CHALLENGING PROBLEMS

WORTH SOLVING

ROBERT KAPLINSKY

robert@robertkaplinsky.com

robertkaplinsky.com

@robertkaplinsky

WANT THE RESOURCES?

Text the message:

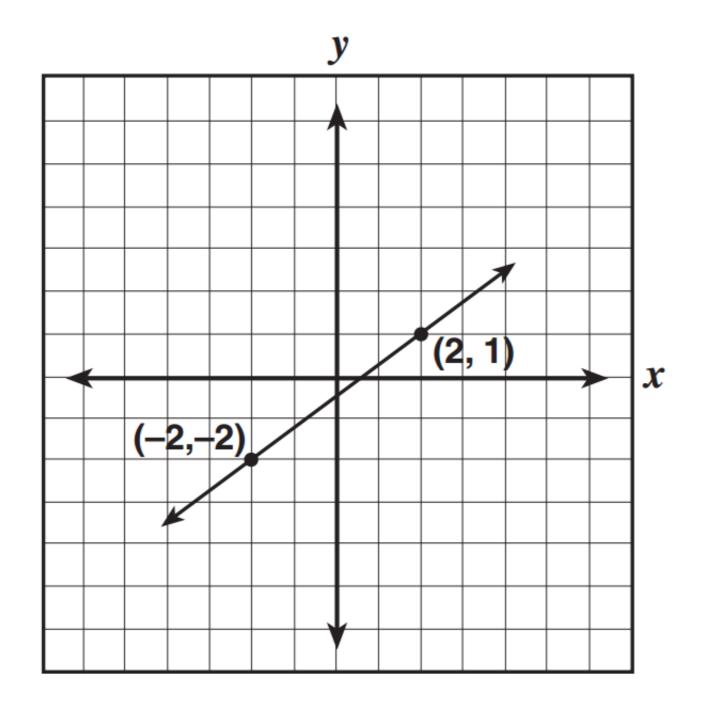
PROBLEMS

To 44222

GOALS

- ☐ WHY DO WE NEED THEM?
- ☐ WHY ARE THEY DIFFERENT?
- ☐ HOW DO YOU IMPLEMENT THEM?
- ☐ HOW DO YOU CREATE YOUR OWN?
- WHERE DO YOU GET OTHERS?

				Mathematics Clusters												
					(Clusters where the percent correct is shown in bold represent proficiency for that cluster.)											
								Quant	itative							
								relations	hips and	Multi-step	problems,			Statisti	Statistics, data	
						Exponents	s, powers,	evalu	ating	graphir	ng, and	Measurement and		analysis, and		
				Rational	numbers	and	roots	expre	ssions	func	tions	geor	netry	prob	ability	
		Perf.	Scaled	Number	Percent	Number	Percent	Number	Percent	Number	Percent	Number	Percent	Number	Percent	
Student Name	ID Number	Level	Score	Correct	Correct	Correct	Correct	Correct	Correct	Correct	Correct	Correct	Correct	Correct	Correct	
KON, MTM.	176.75	ADV	476	13	93%	8	100%	8	80%	14	93%	12	92%	5	100%	
ACCRECATE AND ADDRESS OF	17,750	ADV	464	13	93%	7	88%	8	80%	15	100%	11	85%	5	100%	
Record, Services	177040	ADV	453	10	71%	8	100%	10	100%	14	93%	11	85%	5	100%	
NOTES, MCDRON	10,700	ADV	453	13	93%	8	100%	9	90%	12	80%	11	85%	5	100%	
Married Co., or Married Co.	1796.07	ADV	444	14	100%	7	88%	8	80%	13	87%	10	77%	5	100%	
THERMAN, MICLAY	17,7000	ADV	444	12	86%	8	100%	8	80%	15	100%	10	77%	4	80%	
HAZINGTON, A STANSON	100	ADV	444	13	93%	8	100%	8	80%	14	93%	9	69%	5	100%	
percent, second	100	ADV	435	12	86%	6	75%	9	90%	14	93%	10	77%	5	100%	
ROCC, ADROPA	17 10 10	ADV	435	12	86%	6	75%	8	80%	14	93%	11	85%	5	100%	
SHEETE, MITTER	17,0040	ADV	435	13	93%	7	88%	9	90%	12	80%	10	77%	5	100%	
BOARDON, STREET	176.00	ADV	427	13	93%	6	75%	9	90%	12	80%	10	77%	5	100%	
CHARGO, UNK	1777	ADV	427	13	93%	7	88%	6	60%	13	87%	11	85%	5	100%	
HOMES, BENEDICT		ADV	427	14	100%	5	63%	7	70%	14	93%	10	77%	5	100%	
ACCRETA, DANSELL	100	ADV	421	13	93%	6	75%	6	60%	14	93%	10	77%	5	100%	
STREET, STREET	100,754	ADV	421	11	79%	5	63%	9	90%	13	87%	11	85%	5	100%	
HARRIS, HARRISTA	17,000,00	ADV	414	12	86%	6	75%	8	80%	11	73%	11	85%	5	100%	
RETER THE COLUMN	177	ADV	414	12	86%	8	100%	8	80%	13	87%	8	62%	4	80%	
MARKET BY THE PARTY	17 (1988)	PRO	408	11	79%	6	75%	9	90%	11	73%	10	77%	5	100%	
AUTHOR, MICTIGAT	1777274	PRO	402	12	86%	8	100%	9	90%	8	53%	11	85%	3	60%	
SATISFACE, ASSESSED.	17270	PRO	402	8	57%	7	88%	8	80%	13	87%	10	77%	5	100%	
METHODOLIC, GRACE	1777	PRO	402	13	93%	6	75%	7	70%	13	87%	8	62%	4	80%	
MARKETON, SELVICE	572,000	PRO	402	11	79%	5	63%	7	70%	11	73%	12	92%	5	100%	
ROBERT MARKET	577908	PRO	402	13	93%	7	88%	9	90%	10	67%	7	54%	5	100%	
Material State of Sta	177000	PRO	402	13	93%	7	88%	7	70%	11	73%	8	62%	5	100%	
AUTOM, DANSOLA	96/5/80	PRO	396	10	71%	6	75%	9	90%	14	93%	7	54%	4	80%	
STATE OF THE OWNER.	177400	PRO	396	12	86%	8	100%	6	60%	9	60%	11	85%	4	80%	



