## MATH MODELING CAN

## MAKE YOU FILTHY RICH

## ROBERT KAPLINSKY

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## 

Sports Major League baseball has rules for the dimensions of the baseball diamond. A model of the diamond is shown.

1. On the model, the distance from the pitching mound to home plate is 1.3 inches. Is 1.3 a rational number? Explain.


## Content Standards

8.NS.1, 8.NS.2, 8.EE. 2

Mathematical Practices
1, 3, 4, 6
2. On the model, the distance from first base to second base is 2 inches. Is 2 a rational number? Explain.
3. The distance from home plate to second base is $\sqrt{8}$ inches. Using a calculator, find $\sqrt{8}$. Does it appear to terminate or repeat?


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Common Core State Standards

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20 INOVIUUAL BABS: $\quad 1 / 802$.EACH, $\quad 102$. EACH, TOTAL NET WT. $195 / 8 \mathrm{ZZ}$ ( $1 \mathrm{LB} .35 / 8 \mathrm{OZ}$ ) 556.3 g

## THINKING TIME

- Why did many of you expect there to be five of each?
- Why was it not five of each?
- How might they decide on this combination?


20 INDINIUUAL BAGS: $10 Z$. EACH, TOTAL NET WT. 2002 ( 1 LB. $40 Z$ OZ) 567 g

## GOALS

## ■ HOW DO WE MAKE SENSE OF MATH MODELING?

\author{

- IS IT JUST ANSWERING QUESTIONS?
}


## - HOW DO YOU PROFIT FROM MATH MODELING?

## - HOW DO WE HELP OUR STUDENTS IMPROVE?

 - WHERE CAN WE FIND MORE RESOURCES?




## Spies

## Analysts



Model






















## Spies

## Analysts

## Model




## Spies

## Analysts



Model


# All models are wrong, but some are useful. GEORGE E. P. BOX 



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## Analysts

## Model

## THINKING TIME



## Robert Kaplinsky

@robertkaplinsky
Hey \#MTBoS, can you do me a favor and complete this 3 question anonymous survey about your favorite chips? I need data for a presentation. Please RT. goo.gl/forms/etPtujll... \#iteachmath

notued form
Favorite Chips
Please complete this anonymous survey. I'll be using this data in a presentation.

8:05 PM - 4 Feb 2018

63 Retweets 45 Likes (6) 3

Favorite Chips (Responses)
File Edit View Insert Format Data Tools Form Add-ons Help

## $f_{X}$ Timestamp

|  | A | B | c | D | E | F | G | H |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Timestamp | Lays (Classic) | Doritos (Nacho Cheese) | Doritos (Cool Ranch) | Cheetos (Crunchy) | Sun Chips (Original) | Fritos (Original) | Time Zone |
| 2 | 2/4/2018 20:06:53 | 6 | 5 | 4 | 2 | 3 | 1 | Central Time Zone |
| 3 | 2/4/2018 20:06:55 | 1 | 5 | 6 | 3 | 2 | 4 | Eastern Time Zone |
| 4 | 2/4/2018 20:06:56 | 5 | 2 | 1 | 3 | 6 | 4 | Central Time Zone |
| 5 | 2/4/2018 20:06:57 | 2 | 1 | 6 | 3 | 5 | 4 | Pacific Time Zone |
| 6 | 2/4/2018 20:07:36 | 4 | 1 | 2 | 3 | 5 | 6 | Pacific Time Zone |
| 7 | 2/4/2018 20:08:02 | 5 | 1 | 6 | 4 | 2 | 3 | Pacific Time Zone |
| 8 | 2/4/2018 20:08:05 | 6 | 2 | 4 | 3 | 5 | 1 | Pacific Time Zone |
| 9 | 2/4/2018 20:08:07 | 4 | 2 | 1 | 5 | 3 | 6 | Pacific Time Zone |
| 10 | 2/4/2018 20:08:29 | 5 | 3 | 4 | 1 | 6 | 2 | Central Time Zone |
| 11 | 2/4/2018 20:08:56 | 4 | 5 | 6 | 1 | 2 | 3 | Central Time Zone |
| 12 | 2/4/2018 20:09:54 | 5 | 6 | 5 | 6 | 5 | 4 | Pacific Time Zone |
| 13 | 2/4/2018 20:10:01 | 4 | 2 | 3 | 1 | 5 | 6 | Pacific Time Zone |
| 14 | 2/4/2018 20:10:04 | 6 | 2 | 3 | 1 | 5 | 4 | Central Time Zone |
| 15 | 2/4/2018 20:10:04 | 3 | 5 | 6 | 1 | 4 | 2 | Central Time Zone |
| 16 | 2/4/2018 20:10:05 | 4 | 2 | 6 | 1 | 3 | 5 | Eastern Time Zone |
| 17 | 2/4/2018 20:10:06 | 3 | 2 | 6 | 5 | 1 | 2 | Pacific Time Zone |
| 18 | 2/4/2018 20:10:10 | 4 | 2 | 6 | 3 | 5 | 1 | Mountain Time Zone |
| 19 | 2/4/2018 20:10:12 | 3 | 1 | 5 | 6 | 2 | 4 | Eastern Time Zone |
| 20 | 2/4/2018 20:10:26 | 5 | 3 | 6 | 2 | 4 | 1 | Pacific Time Zone |

