MATH MODELING CAN

MAKE YOU FILTHY RICH

ROBERT KAPLINSKY

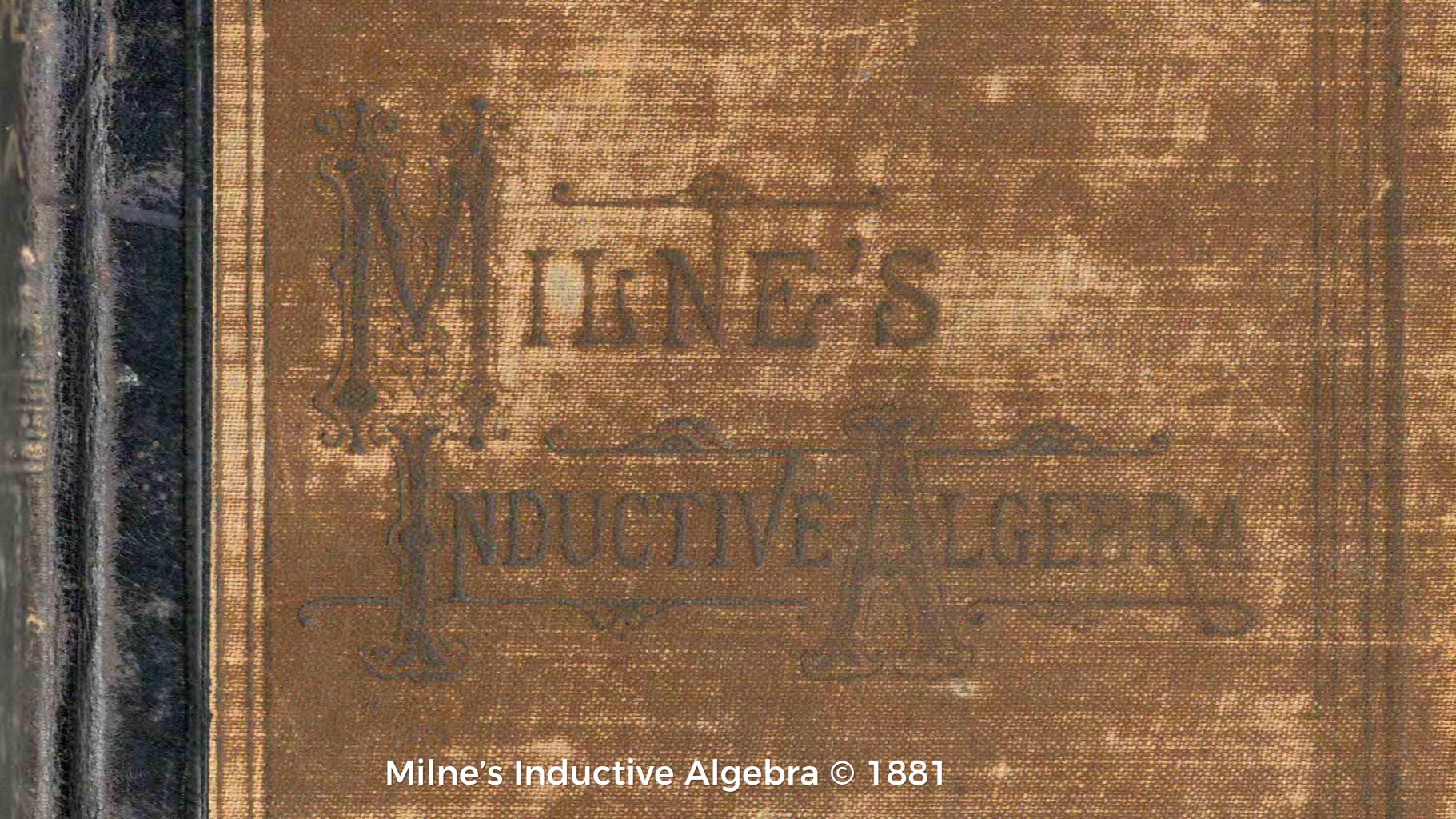
robert@robertkaplinsky.com

robertkaplinsky.com

@robertkaplinsky



Why do we nave word oroblems?

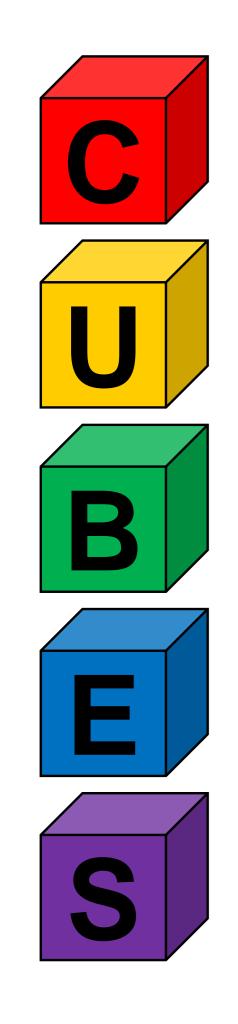


183. DIRECTIONS FOR SOLVING.—Represent one of the unknown quantities by x, and from the conditions of the problem find an expression for each of the other quantities given.

Find from the problem two expressions that are equal, and express them as an equation.

Solve the equation.

- 51. When the half of a certain number is added to the number, the sum is as much more than 60 as the number is less than 65. What is the number?
- 52. The difference between two numbers is 8, and the quotient arising from dividing the greater by the less is 3. What are the numbers?
- 53. A man left one-half of his property to his wife, one-sixth to his children, a twelfth to his brother, and the rest, which was \$600, to charitable purposes. How much property had he?



CIRCLE the numbers

UNDERLINE the question

BOX the key words

ELIMINATE info not needed

SOLVE and check <

In a class of 30 children, there are 3) girls for every 2 boys. How many girls are there altogether?

Source: Marilyn Burns

There are 125 sheep and 5 dogs in a flock. How old is the shepherd?

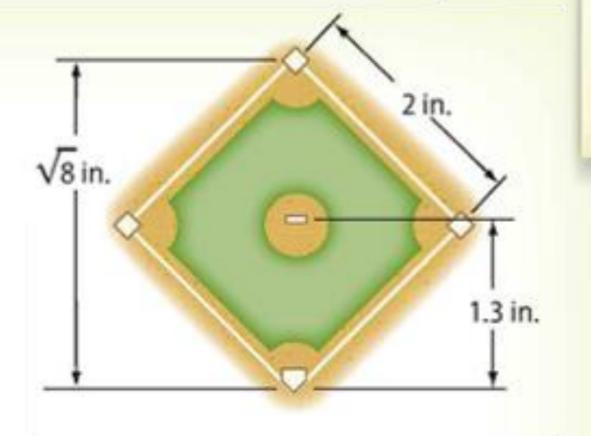


Making sense:8 Not making sense: 24



Sports Major League baseball has rules for the dimensions of the baseball diamond. A model of the diamond is shown.

 On the model, the distance from the pitching mound to home plate is 1.3 inches. Is 1.3 a rational number? Explain.





8.NS.1, 8.NS.2, 8.EE.2

Mathematical Practices 1, 3, 4, 6

On the model, the distance from first base to second base is 2 inches. Is 2 a rational number? Explain.

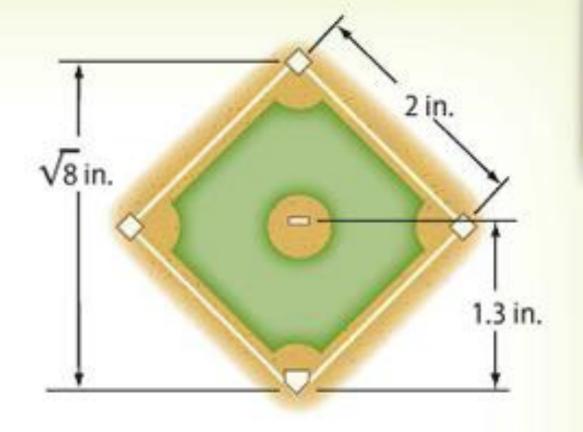
3. The distance from home plate to second base is $\sqrt{8}$ inches. Using a calculator, find $\sqrt{8}$. Does it appear to terminate or repeat?





Sports Major League baseball has rules for the dimensions of the baseball diamond. A model of the diamond is shown.

 On the model, the distance from the pitching mound to home plate is 1.3 inches. Is 1.3 a rational number? Explain.





Content Standards

8.NS.1, 8.NS.2, 8.EE.2

Mathematical Practices

1, 3, 4, 6

On the model, the distance from first base to second base is 2 inches. Is 2 a rational number? Explain.

3. The distance from home plate to second base is $\sqrt{8}$ inches. Using a calculator, find $\sqrt{8}$. Does it appear to terminate or repeat?





Doritos & Cheetos Mix 20

DORITOS® Nacho Cheese Flavored Tortilla Chips 1 OZ. EA. DORITOS® COOL RANCH® Flavored Tortilla Chips 1 OZ. EA. CHEETOS® Puffs Cheese Flavored Snacks 7/8 OZ. EA. CHEETOS® Crunchy Cheese Flavored Snacks 1 OZ. EA.

20 INDIVIDUAL BAGS: 1/8 OZ. EACH, 1 OZ. EACH, TOTAL NET WT. 19 5/8 OZ. (1 LB. 3 5/8 OZ.) 556.3 g

WARNING, PREVENT ENTANGLEMENT AND STRANGULATION, KEEP THIS BAG AWAY FROM YOUNG CHILDREN, IT IS NOT A TOY

THINKING TIME

- Why did many of you expect there to be five of each?
- Why was it not five of each?
- How might they decide on this combination?



Classic Mix 20 Singles

LAY'S® Classic Potato Chips, DORITOS® Nacho Cheese Flavored Tortilla Chips, DORITOS® COOL RANCH® Flavored Tortilla Chips, CHEETOS® Crunchy Cheese Flavored Snacks, SUNCHIPS® Original Multigrain Snacks, FRITOS® Original Com Chips (All 1 OZ. Each)

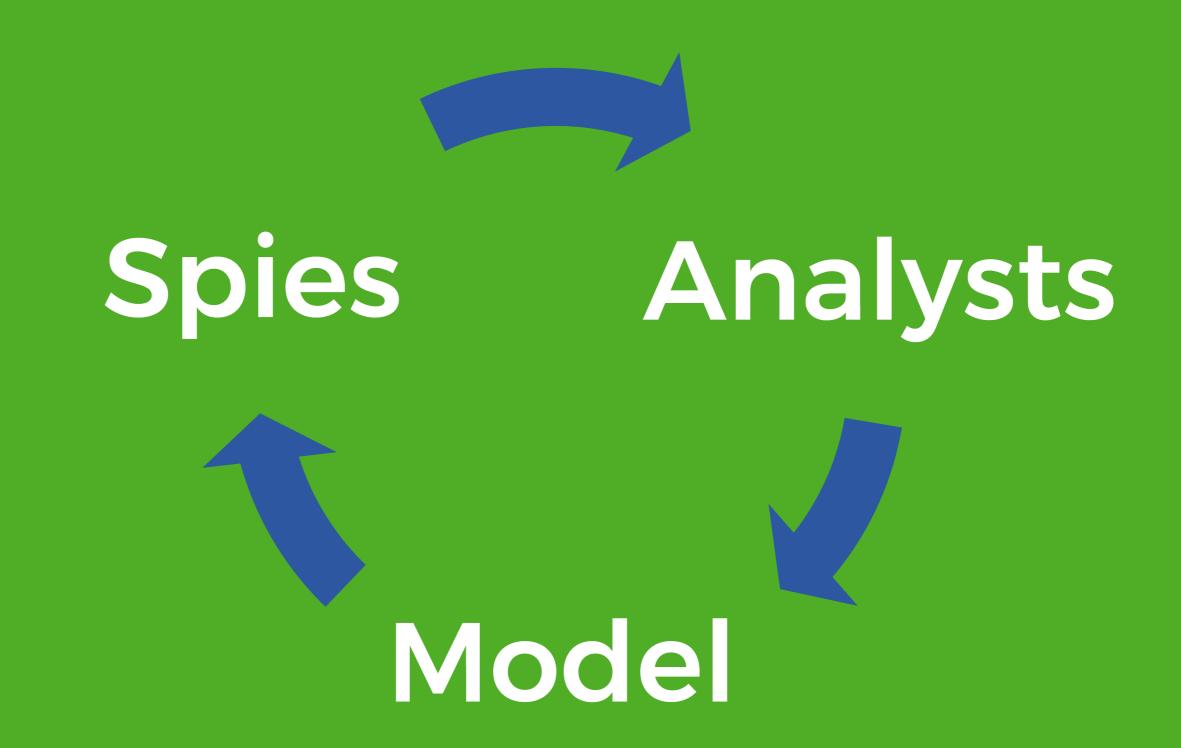
GOALS

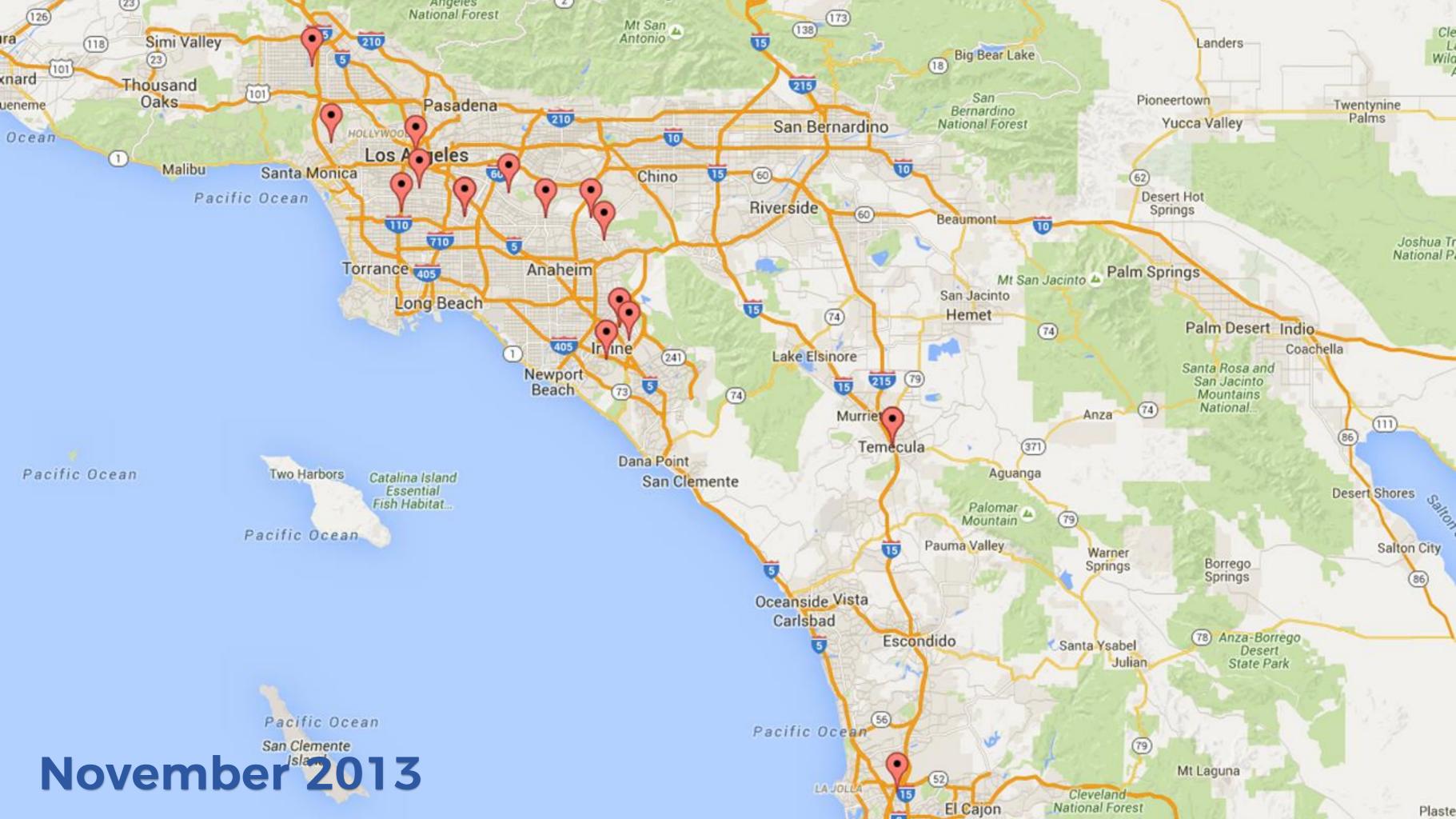
- HOW DO WE MAKE SENSE OF MATH MODELING?
- ☐ IS IT JUST ANSWERING QUESTIONS?
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- ☐ HOW DO WE HELP OUR STUDENTS IMPROVE?
- ☐ WHERE CAN WE FIND MORE RESOURCES?

