
**Model**



November 2013

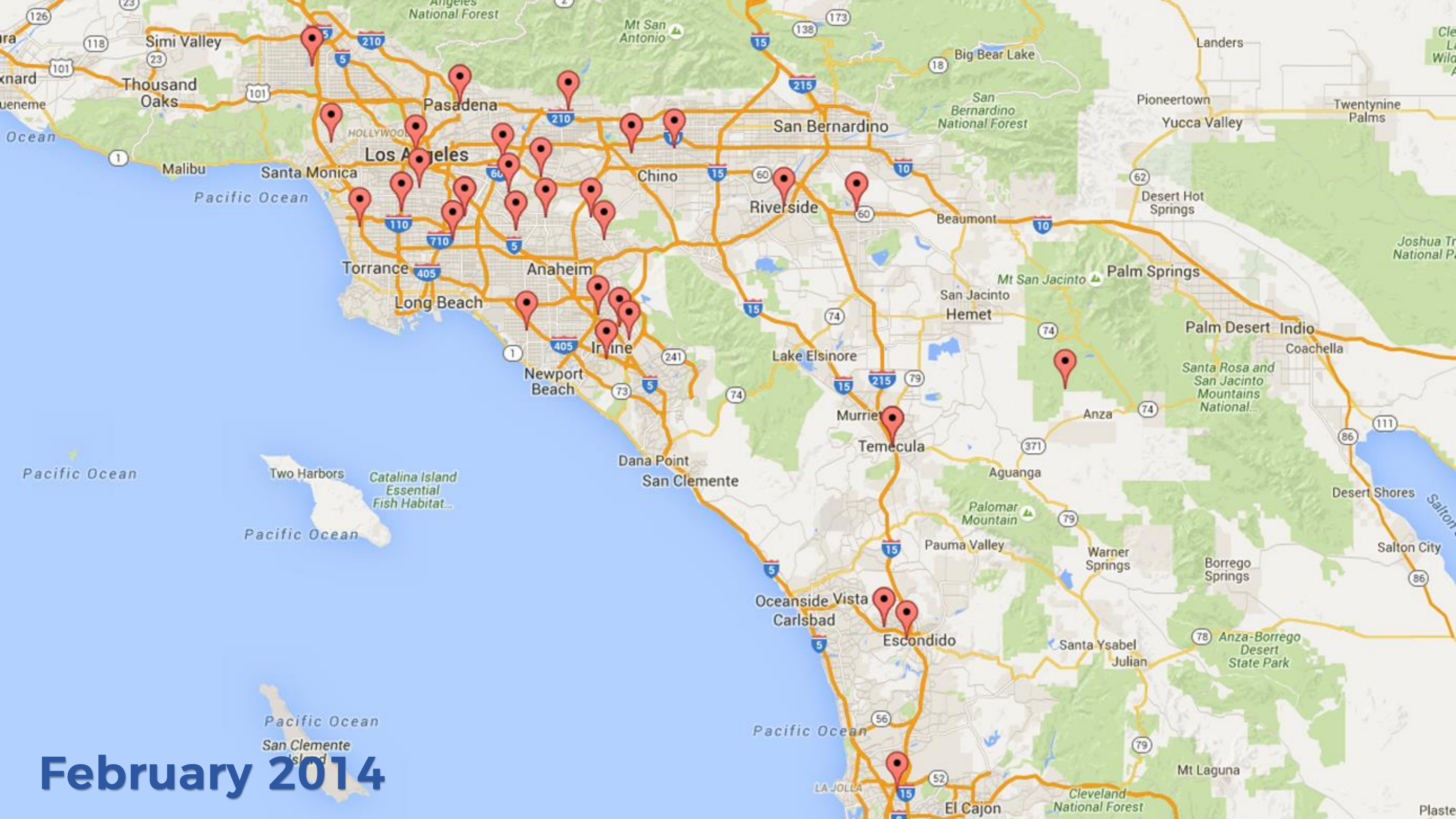


December 2013

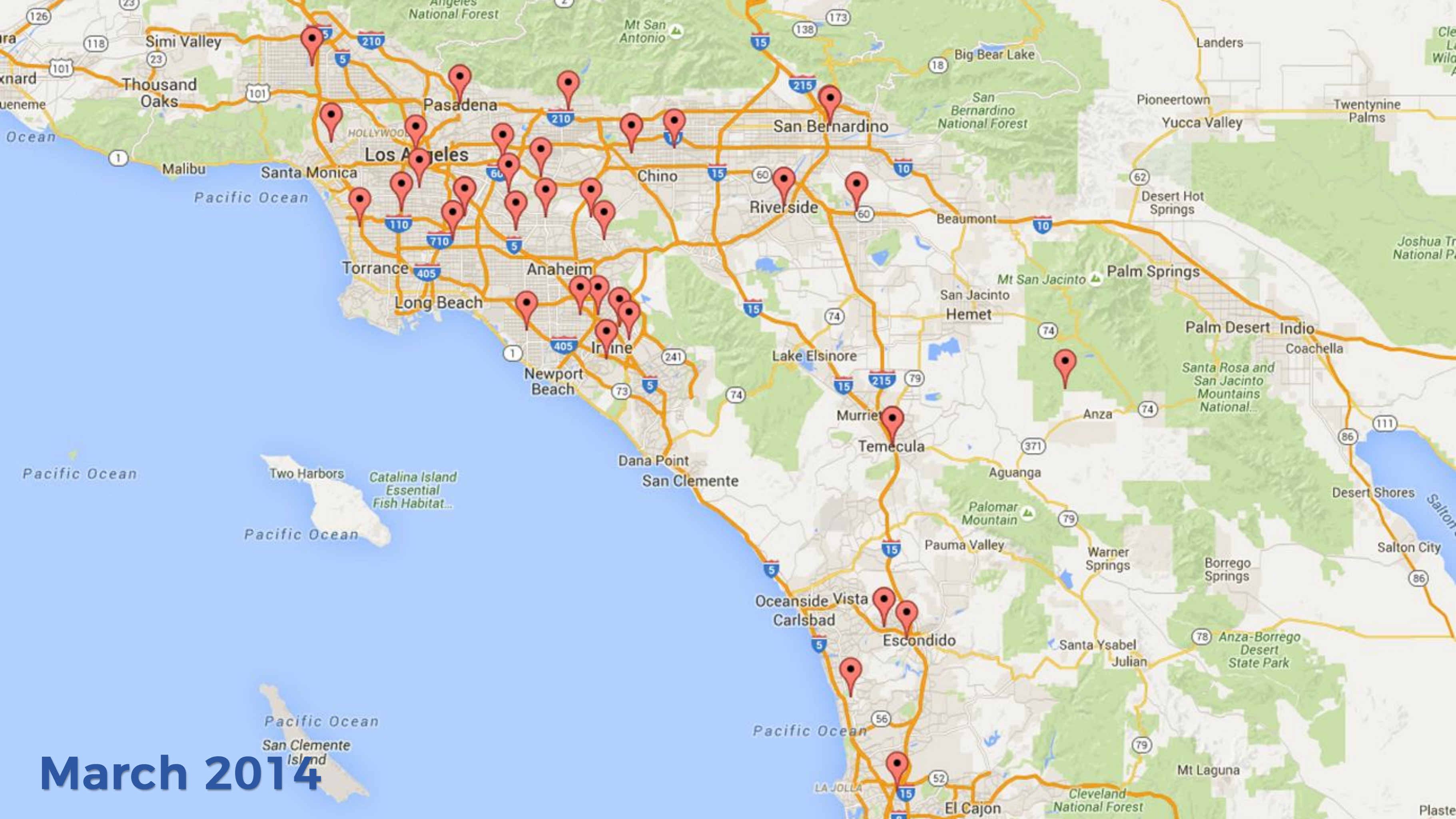


January 2014

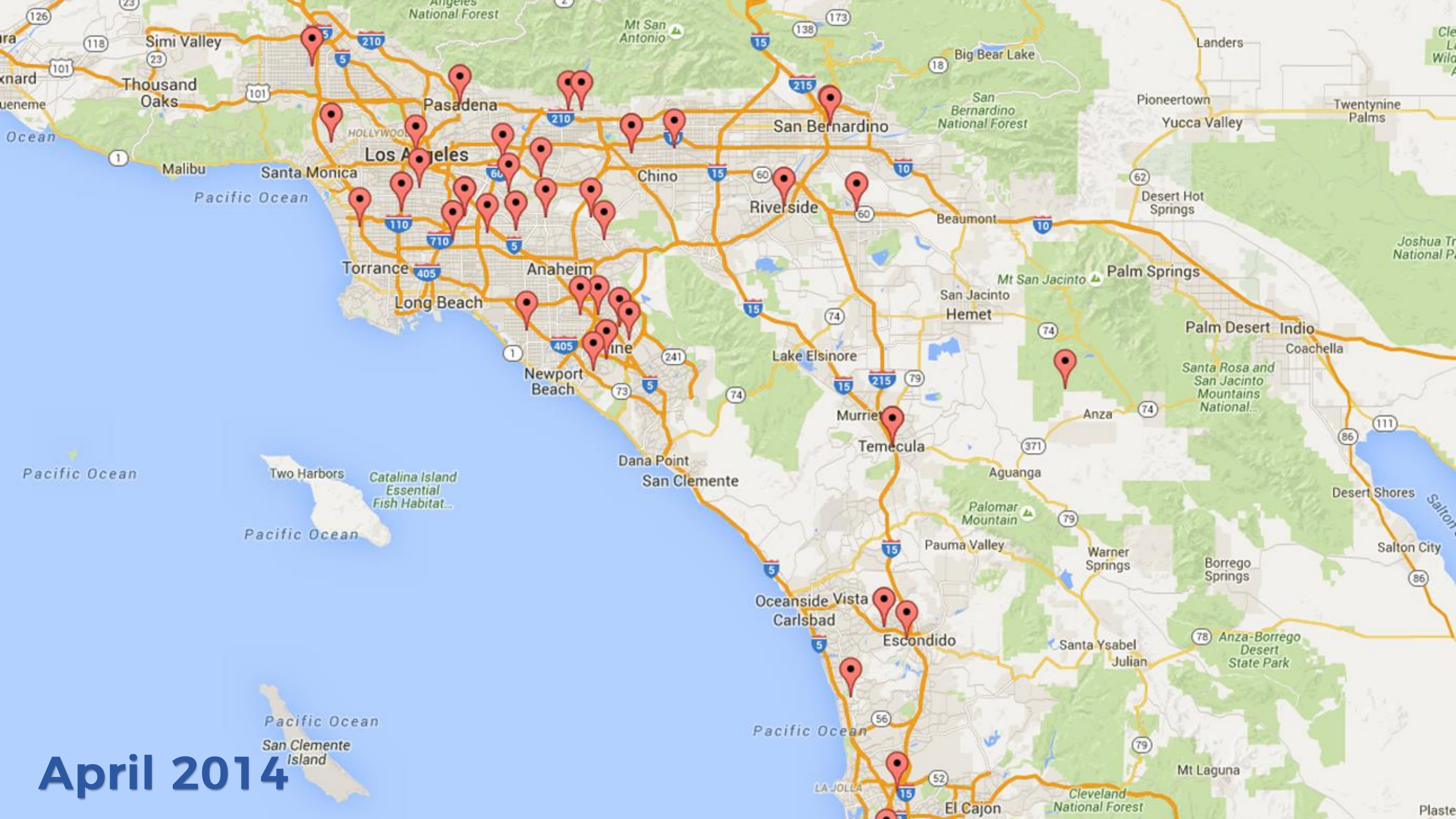




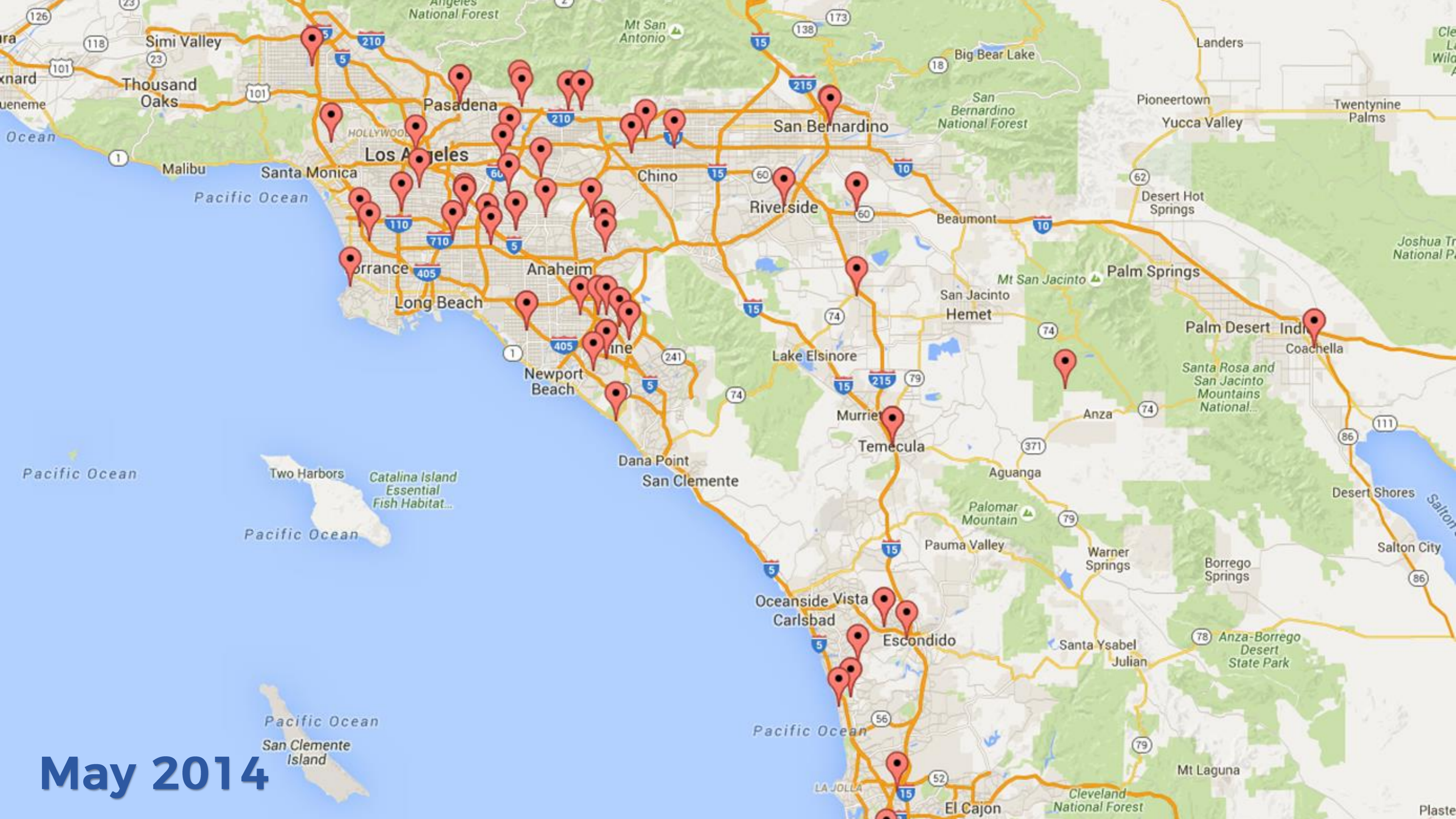
February 2014



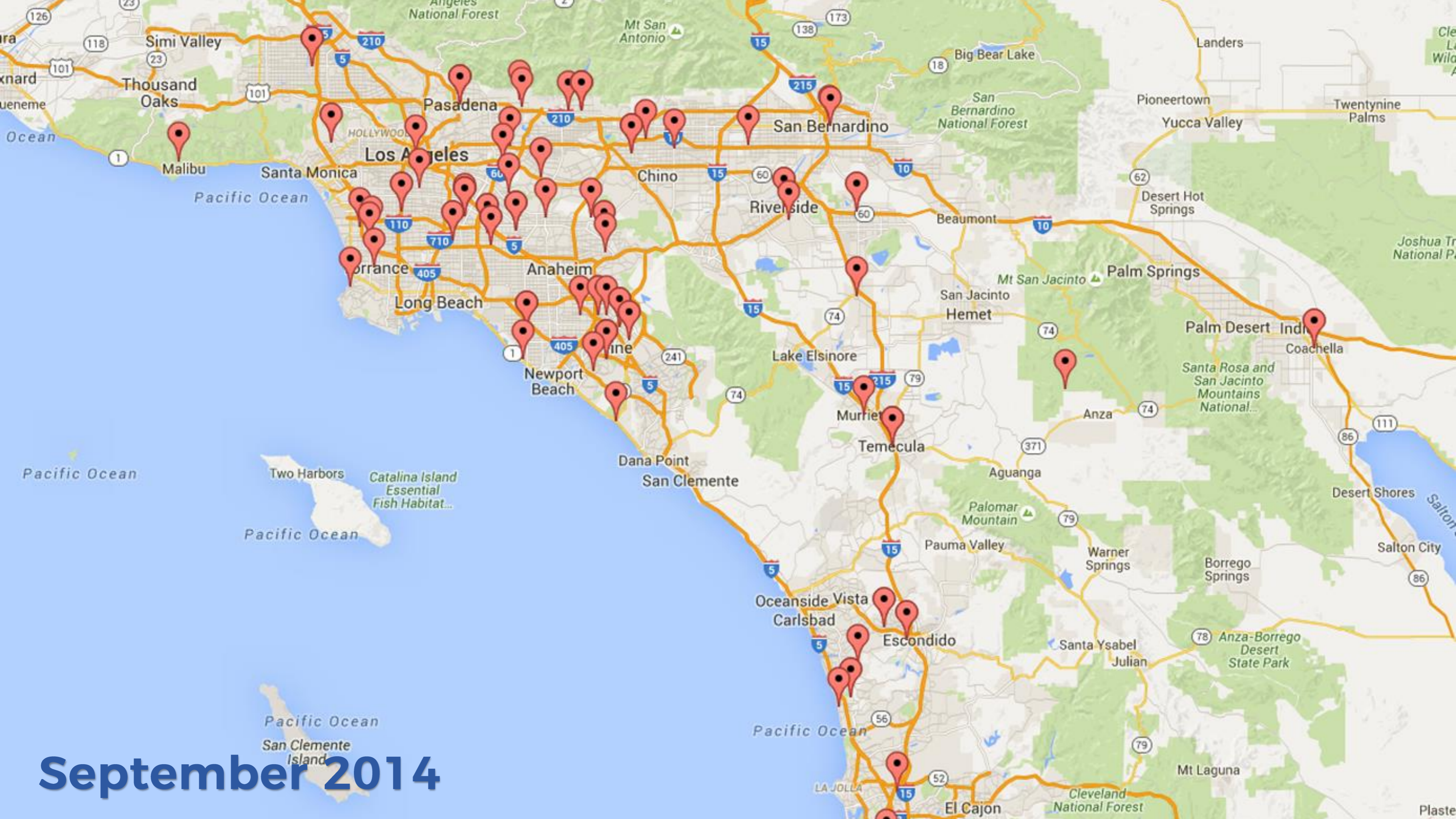
March 2014



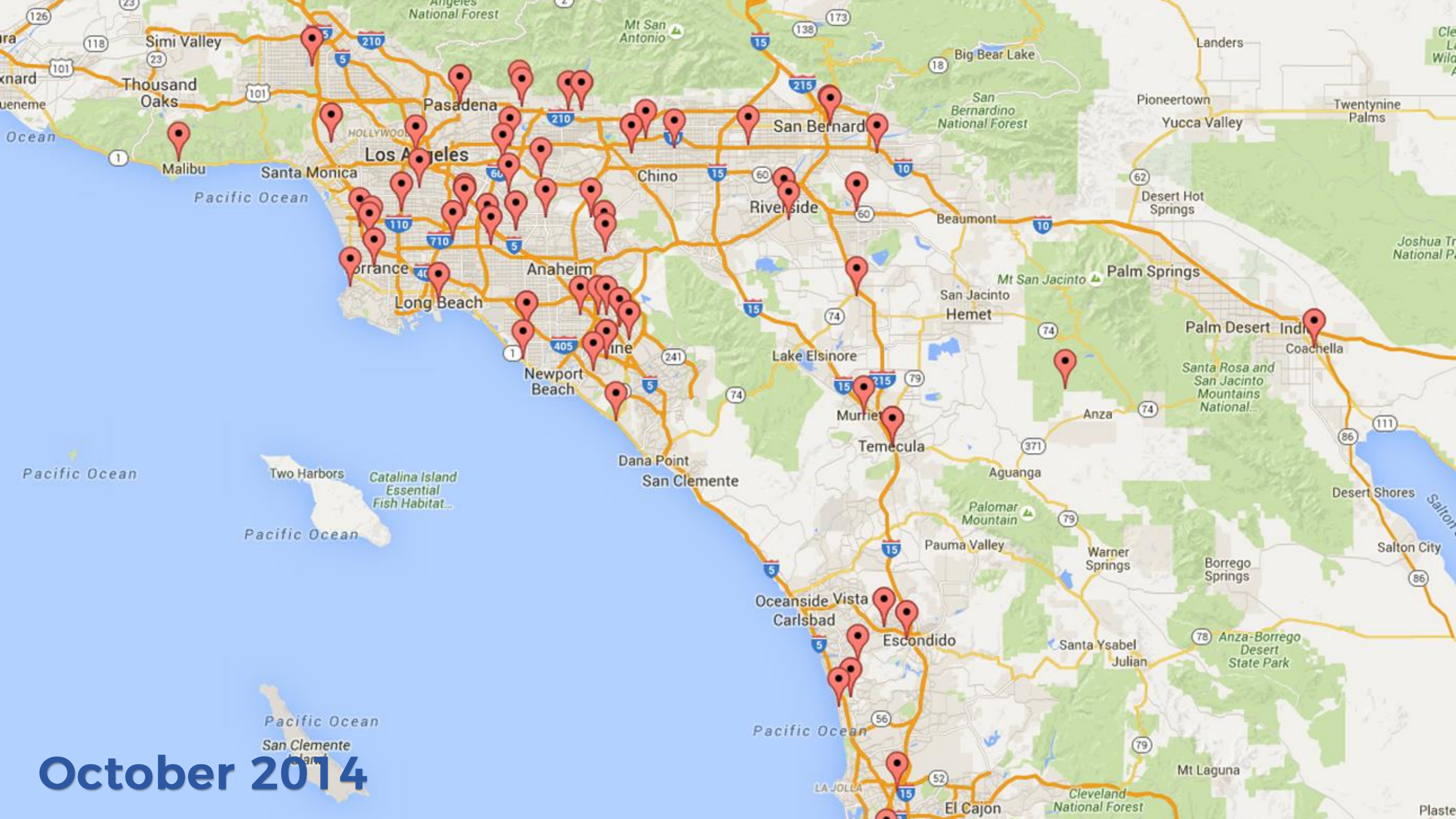
April 2014



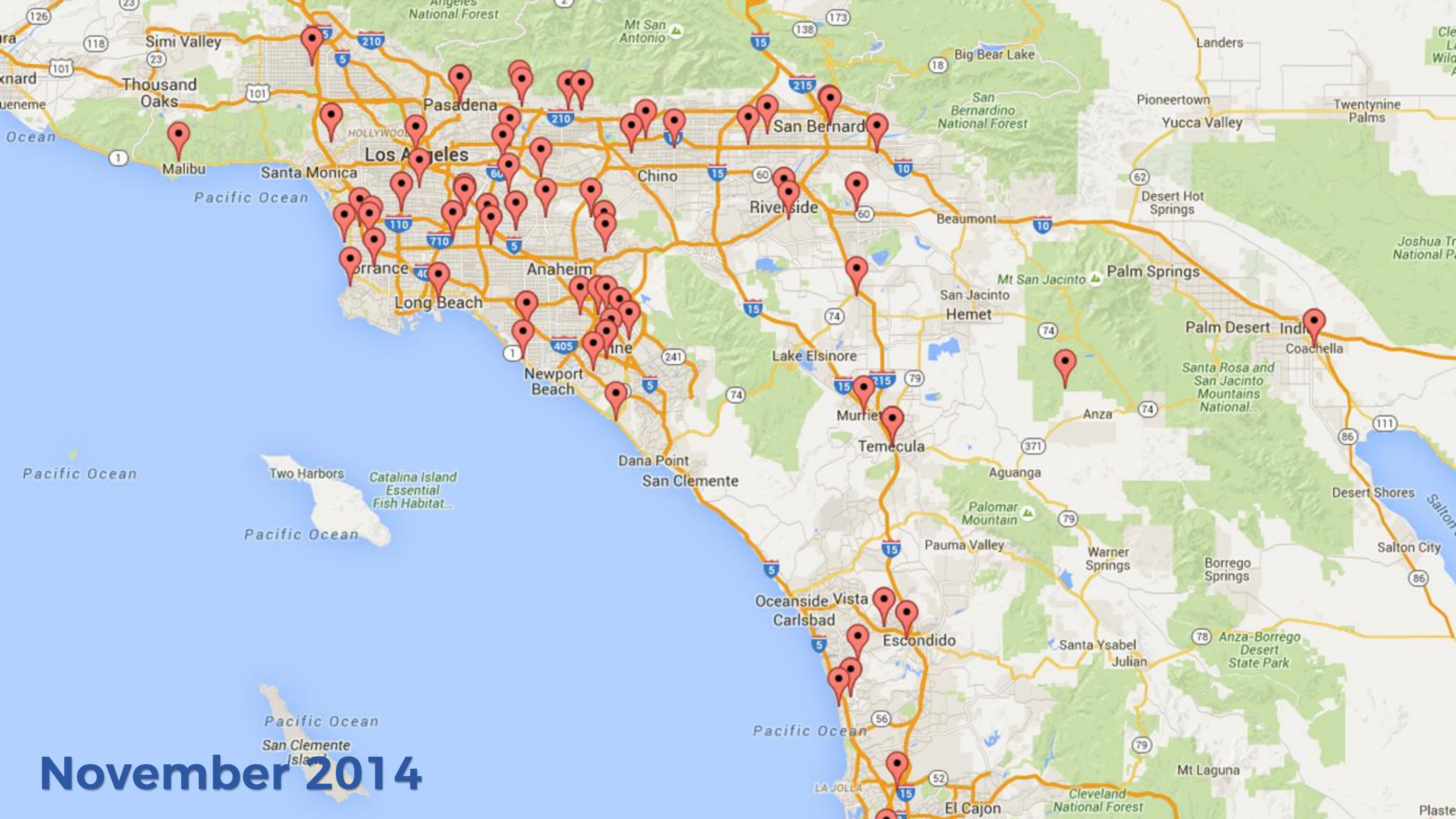
May 2014



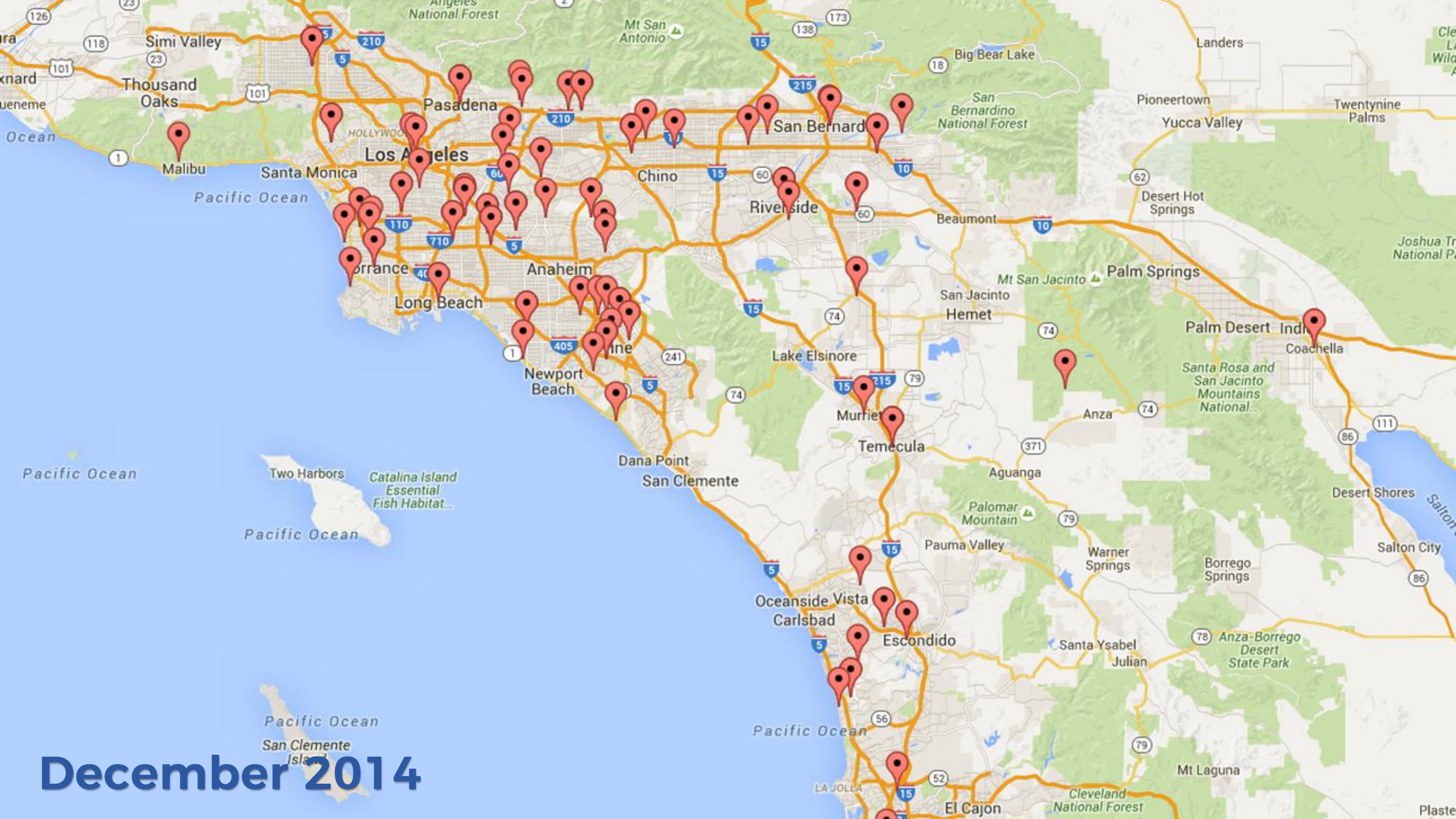
September 2014



October 2014



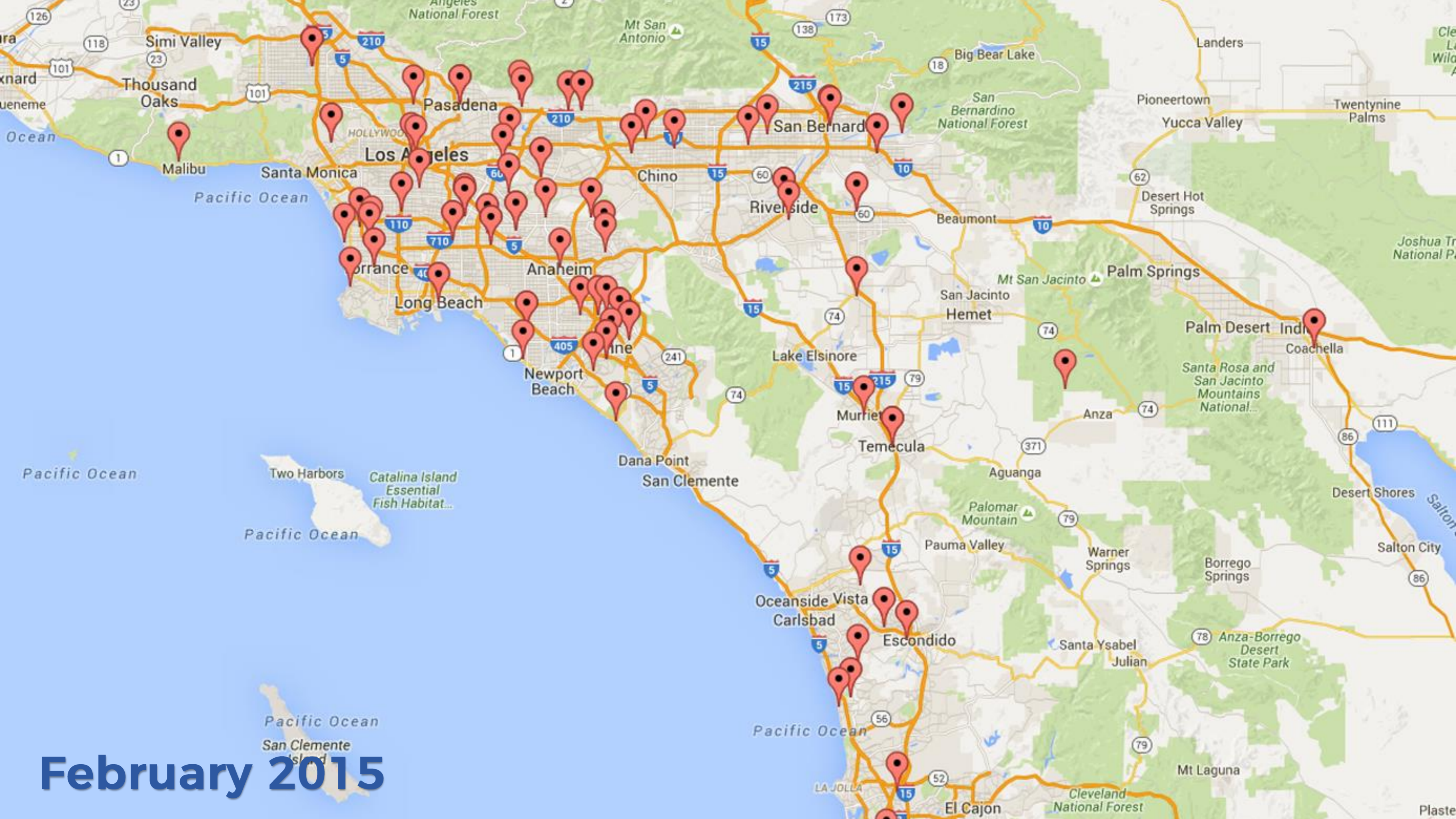
November 2014



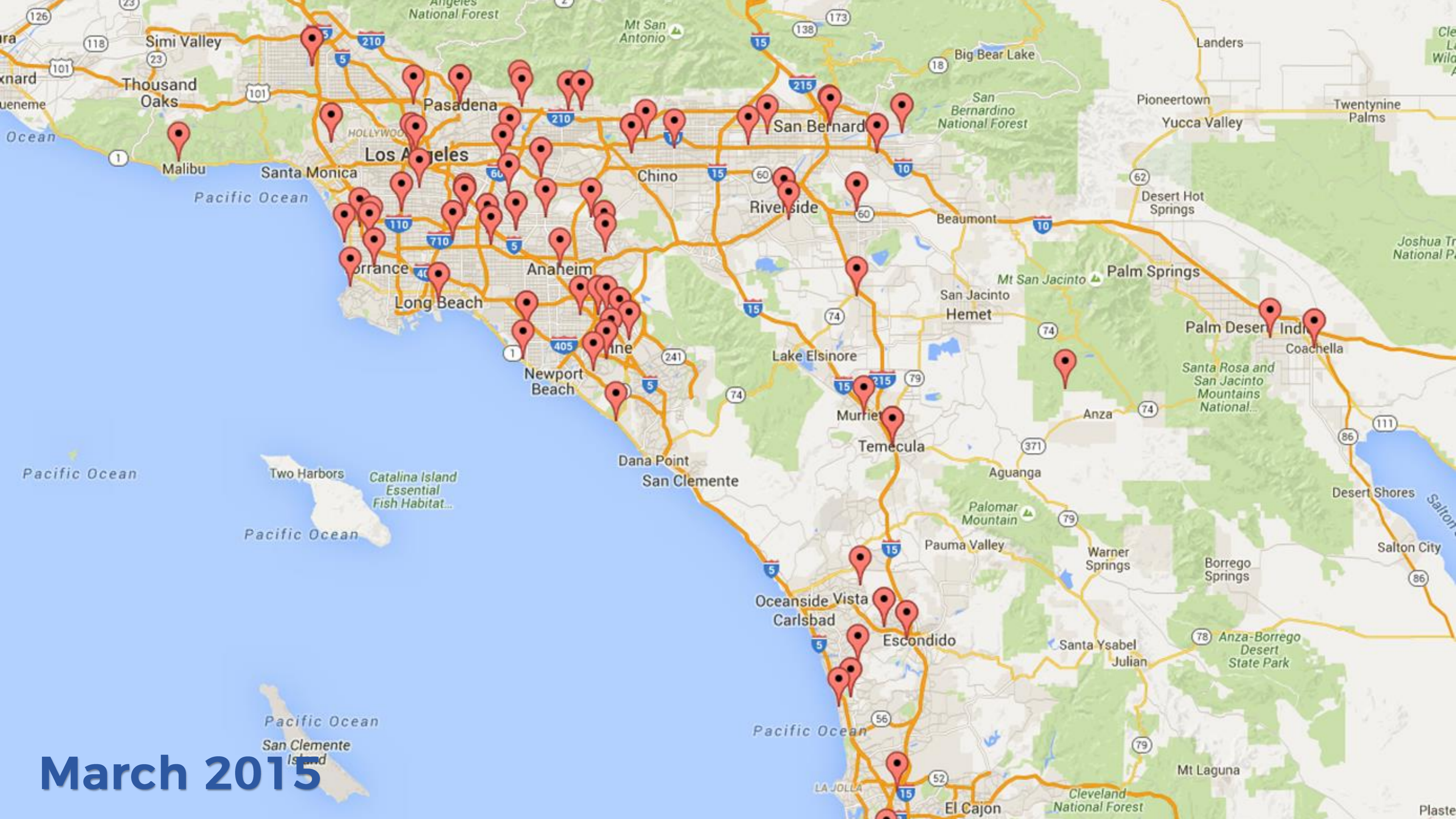
December 2014



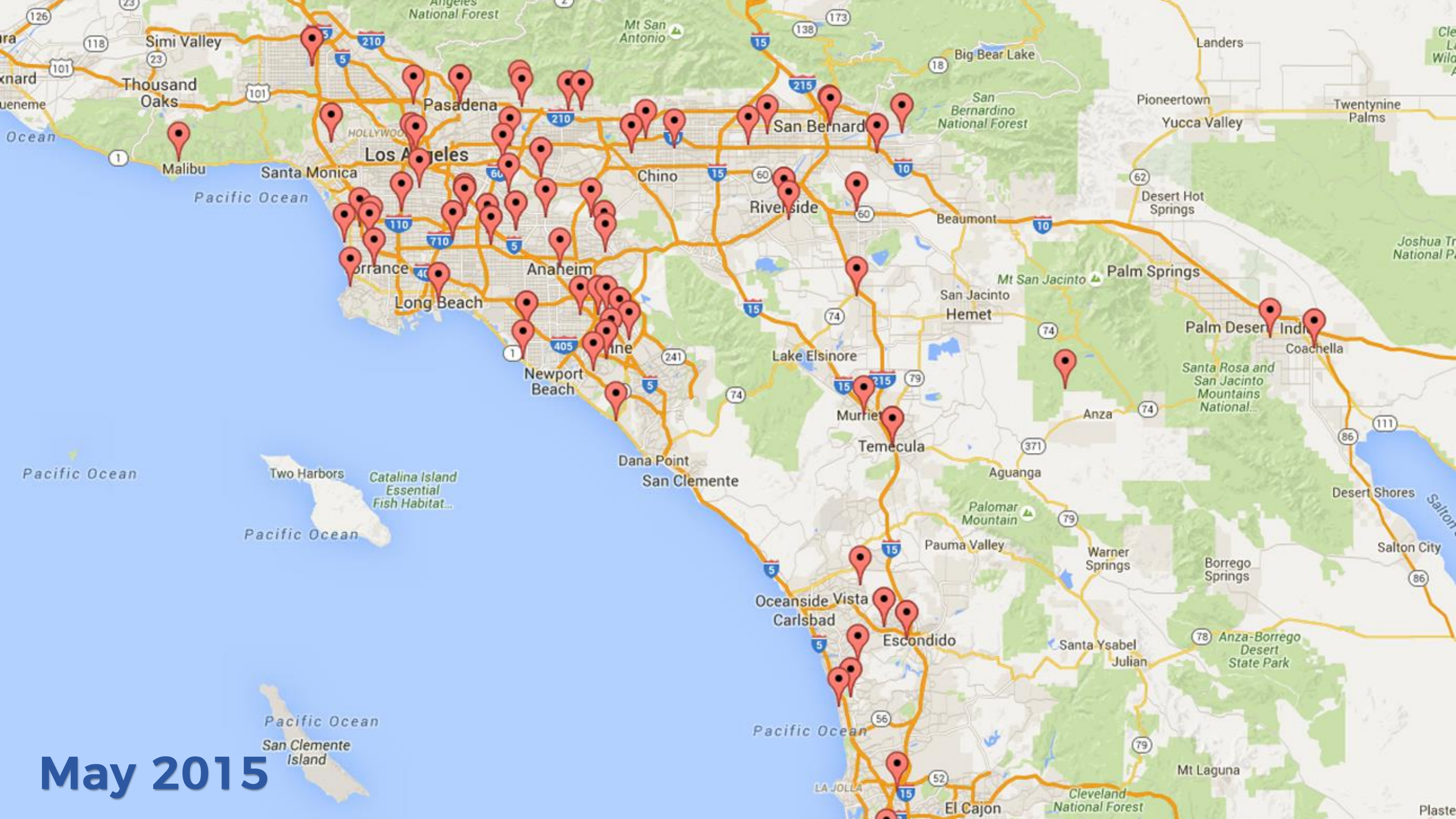




February 2015



March 2015

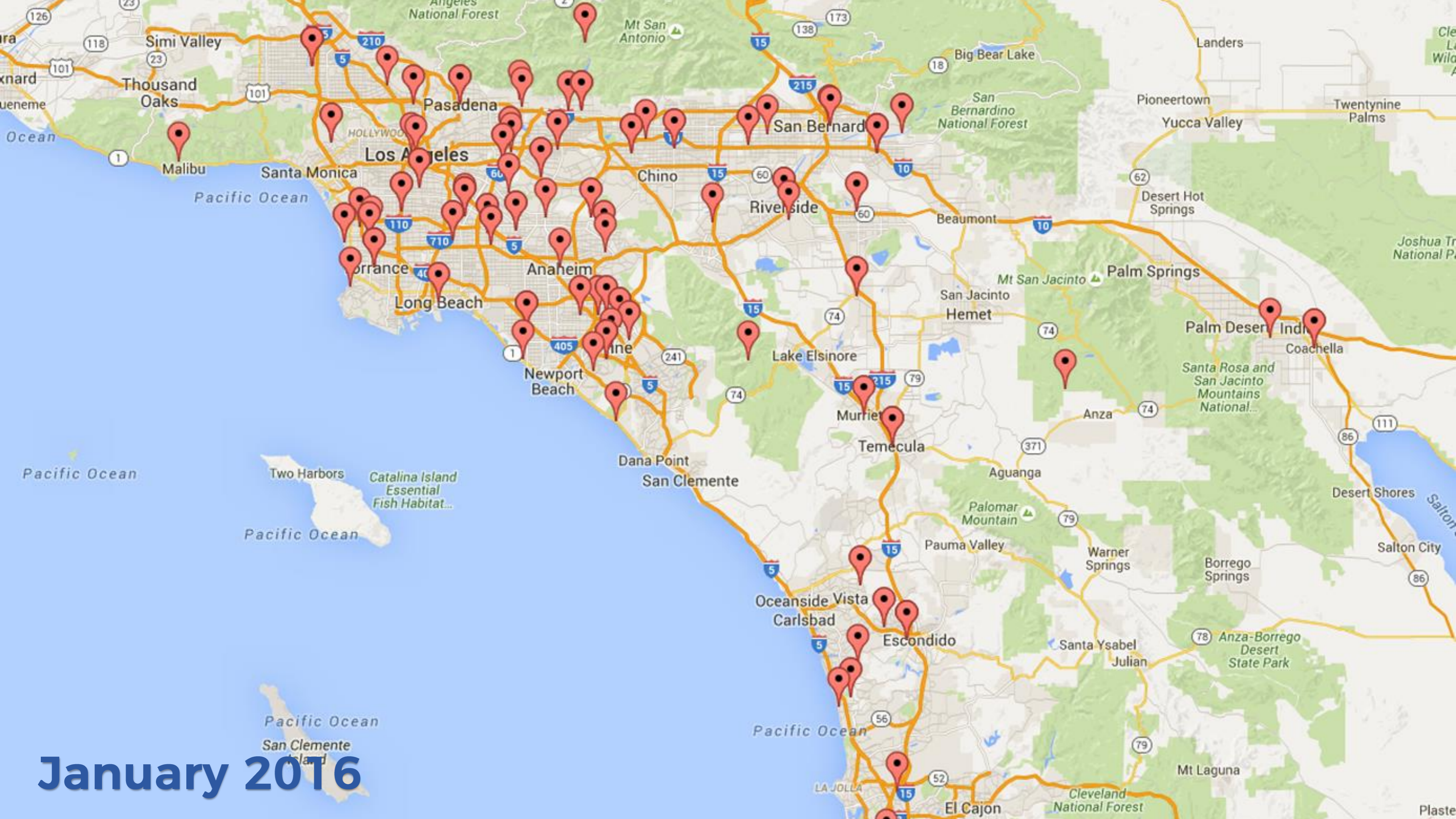


May 2015









January 2016






**Spies**

**Analysts**

**Model**



All models are  
wrong, but some  
are useful.

**GEORGE E. P. BOX**



# Classic Mix

**20**  
Singles

LAY'S® Classic Potato Chips, DORITOS® Nacho Cheese Flavored Tortilla Chips, DORITOS® COOL RANCH® Flavored Tortilla Chips, CHEETOS® Crunchy Cheese Flavored Snacks, SUNCHIPS® Original Multigrain Snacks, FRITOS® Original Corn Chips (All 1 OZ. Each)

20 INDIVIDUAL BAGS: 1 OZ. EACH, TOTAL NET WT. 20 OZ. (1 LB. 4 OZ.) 567 g

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**Spies**

**Analysts**

**Model**

# THINKING TIME

EASY TO STORE.



Classic Mix **20**  
Singles

4 LAY'S® Classic Potato Chips, 4 DORITOS® Nacho Cheese Flavored Tortilla Chips, 2 DORITOS® COOL RANCH® Flavored Tortilla Chips, 4 CHEETOS® Crunchy Cheese Flavored Snacks, 2 SUNCHIPS® Original Multigrain Snacks, 4 FRITOS® Original Corn Chips (All 1 OZ. Each)  
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**Robert Kaplinsky**

@robertkaplinsky



Hey #MTBoS, can you do me a favor and complete this 3 question anonymous survey about your favorite chips? I need data for a presentation. Please RT.

[goo.gl/forms/etPtujll...](https://goo.gl/forms/etPtujll...) #iteachmath



