WHY WE SHOULD RECONSIDER (AND WHAT WE SHOULD BE DOING INSTEAD)

ROBERT KAPLINSKY

robert@robertkaplinsky.com

robertkaplinsky.com/worksheetresources

@robertkaplinsky

GOALS

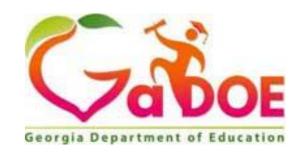
- □ WHO AM !?
- ☐ WHAT'S WRONG WITH WORKSHEETS?
- ☐ WHAT SHOULD WE BE DOING INSTEAD?
- HOW DO WE DO IT IN OUR CLASSROOMS?
- ☐ WHERE DO WE GET MORE PROBLEMS?
- ☐ WHAT COMES NEXT?



















EDUCATION WEEK

едиторіа





GOALS

- WHO AM !?
- ☐ WHAT'S WRONG WITH WORKSHEETS?
- ☐ WHAT SHOULD WE BE DOING INSTEAD?
- HOW DO WE DO IT IN OUR CLASSROOMS?
- ☐ WHERE DO WE GET MORE PROBLEMS?
- ☐ WHAT COMES NEXT?

One-Step Equations

Date_____ Period____

Solve each equation.

1)
$$26 = 8 + v$$

2)
$$3 + p = 8$$

3)
$$15 + b = 23$$

4)
$$-15 + n = -9$$

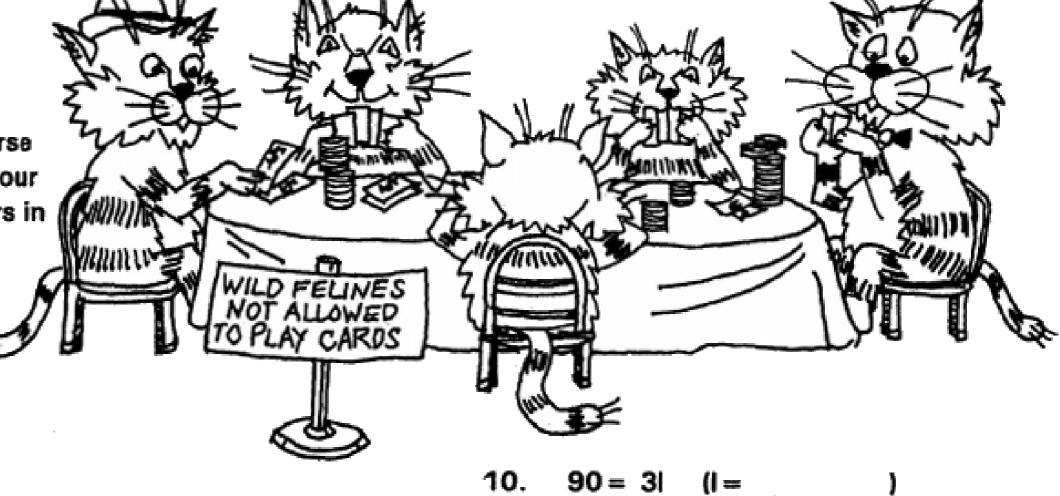
5)
$$m+4=-12$$

6)
$$x - 7 = 13$$

Why shouldn't some cats play cards?

operation. Use a calculator where necessary. Find your answer in the decoder. Each time your answer occurs in the decoder, write the letter of the problem above it.