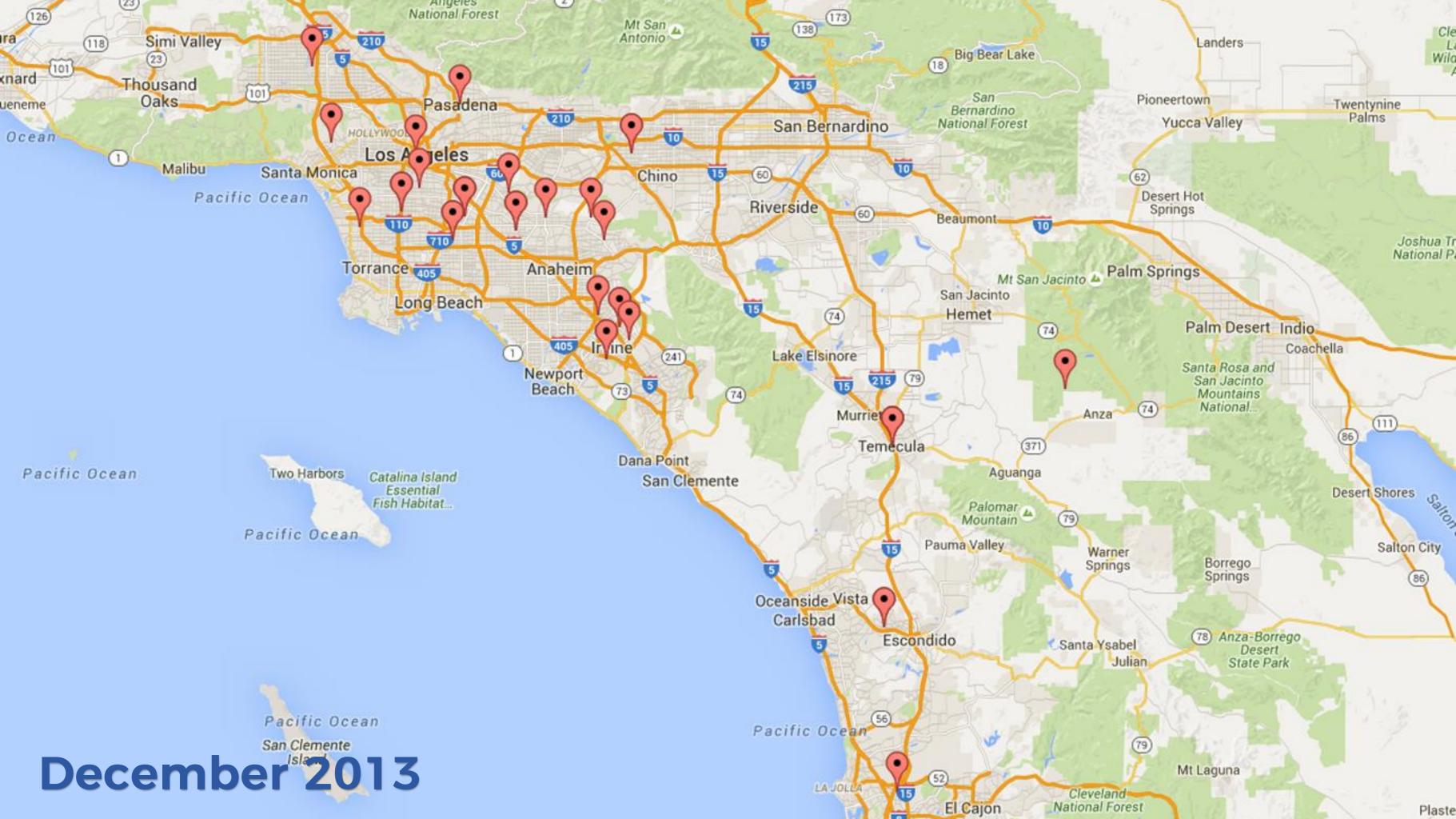


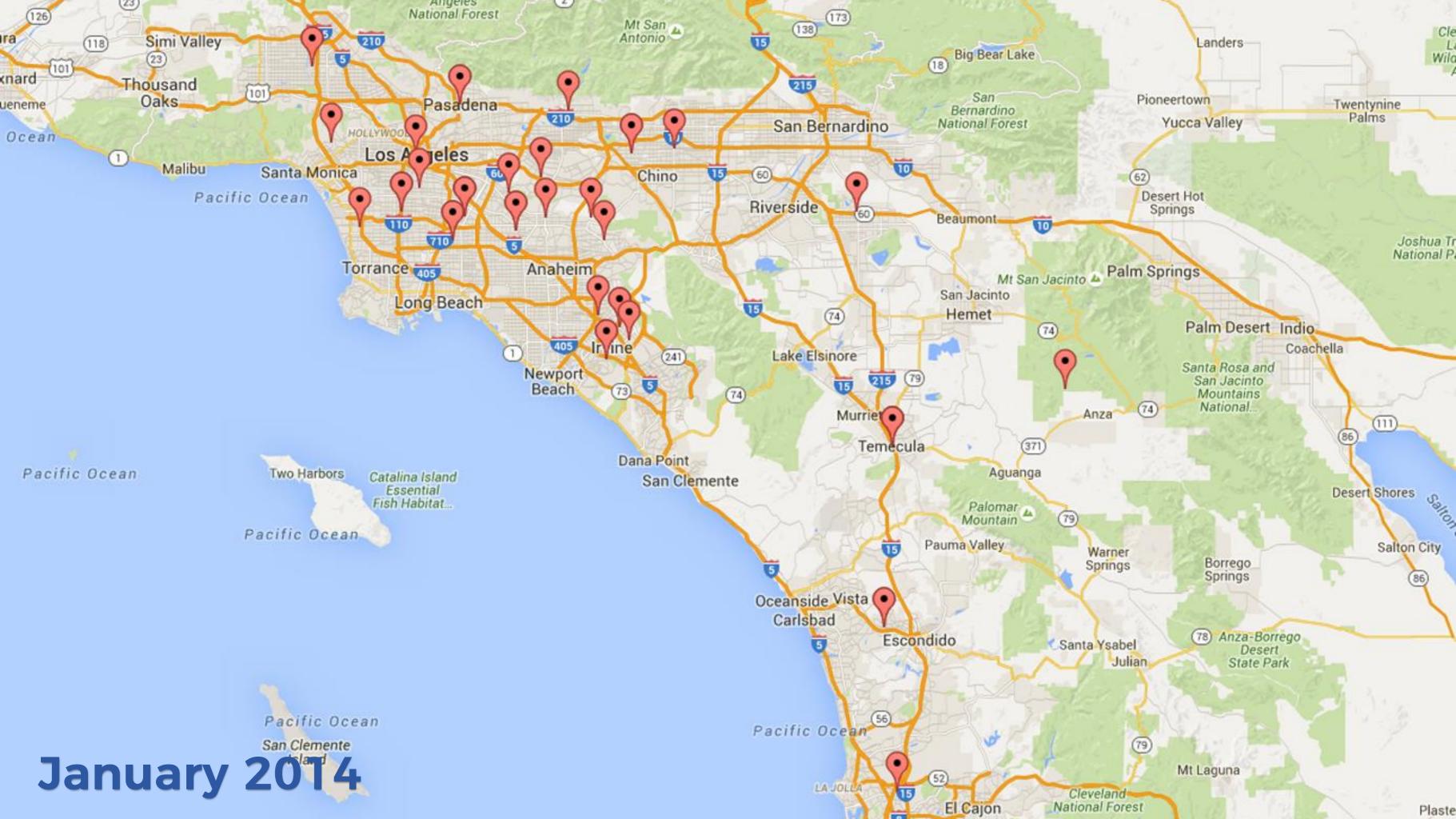


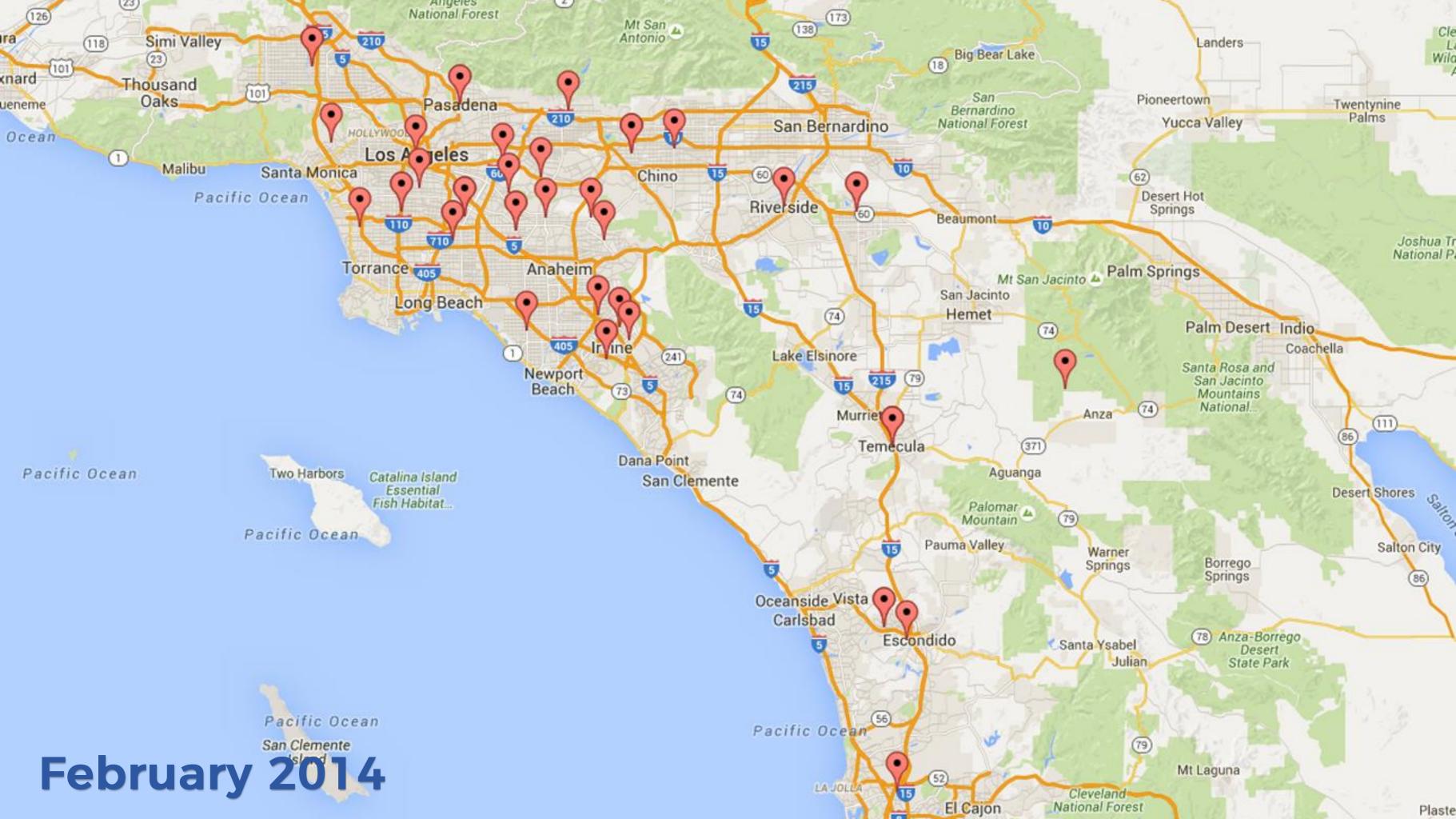


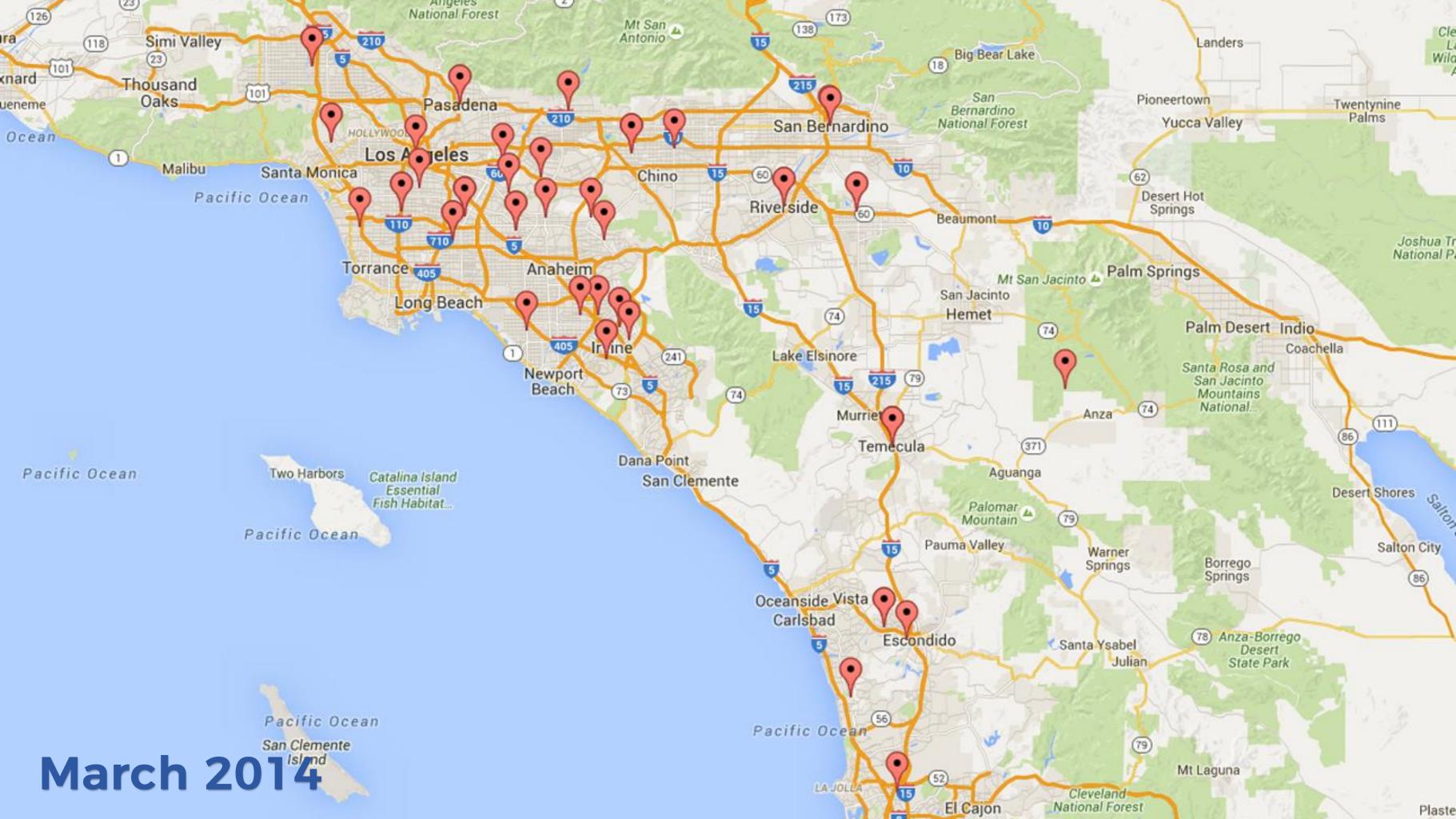


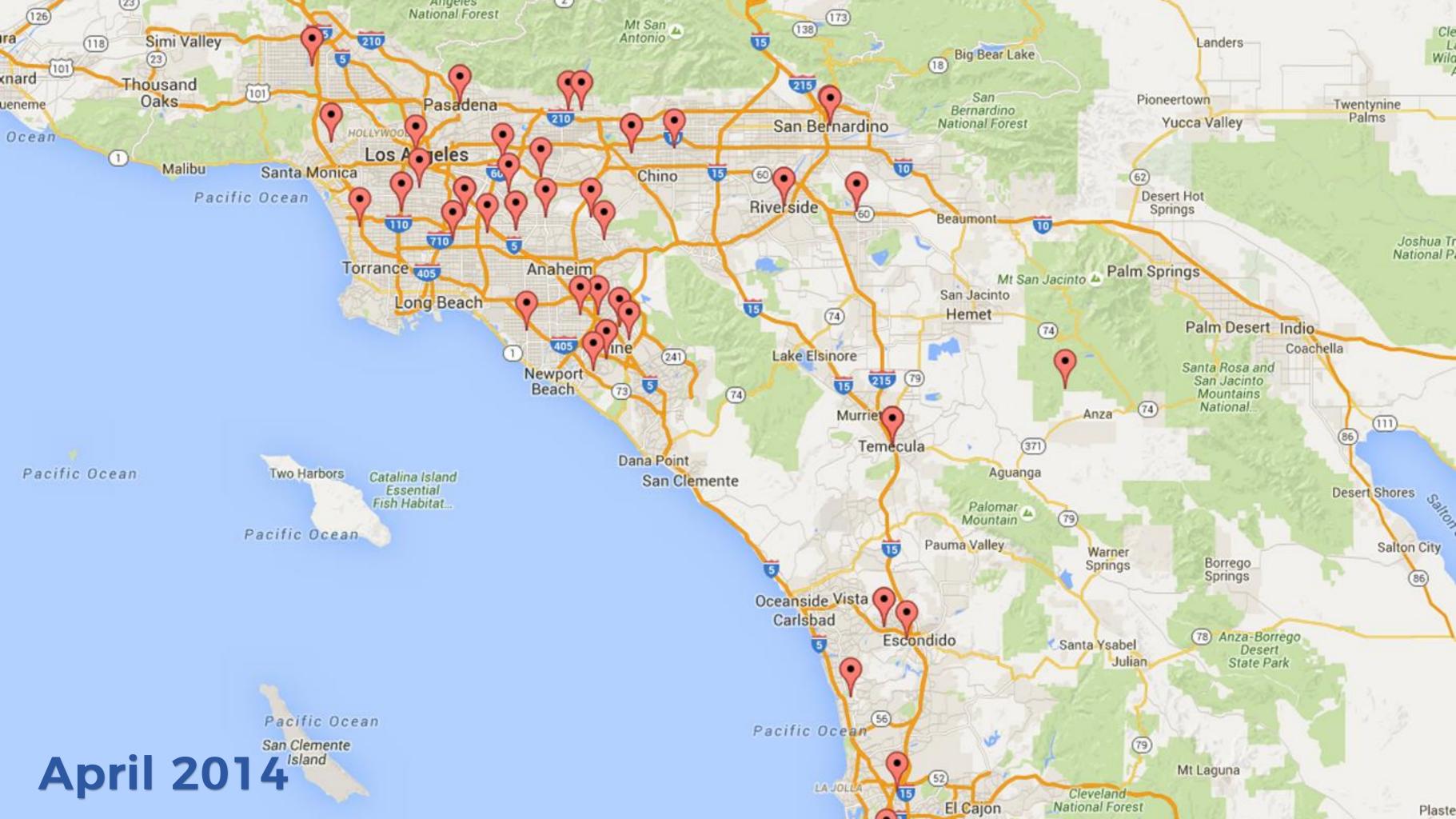


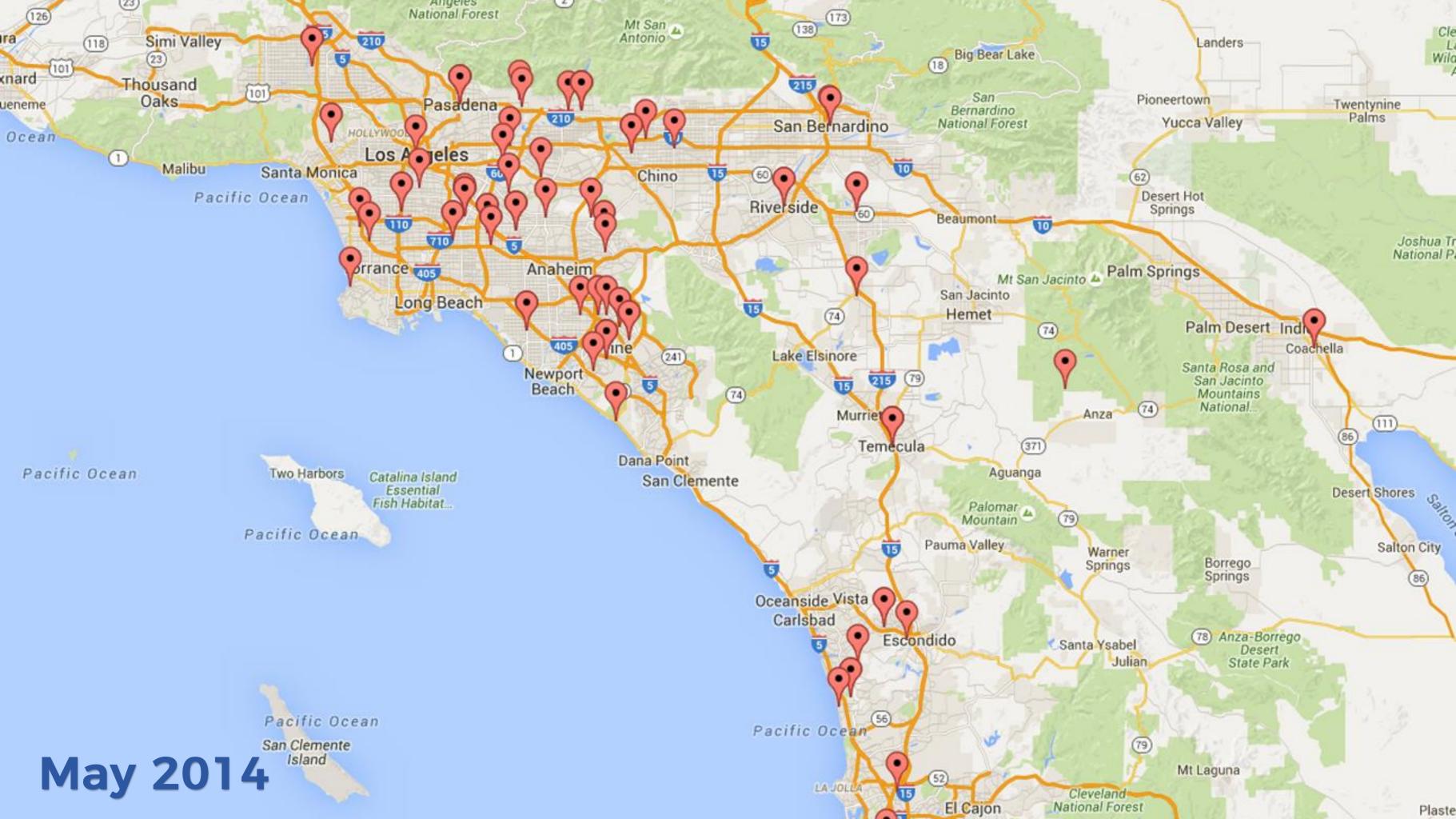


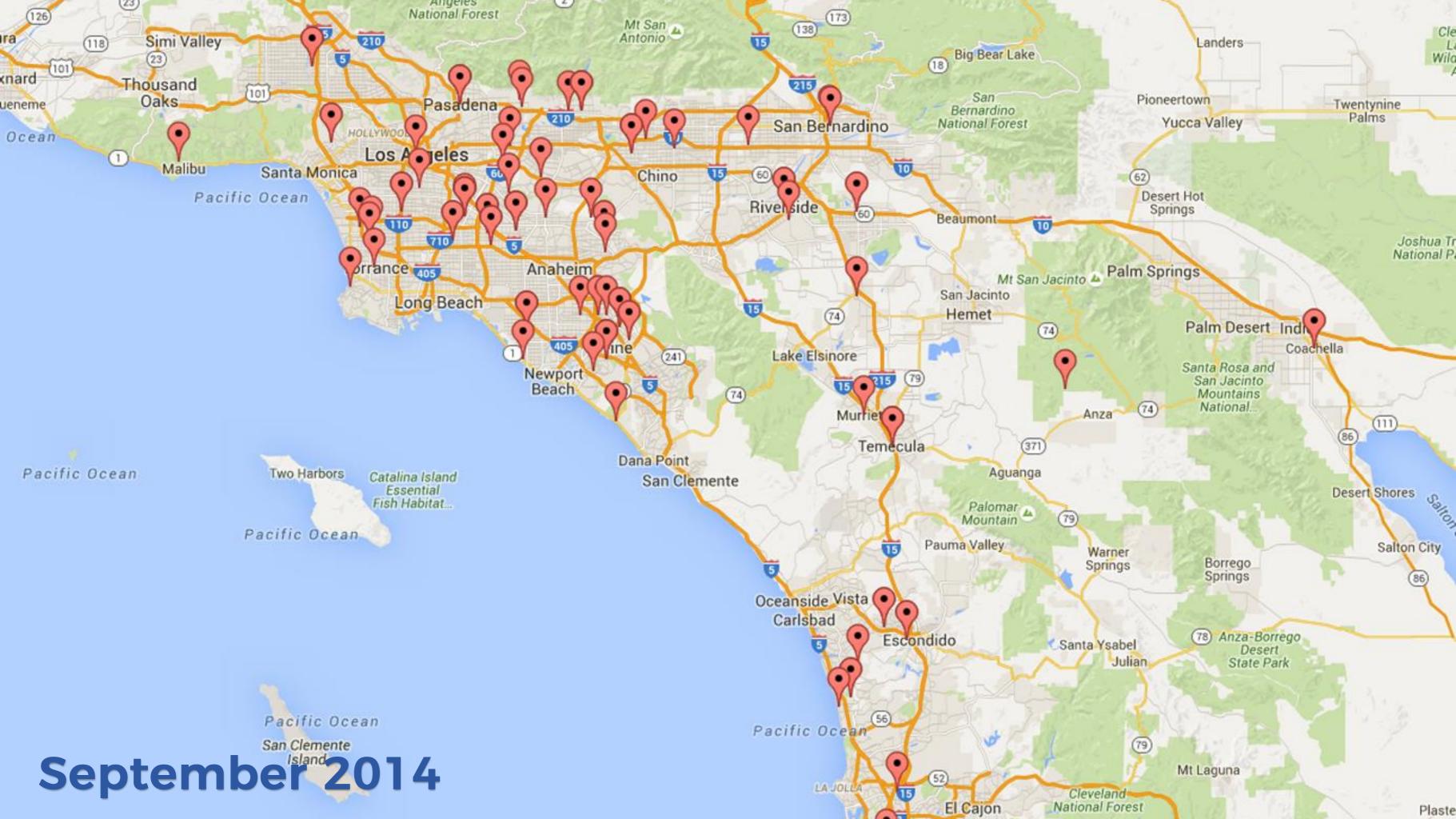


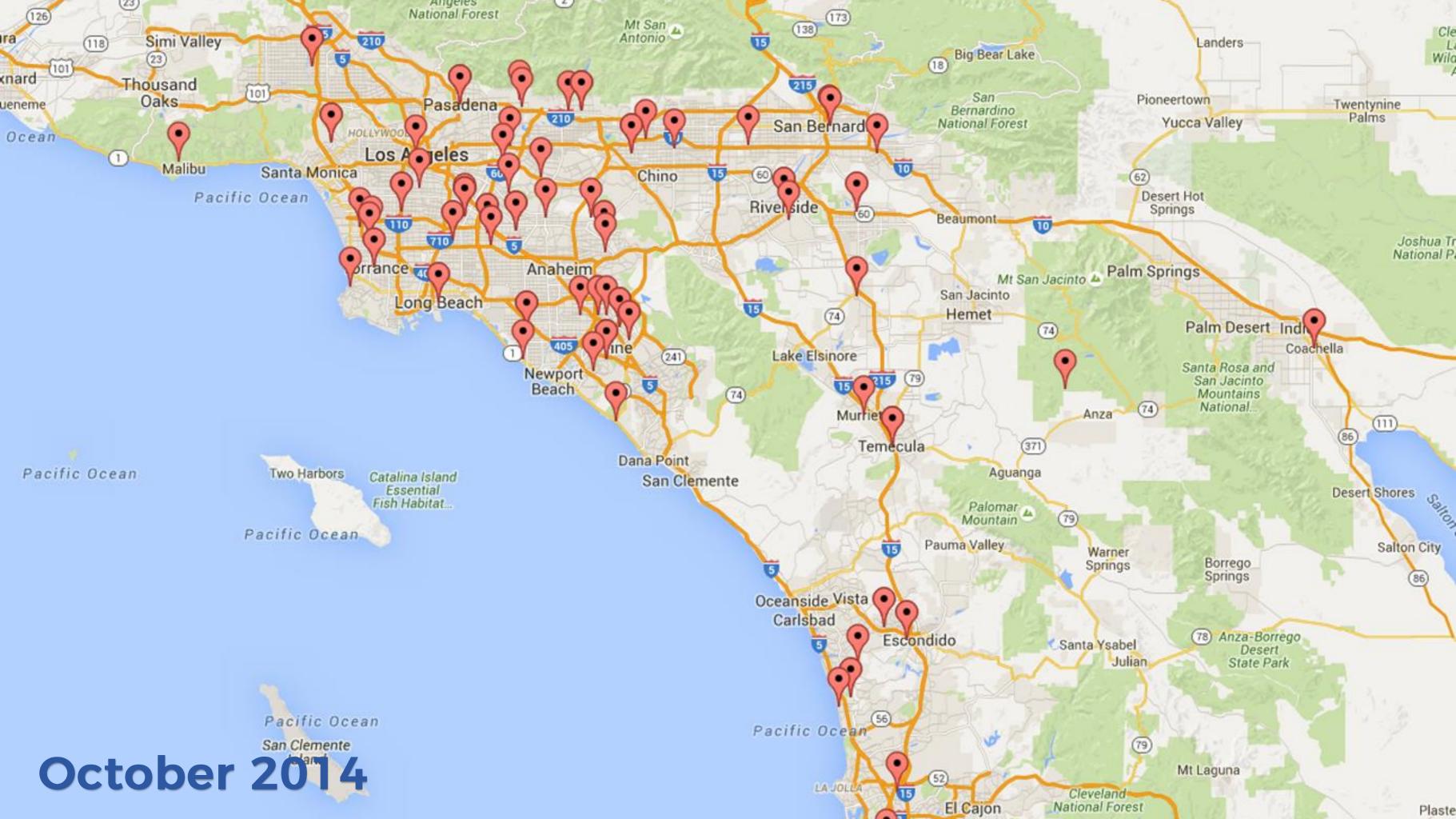


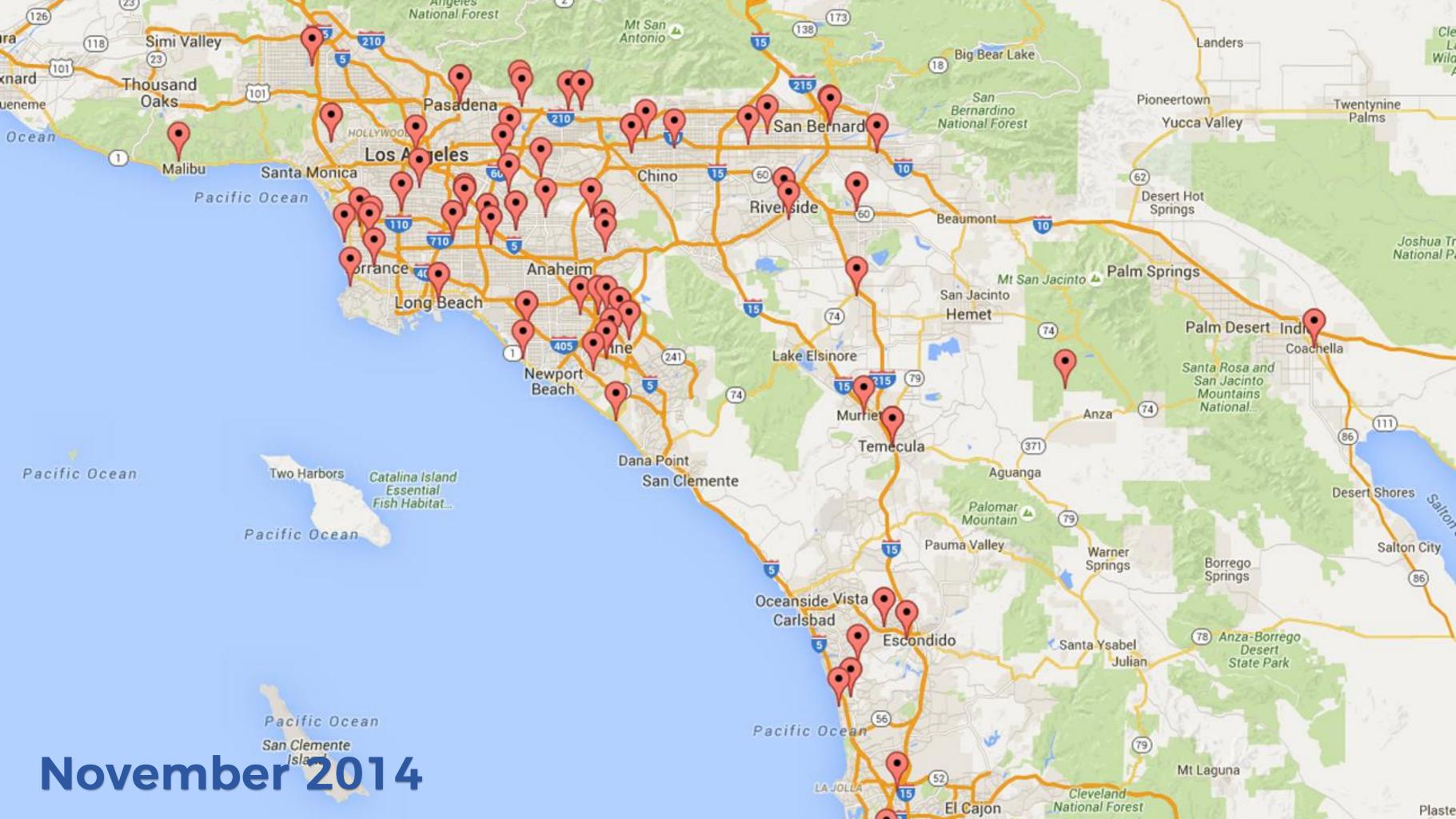


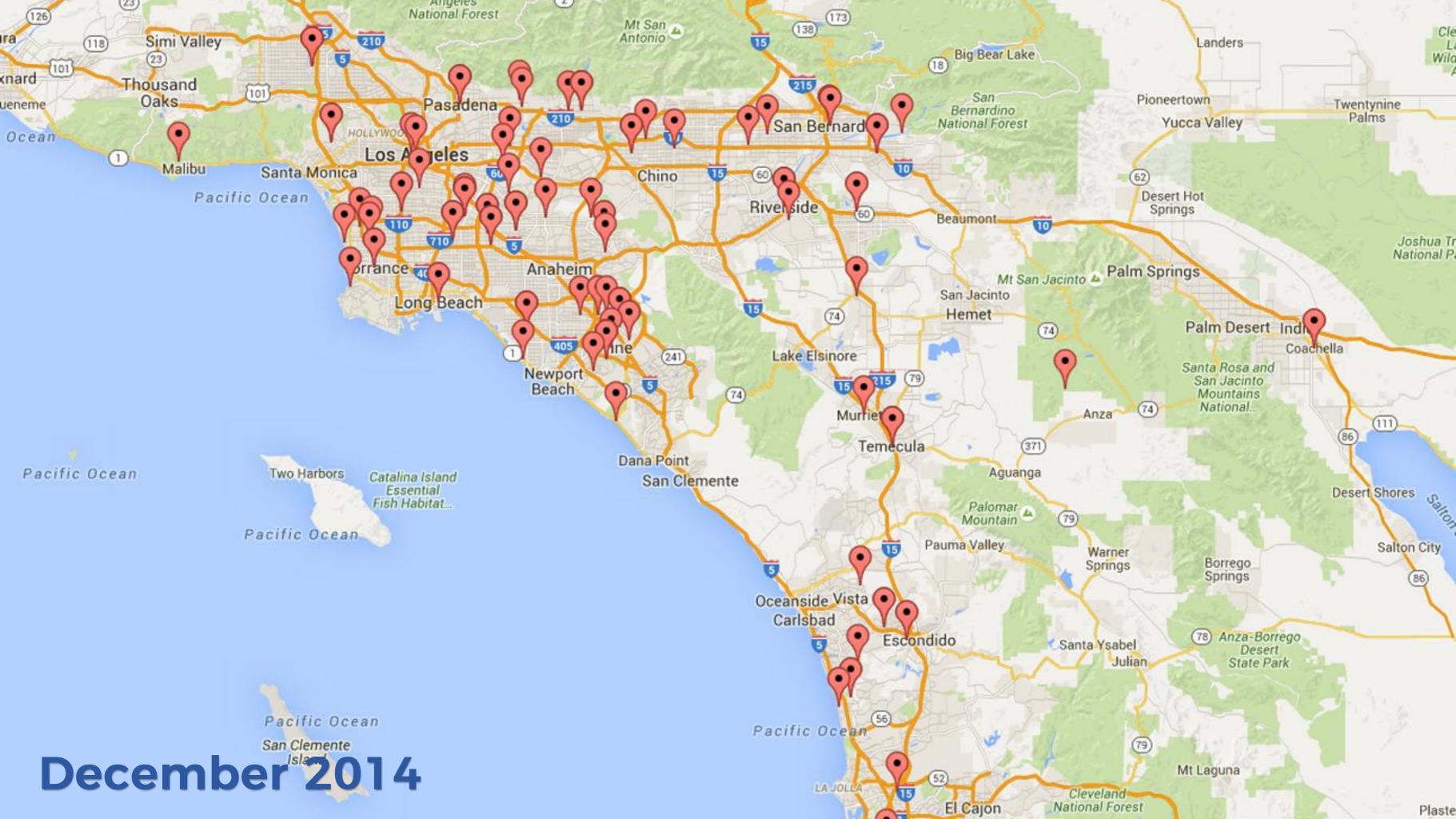


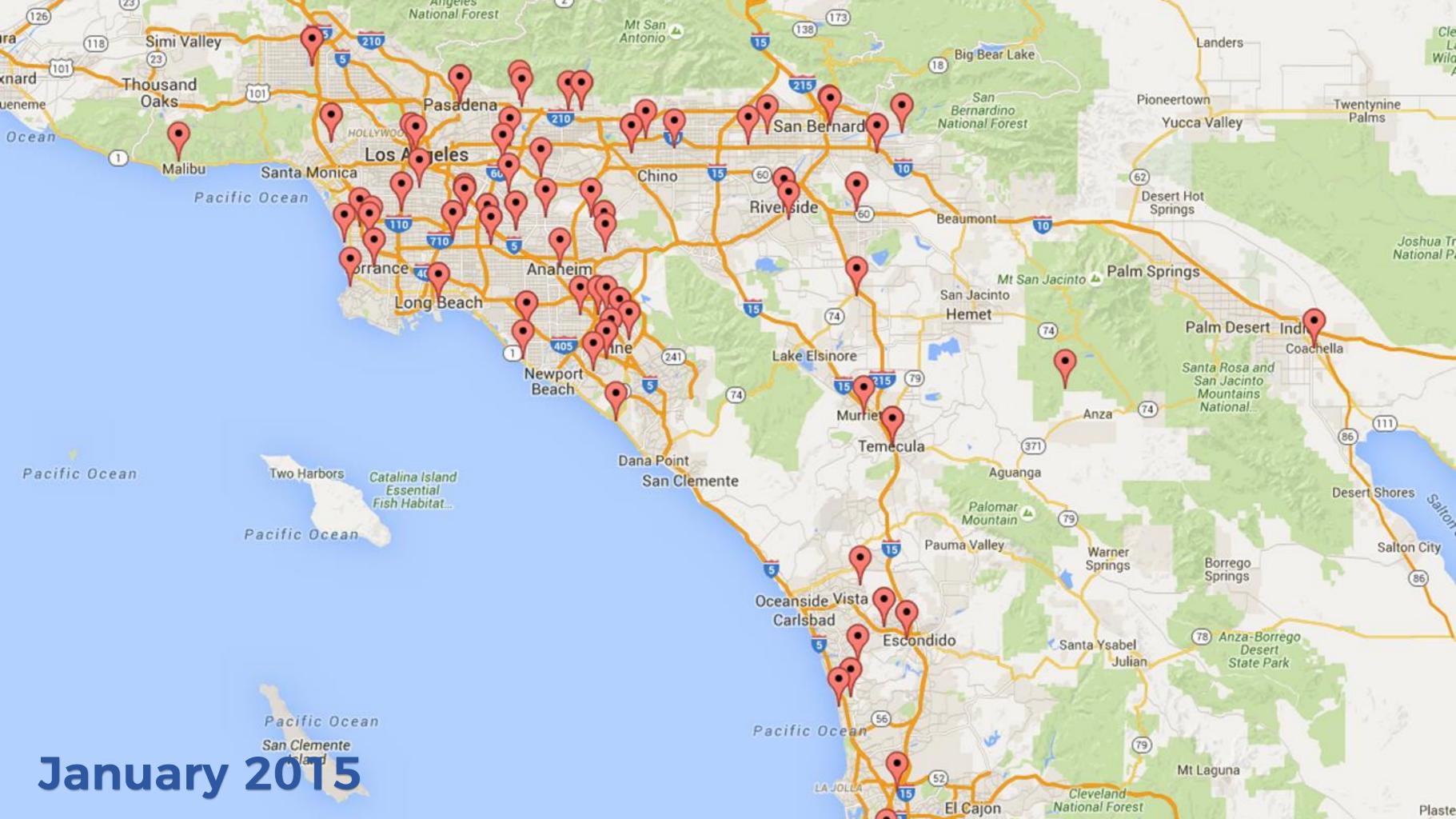


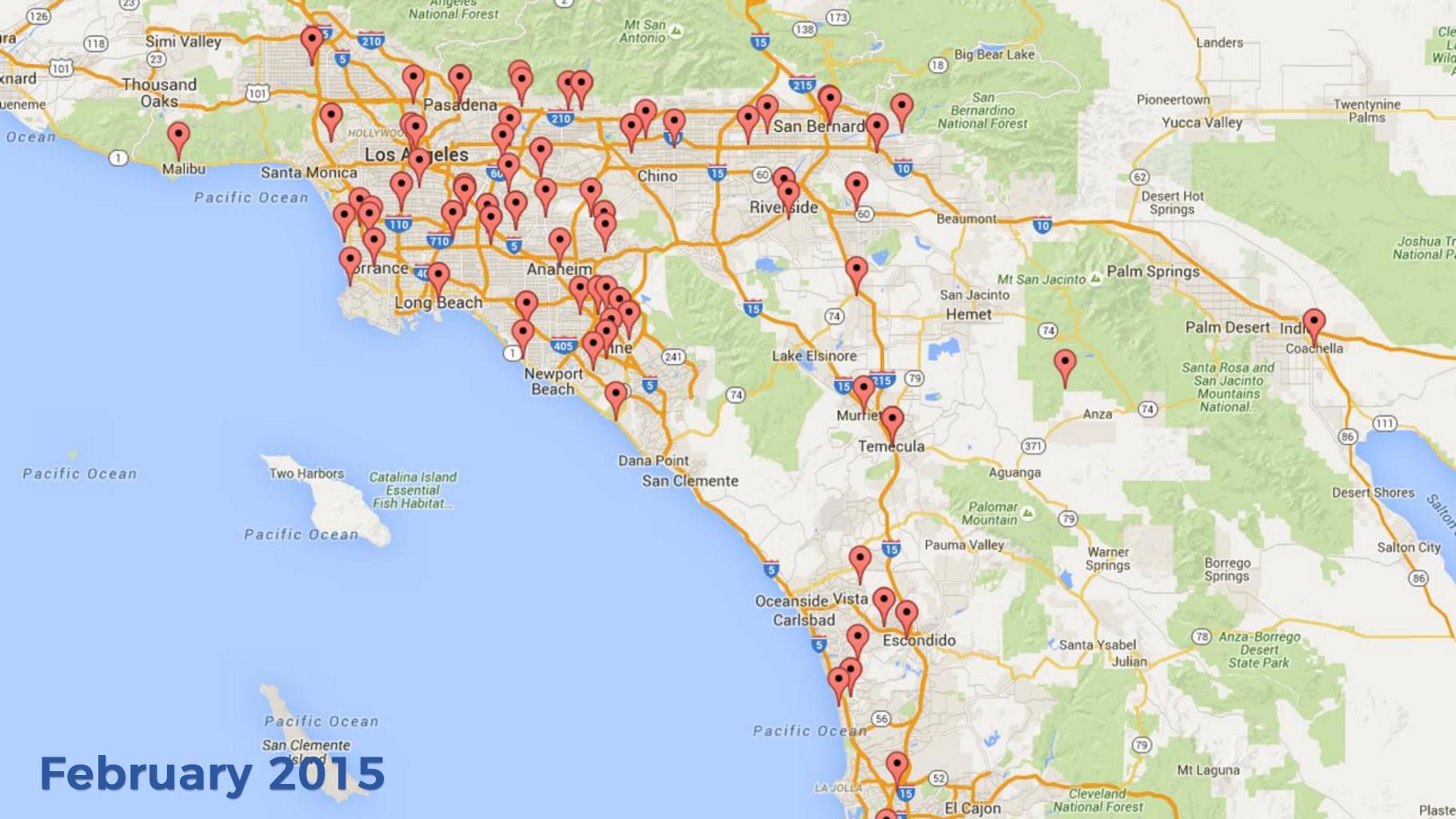


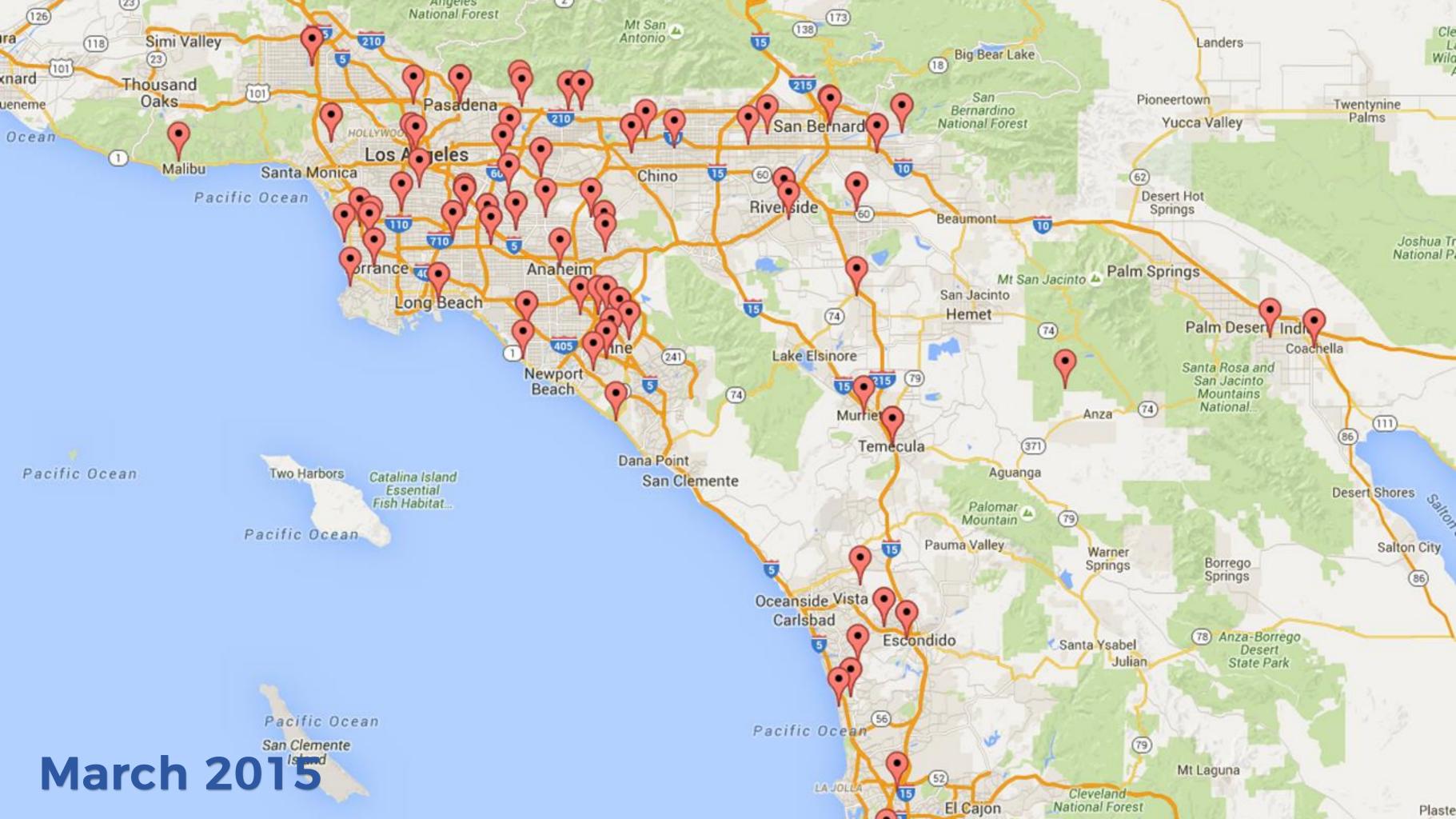


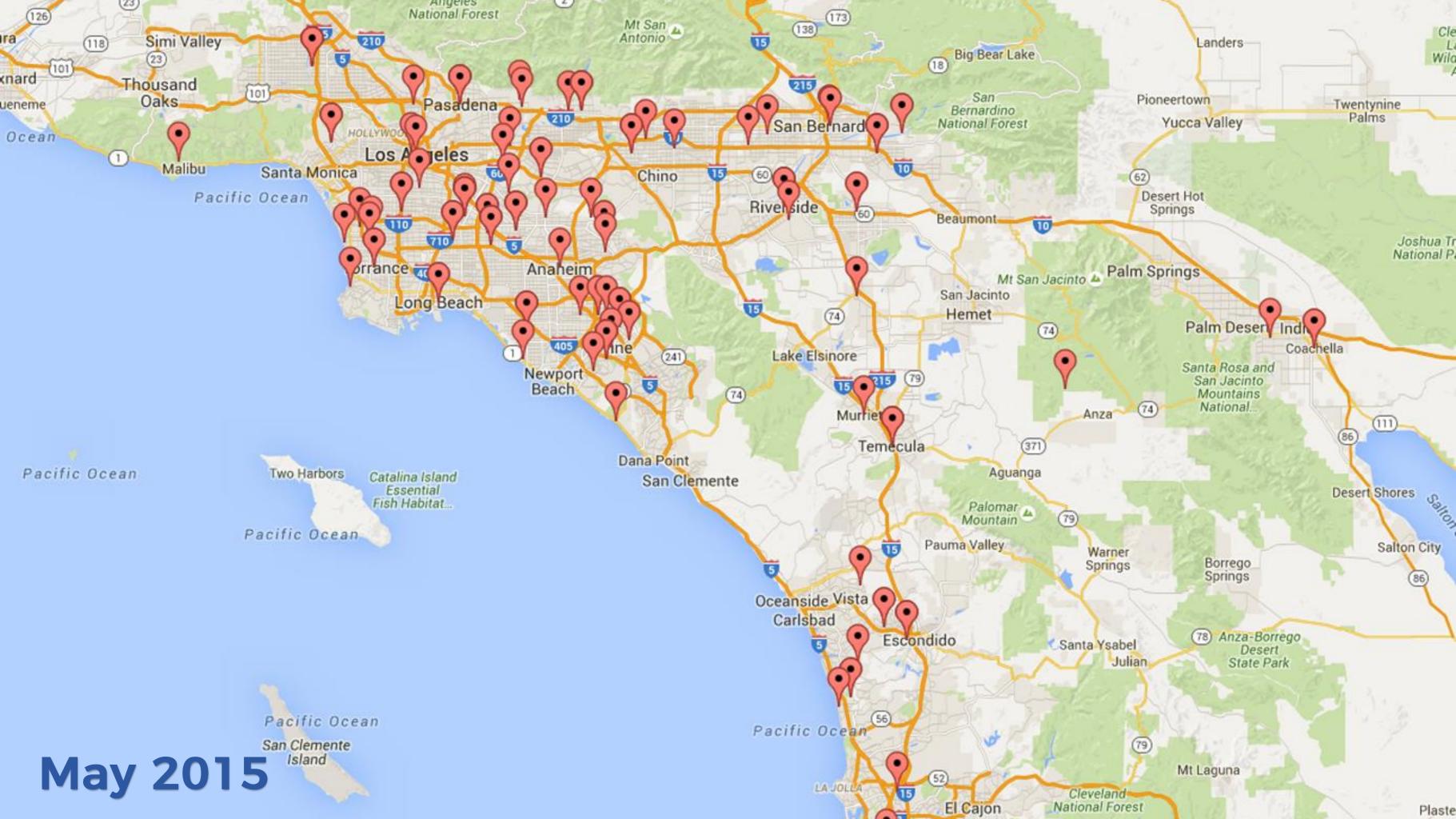