- $\mathbf{A} = \frac{1}{2}$
- $\mathbf{B} = \frac{3}{4}$
- **C** 1
- $\mathbf{D} \quad \frac{4}{3}$



				Mathematics Clusters											
					(Clusters where the percent correct is shown in bold represent proficiency for that cluster.)										
								Quant	itative						
								relations	hips and	Multi-step	problems,			Statisti	cs, data
						Exponent	s, powers,	evalu	ıating	graphir	ng, and	Measure	ment and	analys	sis, and
				Rational	numbers	and	roots	expre	ssions	func	tions	geor	netry	prob	ability
		Perf.	Scaled	Number	Percent	Number	Percent	Number	Percent	Number	Percent	Number	Percent	Number	Percent
Student Name	ID Number	Level	Score	Correct	Correct	Correct	Correct	Correct	Correct	Correct	Correct	Correct	Correct	Correct	Correct
KON, KON	176.756	ADV	476	13	93%	8	100%	8	80%	14	93%	12	92%	5	100%
ACCRECATE AND ADDRESS OF	1000	ADV	464	13	93%	7	88%	8	80%	15	100%	11	85%	5	100%
MARKET SHARE	177040	ADV	453	10	71%	8	100%	10	100%	14	93%	11	85%	5	100%
BOTO, DODGO						8	100%					11	85%	5	100%
Married Co., or Spinster,	1796.0											10	77%	5	100%
THERMAN, MICLAY												10	77%	4	80%
DECISIONAL EXHIBIT	100.00				711		1					9	69%	5	100%
SECURE, SCORE	100			12			75		0%	1111		10	77%	5	100%
MOREL, ADMINIS	17 700 04			12			759		0%		b	11	85%	5	100%
DESCRIPTION OF THE PERSON NAMED IN	17,0040	A					88%				6	10	77%	5	100%
STANSON, STANSON	176.00	A.				6	75%				%	10	77%	5	100%
CHARGO, UNK	1771000	AD				7	88%				37%	11	85%	5	100%
HOME BOOK TO	100	ADV				5	63%				93%	10	77%	5	100%
ACCRETA, DANGER.	100	ADV	42.		93 %	6	75%	6			93%	10	77%	5	100%
STREET, MICHIGAN	800,754	ADV	421	11	79%	5	63%	9	90%	13	87%	11	85%	5	100%
HARRIS, HARRISTA	17,000,00	ADV	414	12	86%	6	75%	8	80%	11	73%	11	85%	5	100%
RCYCL, THROUGH	177,000	ADV	414	12	86%	8	100%	8	80%	13	87%	8	62%	4	80%
STATE OF THE PERSON NAMED IN	17 (1900)	PRO	408	11	79%	6	75%	9	90%	11	73%	10	77%	5	100%
Acres, Married	1,777,276	PRO	402	12	86%	8	100%	9	90%	8	53%	11	85%	3	60%
SATISFACE AND RESIDENCE	17,770	PRO	402	8	57%	7	88%	8	80%	13	87%	10	77%	5	100%
STREET, SHATT	572796	PRO	402	13	93%	6	75%	7	70%	13	87%	8	62%	4	80%
MARKETON, DESCRIPTION	1077	PRO	402	11	79%	5	63%	7	70%	11	73%	12	92%	5	100%
NAME OF TAXABLE PARTY.	177908	PRO	402	13	93%	7	88%	9	90%	10	67%	7	54%	5	100%
BARNESSON, SERVICES	17700	PRO	402	13	93%	7	88%	7	70%	11	73%	8	62%	5	100%
ALTERNATION AND LA	10075.00	PRO	396	10	71%	6	75%	9	90%	14	93%	7	54%	4	80%
STATE OF THE PARTY.	177400	PRO	396	12	86%	8	100%	6	60%	9	60%	11	85%	4	80%