**Favorite Chips**

Please complete this anonymous survey. I'll be using this data in a presentation.

[docs.google.com](https://docs.google.com)

8:05 PM - 4 Feb 2018

**63** Retweets **45** Likes



18

63

45



# Favorite Chips (Responses)

File Edit View Insert Format Data Tools Form Add-ons Help

Comments

Share

100%
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Arial
10
**B** *I* ~~U~~ A



...

*fx* Timestamp

|    | A                 | B              | C                      | D                    | E                 | F                    | G                 | H                  |
|----|-------------------|----------------|------------------------|----------------------|-------------------|----------------------|-------------------|--------------------|
| 1  | Timestamp         | Lays (Classic) | Doritos (Nacho Cheese) | Doritos (Cool Ranch) | Cheetos (Crunchy) | Sun Chips (Original) | Fritos (Original) | Time Zone          |
| 2  | 2/4/2018 20:06:53 | 6              | 5                      | 4                    | 2                 | 3                    | 1                 | Central Time Zone  |
| 3  | 2/4/2018 20:06:55 | 1              | 5                      | 6                    | 3                 | 2                    | 4                 | Eastern Time Zone  |
| 4  | 2/4/2018 20:06:56 | 5              | 2                      | 1                    | 3                 | 6                    | 4                 | Central Time Zone  |
| 5  | 2/4/2018 20:06:57 | 2              | 1                      | 6                    | 3                 | 5                    | 4                 | Pacific Time Zone  |
| 6  | 2/4/2018 20:07:36 | 4              | 1                      | 2                    | 3                 | 5                    | 6                 | Pacific Time Zone  |