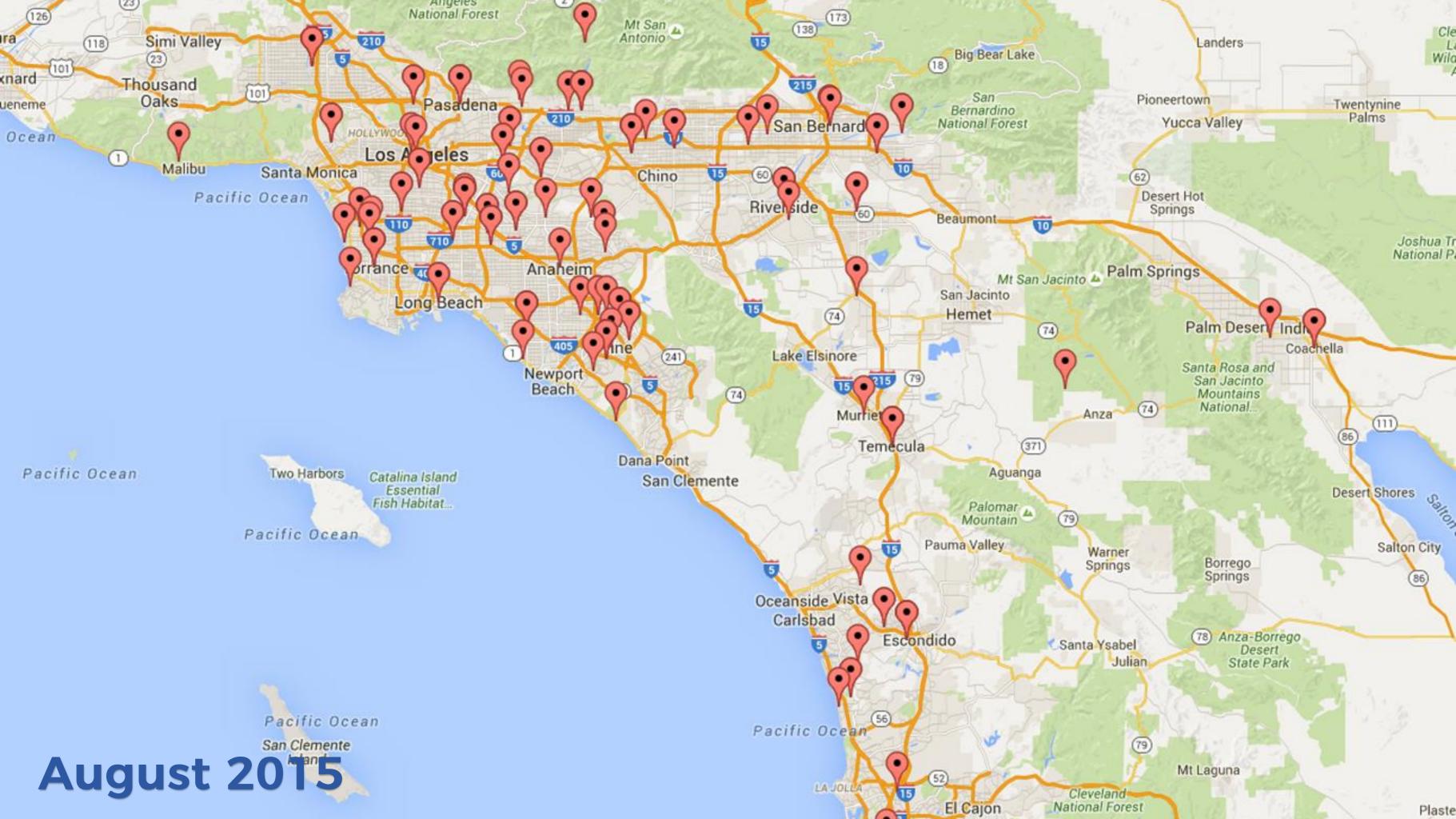


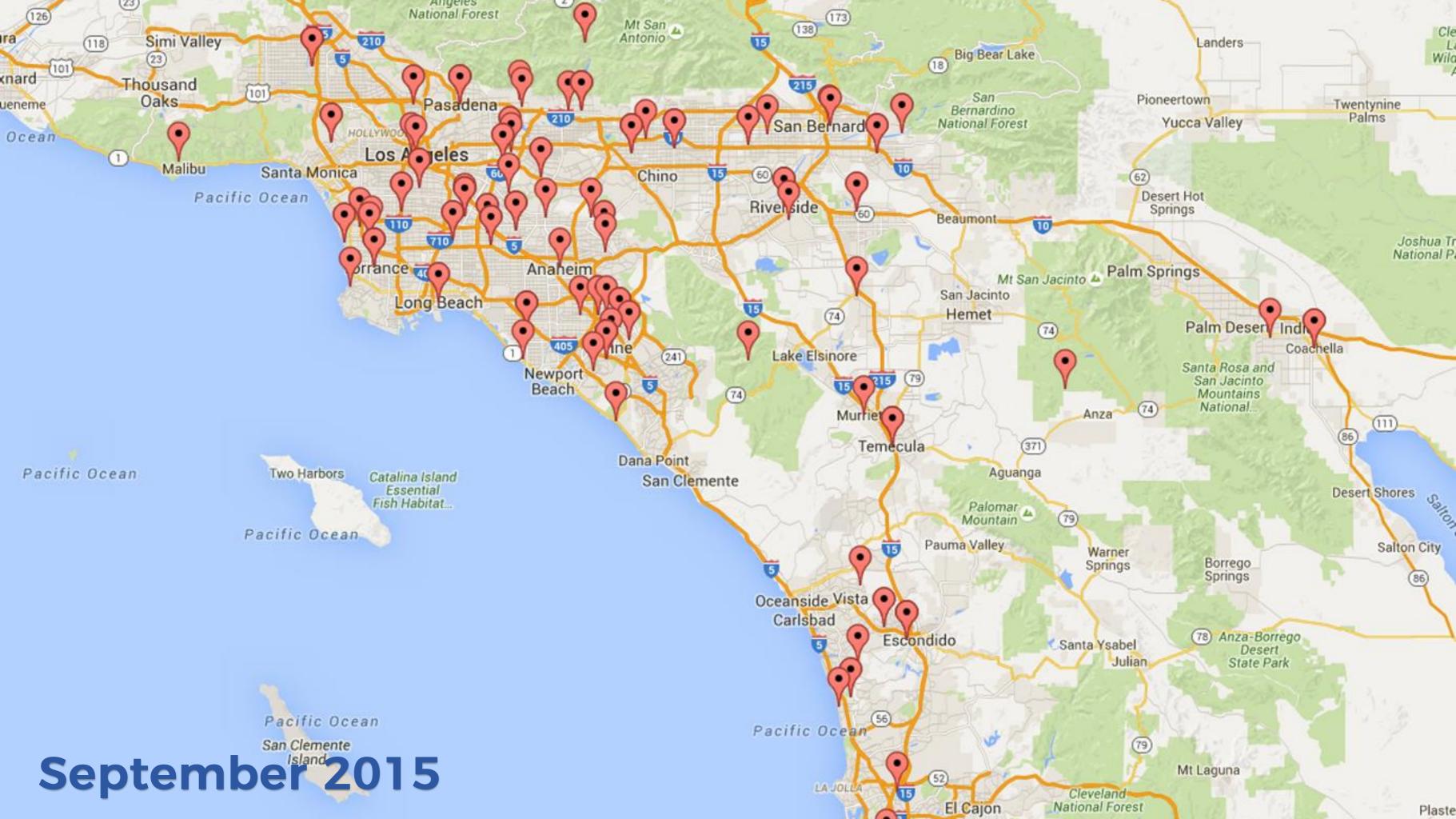


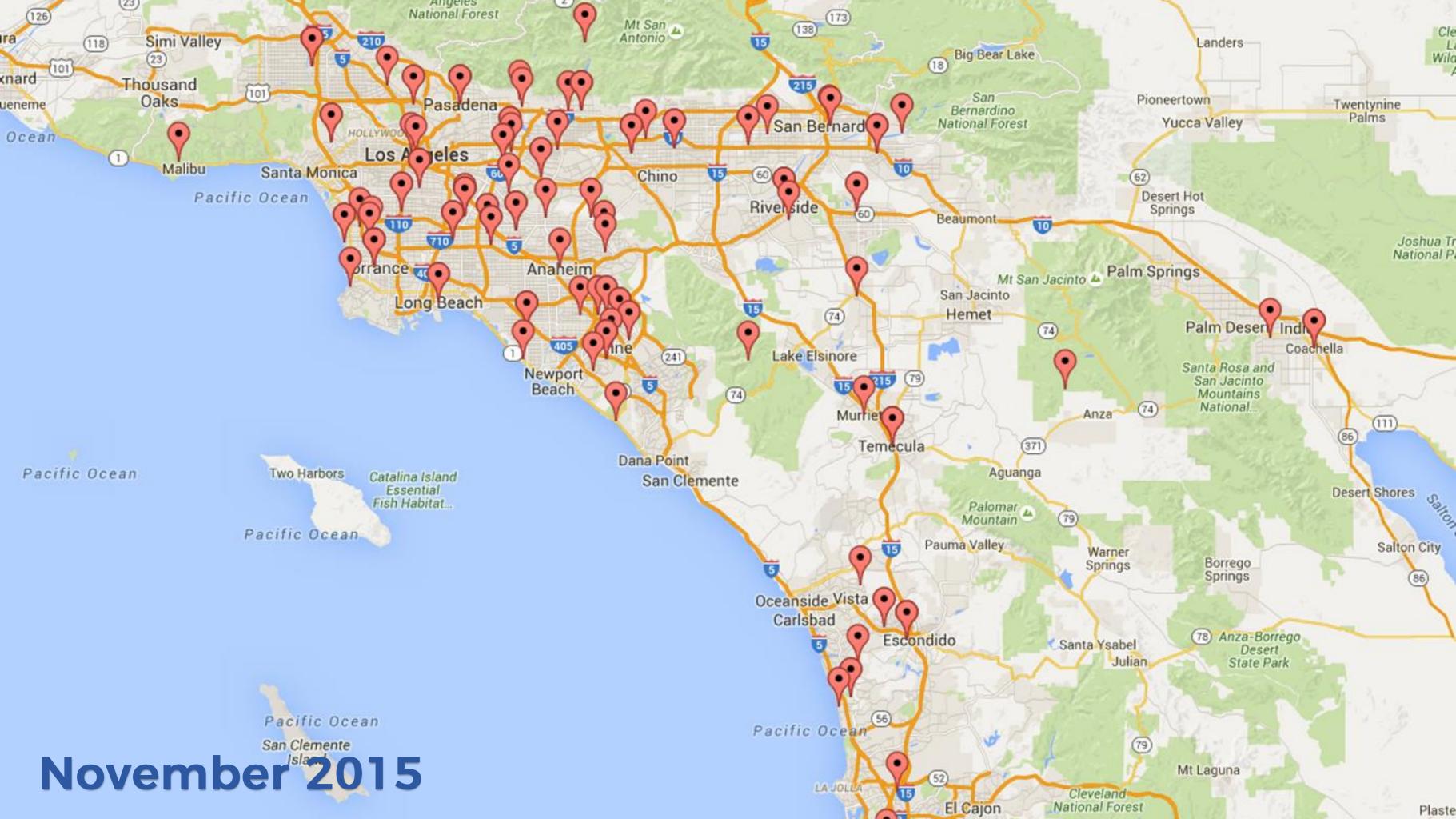


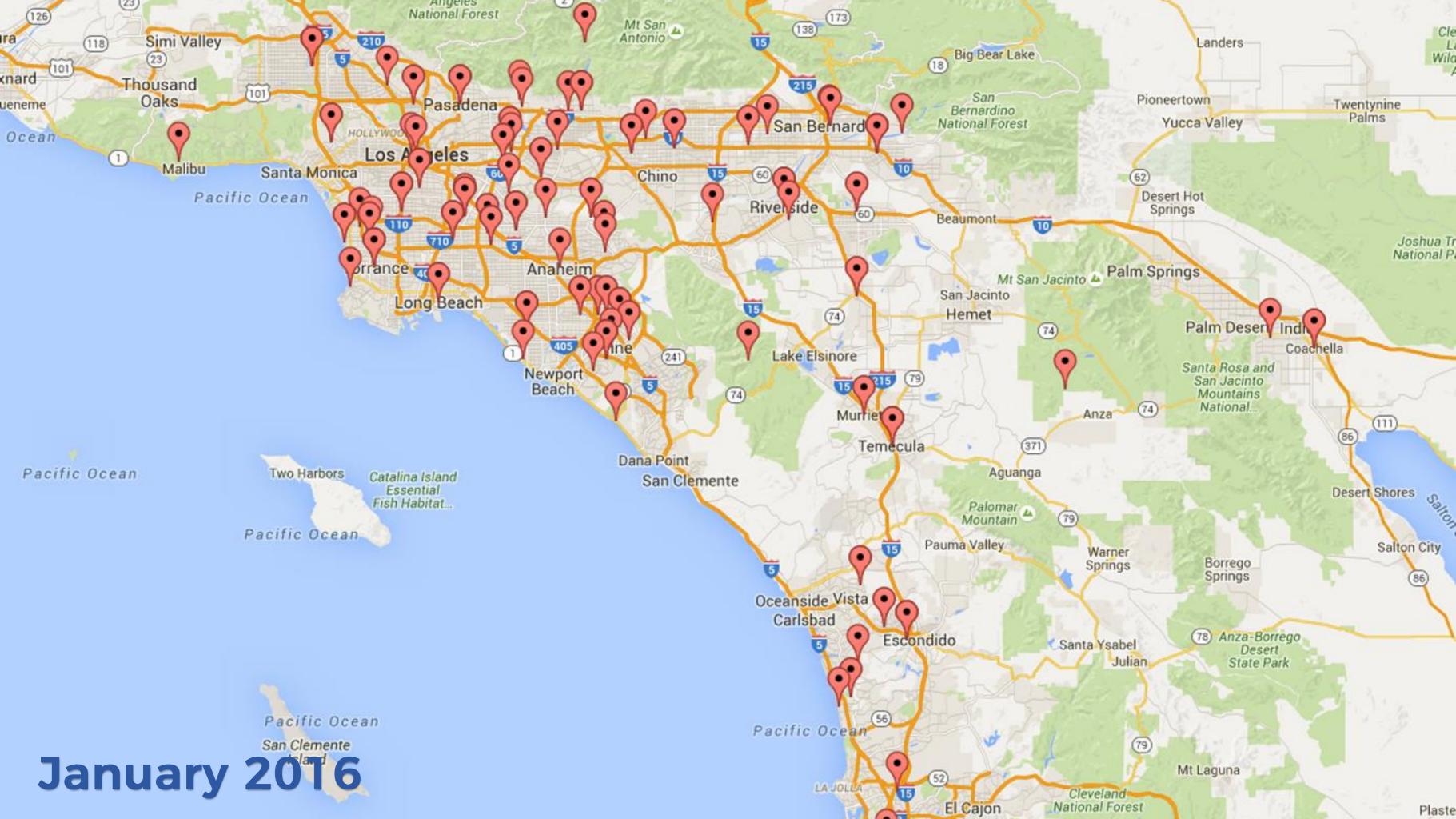


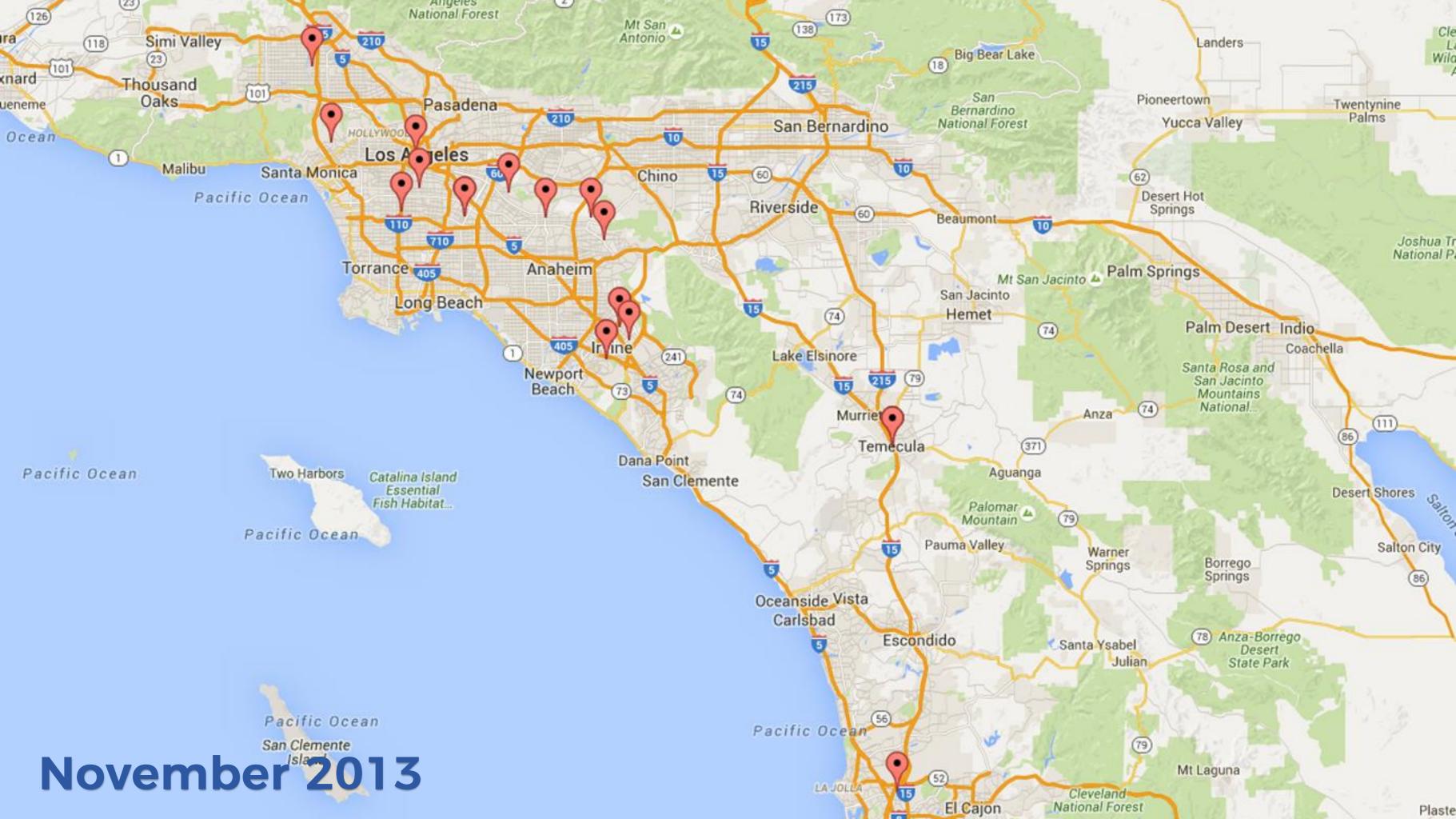








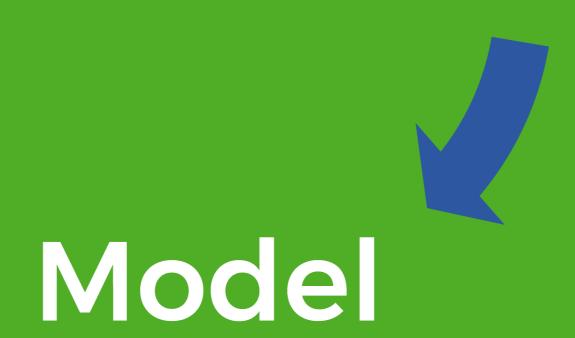


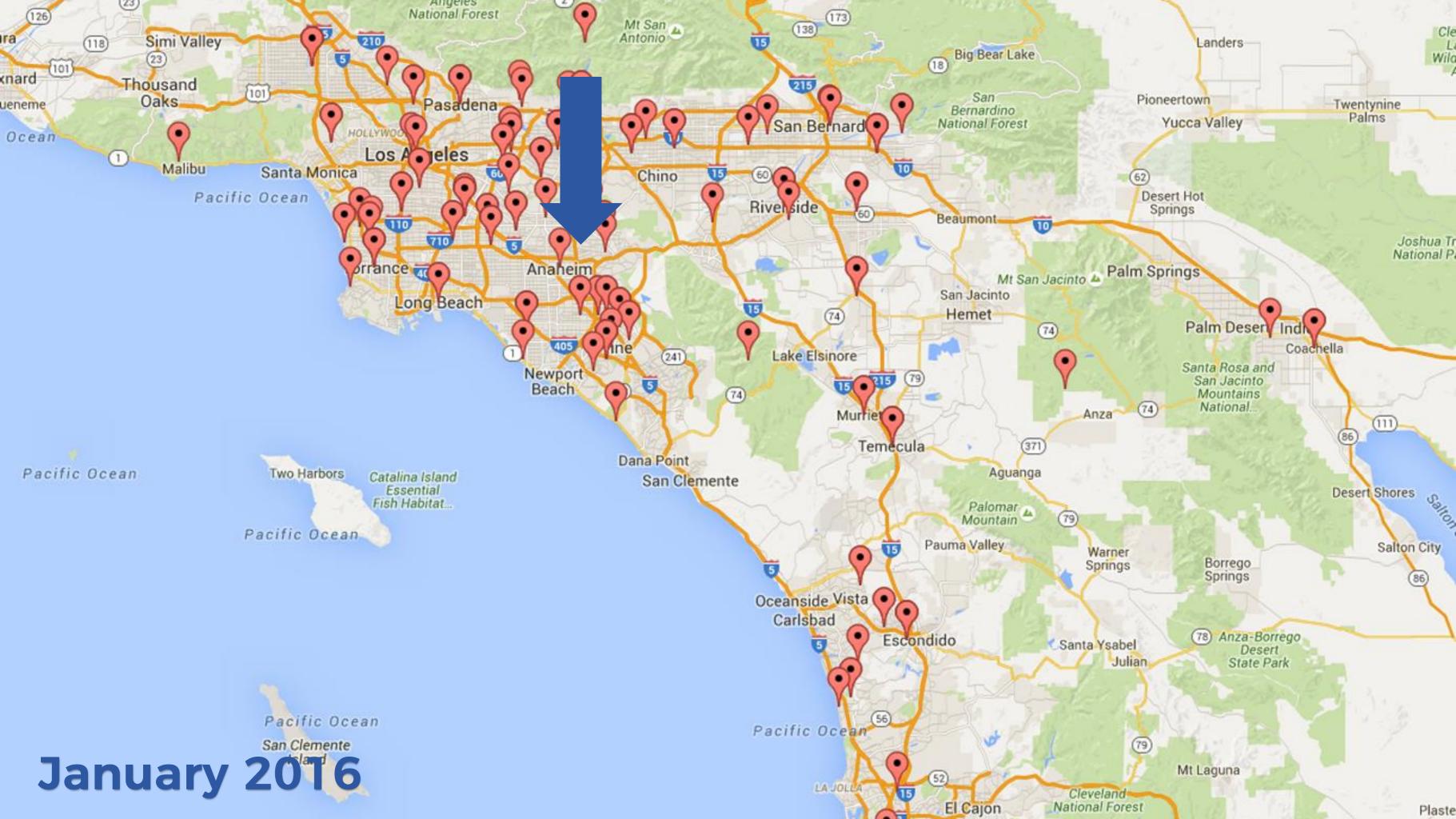


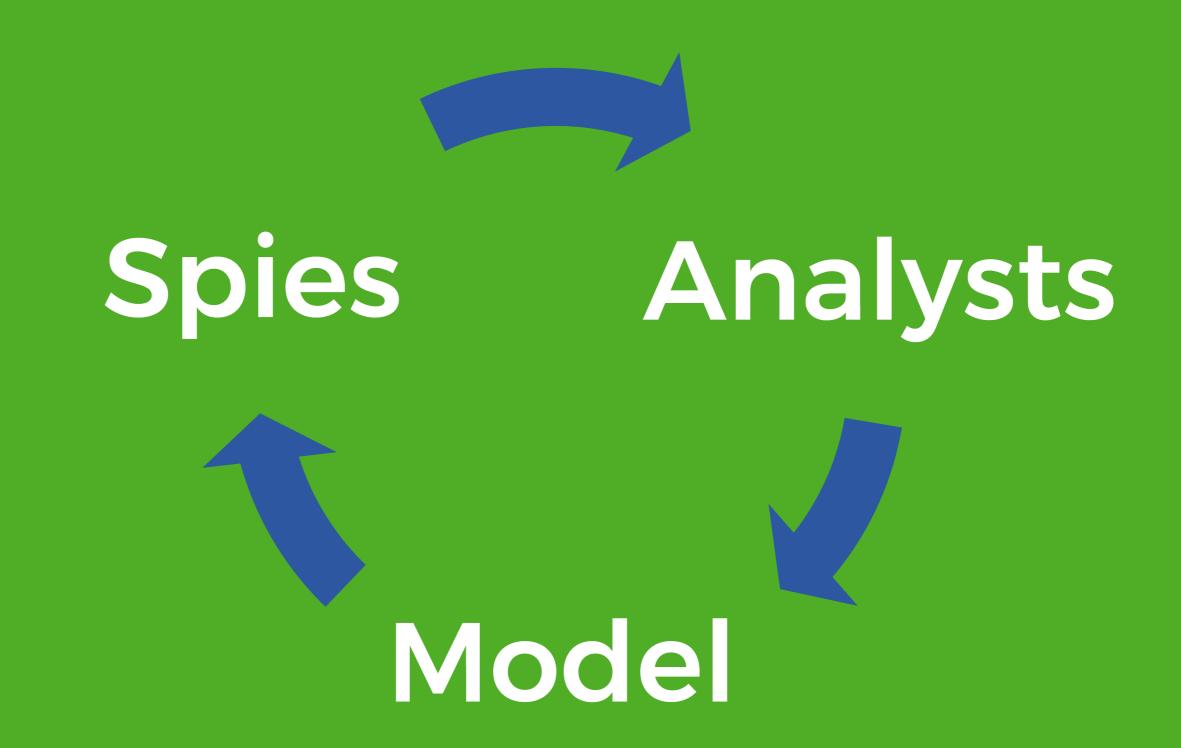


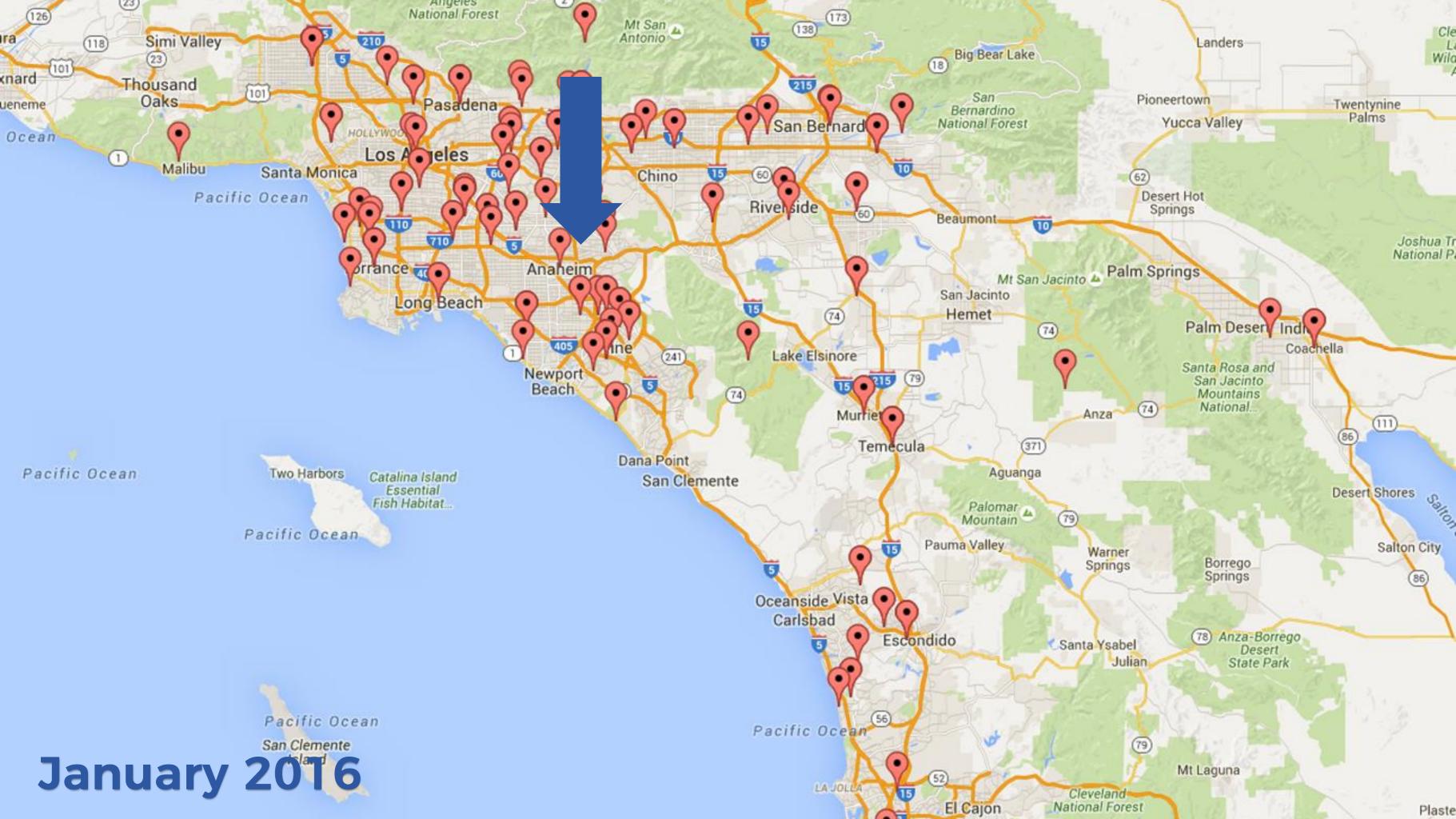
Spies

Analysts









All models are wrong, but some are useful.

GEORGE E. P. BOX



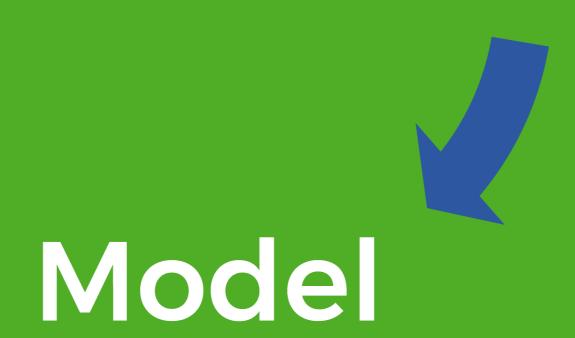
Classic Mix 20 Singles

LAY'S® Classic Potato Chips. DORITOS® Nacho Cheese Flavored Tortilla Chips. DORITOS® COOL