GOALS

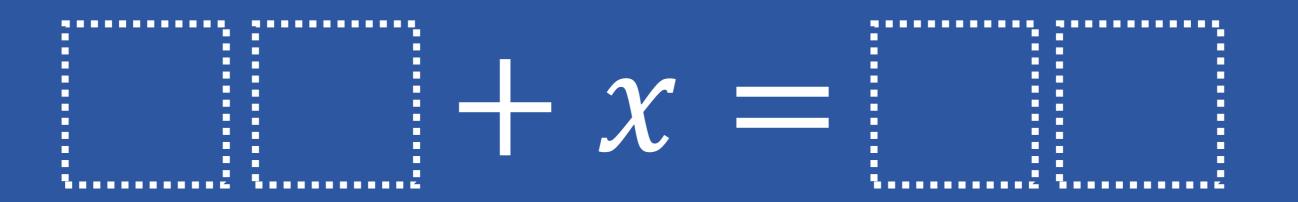
- WHY DO WE NEED THEM?
- ☐ WHY ARE THEY DIFFERENT?
- HOW DO YOU IMPLEMENT THEM?
- ☐ HOW DO YOU CREATE YOUR OWN?
- ☐ WHERE DO YOU GET OTHERS?

PROBLEM ONE Solve for x.

$$21 + x = 70$$

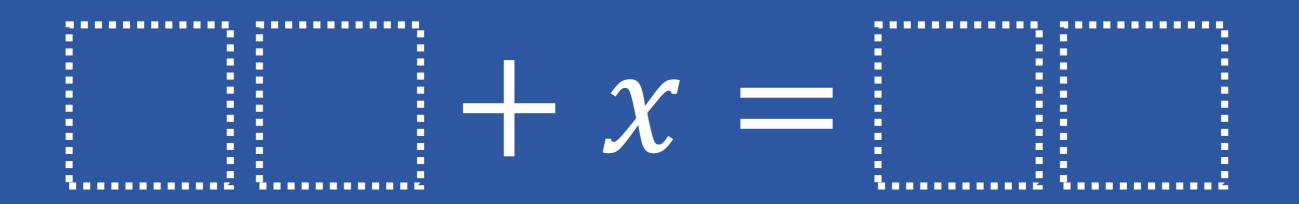
PROBLEM TWO

Using the digits 1 to 9, at most one time each, create two equations: one where x has a positive value and one where x has a negative value.



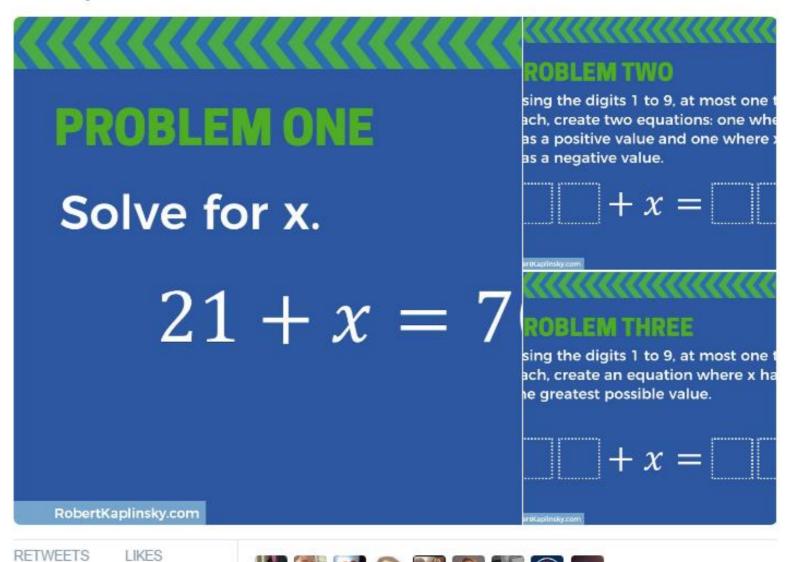
PROBLEM THREE

Using the digits 1 to 9, at most one time each, create an equation where x has the greatest possible value.





MS & HS #MTBoS Ts, please ask your Ss these 3 ?s and put the % who answered correctly here: docs.google.com/forms/d/e/1FAI Answers at top of form.