1.
$$3 + g = 13 (g = ____)$$



7.
$$\frac{i}{2.3} = 6.7 \quad (i = ____)$$

12.
$$\underline{b} = 31 \ (b = \underline{\hspace{1cm}})$$

11. 7.2 = 0.36n (n = ____)

9.
$$180 = t - 35 (t =)$$

13.
$$4c = 60 (c =$$

WORKSHEET CONCERNS

- OFTEN FEELS LIKE BUSY WORK
- DON'T REALLY BUILD SENSE MAKING
- RARELY LEAD TO GREAT CONVERSATIONS
- DON'T GIVE US RICH INFORMATION

GOALS

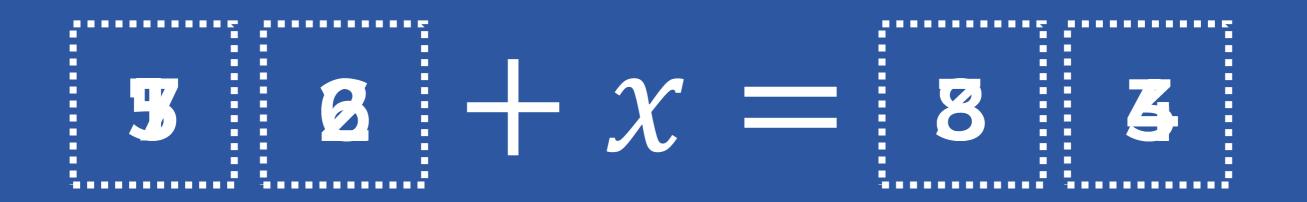
- WHO AM !?
- WHAT'S WRONG WITH WORKSHEETS?
- ☐ WHAT SHOULD WE BE DOING INSTEAD?
- HOW DO WE DO IT IN OUR CLASSROOMS?
- ☐ WHERE DO WE GET MORE PROBLEMS?
- ☐ WHAT COMES NEXT?

PROBLEM ONE Solve for x.

$$21 + x = 70$$

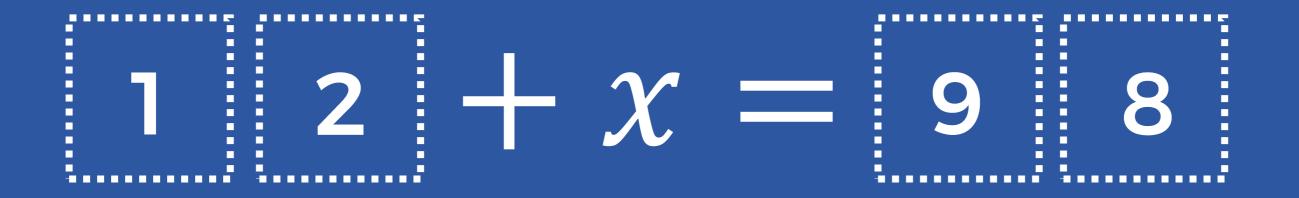
PROBLEM TWO

Using the digits 1 to 9 at most one time each, fill in the boxes to create two equations: one where x has a positive value and one where x has a negative value. You may reuse digits for each equation.



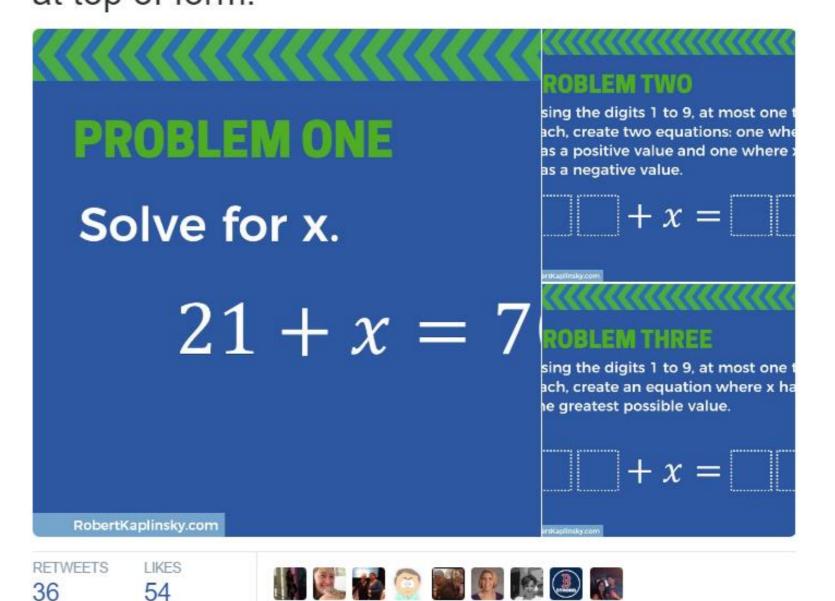
PROBLEMTHREE

Using the digits 1 to 9 at most one time each, fill in the boxes to create an equation where x has the greatest possible value.