| 7  | 2/4/2018 20:08:02 | 5              | 1                      | 6                    | 4                 | 2                    | 3                 | Pacific Time Zone  |
| 8  | 2/4/2018 20:08:05 | 6              | 2                      | 4                    | 3                 | 5                    | 1                 | Pacific Time Zone  |
| 9  | 2/4/2018 20:08:07 | 4              | 2                      | 1                    | 5                 | 3                    | 6                 | Pacific Time Zone  |
| 10 | 2/4/2018 20:08:29 | 5              | 3                      | 4                    | 1                 | 6                    | 2                 | Central Time Zone  |
| 11 | 2/4/2018 20:08:56 | 4              | 5                      | 6                    | 1                 | 2                    | 3                 | Central Time Zone  |
| 12 | 2/4/2018 20:09:54 | 5              | 6                      | 5                    | 6                 | 5                    | 4                 | Pacific Time Zone  |
| 13 | 2/4/2018 20:10:01 | 4              | 2                      | 3                    | 1                 | 5                    | 6                 | Pacific Time Zone  |
| 14 | 2/4/2018 20:10:04 | 6              | 2                      | 3                    | 1                 | 5                    | 4                 | Central Time Zone  |
| 15 | 2/4/2018 20:10:04 | 3              | 5                      | 6                    | 1                 | 4                    | 2                 | Central Time Zone  |
| 16 | 2/4/2018 20:10:05 | 4              | 2                      | 6                    | 1                 | 3                    | 5                 | Eastern Time Zone  |
| 17 | 2/4/2018 20:10:06 | 3              | 2                      | 6                    | 5                 | 1                    | 2                 | Pacific Time Zone  |