$\square$

- The available data includes:
- Lays, Nacho Cheese Doritos, Cool Ranch Doritos, Cheetos, Sun Chips, and Fritos ranked from 1 to 6
- Geographic region: West, Central, or Eastern


## ANALYSTS' JOB FOR THE TOP 1

1. Count all the first place votes for each chip type.
2. Divide the total first place votes for each chip type by the total number of votes.
3. Multiply that fraction by 20 to find how many bags there would be in a twenty pack, rounding as necessary.

## ANALYSTS' EXAMPLE



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## CHIP BAG RESULTS



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- How do we protect our planes?
- Which parts of the planc are boing
hit by the mest buHlete?
- Which parts of the plane are the most critical to protect?

- How do we find the fastest route for cach customer?
- How do we find the fastest route for each customer without impacting our other customers?


20 INDNIDUAL BAGS: 1 OZ. EACH, TOTAL NEE WT. 20 0Z. ( 1 LB. $40 Z$ OZ. 567 g
- How many of cach flavor should we put in a package?
- How many of each flaver should we put in a package for each region?
- How can we determine if the extra cost of creating different packages will make us more money?


# Mathematically proficient students who can apply what they know are comfortable making assumptions and approximations to simplify a complicated situation, realizing that these may need revision later. 

CCsS


They routinely interpret their mathematical results in the context of the situation and reflect on whether the results make sense, possibly improving the model if it has not served its purpose.

Ccss


4

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## Spies

## Analysts



Model

## They used 25 products for a pregnancy prediction' score including: <br> - unscented lotion <br> - mineral supplements <br> - cotton balls

Source: New York Times
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## Spies

## Analysts



Model

# Priority is determined by: 

- passenger's fare class
- itinerary
- frequent flyer program membership
- check-in time

Source: United Airlines

- News Feed
- Messenger
$\square$ Watch

4. Mark Marklace

## Explore

E Pages
(25) Events
(127) Groups

24 Friend Lists
(2) On This Day
ce Insights
2: Games
(-) Fundraisers
6) Live Video
(-) Pokes

- See More.

Create
Ad Page Group Event Fundraiser


What's on your mind, Robert?Photo/Video
Feeling/Activity

 $0 \pm 4$



## 

## Trending



- Het*
 nincimen
an Hationtis \#nor


$\rightarrow$ tivn
 ancentinn man
Haita

Watchlist: Latest Episodes (1)


See All

Sponsored



## Spies

## Analysts



Model

## The stories that show in your News

## Feed are influenced by:

- friends you interact with the most
- the number of comments and likes a post receives
- what kind of story it is (ex: photo, video, status update)
Source: Facebook
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## MORE EXAMPLES

- How does US News and World Reports rank colleges?
- How does Google know which results to show?
- How do sports teams know who to draft?
- How does Amazon know what products to recommend?
- How does Zillow estimate home prices?
- How does Pandora know what music to play?
- How does eHarmony know which people to show you?
- How do they figure out who should speak at a conference?


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$\qquad$
$\qquad$
$\qquad$

| What problem are you trying to figure out? | What estimates do you have? |
| :---: | :---: |
|  | Place your estimate on the number line. |
| What info do you already know about the problem? | What info do you need y ou the problem? |
| TOP SECRET! |  |
| What is your conclusion? How did you reach that conclusion? |  |

Your work
[DANGER




## Spies

## Analysts



Model

$\qquad$
$\qquad$ Date: $\qquad$


What is your conclusion? How did you reach that conclusion?
$\qquad$ Period: $\qquad$ Date: $\qquad$




Your work


Total bundles: 3,740 rot 10 s at at 8 ss $=3,961$ bundles

$2=10 x$

## $w$

## $2+$

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## PBLRESOURCES

- Problem-based lesson search engine: robertkaplinsky.com/prbl-search-engine
- My lessons (Elementary, Middle, and High School) robertkaplinsky.com/lessons
- Dan Meyer (Middle and High School) threeacts.mrmeyer.com
- Andrew Stadel (Elementary and Middle School) www.estimation180.com/lessons.html
- Graham Fletcher (Elementary and Middle School) gfletchy.com/3-act-lessons

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## Home

## Math resources that create problem solvers, not robots.

Download my favorite lessons for elementary, middle, and high school.