54



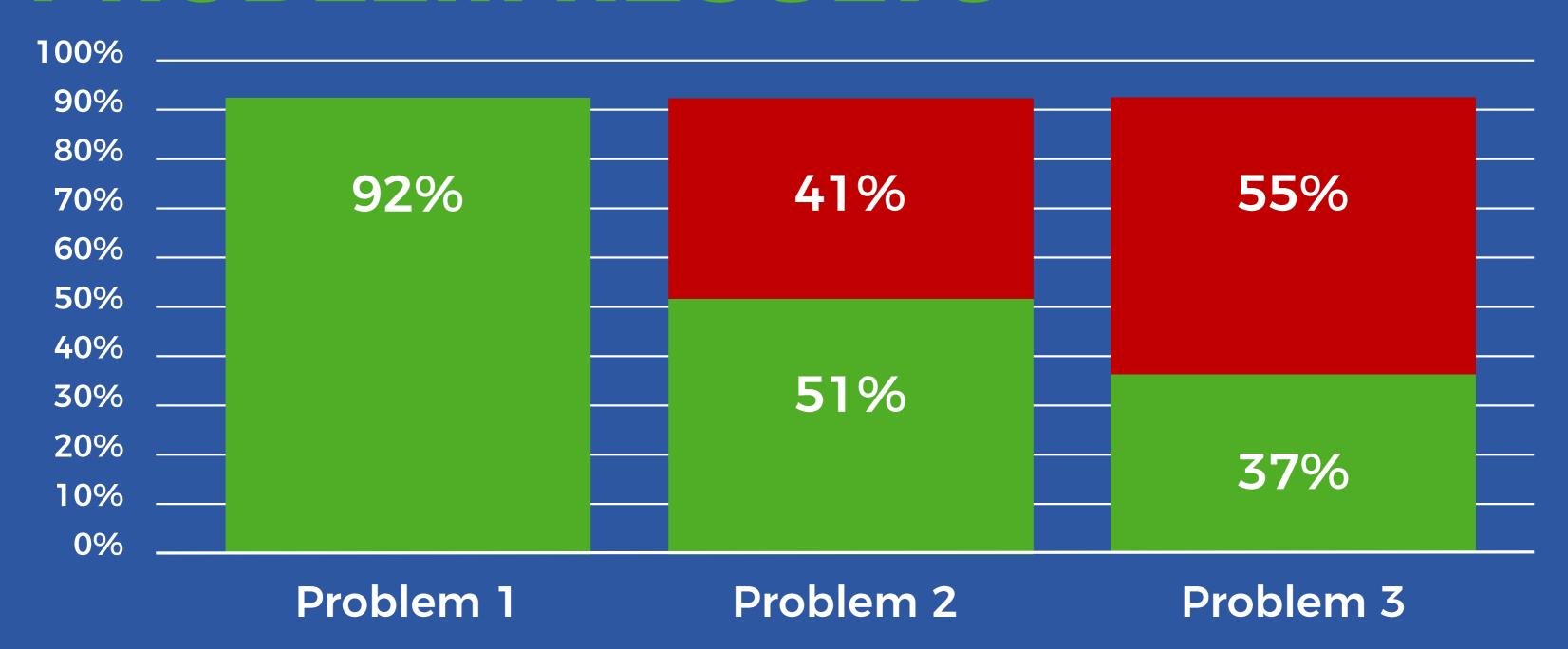








PROBLEM RESULTS



Depth of Knowledge Matrix - Secondary Math

Topic	Dividing Fractions	Solving Two-Step Equations	Exponents	Solving Equations with
				Variables on Both Sides
CCSS	• 6.NS.1	• 7.EE.4a	• 8.EE.1	• 8.EE.8
Standard(s)				 A-REI.3
DOK 1	Evaluate.	Solve for x.	Evaluate.	Solve for x.
Example	$\frac{4}{9} \div \frac{2}{5}$	2x + 3 = 9	3 ⁴	3x + 2 = -2x + 4
DOK 2	Use the digits 1 to 9, at most	Use the digits 1 to 9, at most	Use the digits 1 to 9, at most	Use the digits 1 to 9, at most
Example	one time each, to fill in the	one time each, to create two	one time each, to fill in the	two times each, to fill in the
	boxes to make two different	equations: one where x has a	boxes to make two true	boxes to make an equation
	pairs of fractions that have a	positive value and one where	number sentences.	with no solutions.
	quotient of 2/3.	x has a negative value.		
	$\frac{1}{3}$		= 64	
DOK 3	Use the digits 1 to 9, at most	Use the digits 1 to 9, at most	Use the digits 1 to 9, at most	Use the digits 1 to 9, at most
Example	one time each, to fill in the	one time each, to create an	one time each, to fill in the	one time each, to fill in the
	boxes to make two fractions	equation where x has the	boxes to make a result that	boxes so that the solution is
	that have a quotient that is as	greatest possible value.	has the greatest value	closest to zero.
	close to 4/11 as possible.		possible.	
	•			