RANCH® Flavored Tortilla Chips. CHEETOS® Crunchy Cheese Flavored Snacks. SUNCHIPS® Original Multigrain Snacks. FRITOS® Original Com Chips (All 1 OZ. Each)



Spies

Analysts





EASY TO STORE.



20 INDIVIDUAL BAGS: 1 OZ, EACH, TOTAL NET WT. 20 OZ. (1 LB. 4 OZ.) 567 g & WARNING: PREVENT ENTANGLEMENT AND STRANGULATION. KEEP



Hey #MTBoS, can you do me a favor and complete this 3 question anonymous survey about your favorite chips? I need data for a presentation. Please RT.

goo.gl/forms/etPtujll... #iteachmath



Favorite Chips

Please complete this anonymous survey. I'll be using this data in a presentation.

docs.google.com

8:05 PM - 4 Feb 2018

63 Retweets **45** Likes













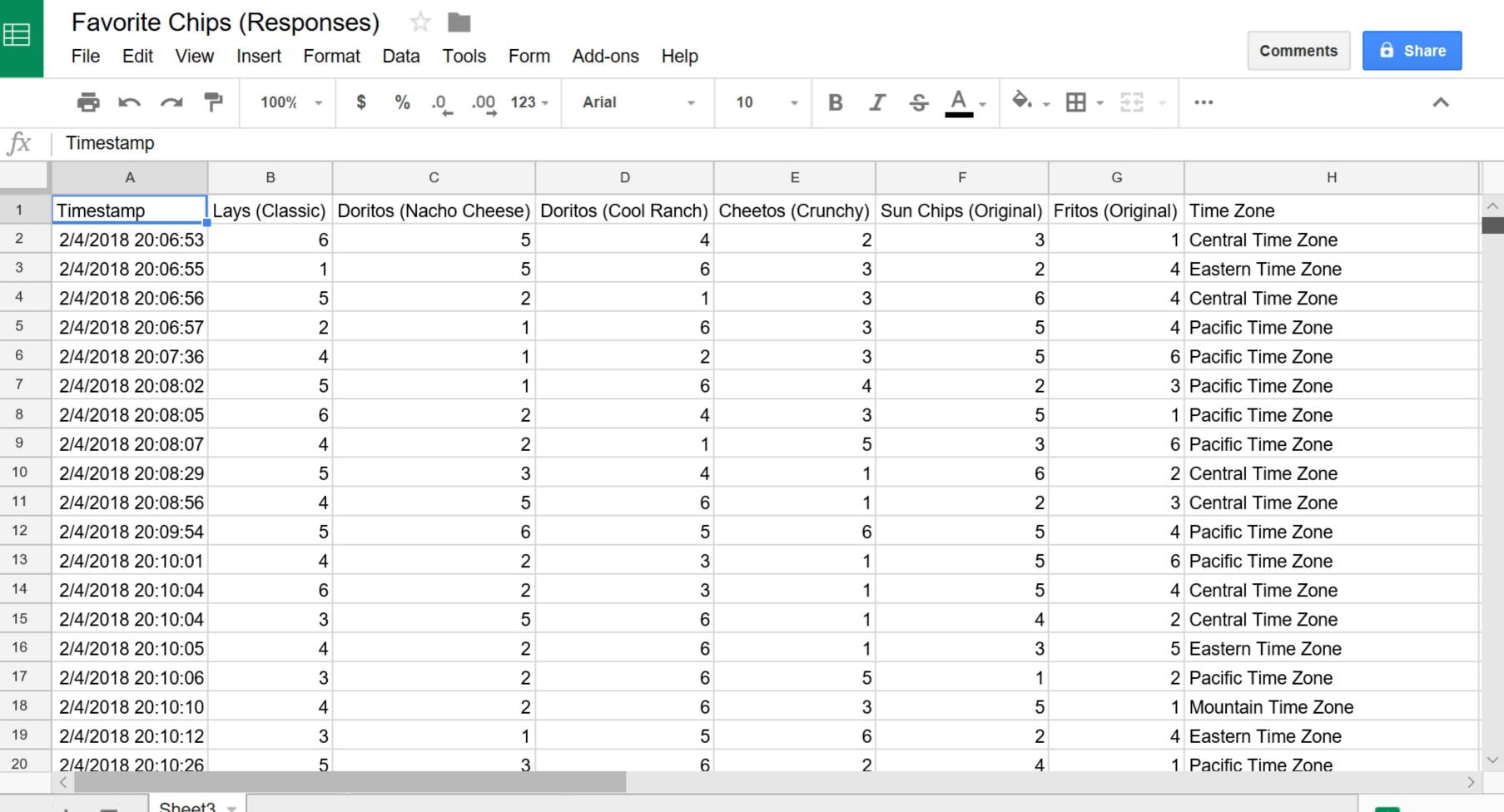






□ 18 □ 63 □ 45





THINKING TIME

- · The available data includes:
 - Lays, Nacho Cheese Doritos, Cool Ranch Doritos, Cheetos, Sun Chips, and Fritos ranked from 1 to 6
 - Geographic region: West, Central, or Eastern

ANALYSTS' JOB FOR THE TOP 1

- 1. Count all the first place votes for each chip type.
- 2. Divide the total first place votes for each chip type by the total number of votes.
- 3. Multiply that fraction by 20 to find how many bags there would be in a twenty pack, rounding as necessary.