What happens next?



Take my online workshop for more implementation support.
$\qquad$ Blog Resources Speaking About Contact

Lessons


## Resources

Depth of Knowledge

- Open Middle
- Open Middle Worksheet - English(student version)
- Open Middle Worksheet - English (document camera version)
- Open Middle Worksheet - Spanish (student version)
- Open Middle Worksheet - Spanish(document camera version)
- Robert's blog.posts on Depth of Knowledge
- Tool to Distinguish Between Depth of Knowledge Levels


## Problem-Based Lesson Tools

- Problem-Based Lesson Search Engine
- Problem Solving Framework v8. 1
- Robert's blog.posts on Problem-Based Learning

Problem-Based Lesson Sources

- 101 Questions
- Andrew Gael
- Andrew Stadel
- Catherine Castillo
- Christina Tondevold
- Dan Meyer
- Dane Ehlert
- Emergent Math's Problem Based Curriculum Maps


Robert Kaplinsky's Problem-Based Lessons
File Edit View Insert Format Data Tools Add-ons Help All changes saved in Drive


| $f x$ |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | A | B | c | D | E | F | G | H |  |
| 1 | Lesson | Concept / Skill | Standard $1$ | Standard $2$ | Standard $3$ | Standard <br> 4 | Standard $5$ | Standard $6$ | Stan $7$ |
| 2 | How Much Money Were Those Pennies? | Money, Multiply ing Decimals, Proportions | 4.MD. 2 | 5.NBT. 5 | 5.NBT. 7 | 7.RP. 3 |  |  |  |
| 3 | How Can We \#SaveNelly? | Dividing Decimals | 6.NS. 3 |  |  |  |  |  |  |
| 4 | How Many Chip Bags Will There Be? | Ratio and Proportions, Population Sampling | 6. RP. 3 | 6. RP.3C | 7.RP. 2 | 7.RP. 3 | 7.SP. 1 | 7.SP. 2 |  |
| 5 | How Can We Make Stronger Passwords? | Permutations, Combinations, Probability, Exponents, Exponential Growth | 7.SP. 8 | 8.EE. 1 | S-MD. 7 | S-CP. 5 | S-CP. 9 |  |  |
| 6 | How Many Hot Dogs And Buns Should He Buy? | Least Common Multiple (LCM) | 6.NS. 4 |  |  |  |  |  |  |
| 7 | What Does 2000 Calories Look Like? | Unit Rates, Ratios, Solving Equations, and Solving Inequalities | 6.EE. 3 | 6.EE. 4 | 6.EE. 5 | 6.EE. 6 | 6.EE. 7 | 6.EE. 8 | 6. RP. |
| 8 | How Much Money Are The Coins Worth? | Decimal Operations and Coin Counting | 2.MD. 8 | 5.NBT. 7 | 6.NS. 3 |  |  |  |  |
| 9 | How Many Times Will A Case of Paper Jam? | Interpreting Percentages | 6. RP.3c | 7.RP. 3 |  |  |  |  |  |
| 10 | How Many Soda Combinations Are There On A Coke Freestyle? | Counting, Composing, and Decomposing Numbers | K.CC. 5 | K.CC. 6 | K.OA. 1 | K.OA. 2 | K. OA. 3 | K.OA. 4 | K.NB |
| 11 | What Should The Freeway Sign Show? | Fractions on Number Lines, Converting Units, Decimal and Fraction Operations | 3.NF. 1 | 3.NF. 2 | 3.NF.2a | 3.NF.2b | 3.NF. 3 | 3.NF.3a | 4. MD |
| 12 | How Fast Was The Fastest Motorcycle Speeding Ticket Ever? | Converting Units and Unit Rates | 5.MD. 1 | 6.RP.3d | 7.RP. 1 | N.Q. 1 |  |  |  |
| 13 | How Much Did Patrick Peterson Lose By Not Cashing His Check? | Compound and/or Simple Interest | 7.RP. 3 | N-RN. 2 | A-SSE. 1 | A-SSE.3C | A-SSE. 4 | A-REI. 11 | F-IF |