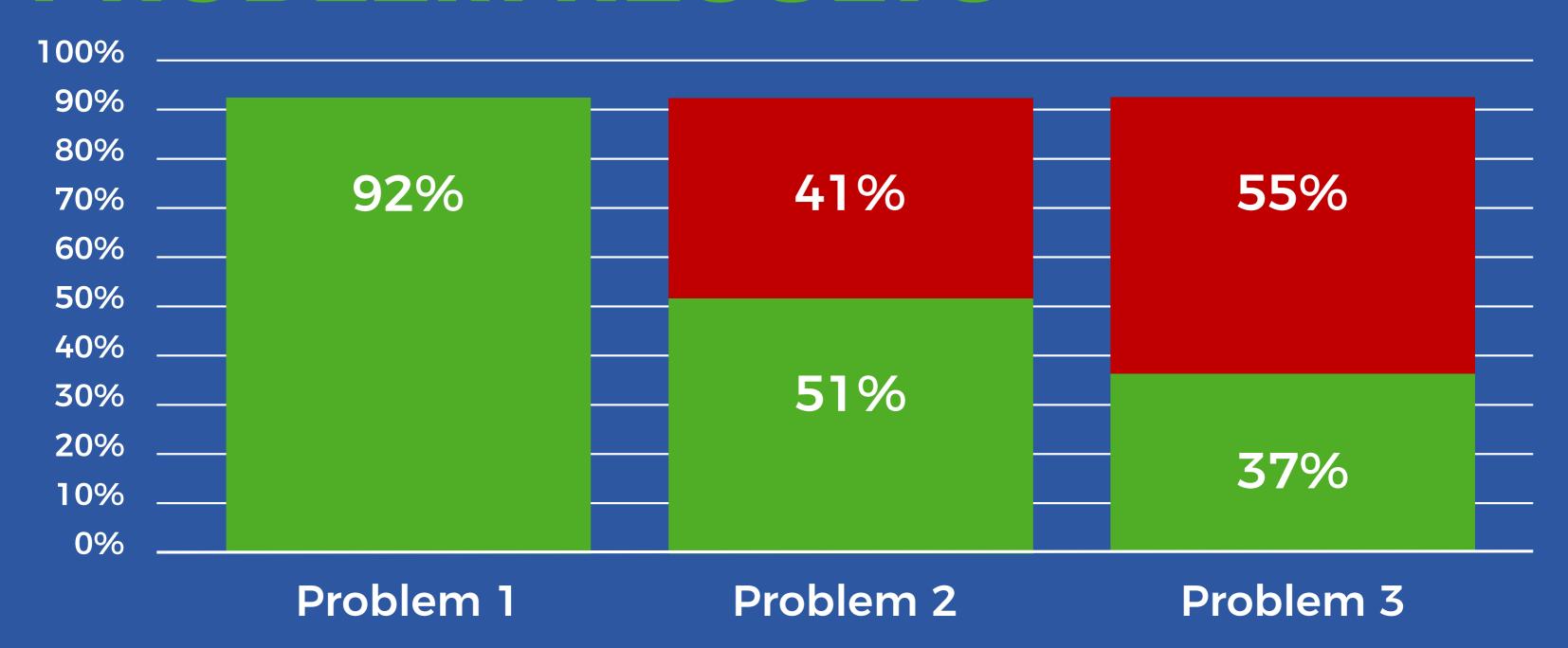


MS & HS #MTBoS Ts, please ask your Ss these 3 ?s and put the % who answered correctly here: docs.google.com/forms/d/e/1FAI Answers at top of form.