| 18 | 2/4/2018 20:10:10 | 4              | 2                      | 6                    | 3                 | 5                    | 1                 | Mountain Time Zone |
| 19 | 2/4/2018 20:10:12 | 3              | 1                      | 5                    | 6                 | 2                    | 4                 | Eastern Time Zone  |
| 20 | 2/4/2018 20:10:26 | 5              | 3                      | 6                    | 2                 | 4                    | 1                 | Pacific Time Zone  |

+ ≡ Sheet3

Explore



# THINKING TIME

- The available data includes:
  - Lays, Nacho Cheese Doritos, Cool Ranch Doritos, Cheetos, Sun Chips, and Fritos ranked from 1 to 6
  - Geographic region: West, Central, or Eastern

# ANALYSTS' JOB FOR THE TOP 1

1. **Count** all the first place votes for each chip type.
2. **Divide** the total first place votes for each chip type by the total number of votes.
3. **Multiply that fraction** by 20 to find how many bags there would be in a twenty pack, **rounding** as necessary.

# ANALYSTS' EXAMPLE

|  |  |  |  |  |  |  |
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# ANALYSTS' JOB FOR THE TOP 4

1. **Count** all the first, second, third, and fourth place votes for each chip type.
2. **Multiply** the first place votes by four, the second place votes by three, the third place votes by two, and the fourth place votes by one.
3. **Add** the weighted votes for each chip type and **divide** by the total number of weighted votes.
4. **Divide** the weighted votes for each chip type by the total number of votes.
5. **Multiply that fraction** by 20 to find how many bags there would be in a twenty pack, **rounding** as necessary.

# ANALYSTS' EXAMPLE

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# CHIP BAG RESULTS

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# GOALS

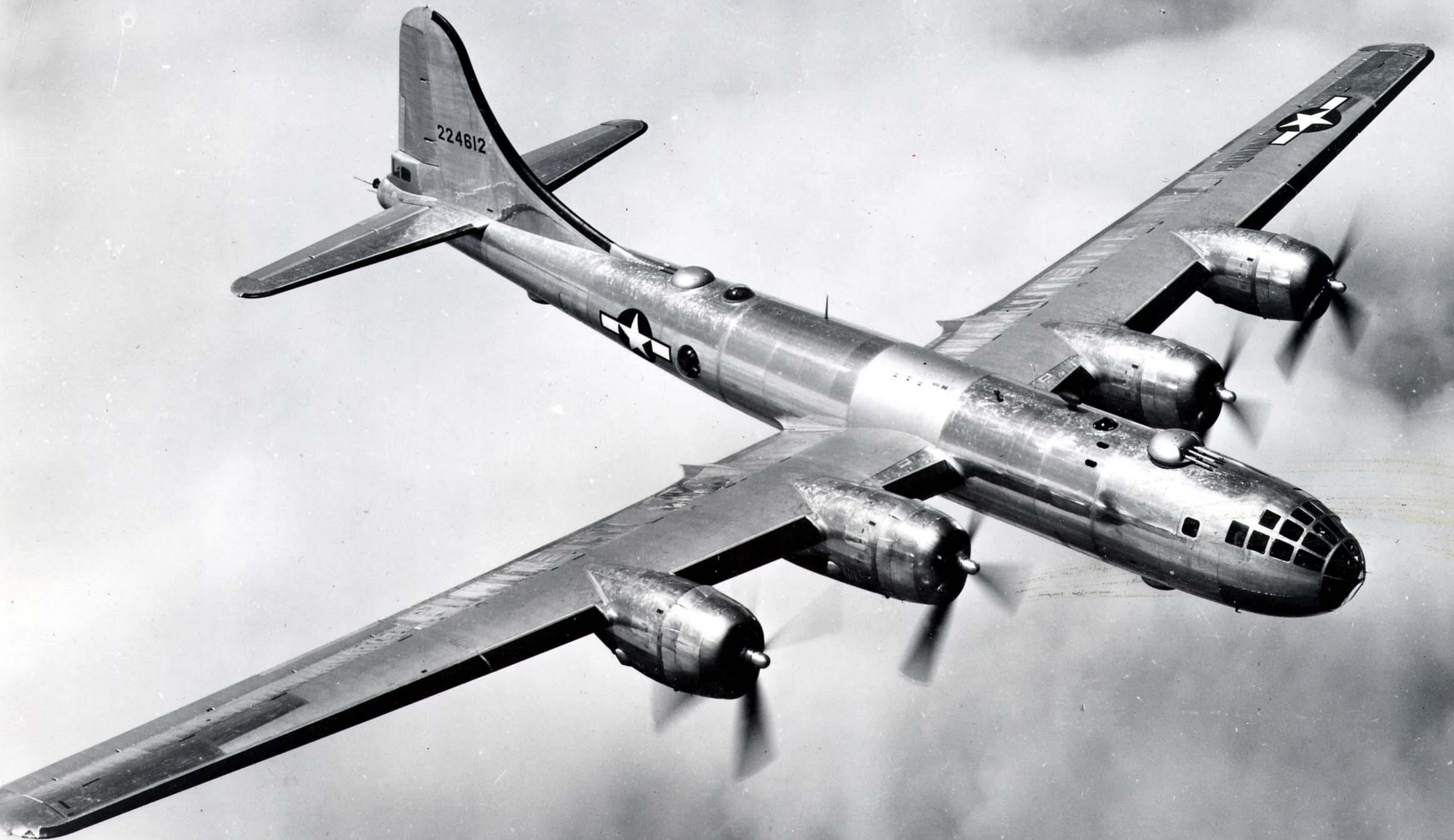
HOW DO WE MAKE SENSE OF MATH MODELING?