Depth of Knowledge Matrix - Secondary Math

Topic	Geometric Proofs	Complex Numbers	Trigonometric Functions	Definite Integral
CCSS Standard(s)	• G-CO.11	• N-CN.2	• F-TF.3	• N/A
DOK 1 Example	Add one geometric marking to demonstrate the quadrilateral is a square.	Multiply the binomials. $(3+4i)(2+3i)$	Evaluate. $\sin\frac{\pi}{3}$	Solve. $\int_{2}^{6} x^{3} dx$
DOK 2 Example	Use exactly 5 geometric markings to show that a quadrilateral is a square.	Use the integers -9 to 9, at most one time each, to fill in the boxes twice: once to make a positive real number product and once to make a negative real number product. (+ i) (+ i)	Use the digits 1 to 9, at most one time each, to fill in the boxes and make two true number sentences. $\sin \frac{\pi}{1-\pi} = 0$	Use the digits 1 to 9, at most one time each, to fill in the boxes and make a positive and a negative solution. $\int_{-\infty}^{+\infty} x^{-x} dx$
DOK 3 Example	What is the least number of geometric markings needed to demonstrate that a quadrilateral is a square?	Use the integers -9 to 9, at most one time each, to fill in the boxes and make a real number product with the greatest value. (+ i) (+ i)	Use the digits 1 to 9, at most one time each, so that the function has the greatest possible value. $\sin \frac{\pi}{1-\pi} = \frac{\sqrt{1-\pi}}{1-\pi}$	Use the digits 1 to 9, at most one time each, to fill in the boxes and make a solution that is as close to 100 as possible. $\int_{-\infty}^{\infty} x^{-1} dx$



DOK ONE

$$6.9 + a = 46$$

DOK TWO

11. Anton walked 8.9 miles of his 13.5-mile goal for this week. Use the equation m + 8.9 = 13.5 to find which path Anton should walk so that he meets

his goal for the week.

Path Lengths							
Meadow Path	3.2 miles						
Circle Path	4.2 miles						
Oak Tree Path	4.6 miles						

DOKTHREE

14. Reasoning Kyle bought a movie ticket for \$8.45 and a drink for \$1.80. He had just enough money remaining to buy a large popcorn. How much money did Kyle start with? Write an equation to show

your reasoning. © MP.2

Cost of Popcorn						
Small	\$2.85					
Medium	\$3.75					
Large	\$4.75					
Extra Large	\$4.85					

GOALS

- WHY DO WE NEED THEM?
- WHY ARE THEY DIFFERENT?
- HOW DO YOU IMPLEMENT THEM?
- ☐ HOW DO YOU CREATE YOUR OWN?
- ☐ WHERE DO YOU GET OTHERS?

IMPLEMENTATION

Open Middle Worksheet

First attempt:	Points	:	_/2	attem	ipt	_/2 exp	lanation
What did you learn from this atte	emnt?	How	will	VOUL	strateav	change	on vour
next attempt?	cilipi	110 11	*****	7001	sir dieg /	change	011 / 001
•							

Name:	Period: Date:
First attempt:	Points:/2 attempt/2 explanation
What did you learn from this attempt? How will your str	rategy change on your next attempt?
Second attempt:	Points:/2 attempt/2 explanation

IMPLEMENTATION

- Open Middle Worksheet
- Classwork
 - Single problem for entire class
 - Extensions menu

QUESTION

Use the digits 1 to 9, at most one time each, to create an equation where x has the greatest possible value.

4 points

QUESTION #4

Use the digits 1 to 9, at most one time each, to make each equation true.

UESTION #2

Solve for x.

$$3x + 7 = 19$$

1 point SOLVING EQUATIONS

EXTENSION MENU

You must earn <u>at least 12</u>
<u>points</u> by doing the
problems of your choice.
Circle the auestions you

QUESTION #3

Use the digits 1 to 9, at most one time each, to create two equations: one where x has a positive value and one where x has a negative value.

$$+x=$$
 2 points

QUESTION #5

Use the digits 1 to 9, at most one time each, to create an equation where x has the greatest possible value.

IMPLEMENTATION

- Open Middle Worksheet
- Classwork
 - Single problem for entire class
 - Extensions menu
- Homework
- Assessments

GOALS

- WHY DO WE NEED THEM?
- WHY ARE THEY DIFFERENT?
- M HOW DO YOU IMPLEMENT THEM?
- ☐ HOW DO YOU CREATE YOUR OWN?
- ☐ WHERE DO YOU GET OTHERS?

STEP ONE

- Find a One-Operation Problem
 - Addition
 - Subtraction
 - Multiplying
 - Dividing
 - Exponents (including square root)
 - Trigonometric functions

ADDING 2-DIGIT NUMBERS

Solve.

MULTIPLYING FRACTIONS

Solve.