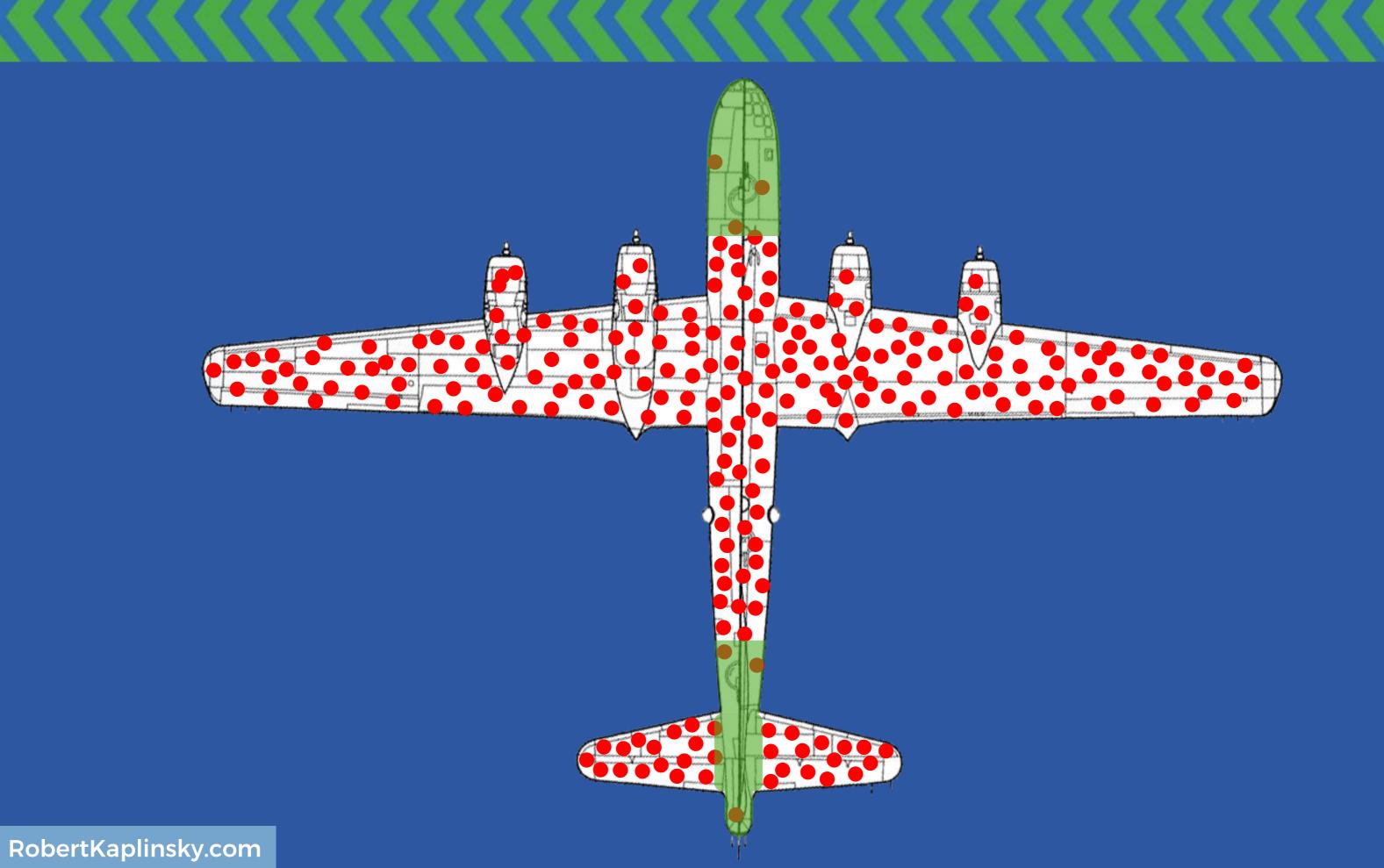
ANALYSTS' EXAMPLE

CHIP BAG RESULTS

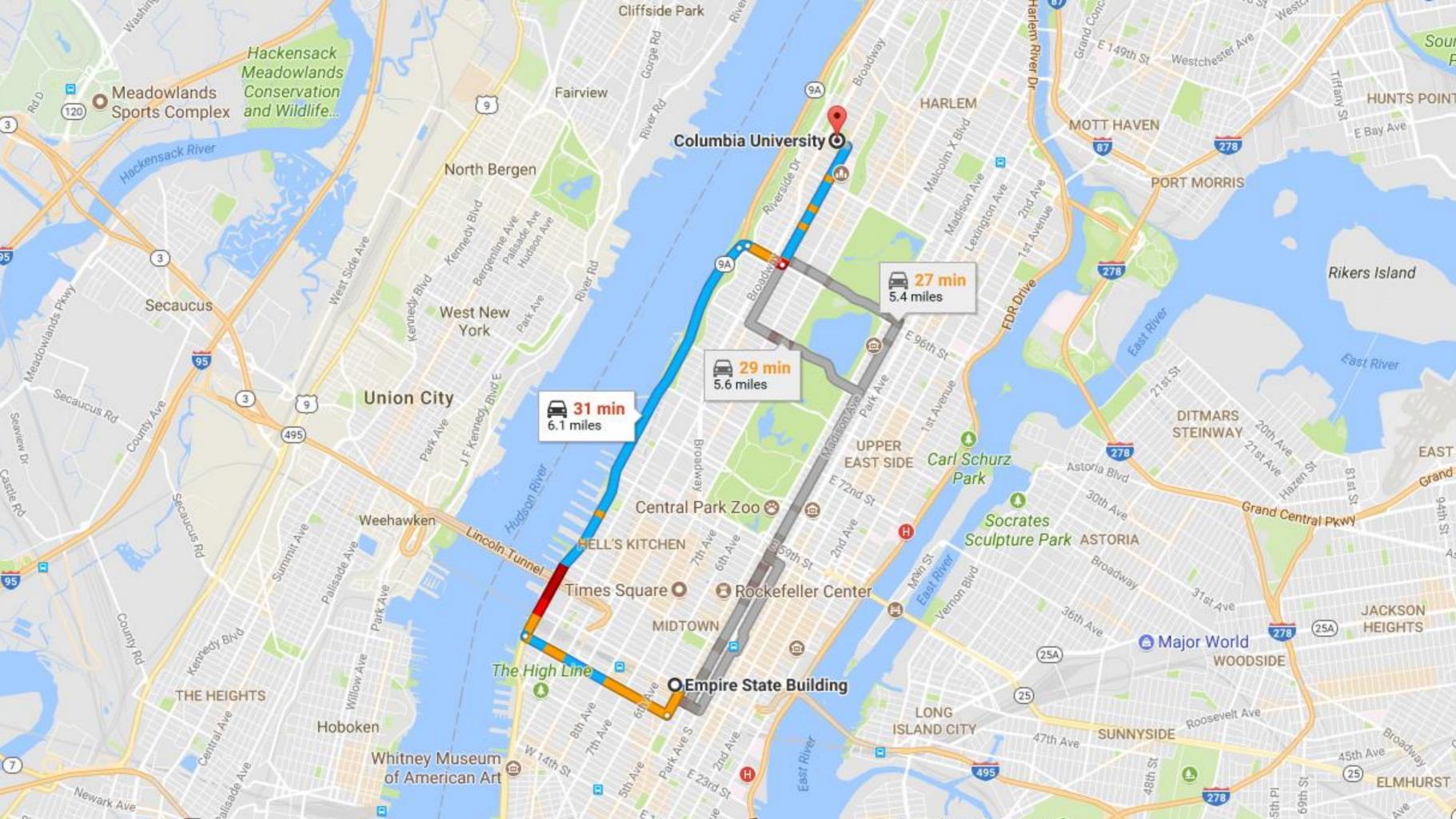
GOALS

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- · How do we protect our planes?
- Which parts of the plane are being hit by the most bullets?
- Which parts of the plane are the most critical to protect?



- How do we find the fastest route for each customer?
- How do we find the fastest route for each customer without impacting our other customers?



Classic Mix 20 Singles

4 LAY'S® Classic Potato Chips, 4 DORITOS® Nacho Cheese Flavored Tortilla Chips, 2 DORITOS® COOL RANCH® Flavored Tortilla Chips, 4 CHEETOS® Crunchy Cheese Flavored Snacks, 2 SUNCHIPS® Original Multigrain Snacks, 4 FRITOS® Original Com Chips (All 1 OZ. Each)

- How many of each flavor should we put in a package?
- How many of each flavor should we put in a package for each region?
- How can we determine if the extra cost of creating different packages will make us more money?

Mathematically proficient students who can apply what they know are comfortable making assumptions and approximations to simplify a complicated situation, realizing that these may need revision later.

CCSS MATH PRACTICE 4

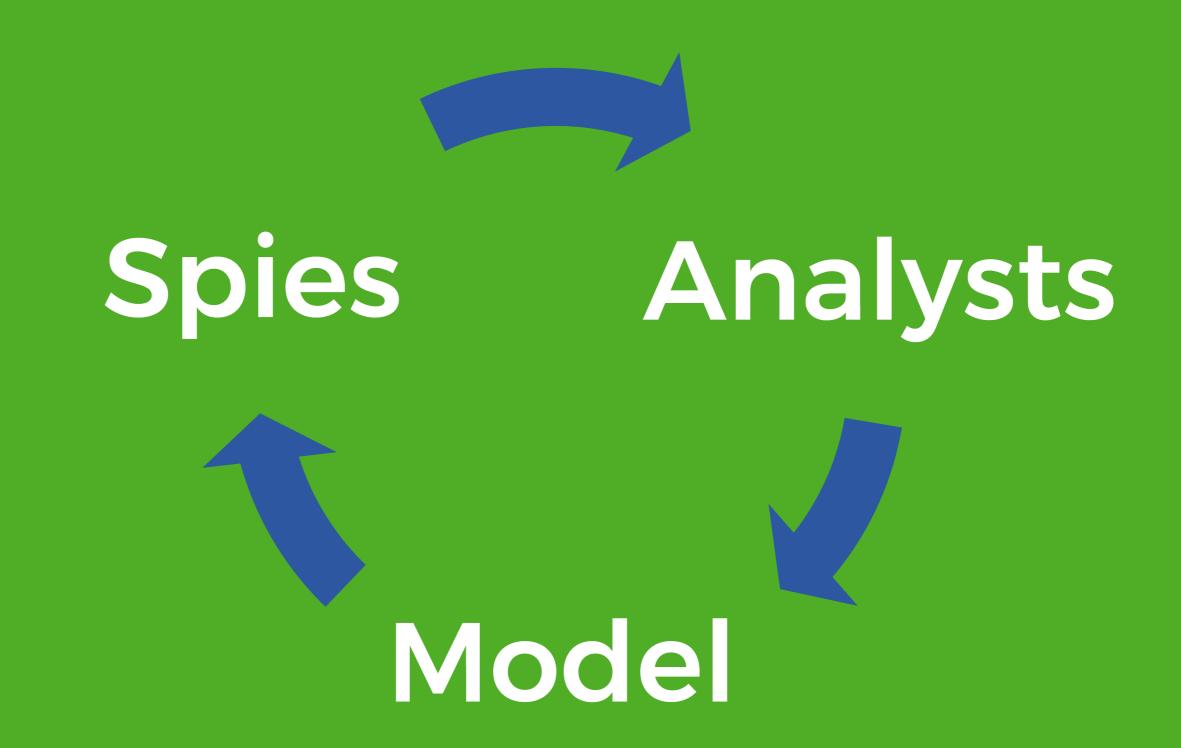
They routinely interpret their mathematical results in the context of the situation and reflect on whether the results make sense, possibly improving the model if it has not served its purpose.

CCSS MATH PRACTICE 4

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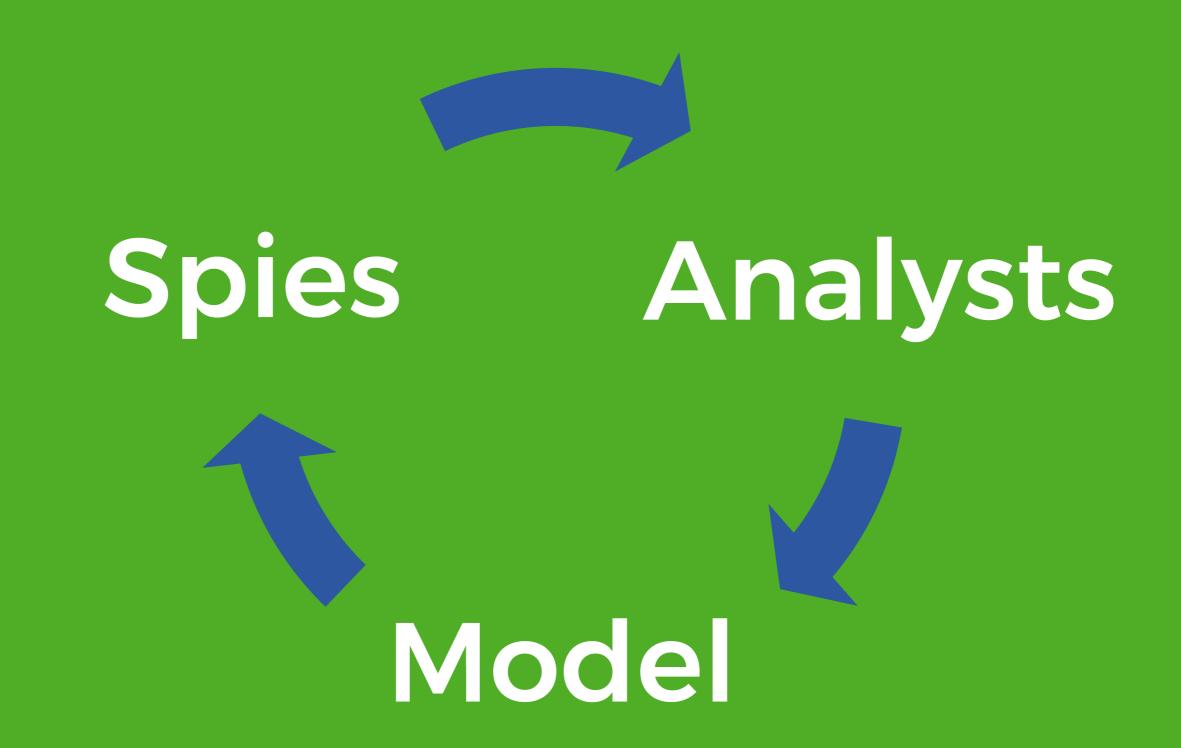


They used 25 products for a pregnancy prediction' score including:

- unscented lotion
- mineral supplements
- cotton balls

Source: New York Times

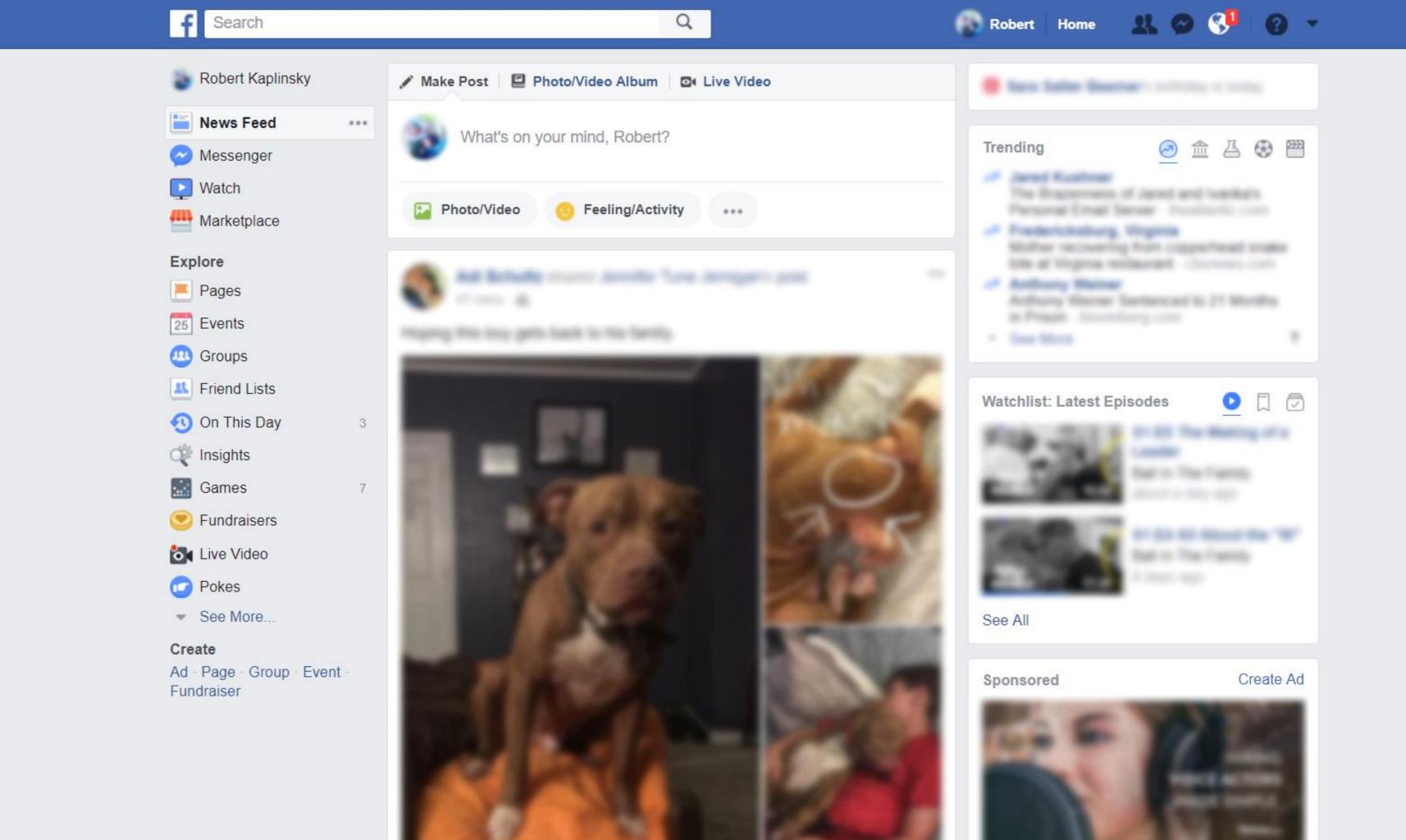


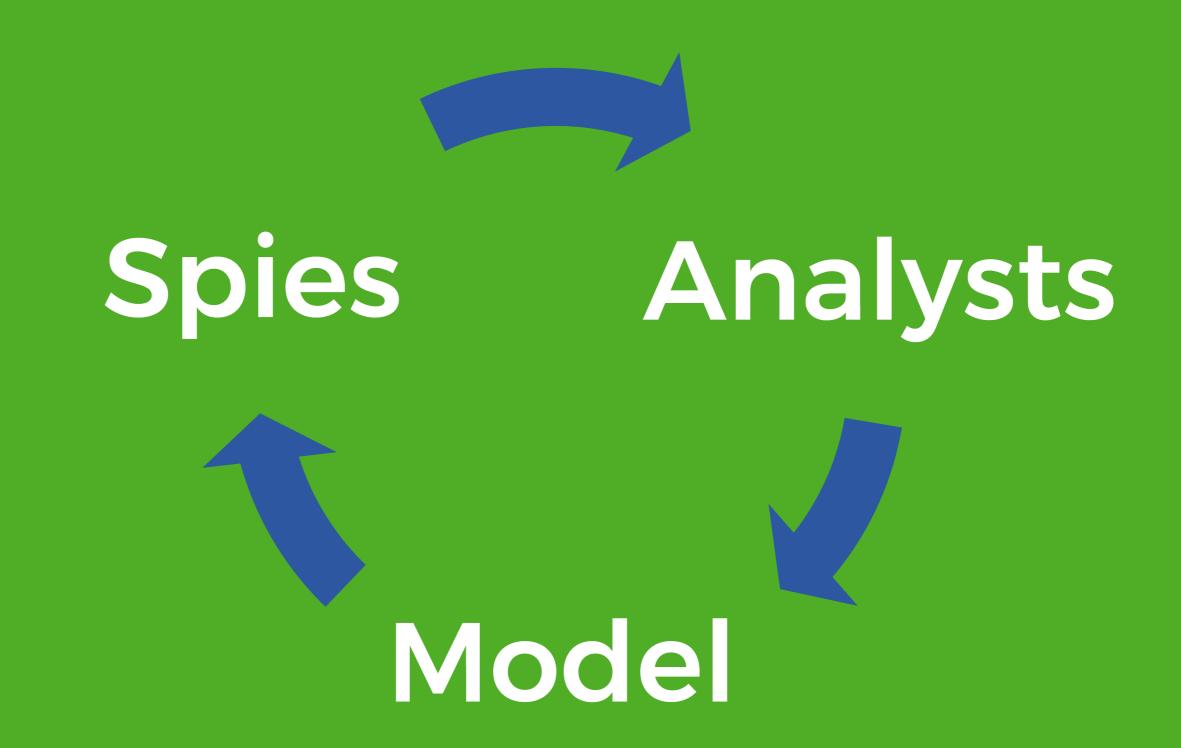


Priority is determined by:

- · passenger's fare class
- itinerary
- frequent flyer program membership
- check-in time

Source: United Airlines

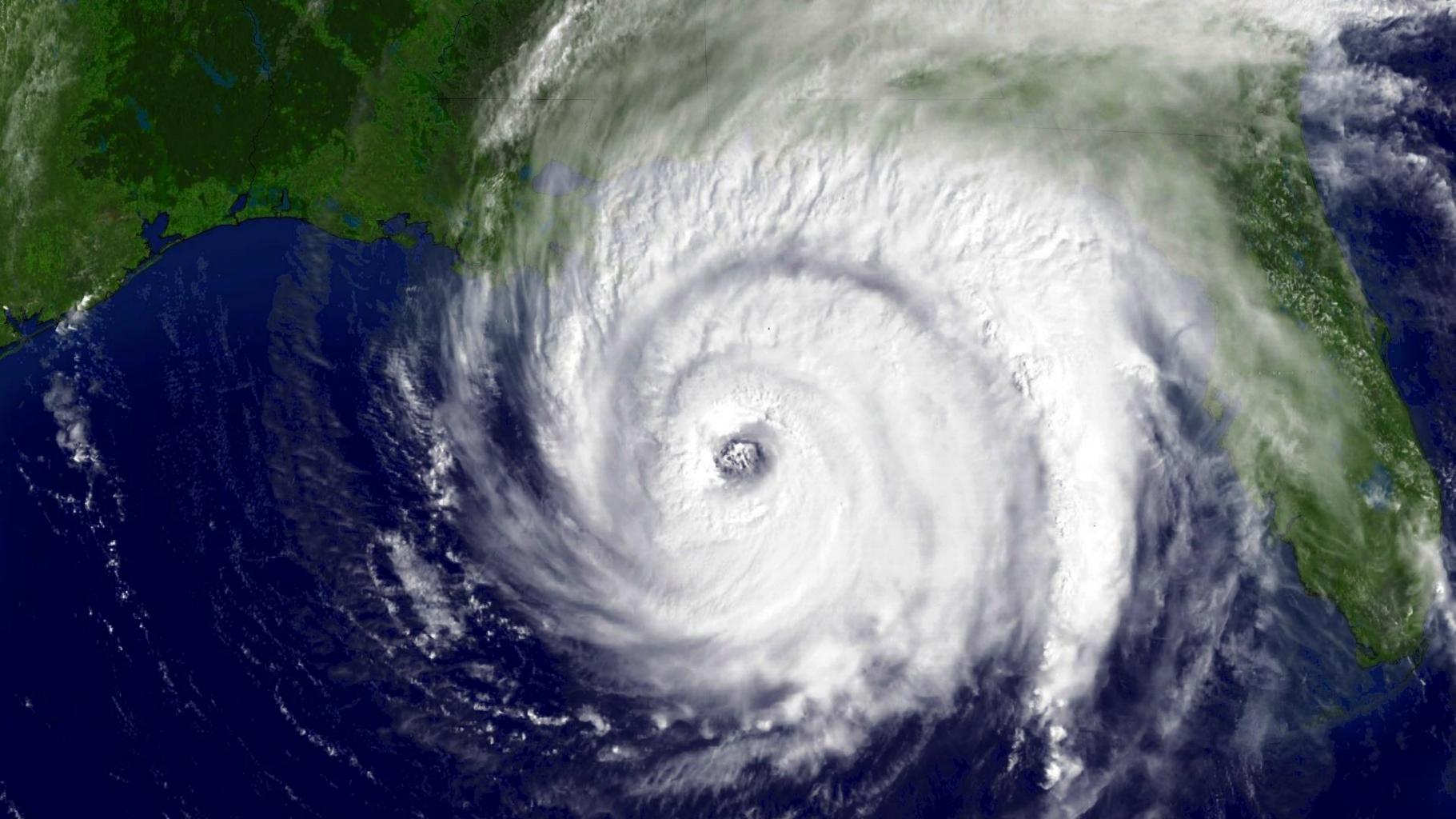


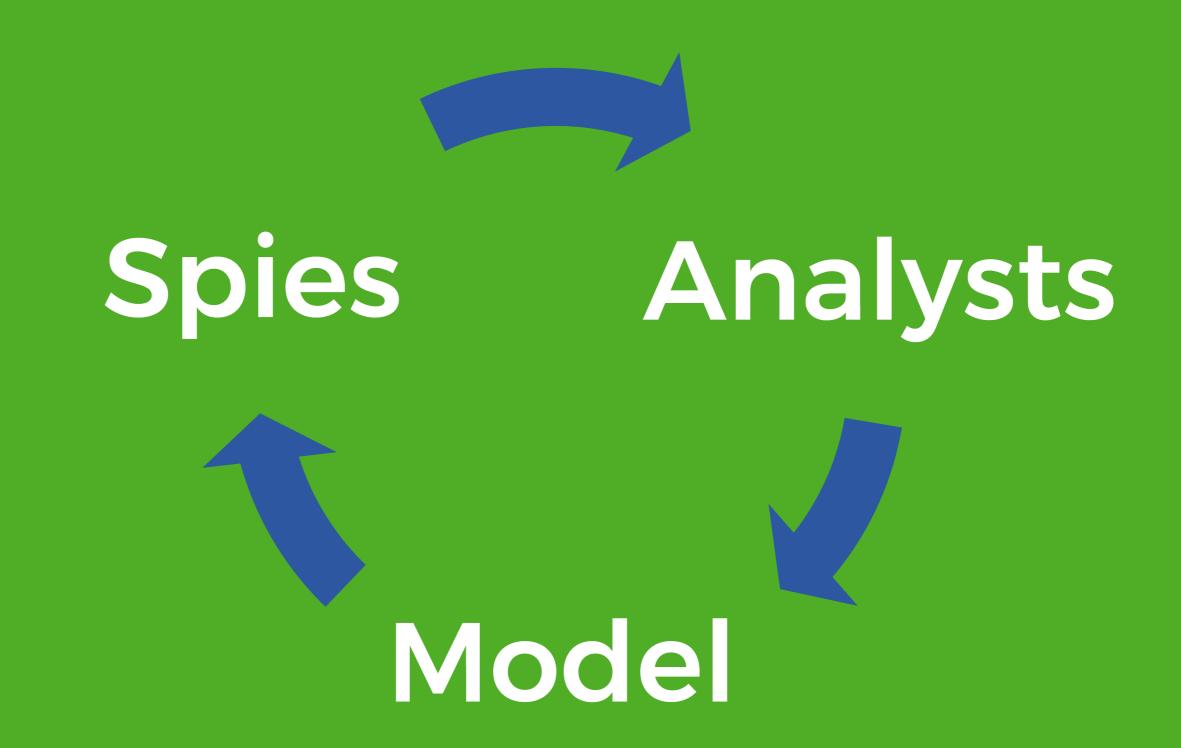


The stories that show in your News Feed are influenced by:

- friends you interact with the most
- the number of comments and likes a post receives
- what kind of story it is (ex: photo, video, status update)

Source: Facebook







The index has three levels:

- Green: full menu restaurant has power and damage is limited.
- Yellow: limited menu no power or only power from a generator, or food supplies may be low.
- Red: the restaurant is closed indicating severe damage.