IS IT JUST ANSWERING QUESTIONS?

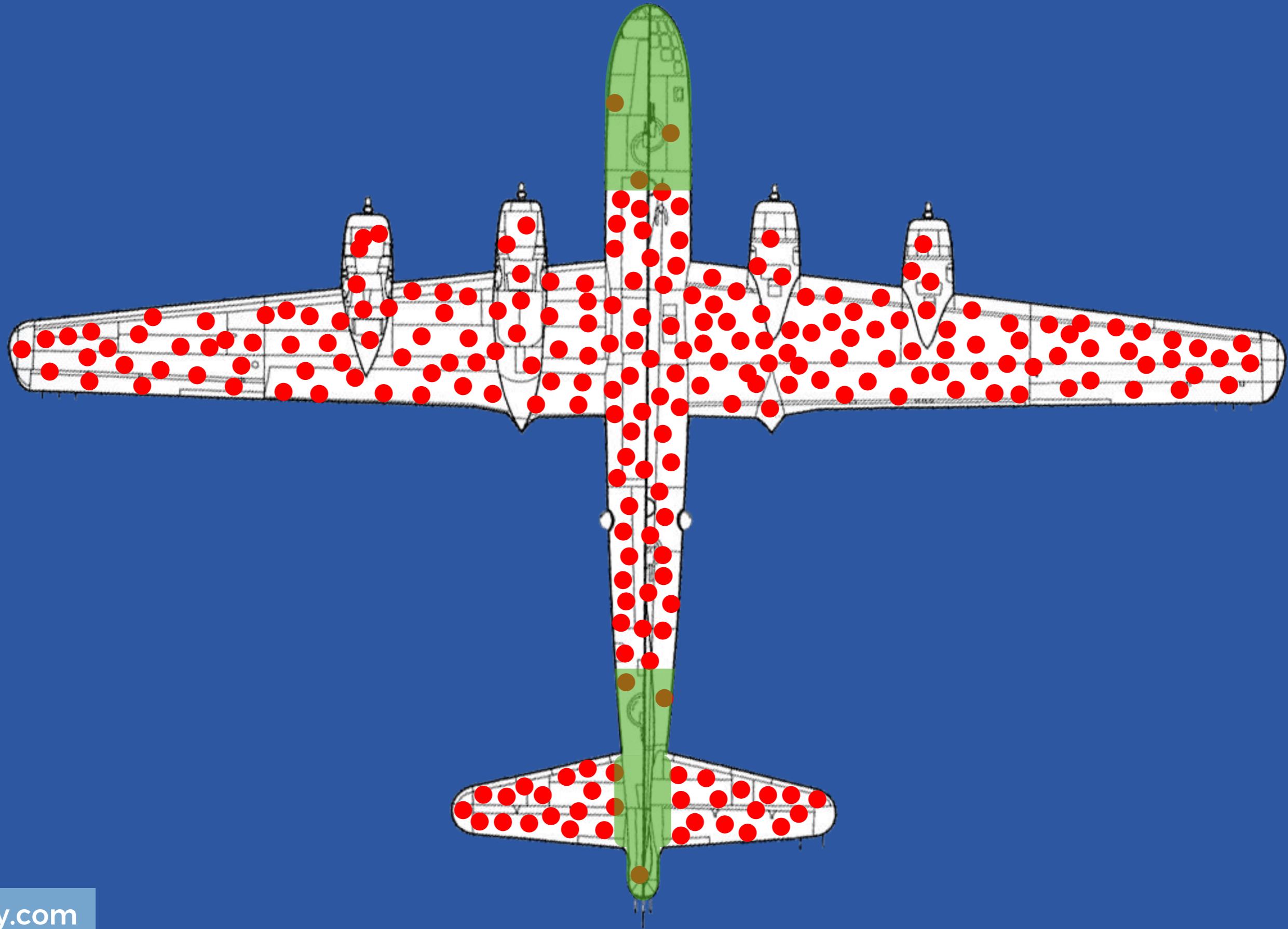
HOW DO YOU PROFIT FROM MATH MODELING?

HOW DO WE HELP OUR STUDENTS IMPROVE?

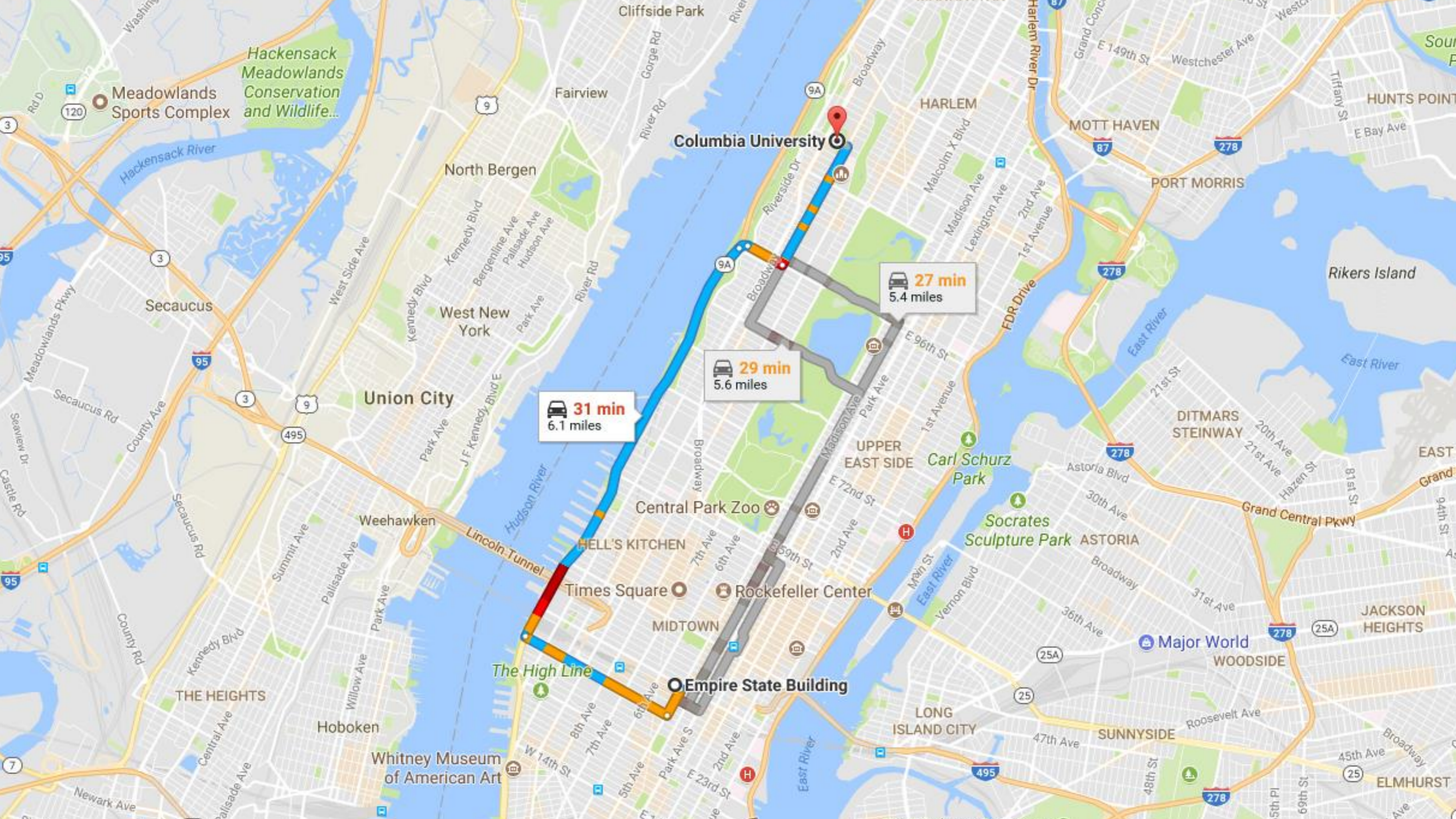
WHERE CAN WE FIND MORE RESOURCES?







- ~~How do we protect our planes?~~
- ~~Which parts of the plane are being hit by the most bullets?~~
- Which parts of the plane are the most critical to protect?



Columbia University

Empire State Building

31 min  
6.1 miles

29 min  
5.6 miles

27 min  
5.4 miles

- ~~How do we find the fastest route for each customer?~~
- How do we find the fastest route for each customer without impacting our other customers?



# Classic Mix

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Singles

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- ~~How many of each flavor should we put in a package?~~
- ~~How many of each flavor should we put in a package for each region?~~
- How can we determine if the extra cost of creating different packages will make us more money?

Mathematically proficient students who can apply what they know are comfortable making assumptions and approximations to simplify a complicated situation, realizing that these may need revision later.

**CCSS MATH PRACTICE 4**

They routinely interpret their mathematical results in the context of the situation and reflect on whether the results make sense, possibly improving the model if it has not served its purpose.

## CCSS MATH PRACTICE 4



# GOALS

HOW DO WE MAKE SENSE OF MATH MODELING?

IS IT JUST ANSWERING QUESTIONS?

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WHERE CAN WE FIND MORE RESOURCES?




TARGET PARKING



**Spies**

**Analysts**

**Model**



**They used 25 products for a pregnancy prediction' score including:**

- **unscented lotion**
- **mineral supplements**
- **cotton balls**

**Source: New York Times**

# ANALYSTS' EXAMPLE

1. Add the number of bottles of unscented lotion, jars of mineral supplements, and bags of cotton balls.
2. Multiply that times the day of the week.
3. Click your heels twice.
4. Repeat the phrase "There's no place like home!"



UNITED



4047

B G →

B →

← G A

A319  
4047

**Spies**

**Analysts**

**Model**

# Priority is determined by:

- passenger's fare class
- itinerary
- frequent flyer program membership
- check-in time

Source: United Airlines





Search



Robert

Home



Robert Kaplinsky

News Feed

Messenger

Watch

Marketplace

Explore

Pages

Events

Groups

Friend Lists

On This Day 3

Insights

Games 7

Fundraisers

Live Video

Pokes

See More...

Create

Ad · Page · Group · Event · Fundraiser

Make Post | Photo/Video Album | Live Video

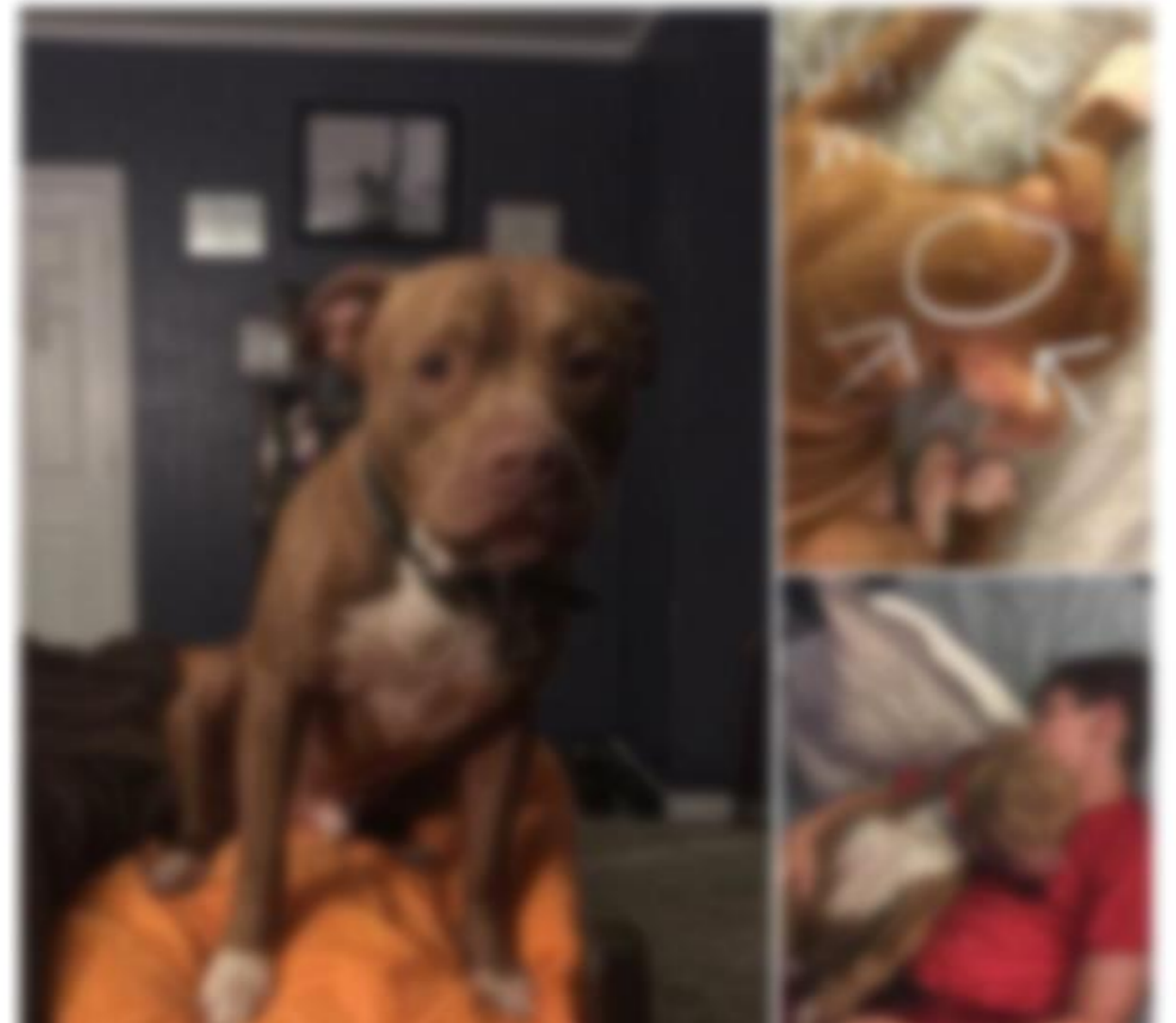
What's on your mind, Robert?