36

PROBLEM RESULTS



Depth of Knowledge Matrix - Elementary Math

Topic	Adding 1-Digit Numbers (< 5)	Equality	Interpreting Data	Money
CCSS Stand.	• K.OA.5	• 1.OA.7	• 1.MD.4	• 2.MD.8
DOK 1	Solve.	Determine whether the	How many people were	If you have 1 quarter, 4
Example		number sentence is true or	surveyed?	dimes, 2 nickels, and 3
	3 + 1 =	false.	3+	pennies, how many cents do
		4 + 1 = 5 - 2	2 — Blue Red Yellow Favorite Color	you have?
DOK 2	Using the digits 1 to 5 at	Using the digits 1 to 9 at most	Make a graph that shows a	Make 72¢ in two different
Example	most one time each, fill in the	one time each, fill in the boxes	possible result of 7 students'	ways with either quarters,
	boxes to create two true	to create two true number	favorite color.	dimes, nickels, or pennies.
	number sentences.	sentences.	3 +	
	+ <u></u> =	[_]+[_]=[_]-[_]	1—	
			Blue Red Yellow Favorite Color	
DOK 3	Using the digits 1 to 5 at	Using the digits 1 to 9 at most	Make a graph that shows a	Make 72¢ using exactly 9
Example	most one time each, fill in the	one time each, fill in the boxes	possible result of 7 students'	coins that are either quarters,
	boxes to create a true	to create a true number	favorite color with red being	dimes, nickels, or pennies.
	number sentences with the	sentence with the greatest	the most popular color.	
	greatest possible sum.	possible value.	3 +	
			1 —	
			Blue Red Yellow Favorite Color	

Depth of Knowledge Matrix - Elementary Math

Topic	Subtracting 3-Digit Numbers	Operations with Time	Comparing Fractions	Multiplying Decimals
CCSS Stand.	• 3.NBT.2	• 3.MD.1	• 4.NF.2	• 5.NBT.7
DOK 1	Solve.	What time will it be 14	Place a < or > between the	Solve.
Example		minutes after 1:27 pm?	two fractions to make a true	
	821 - 357 =		number sentence.	$3.4 \times 2.5 =$
			4 3	
			$\frac{1}{7}$ $\frac{3}{5}$	
			7 5	
DOK 2	Using the digits 1 to 9 at	Using the digits 1 to 9 at most	Using the digits 1 to 9 at most	Using the digits 1 to 9 at most
Example	most one time each, fill in the	one time each, fill in the boxes	one time each, fill in the boxes	one time each, fill in the boxes
	boxes to make two different	to make a time that is 4:37	to create two different	to make a true number
	pairs of three-digit numbers	pm.	fractions: one that is less than	sentence.
	that form a true number		one half and one that is more	
	sentence.	minutes after	than one half.	. × 3.2=
	-291=	[] pm	$\frac{}{} < \frac{1}{2}$ and $\frac{}{} > \frac{1}{2}$	
DOK 3	Using the digits 1 to 9 at	Using the digits 1 to 9 at most	Using the digits 1 to 9 at most	Using the digits 1 to 9 at most
Example	most one time each, fill in the	one time each, fill in the boxes	one time each, fill in the boxes	one time each, fill in the boxes
	boxes to make a difference	to make the latest possible	to create a fraction that is as	so that the product is as close
	that is as close to 329 as	time.	close to 5/11 as possible.	to 50 as possible.
	possible.		ŗ ₁	
		minutes after		×=
		: pm		
		hammed hammed to	<u></u>	