THINKINGTIME

STEP TWO

- Go from DOK 1 to DOK 2
 - Strategically remove some information from the problem to prevent immediate calculation
 - Increase the quantity of solutions needed to increase the need to look for patterns

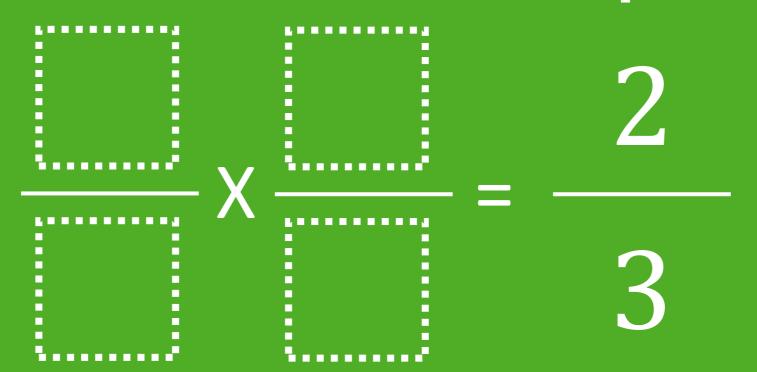
ADDING 2-DIGIT NUMBERS

Using the digits 1 to 9, at most one time each, fill in the boxes to make two different pairs of two-digit numbers that have a sum of 71.

$$+ = 71$$

MULTIPLYING FRACTIONS

Using the digits 1 to 9, at most one time each, fill in the boxes to make two different pairs of fractions that have a product of 2/3.



THINKING TIME

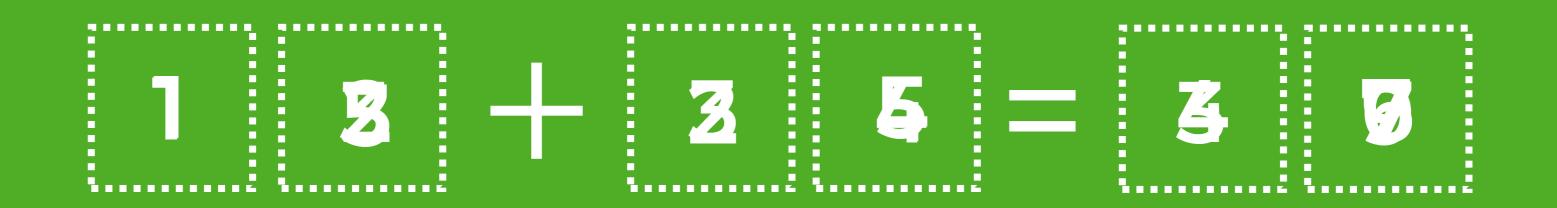
- · Go from DOK 1 to DOK 2
 - Strategically remove some information from the problem to prevent immediate calculation
 - Increase the quantity of solutions needed to increase the need to look for patterns

STEP THREE

- Go from DOK 2 to DOK 3
 - Introduce the need to optimize the solution by making the greatest or least product / sum / difference / quotient / answer.
 - Another optimization option is make the answer closest to a specific value.

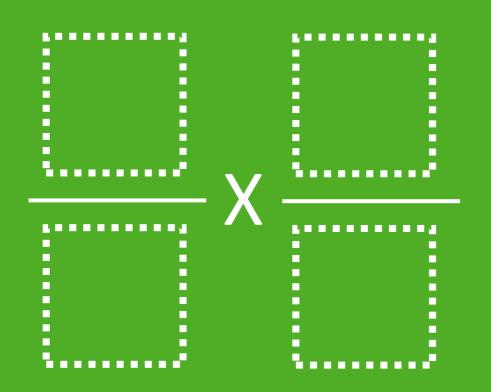
ADDING 2-DIGIT NUMBERS

Using the digits 1 to 9, at most one time each, fill in the boxes to make the smallest sum.



MULTIPLYING FRACTIONS

Using the digits 1 to 9, at most one time each, fill in the boxes to make two fractions that have a product that is as close to 4/11 as possible.



THINKING TIME

- · Go from DOK 2 to DOK 3
 - Introduce the need to optimize the solution by making the greatest or least product / sum / difference / quotient / answer.
 - Another optimization option is make the answer closest to a specific value.

3 Steps to Increase Math DOK Levels

Step 1: Find a One-Operation Problem

- Procedural problems with one operation are easiest to modify.
- Other problems may also be modified but may not be as easy.