Photo/Video

Feeling/Activity

More options

Ad: Add Schedule...  
Missing this dog gets back to his family



News: New Father... activities in today

Trending

- James Madison: The Dissolution of James and Barbara's Personal Email Server
- Fredericksburg, Virginia: Mother recovering from copperhead snake bite at Virginia Wildlife
- Anthony Weiner: Anthony Weiner Sentenced to 21 Months in Prison

Watchlist: Latest Episodes

- Episode: The Making of a Legend
- Episode: Fall to the Family
- Episode: The Making of a Legend
- Episode: Fall to the Family

See All

Sponsored Create Ad



**Spies**

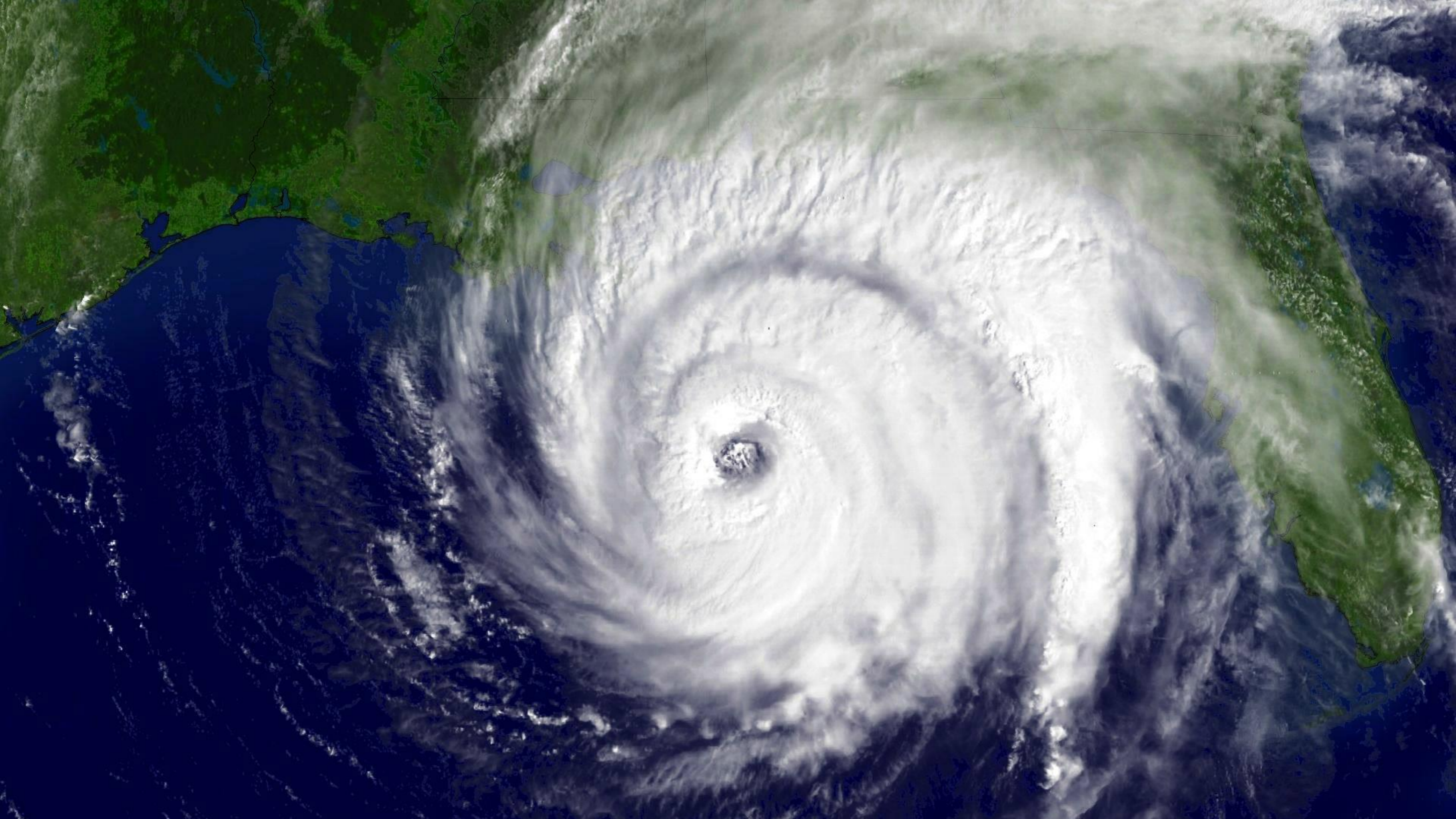
**Analysts**

**Model**

# The stories that show in your News Feed are influenced by:

- friends you interact with the most
- the number of comments and likes a post receives
- what kind of story it is (ex: photo, video, status update)

Source: Facebook



**Spies**

**Analysts**

**Model**



**WAFFLE HOUSE**

**WAFFLE HOUSE**

# The index has three levels:

- **Green**: full menu - restaurant has power and damage is limited.
- **Yellow**: limited menu - no power or only power from a generator, or food supplies may be low.
- **Red**: the restaurant is closed - indicating severe damage.

Source: Wikipedia

# MORE EXAMPLES

- How does US News and World Reports rank colleges?
- How does Google know which results to show?
- How do sports teams know who to draft?
- How does SpaceX make boosters land standing up?
- How does Zillow estimate home prices?
- How does Pandora know what music to play?
- How did the BCS rank college football teams?
- How do they figure out who should speak at a conference?



# GOALS

HOW DO WE MAKE SENSE OF MATH MODELING?

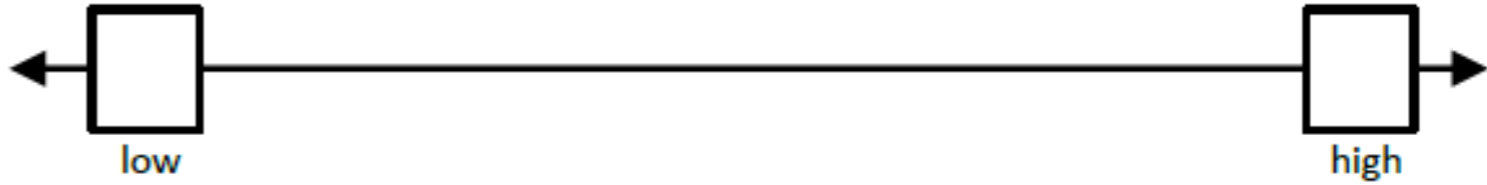
IS IT JUST ANSWERING QUESTIONS?

HOW DO YOU PROFIT FROM MATH MODELING?

HOW DO WE HELP OUR STUDENTS IMPROVE?

WHERE CAN WE FIND MORE RESOURCES?

Name: \_\_\_\_\_ Period: \_\_\_\_\_ Date: \_\_\_\_\_

| What problem are you trying to figure out?                  | What estimates do you have?  |
|---|--|
|   |  <p data-bbox="2059 714 2768 752">Place your estimate on the number line.</p> |
| What info do you already know about the problem?            | What info do you need about the problem?   |
| <p data-bbox="736 1001 1685 1365"><b>TOP SECRET!</b></p>    | <p data-bbox="1725 767 2558 1103"><b>SPIES ONLY</b></p>  |
| What is your conclusion? How did you reach that conclusion? |  |