Depth of Knowledge Matrix - Secondary Math

Topic	Dividing Fractions	Solving Two-Step Equations	Exponents	Solving Equations with Variables on Both Sides
CCSS Standard(s)	• 6.NS.1	• 7.EE.4a	• 8.EE.1	8.EE.8A-REI.3
DOK 1	Evaluate.	Solve for x.	Evaluate.	Solve for x.
Example	$\frac{4}{9} \div \frac{2}{5}$	2x + 3 = 9	34	3x + 2 = -2x + 4
DOK 2	Using the digits 1 to 9 at most	Using the digits 1 to 9 at most	Using the digits 1 to 9 at most	Using the digits 1 to 9 at most
Example	one time each, fill in the boxes to make two different pairs of fractions that have a quotient of $2/3$. ${} \div {} = \frac{2}{3}$	one time each, fill in the boxes to create two equations: one where x has a positive value and one where x has a negative value.	one time each, fill in the boxes to make two true number sentences. = 64	times each, fill in the boxes to make an equation with no solutions. $x + y = x + y$
DOK 3	Using the digits 1 to 9 at most	Using the digits 1 to 9 at most	Using the digits 1 to 9 at most	Using the digits 1 to 9 at most
Example	one time each, fill in the boxes to make two fractions that have a quotient that is as close to 4/11 as possible.	one time each, fill in the boxes to create an equation where <i>x</i> has the greatest possible value.	one time each, fill in the boxes to make a result that has the greatest value possible.	one time each, fill in the boxes so that the solution is closest to zero.
		x+=	—	

Depth of Knowledge Matrix - Secondary Math

Topic	Geometric Proofs	Complex Numbers	Trigonometric Functions	Definite Integrals	
CCSS Standard(s)	• G-CO.11	• N-CN.2	• F-TF.3	• N/A	
DOK 1 Example	Add one geometric marking to demonstrate the quadrilateral is a square.	Multiply the binomials. $(3 + 4i)(2 + 3i)$	Evaluate. $\sin\frac{\pi}{3}$	Solve. $\int_{2}^{6} x^{3} dx$	
DOK 2 Example	Use exactly five geometric markings to show that a quadrilateral is a square.	Using the integers -9 to 9 at most one time each, fill in the boxes twice: once to make a positive real number product and once to make a negative real number product. (+ i) (+ i)	Using the digits 1 to 9 at most one time each, fill in the boxes to make two true number sentences. $\sin\frac{\pi}{2}=1$	Using the digits 1 to 9 at most one time each, fill in the boxes to make a positive and a negative solution. $\int_{-\infty}^{+\infty} x^{-\infty} dx$	
DOK 3 Example	What is the least number of geometric markings needed to demonstrate that a quadrilateral is a square?	Using the integers -9 to 9 at most one time each, fill in the boxes to make a real number product with the greatest value. (+ i)(+ i)	Using the digits 1 to 9 at most one time each, fill in the boxes to find the function's greatest possible value. $\sin \frac{\pi}{2\pi} = \frac{\sqrt{2\pi}}{2\pi}$	Using the digits 1 to 9 at most one time each, fill in the boxes to make a solution that is as close to 100 as possible. $\int_{-\infty}^{+\infty} x^{-1} dx$	



Chrissy Day @ChrissyDay1974

I LOVE Open Middle @robertkaplinsky second graders were working on ____ - ___ Make the smallest difference possible using the digits 1-9 once only. The conversation and perseverance was something I had never seen from these kids!