Adding 2-Digit Numbers

Multiplying Fractions

$$\frac{3}{7} \times \frac{2}{9} =$$

Trigonometry

Solve.

$$\sin\frac{\pi}{3} =$$

Step 2: Go from DOK 1 to DOK 2

- Strategically remove some information from the problem to prevent immediate calculation
- Increase the quantity of solutions needed to increase the need to look for patterns

Adding 2-Digit Numbers
Using the digits 1 to 9, at most one time each, fill in the boxes

Multiplying Fractions
Using the digits 1 to 9, at most one time each, fill in the boxes

Trigonometry
Using the digits 1 to 9, at most one time each, fill in the boxes

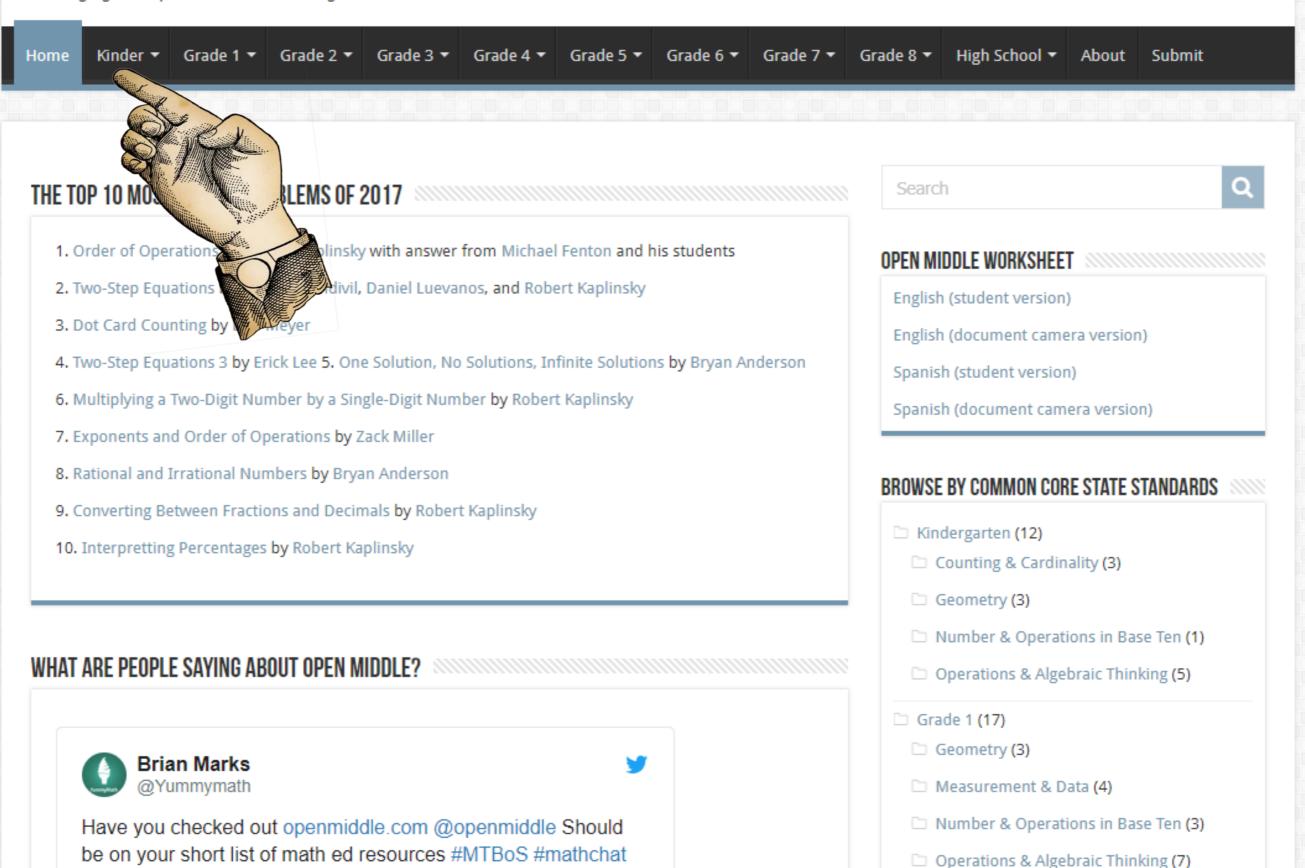
GOALS

- WHY DO WE NEED THEM?
- WHY ARE THEY DIFFERENT?
- M HOW DO YOU IMPLEMENT THEM?
- M HOW DO YOU CREATE YOUR OWN?
- ☐ WHERE DO YOU GET OTHERS?