Source: Wikipedia

MORE EXAMPLES

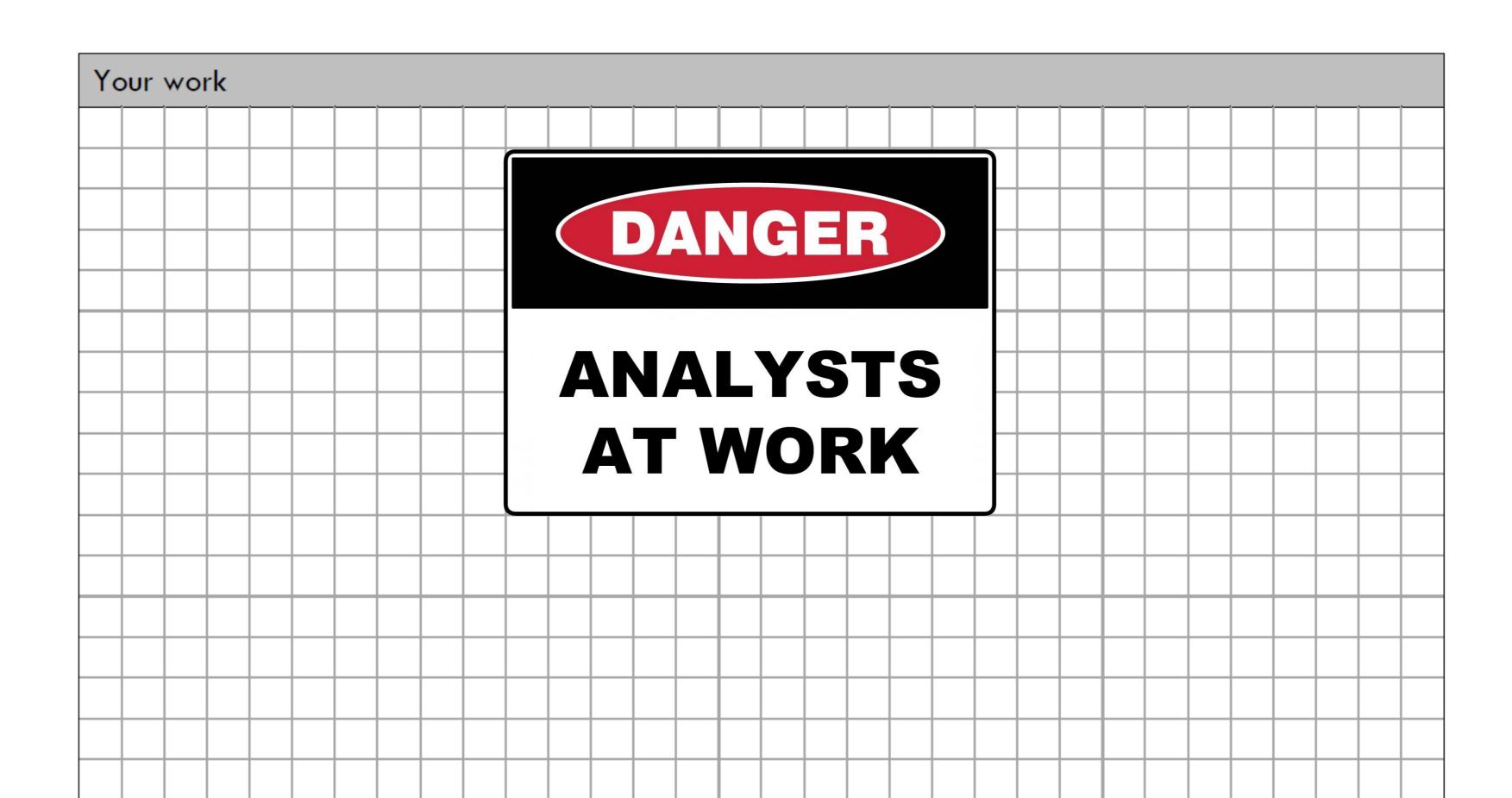
- How does US News and World Reports rank colleges?
- How does Google know which results to show?
- How do sports teams know who to draft?
- How does Amazon know what products to recommend?
- How does Zillow estimate home prices?
- How does Pandora know what music to play?
- How does eHarmony know which people to show you?
- How do they figure out who should speak at a conference?

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Name:	lame:	Period:	Date:
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What problem are you trying to figure out?	What estimates do you have?
	low
	Place your estimate on the number line.
What info do you already know about the problem?	What info do you need to out the problem?
What info do you already know about the problem? TOP SECRET!	SPIES

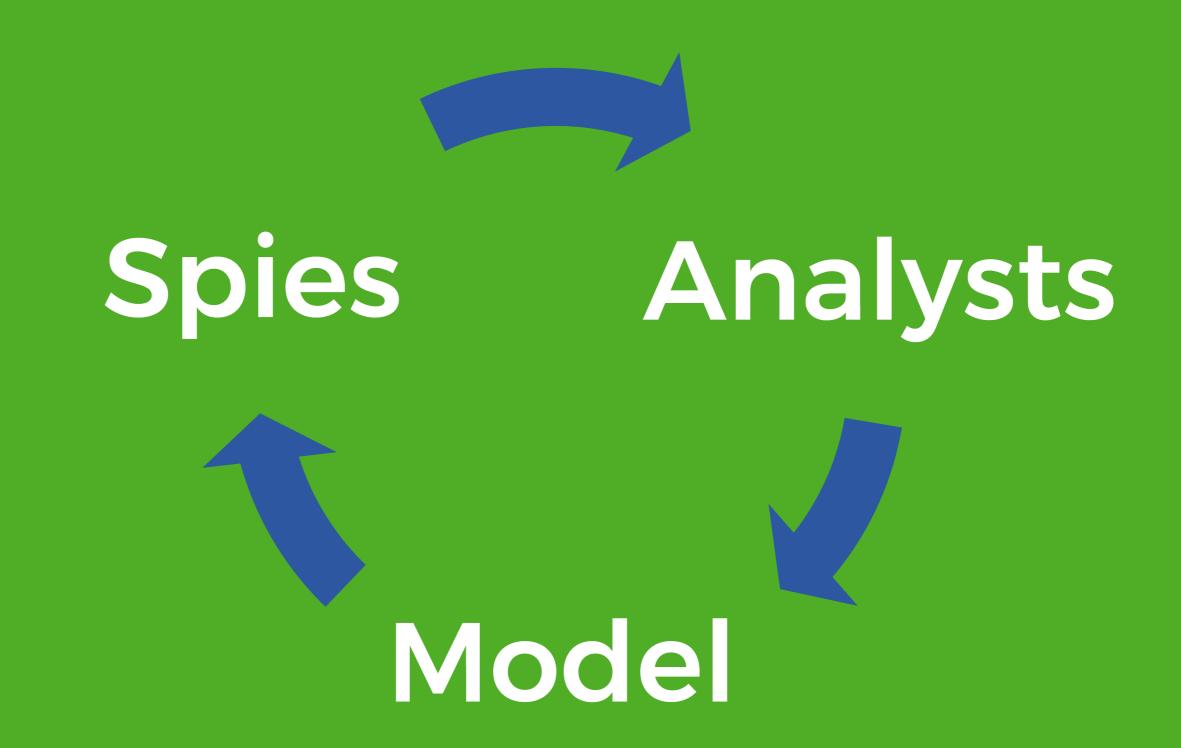


MODELING EXAMPLES

D ELEMENTARY SCHOOL

- D MIDDLE SCHOOL
- HIGH SCHOOL



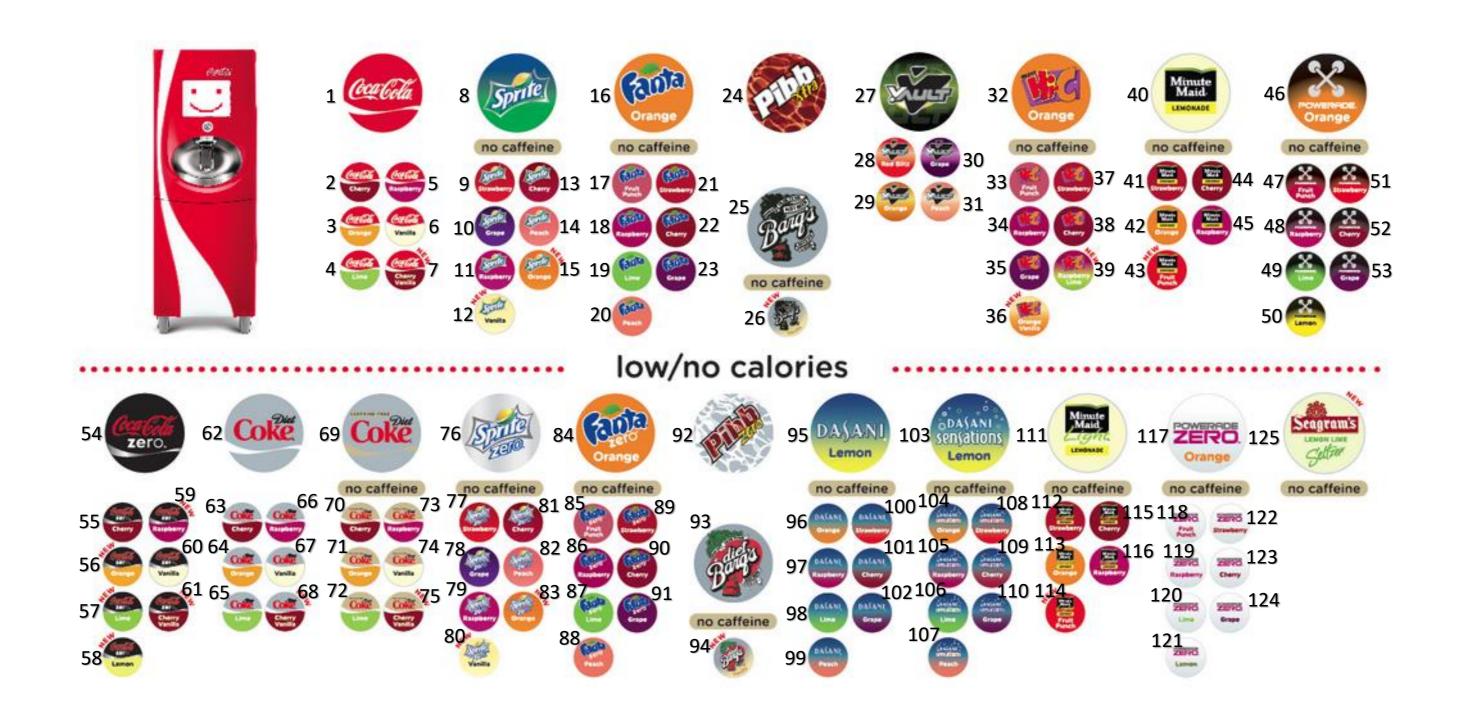




	Name:	Period:	Date:
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What problem are you trying to figure out?	What estimates do you have?
How many beverage choices are there ?	low high
	Place your estimate on the number line.
What info do you already know about the problem?	What info do you need about the problem?
 There are main flavors and added flavors. Lemonade is yummy. 	 How many main flavors are there? How many added flavors are there? Can we mix them all together?

COUNTALL

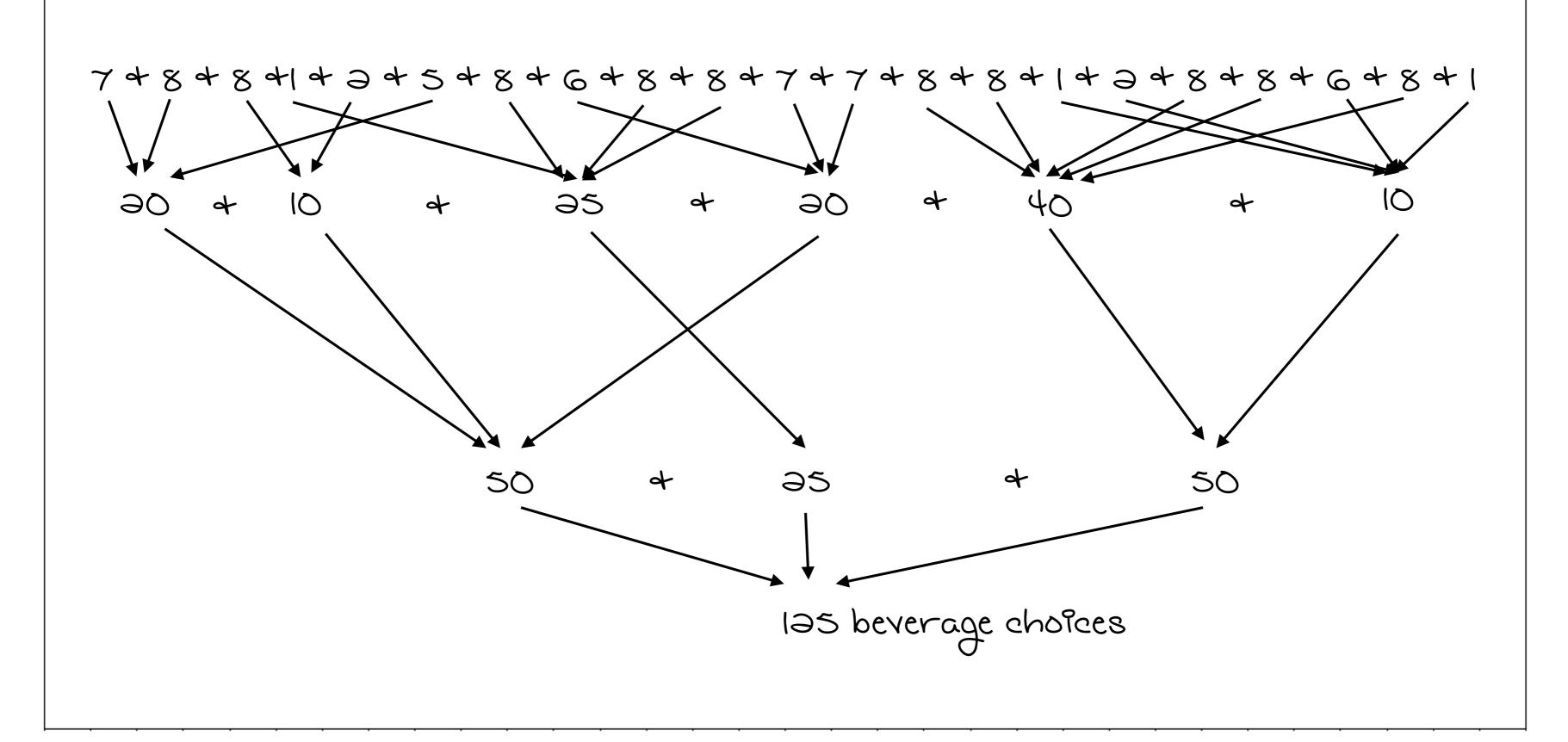


COUNT GROUPS



INVENTED STRATEGY





The main attraction for a busload of Dover fifth-graders was supposed to be the Museum of Fine Arts, but that all changed when they stopped by Kelly's Roast Beef and got a glimpse of their soda-drinking future.

At the entrance of Kelly's sat a sleek Coca-Cola Freestyle fountain crafted to resemble an old-fashioned vending machine, but with a twist: a touchscreen computer embedded in the machine gives customers the option of 125 flavors. You can quench your thirst with a Coke or a Sprite, or try something more exotic — Sprite with Grape or a Hi-C Orange Vanilla.

MODELING EXAMPLES

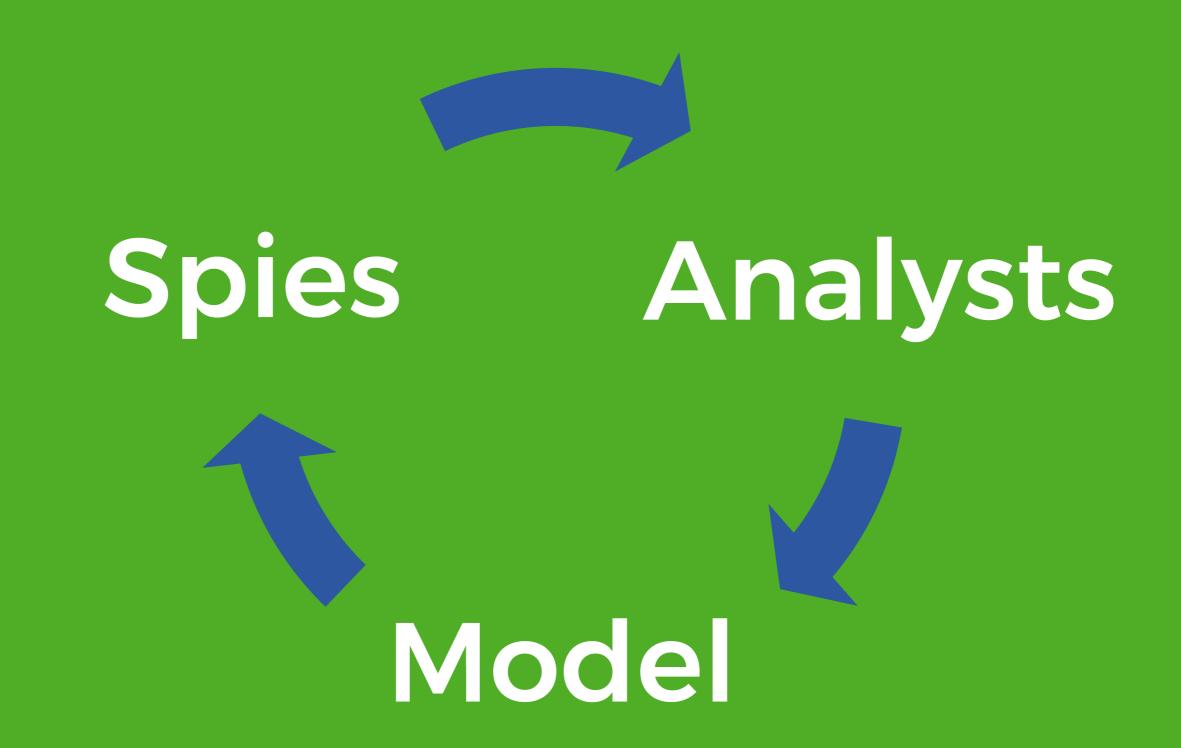


D MIDDLE SCHOOL

HIGH SCHOOL









Name:	Period:	Date:
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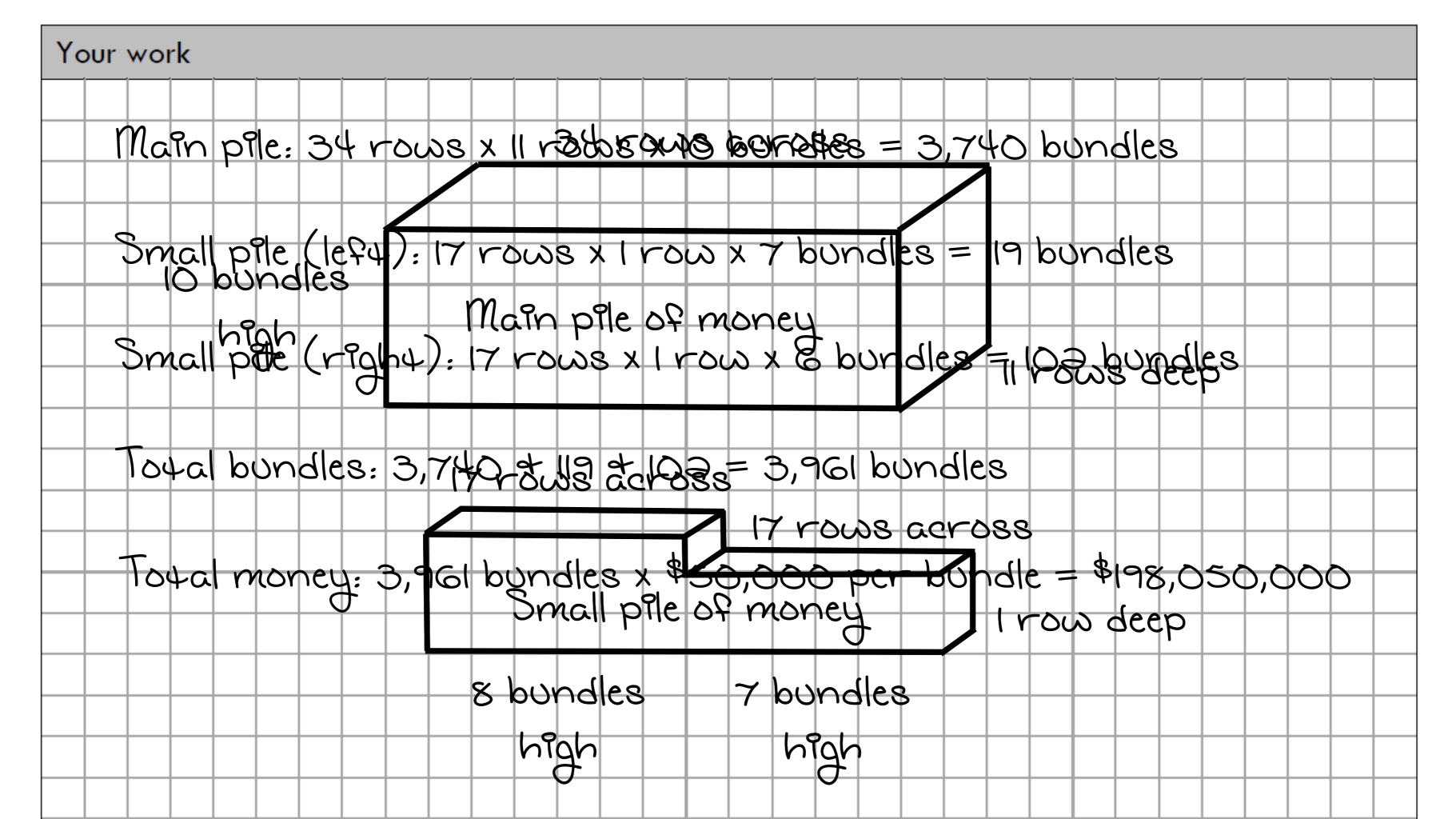
What problem are you trying to figure out?	What estimates do you have?
How much money was 4ha43	No shigh
	Place your estimate on the number line.
What info do you already know about the problem?	What info do you need about the problem?
· There 9s a lot of money.	• Is 94 all the same
· I4 98 9n a p9le.	denomination 3
· I4 98 9n bundles.	· How much does one bill
	weigh 3
	· How much does all the
	money weigh?