5:20 PM · Mar 9, 2019 · Twitter for iPhone

6 Retweets 62 Likes



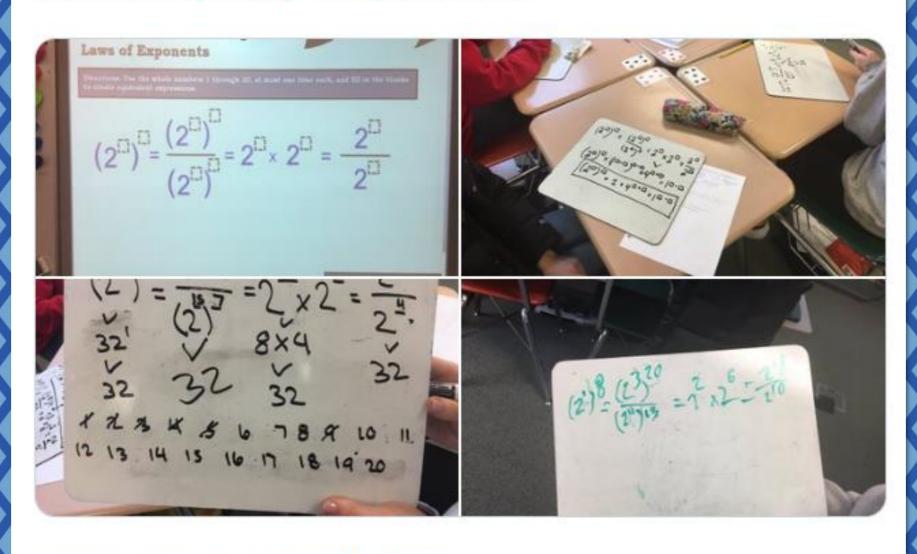
DeLaina Ellis @dellis5th · Jan 11

It was an @openmiddle **showdown** in 5th grade! They could NOT stop! One student even asked me for his paper during recess so he could try to get even closer! #wearegrandview #iteachmath #mtbos #productivestruggle





Kids begging for more time and yelling, "No" when I asked if they wanted a hint! Amazing activity @robertkaplinsky @openmiddle



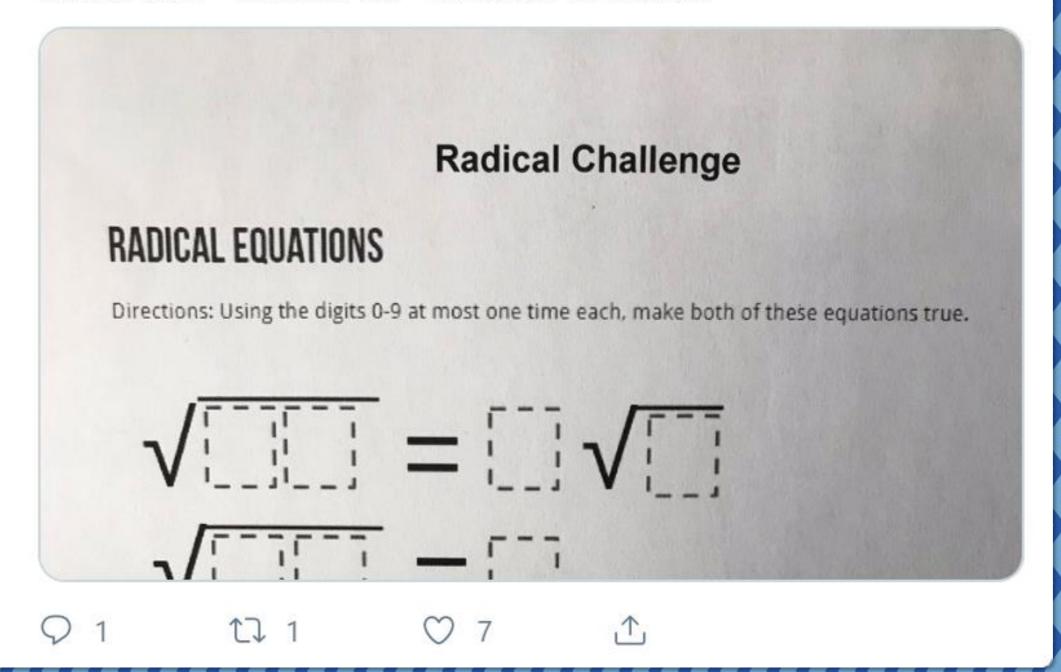
1:30 PM · Mar 8, 2019 · Twitter for iPhone

14 Retweets 98 Likes



Marguerite Spriggs @mspriggs30 · Nov 16, 2018

My **first time trying** an **@openmiddle** problem with my students today. Wasn't sure how it would go or if they'd solve it. After a few minutes going at it (and coming up with more than one solution) they asked "can we do another one?" "That was fun - we should do it more!"