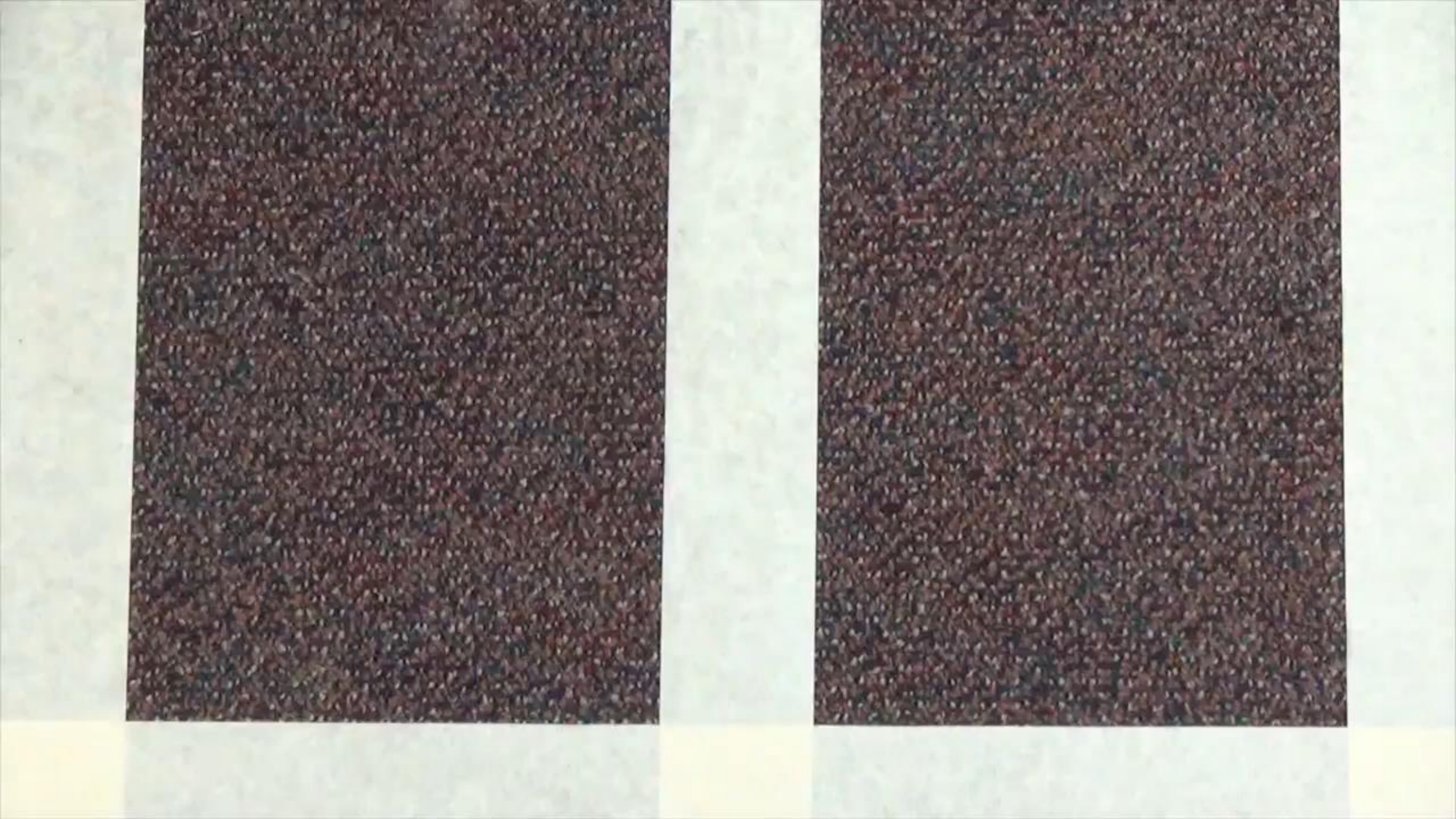
Your work

**DANGER**

**ANALYSTS  
AT WORK**

**NON-STAGGERED**

**STAGGERED**

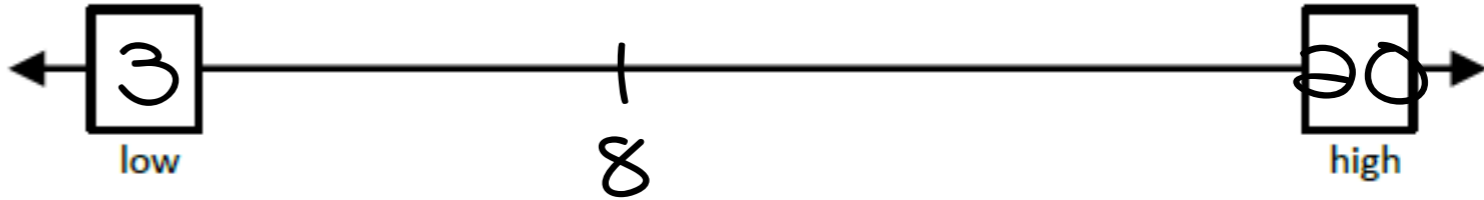


**Spies**

**Analysts**

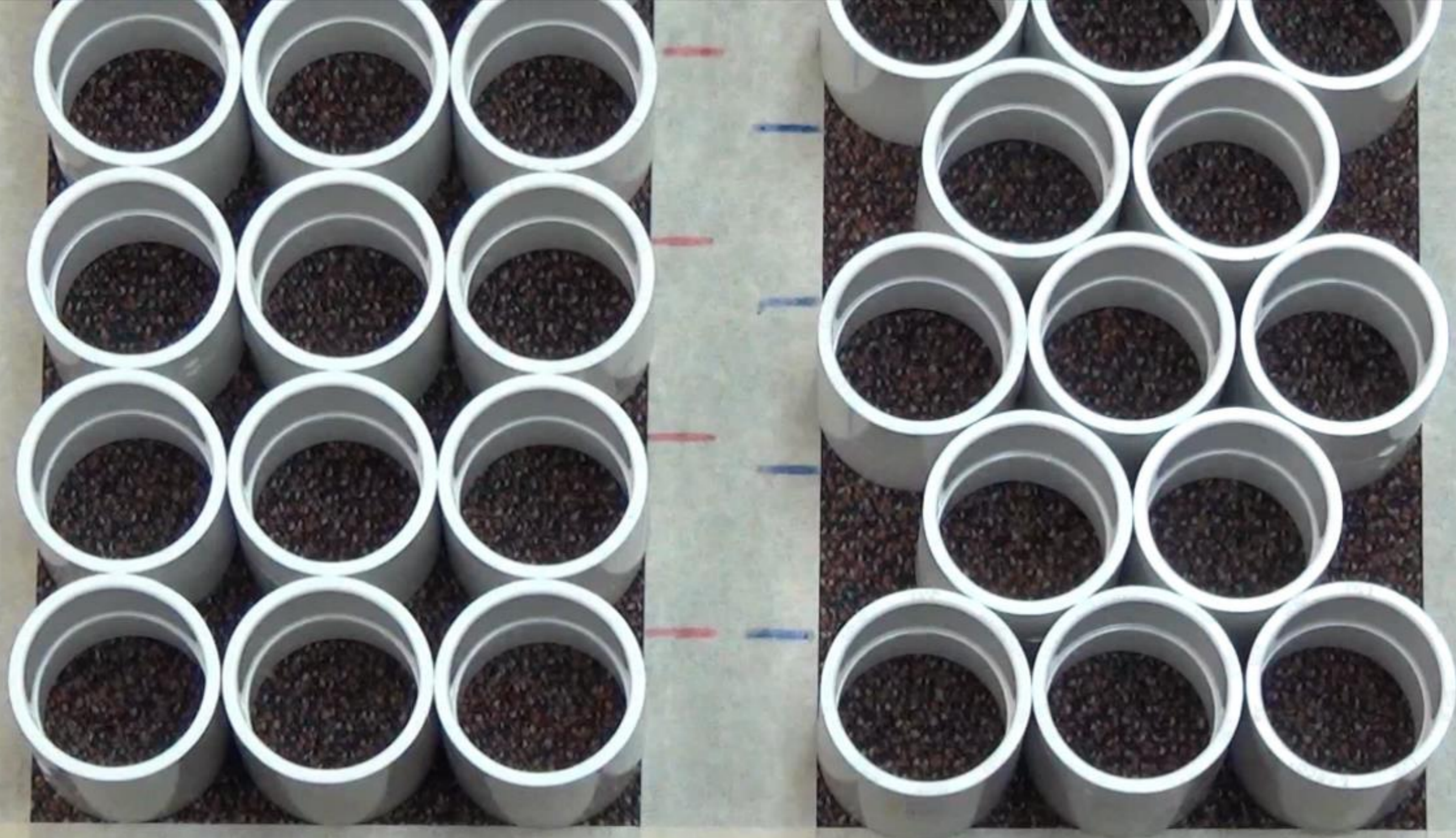
**Model**

# THINKING TIME

| What problem are you trying to figure out?  | What estimates do you have?   |
|---|---|
| <p>How much shorter are 20 layers of non-staggered pipes?</p>   |  <p>(in inches)</p> <p>Place your estimate on the number line.</p> |
| What info do you already know about the problem?  | What info do you need about the problem?  |
| <ul style="list-style-type: none"> <li>• One pile of pipes is staggered.</li> <li>• One pile of pipes is not staggered.</li> <li>• We have to compare 20 layers of each.</li> </ul> | <ul style="list-style-type: none"> <li>• What are the dimensions of a pipe?</li> <li>• What units are we using to measure?</li> </ul>                 |
| What is your conclusion? How did you reach that conclusion?   |   |

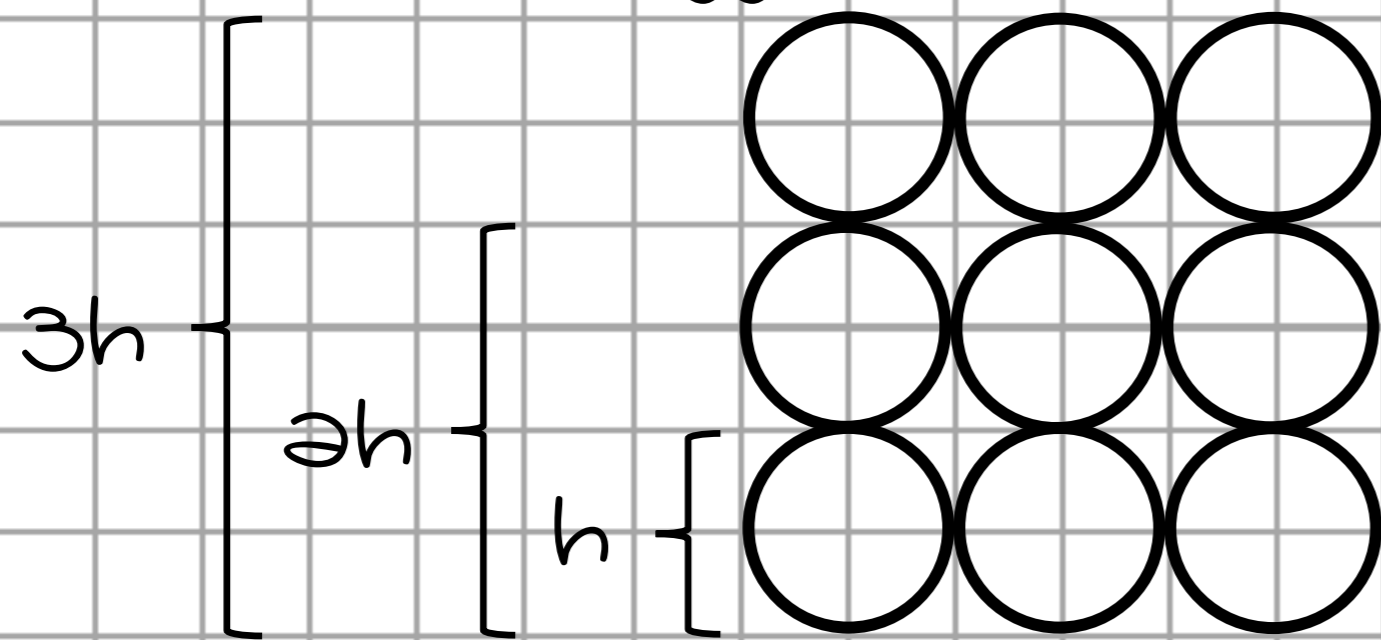






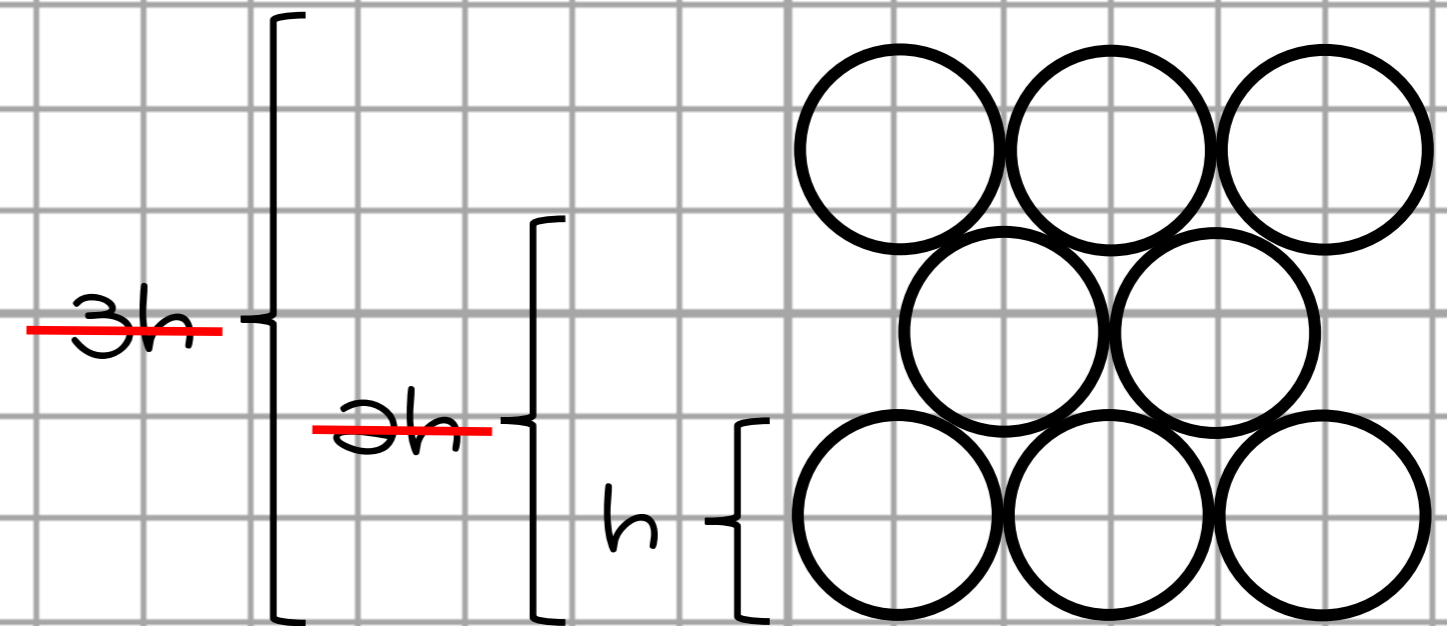
**THINKING TIME**

### Non-staggered pipes



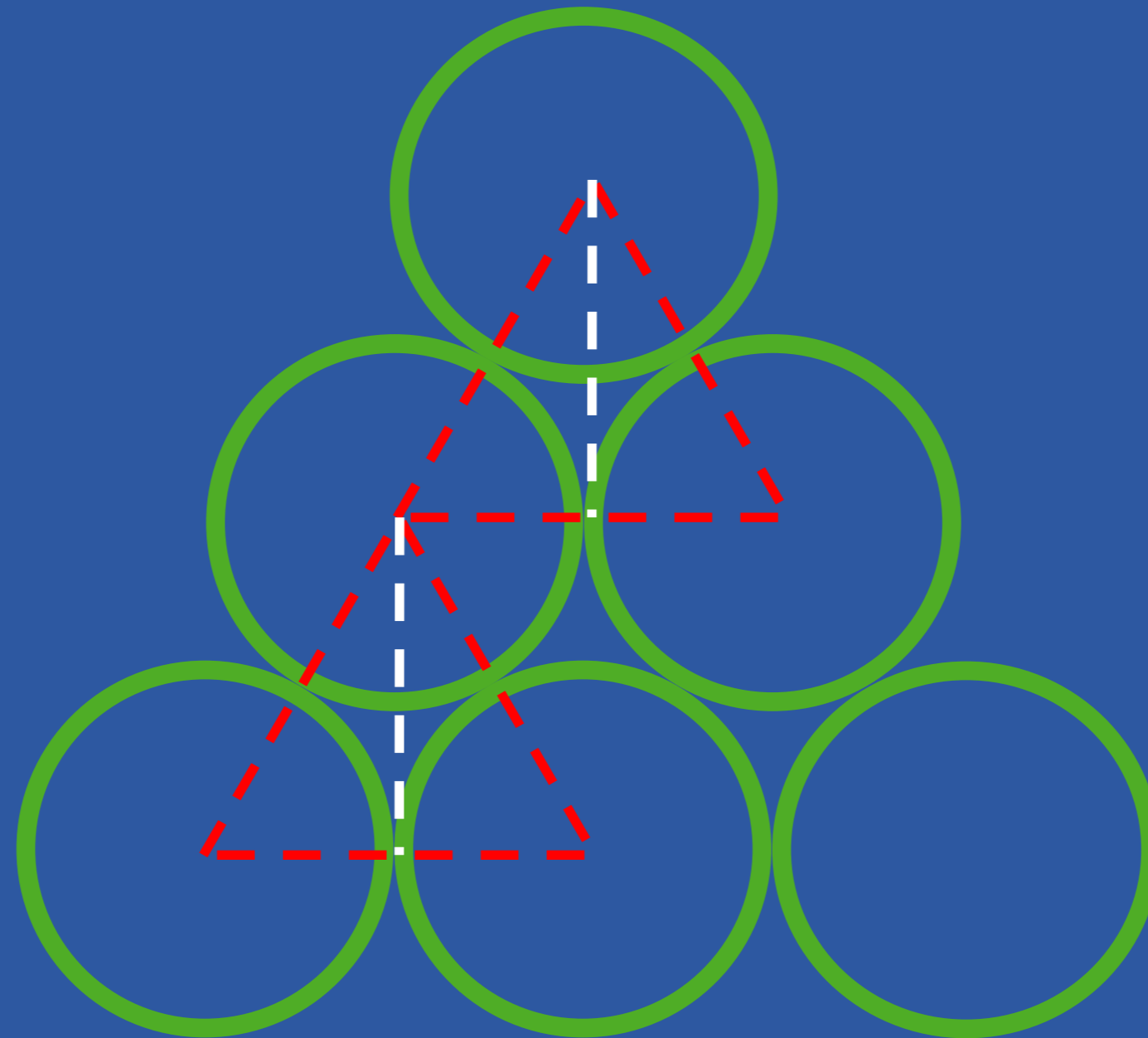
- 1 pipe =  $h$  cm
- 2 pipes =  $2h$  cm
- 3 pipes =  $3h$  cm
- ⋮
- 20 pipes =  $20h$  cm