Open Middle™

Challenging math problems worth solving

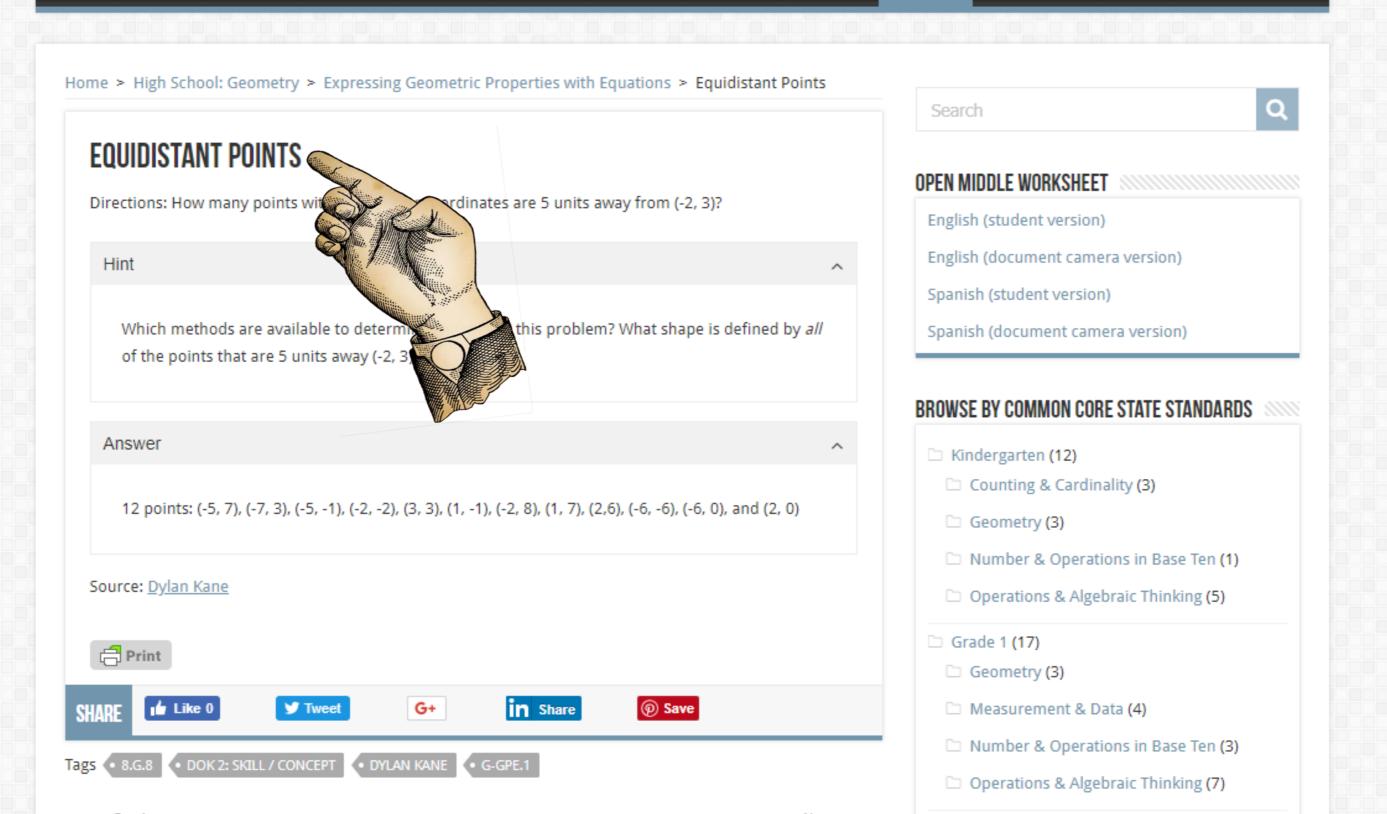
#maths #elemchat

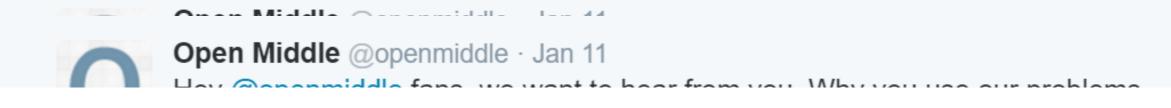


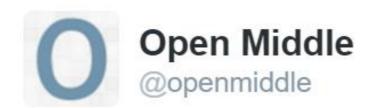
Open Middle™

Challenging math problems worth solving

Home Kinder ▼ Grade 1 ▼ Grade 2 ▼ Grade 3 ▼ Grade 4 ▼ Grade 5 ▼ Grade 6 ▼ Grade 7 ▼ Grade 8 ▼ High School ▼ About Submit







Hey @openmiddle fans, we want to hear from you. Why do you use our problems with your students? Share your success stories or lessons learned.



GOALS

- WHY DO WE NEED THEM?
- WHY ARE THEY DIFFERENT?
- M HOW DO YOU IMPLEMENT THEM?
- M HOW DO YOU CREATE YOUR OWN?
- WHERE DO YOU GET OTHERS?

CALL TO ACTION

Action	Do Now	Start Planning	Yes & No	Don't Do
Incorporate higher DOK problems on assessments.				
Replace all DOK 1 problems with higher DOK problems.				
Share these resources with colleagues to make them aware.				
Find problems I can integrate on Open Middle.				
Use the 3 steps process to strengthen existing problems.				

CHALLENGING PROBLEMS

WORTH SOLVING

ROBERT KAPLINSKY

robert@robertkaplinsky.com

robertkaplinsky.com/cpws

@robertkaplinsky

WANT THE RESOURCES?

Text the message:

PROBLEMS

To 44222