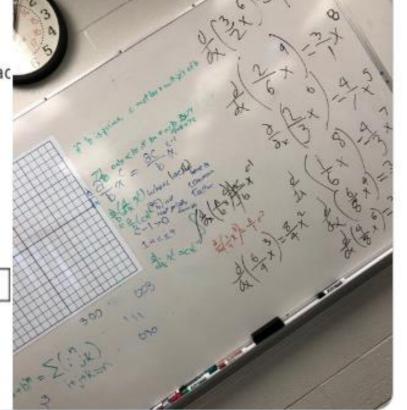


Tried an @openmiddle problem (for the 1st time) with my calculus crew. Left it on the board went to grab a photocopy before class start. Came back and Ss were crowded around the board sharing ideas. It's was magical. I *must* bring these to all my classes #MTBoS #iteachmath

VATIVE POWER RULE

ons: Use the digits 1 to 9, at most one time each create a true derivative statement.

$$\frac{d}{dx} \left(\frac{\Box}{\Box} x^{\Box} \right) = \frac{\Box}{\Box} x^{\Box}$$



2:17 PM · Apr 18, 2019 · Twitter for iPhone

20 Retweets 156 Likes



Replying to @robertkaplinsky @openmiddle and @And02B

My students live for these! Nearly every day I'm asked, "You got anymore of those open problem things for us to solve?"

6:44 PM · Apr 17, 2019 · Twitter for iPhone

5 Likes

OPEN MIDDLE PROBLEM BENEFITS

- KIDS LOVE DOING THEM
- BUILD CONCEPTUAL UNDERSTANDING
- OFTEN LEAD TO GREAT CONVERSATIONS
- REVEAL HIDDEN MISCONCEPTIONS

GOALS

- WHO AM !?
- WHAT'S WRONG WITH WORKSHEETS?
- WHAT SHOULD WE BE DOING INSTEAD?
- HOW DO WE DO IT IN OUR CLASSROOMS?
- ☐ WHERE DO WE GET MORE PROBLEMS?
- ☐ WHAT COMES NEXT?

HOW DO WE DO IT?

Open Middle Worksheet

Name:	Period: Date:
First attempt:	Points:/2 attempt/2 explanation
What did you learn from this attempt? How will your str	rategy change on your next attempt?
Second attempt:	Points:/2 attempt/2 explanation

First attempt:	Points	:	_/2	attem	ipt	_/2 exp	lanation
What did you learn from this atte	emnt?	How	will	VOUL	strateav	change	on vour
next attempt?	cilipi:	110 11	*****	7001	sir dieg /	change	011 / 001
•							

HOW DO WE DO IT?

- Open Middle Worksheet
- Classwork
- Homework
- Assessments

GOALS

- WHO AM !?
- WHAT'S WRONG WITH WORKSHEETS?
- WHAT SHOULD WE BE DOING INSTEAD?
- M HOW DO WE DO IT IN OUR CLASSROOMS?
- ☐ WHERE DO WE GET MORE PROBLEMS?
- ☐ WHAT COMES NEXT?



Kinder ▼ 1st Gr ▼ 2nd Gr ▼ 3rd Gr ▼ 4th Gr ▼ 5th Gr ▼ 6th Gr ▼ 7th Gr ▼ 8th Gr ▼ High School ▼ About ▼ Submit 🝱 English ▼

Q



WANT TO SHARE OPEN MIDDLE WITH OTHERS?

CHECK OUT THESE FREE WEBINARS TO HELP TEACHERS RETHINK CLASSWORK

Elementary Version

Secondary Version

Search OPEN MIDDLE STICKERS Get an Open Middle sticker OPEN MIDDLE WORKSHEET English (student version) English (document camera version) French (student version) French (document camera version)

NUMBER TILES

Printable PDF with the digits 0 to 9

Spanish (document camera version)

Spanish (student version)