Vame:	Period:	Date:

What problem are you trying to figure out?	What estimates do you have?
How much money was 4ha43	low high
	Place your estimate on the number line.
What info do you already know about the problem?	What info do you need about the problem?
• There 9s a lot of money.	• Is 94 all the same
• I4 98 9n a p9le.	denomination 3
• I4 9s 9n bundles.	· How many rows and
	columns are 4here 3
	· How many bills are in one
	stach3









MODELING EXAMPLES



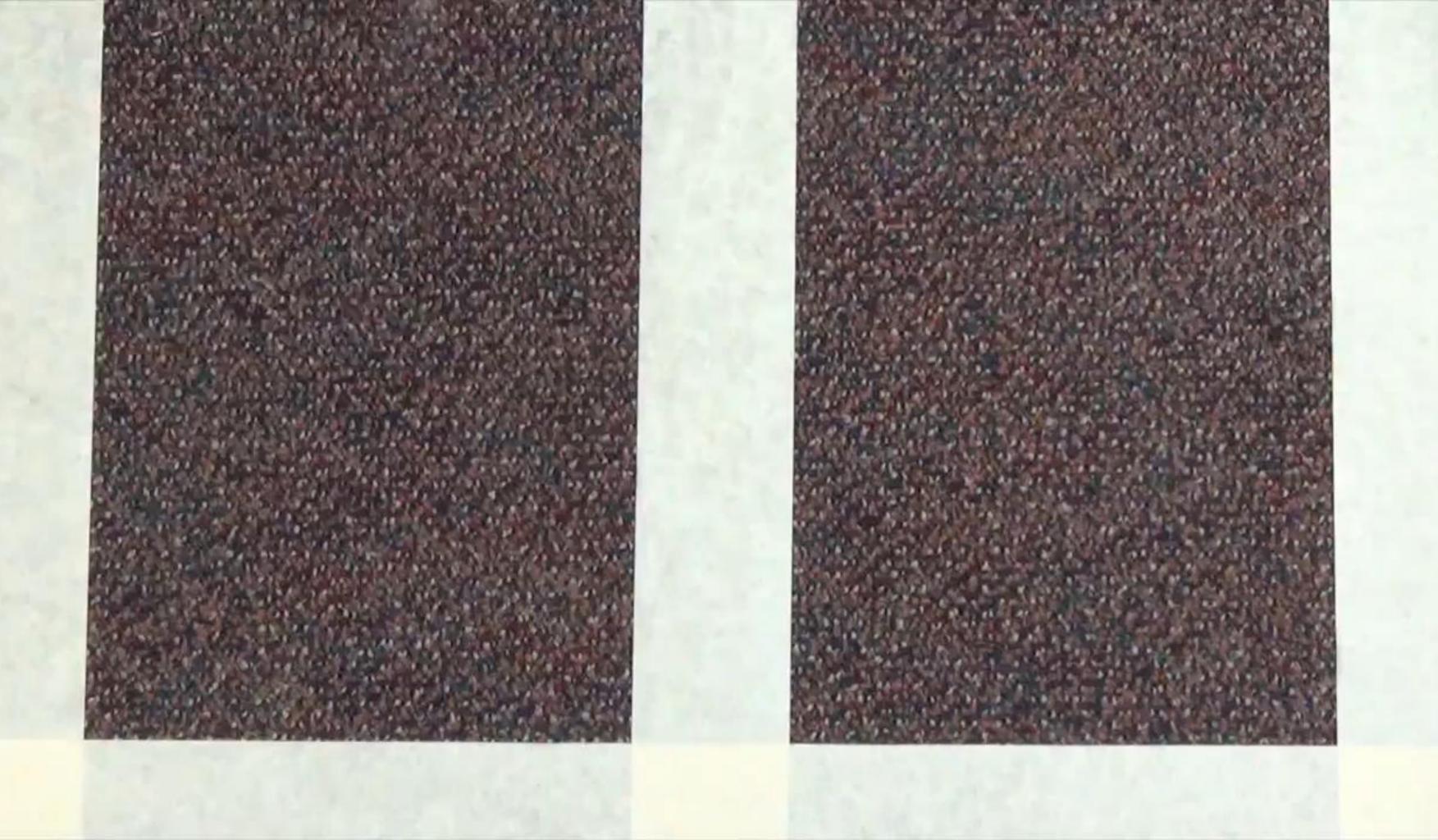
ELEMENTARY SCHOOL

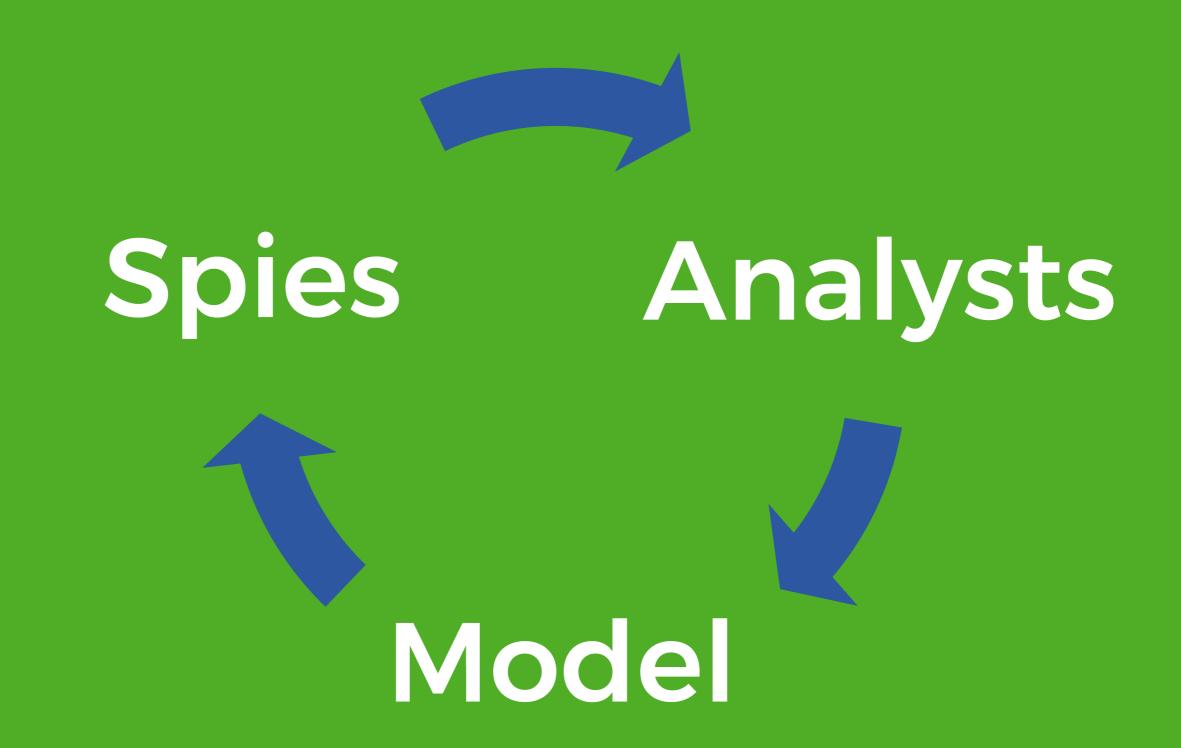


MIDDLE SCHOOL

HIGH SCHOOL









	Name:	Period:	Date:
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What problem are you trying to figure out?	What estimates do you have?
How much shorter are 20 layers of non-staggered pipes 3	1 S high (In Inches) Place your estimate on the number line.
What info do you already know about the problem?	What info do you need about the problem?
 One pile of pipes is staggered. One pile of pipes is not staggered. We have to compare 20 layers of each. 	 What are the dimensions of a pipe if What units are we using to measure?

What is your conclusion? How did you reach that conclusion?



Your work Non-staggered pipes Staggered pipes 3h 1 pipe = h cm 1 pipe = h cm a pipes = 33 cm a pipes = ah cm 3 pipes = 33 cm 3 pipes = 3h cm 20 pipes = 33 cm 20 pipes = 20h cm

MODELING EXAMPLES







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PBL RESOURCES

- Problem-based lesson search engine: robertkaplinsky.com/prbl-search-engine
- My lessons (Elementary, Middle, and High School) robertkaplinsky.com/lessons
- Dan Meyer (Middle and High School) threeacts.mrmeyer.com
- Andrew Stadel (Elementary and Middle School) www.estimation180.com/lessons.html
- Graham Fletcher (Elementary and Middle School) gfletchy.com/3-act-lessons

TAKE MY WORKSHOP



Home

Math resources that create problem solvers, not robots. Download my favorite lessons for elementary, middle, and high school. GET FREE LESSONS TAKE MY WORKSHOP

What happens next?



Keep coming back for more free lessons and resources.



Learn implementation tips from my blog and weekly emails.



Take my online workshop for more implementation support.



Lessons





How Much Money Were Those Pennies?



How Can We #SaveNelly?



How Many Chip Bags Will There Be?

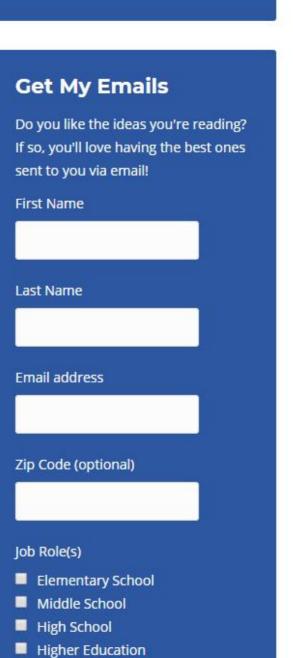








TAKE MY WORKSHOP



TAKE MY WORKSHOP



Resources

Depth of Knowledge

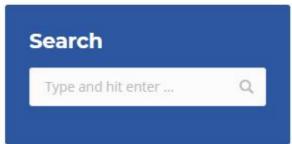
- Open Middle
- Open Middle Worksheet English (student version)
- Open Middle Worksheet English (document camera version)
- Open Middle Worksheet Spanish (student version)
- Open Middle Worksheet Spanish (document camera version)
- Robert's blog posts on Depth of Knowledge
- Tool to Distinguish Between Depth of Knowledge Levels

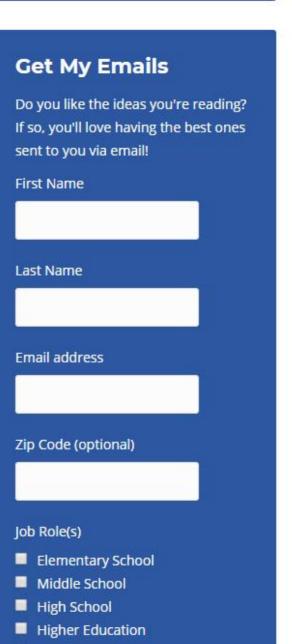
Problem-Based Lesson Tools

- Problem-Based Lesson Search Engine
- Problem Solving Framework v8.1
- Robert's blog posts on Problem-Based Learning

Problem-Based Lesson Sources

- 101 Questions
- Andrew Gael
- Andrew Stadel
- Catherine Castillo
- Christina Tondevold
- Dan Meyer
- Dane Ehlert





Sheet1 ▼

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fx									
	A	В	С	D	Е	F	G	Н	
1	Lesson	Concept / Skill	Standard 1	Standard 2	Standard 3	Standard 4	Standard 5	Standard 6	Stand 7
2	How Much Money Were Those Pennies?	Money, Multiplying Decimals, Proportions	4.MD.2	5.NBT.5	5. NBT.7	7.RP.3			
3	How Can We #SaveNelly?	Dividing Decimals	6.NS.3						
4	How Many Chip Bags Will There Be?	Ratio and Proportions, Population Sampling	6. RP.3	6. RP.3c	7.RP.2	7.RP.3	7.SP.1	7.SP.2	
5	How Can We Make Stronger Passwords?	Permutations, Combinations, Probability, Exponents, Exponential Growth	7.SP.8	8.EE.1	S-MD.7	S-CP.5	S-CP.9		
6	How Many Hot Dogs And Buns Should He Buy?	Least Common Multiple (LCM)	6.NS.4						
7	What Does 2000 Calories Look Like?	Unit Rates, Ratios, Solving Equations, and Solving Inequalities	6.EE.3	6.EE.4	6.EE.5	6.EE.6	6.EE.7	6.EE.8	6.RP.2
8	How Much Money Are The Coins Worth?	Decimal Operations and Coin Counting	2.MD.8	5. NBT.7	6.NS.3				
9	How Many Times Will A Case of Paper Jam?	Interpreting Percentages	6.RP.3c	7.RP.3					
10	How Many Soda Combinations Are There On A Coke Freestyle?	Counting, Composing, and Decomposing Numbers	K.CC.5	K.CC.6	K.OA.1	K.OA.2	K.OA.3	K.OA.4	K.NB
11	What Should The Freeway Sign Show?	Fractions on Number Lines, Converting Units, Decimal and Fraction Operations	3.NF.1	3. NF.2	3.NF.2a	3.NF.2b	3.NF.3	3.NF.3a	4.MD.
12	How Fast Was The Fastest Motorcycle Speeding Ticket Ever?	Converting Units and Unit Rates	5.MD.1	6. RP.3d	7.RP.1	N.Q.1			
13	How Much Did Patrick Peterson Lose By Not Cashing His Check?	Compound and/or Simple Interest	7.RP.3	N-RN.2	A-SSE.1	A-SSE.3c	A-SSE.4	A-REI. 11	F-IF.4
14	How Many Biscuits Can You Make?	Dividing Fractions and Mixed Numbers	5.NF.7	5.NF.7a	5.NF.7b	5.NF.7c	6.NS.1		
15	How Much Bigger Should They Make Zoolander's School?	Scale and Proportions	5.NF.5A	7.RP.2	7.G.1				
16	Where Is The Freeway Sign Located?	Identifying Fractions on a Number Line	3.NF.1	3. NF.2	3.NF.2a	3.NF.2b	3.NF.3	3.NF.3a	3.NF.3
17	How Far Apart Are Exits On A Ring Road?	Arc length measures	G-C.5						
18	How Much Is One Third Of A Cup Of Butter?	Identifying Fractions on a Number Line	3.NF.1	3.NF.2	3.NF.2a	3.NF.2b	3.NF.3	3.NF.3a	3.NF.3
19	How Do Skytypers Write Messages?	Transformations (Rotations, Reflections, Dilations, and Translations)	8.G.1	8.G.2	8.G.3	8.G.4	G-CO.2	G-CO.3	G-CO
20	How Big Is The Bermuda Triangle?	Coordinate Geometry: Area of Triangle	G-GPE.7						
21	What Fraction Of Children Are In The Right Car Seat?	Representing and Comparing Fractions	3.NF.1	3.NF.2	3.NF.3	4. NF.1	4. NF.2		
22	How Much Did The Temperature Drop?	Absolute Value	6.NS.7c	7.NS.1c					
23	How Much Shorter Are Staggered Pipe Stacks?	Circles, Pythagorean Theorem, trigonometric ratios, and linear functions	8.G.7	A-CED.1	A-CED.3	A-CED.4	A-SSE.1a	A-SSE.1b	A-SSI
24	How Do You Write A Check To Pay For Something?	Expanded Form	2.NBT.3	4. NBT.2	5.NBT.3a				
25	How Can We Correct The Scarecrow?	Pythagorean Theorem	8.G.6	G-SRT.4					
26	How Much Does A 100×100 In-N-Out Cheeseburger Cost?	Building and Interpretting Linear Functions	8.F.1	8. F.3	8.F.4	8.F.5	F-IF.4	F-IF.5	F-IF.6
27	How Can We Water All Of The Grass?	Circles, Pythagorean Theorem, trigonometric ratios	7.G.4	8.G.7	G-SRT.8	G-MG.1	G-MG.3		
28	How Much Money IS That?!	Volume of rectangular prism	5.MD.3	5.MD.4	5.MD.5	5.MD.5b	5.MD.5c	6.G.2	7.G.6
29	How Much Money Should Dr. Evil Demand?	Exponential Growth	N-RN.2	A-SSE.1	A-SSE.3c	A-SSE.4	A-REI. 11	F-IF.4	F-IF.7
30	How Tall Is Mini-Me?	Scale and Dividing Decimals	5. NF.5	5.NF.5a	5. NF.5b	6.NS.3			
31	How Did They Make Ms. Pac-Man?	Transformations (Rotations, Reflections, and Translations)	8.G.1	8.G.2	8.G.3	8.G.4	G-SRT.2	G-CO.4	G-CO
32	Which Ticket Option Is The Best Deal?	Unit Rates and Ratios	6.RP.2	6.RP.3	6.RP.3a	6.RP.3b			
33	How Far Apart Are The Freeway Exits?	Fractions on a Number Line and Subtracting Fractions	3.NF.2	3.NF.2b	4. NF.2	4. NF.3a	4. NF.3c	4. NF.3d	5.NF.1
34	Do We Have Enough Paint?	Area	3.MD.5	3.MD.6	3.MD.7				
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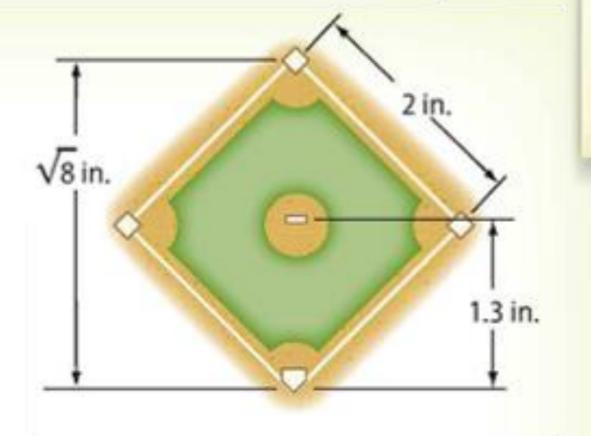
GOALS

- M HOW DO WE MAKE SENSE OF MATH MODELING?
- IS IT JUST ANSWERING QUESTIONS?
- M HOW DO YOU PROFIT FROM MATH MODELING?
- M HOW DO WE HELP OUR STUDENTS IMPROVE?
- WHERE CAN WE FIND MORE RESOURCES?



Sports Major League baseball has rules for the dimensions of the baseball diamond. A model of the diamond is shown.

 On the model, the distance from the pitching mound to home plate is 1.3 inches. Is 1.3 a rational number? Explain.





8.NS.1, 8.NS.2, 8.EE.2

Mathematical Practices 1, 3, 4, 6

On the model, the distance from first base to second base is 2 inches. Is 2 a rational number? Explain.

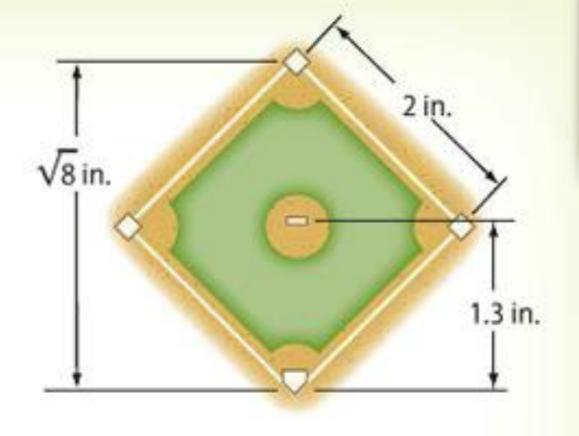
3. The distance from home plate to second base is $\sqrt{8}$ inches. Using a calculator, find $\sqrt{8}$. Does it appear to terminate or repeat?





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Scary & Dangerous







MATH MODELING CAN

MAKE YOU FILTHY RICH

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