| 14 | How Many Biscuits Can You Make? | Dividing Fractions and Mixed Numbers | 5.NF. 7 | 5.NF.7a | 5.NF.7b | 5.NF.7c | 6.NS. 1 |  |  |
| 15 | How Much Bigger Should They Make Zoolander's School? | Scale and Proportions | 5.NF.5A | 7.RP. 2 | 7.G. 1 |  |  |  |  |
| 16 | Where Is The Freeway Sign Located? | Identify ing Fractions on a Number Line | 3.NF. 1 | 3.NF. 2 | 3.NF.2a | 3.NF.2b | 3.NF. 3 | 3.NF.3a | 3.NF. |
| 17 | How Far Apart Are Exits On A Ring Road? | Arc length measures | G-C. 5 |  |  |  |  |  |  |
| 18 | How Much Is One Third Of A Cup Of Butter? | Identify ing Fractions on a Number Line | 3.NF. 1 | 3.NF. 2 | 3.NF.2a | 3.NF.2b | 3.NF. 3 | 3.NF.3a | 3.NF. |
| 19 | How Do Skytypers Write Messages? | Transformations (Rotations, Reflections, Dilations, and Translations) | 8. G. 1 | 8. G. 2 | 8.G. 3 | 8. G. 4 | G-CO. 2 | G-CO. 3 | G-C |
| 20 | How Big Is The Bermuda Triangle? | Coordinate Geometry: Area of Triangle | G-GPE. 7 |  |  |  |  |  |  |
| 21 | What Fraction Of Children Are In The Right Car Seat? | Representing and Comparing Fractions | 3.NF. 1 | 3.NF. 2 | 3.NF. 3 | 4.NF. 1 | 4.NF. 2 |  |  |
| 22 | How Much Did The Temperature Drop? | Absolute Value | 6.NS.7c | 7.NS.1c |  |  |  |  |  |
| 23 | How Much Shorter Are Staggered Pipe Stacks? | Circles, Pythagorean Theorem, trigonometric ratios, and linear functions | 8. G. 7 | A-CED. 1 | A-CED. 3 | A-CED. 4 | A-SSE.1a | A-SSE.1b | A-SS |
| 24 | How Do You Write A Check To Pay For Something? | Expanded Form | 2.NBT. 3 | 4.NBT. 2 | 5.NBT.3a |  |  |  |  |
| 25 | How Can We Correct The Scarecrow? | Pythagorean Theorem | 8. G. 6 | G-SRT. 4 |  |  |  |  |  |
| 26 | How Much Does A 100×100 In-N-Out Cheeseburger Cost? | Building and Interpretting Linear Functions | 8.F. 1 | 8.F. 3 | 8.F. 4 | 8.F. 5 | F-IF. 4 | F-IF. 5 | F-IF |
| 27 | How Can We Water All Of The Grass? | Circles, Pythagorean Theorem, trigonometric ratios | 7.G. 4 | 8.G. 7 | G-SRT. 8 | G-MG. 1 | G-MG. 3 |  |  |
| 28 | How Much Money IS That?! | Volume of rectangular prism | 5.MD. 3 | 5.MD. 4 | 5.MD. 5 | 5.MD.5b | 5.MD.5c | 6.G. 2 | 7.G. 6 |
| 29 | How Much Money Should Dr. Evil Demand? | Exponential Growth | N-RN. 2 | A-SSE. 1 | A-SSE.3C | A-SSE. 4 | A-REI. 11 | F-IF. 4 | F-IF. |
| 30 | How Tall Is Mini-Me? | Scale and Dividing Decimals | 5.NF. 5 | 5.NF.5a | 5.NF.5b | 6.NS. 3 |  |  |  |
| 31 | How Did They Make Ms. Pac-Man? | Transformations (Rotations, Reflections, and Translations) | 8.G. 1 | 8.G. 2 | 8.G. 3 | 8.G. 4 | G-SRT. 2 | G-CO. 4 | G-CO |
| 32 | Which Ticket Option Is The Best Deal? | Unit Rates and Ratios | 6. RP. 2 | 6. RP. 3 | 6.RP.3a | 6.RP.3b |  |  |  |
| 33 | How Far Apart Are The Freeway Exits? | Fractions on a Number Line and Subtracting Fractions | 3.NF. 2 | 3.NF.2b | 4.NF. 2 | 4.NF.3a | 4.NF.3C | 4.NF.3d | 5.NF. |
| 34 | Do We Have Enough Paint? | Area | 3.MD. 5 | 3.MD. 6 | 3.MD. 7 |  |  |  |  |

$+\equiv$ Sheet1 -

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## Scary \& Dangerous




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