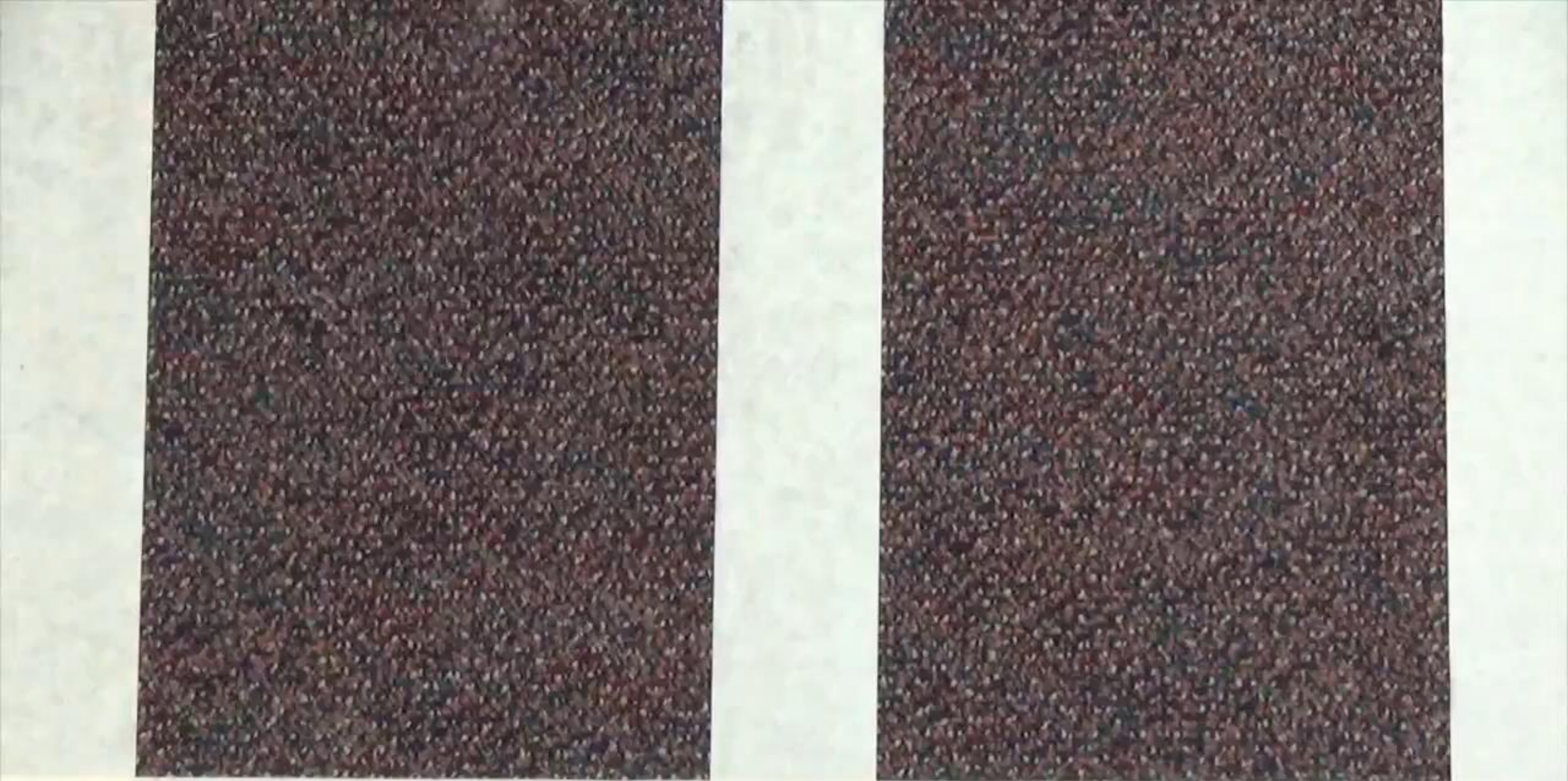
### Staggered pipes



- 1 pipe =  $h$  cm
- 2 pipes =  $3/2 h$  cm
- 3 pipes =  $3/2 h$  cm
- ⋮
- 20 pipes =  $3/2 h$  cm

# STAGGERED PIPES





Layers: 0

# GOALS

HOW DO WE MAKE SENSE OF MATH MODELING?

IS IT JUST ANSWERING QUESTIONS?

HOW DO YOU PROFIT FROM MATH MODELING?

HOW DO WE HELP OUR STUDENTS IMPROVE?

WHERE CAN WE FIND MORE RESOURCES?

# PBL RESOURCES

- Problem-based lesson search engine:  
[robertkaplinsky.com/prbl-search-engine](http://robertkaplinsky.com/prbl-search-engine)
- My lessons (Elementary, Middle, and High School)  
[robertkaplinsky.com/lessons](http://robertkaplinsky.com/lessons)
- Dan Meyer (Middle and High School)  
[threeacts.mrmeyer.com](http://threeacts.mrmeyer.com)
- Andrew Stadel (Elementary and Middle School)  
[www.estimated180.com/lessons.html](http://www.estimated180.com/lessons.html)
- Graham Fletcher (Elementary and Middle School)  
[gfletchy.com/3-act-lessons](http://gfletchy.com/3-act-lessons)





## Home



How Much Money IS That?!  
(Volume of a rectangular prism)

### Search

### Subscribe for Updates

Do you like the ideas you're reading? If so, you'll love having the best ones sent to you via email!

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First Name

### How I Can Help You



#### Real World Problems

My workshops help teachers implement problem-based lessons by helping them experience them from both student and teacher perspective, leading to increase students' success with performance tasks and the Common Core State Standards.



#### Depth of Knowledge

Problems at higher depth of knowledge levels have the potential to challenge your most talented student yet remain accessible to everyone. I can help teachers develop best practices for implementing them so that students persevere longer towards finding the solution.

## Lessons

- [View all](#)
- [Kinder](#)
- [1st](#)
- [2nd](#)
- [3rd](#)
- [4th](#)
- [5th](#)
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### How Much Money Were Those Pennies?



### How Can We #SaveNelly?



### How Many Chip Bags Will There Be?



### How Can We Make Stronger Passwords?

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# GOALS

HOW DO WE MAKE SENSE OF MATH MODELING?

IS IT JUST ANSWERING QUESTIONS?

HOW DO YOU PROFIT FROM MATH MODELING?

HOW DO WE HELP OUR STUDENTS IMPROVE?

WHERE CAN WE FIND MORE RESOURCES?



## Real-World Link



Common Core  
State Standards

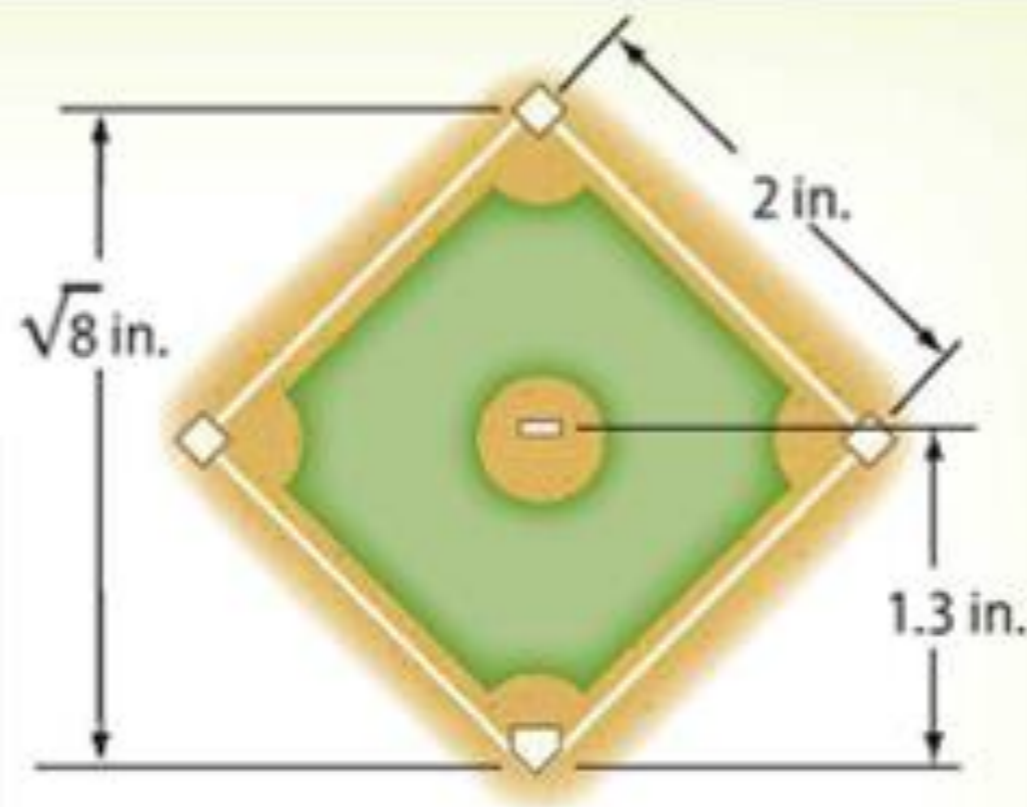
### Content Standards

8.NS.1, 8.NS.2, 8.EE.2

### Mathematical Practices

1, 3, 4, 6

**Sports** Major League baseball has rules for the dimensions of the baseball diamond. A model of the diamond is shown.



1. On the model, the distance from the pitching mound to home plate is 1.3 inches. Is 1.3 a rational number? Explain.

---

2. On the model, the distance from first base to second base is 2 inches. Is 2 a rational number? Explain.

---

3. The distance from home plate to second base is  $\sqrt{8}$  inches. Using a calculator, find  $\sqrt{8}$ . Does it appear to terminate or repeat?





## Real-World Link



## Common Core State Standards

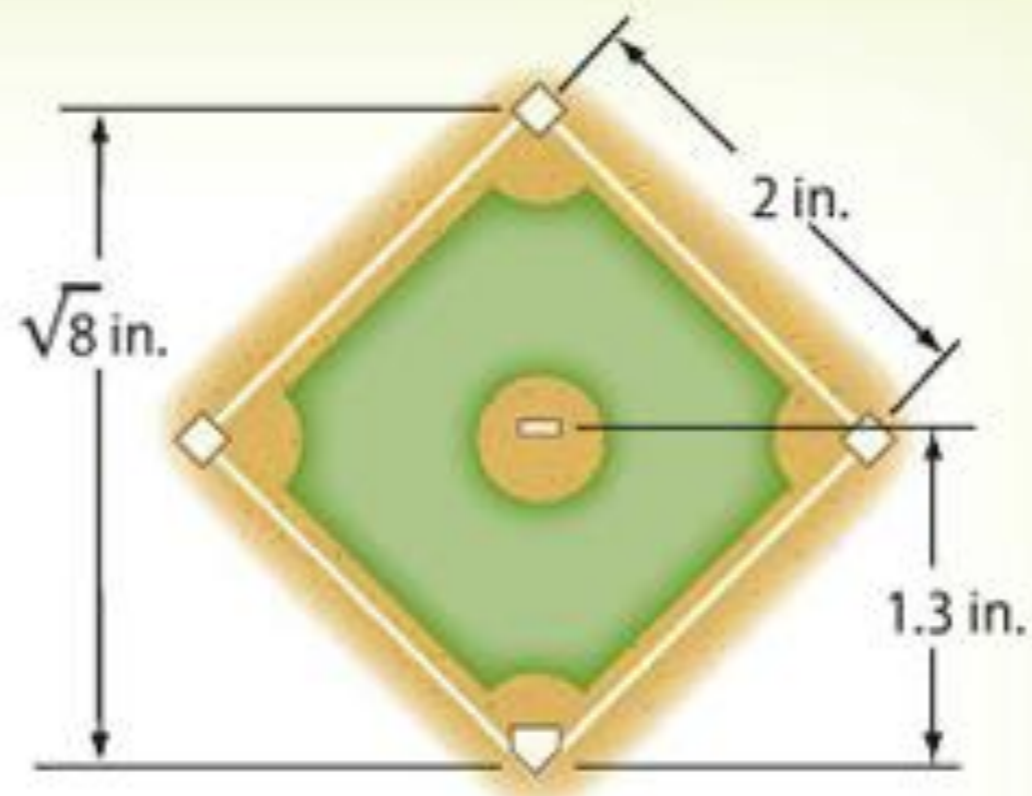
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# Scary & Dangerous



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**MATH MODELING CAN**

**MAKE YOU FILTHY RICH**

**ROBERT KAPLINSKY**

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