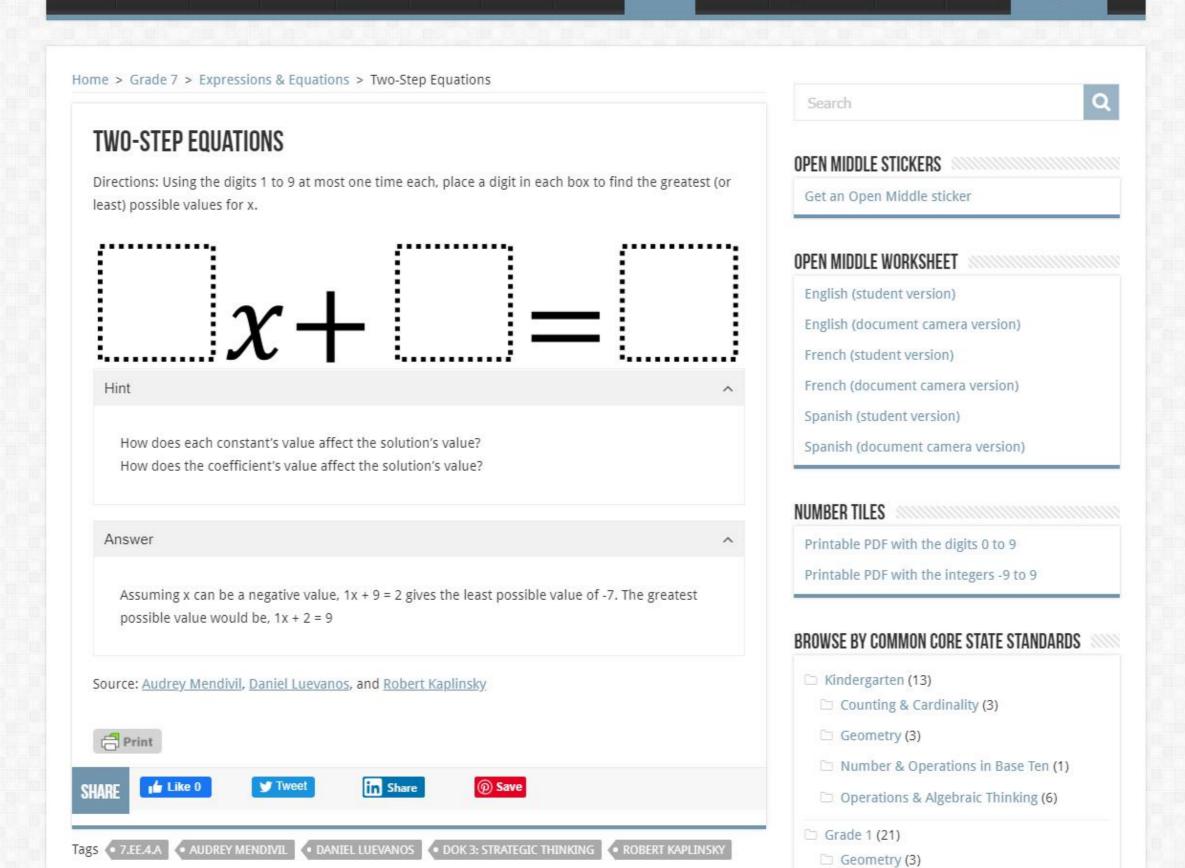
Printable PDF with the integers -9 to 9

BROWSE BY COMMON CORE STATE STANDARDS

- ☐ Kindergarten (13)
- Counting & Cardinality (3)
- Geometry (3)
- Number & Operations in Base Ten (1)
- Operations & Algebraic Thinking (6)
- Grade 1 (21)
- Geometry (3)



Home Kinder ▼ 1st Gr ▼ 2nd Gr ▼ 3rd Gr ▼ 4th Gr ▼ 5th Gr ▼ 6th Gr ▼ 7th Gr ▼ 8th Gr ▼ High School ▼ About ▼ Submit 🝱 English ▼



GOALS

- WHO AM !?
- WHAT'S WRONG WITH WORKSHEETS?
- WHAT SHOULD WE BE DOING INSTEAD?
- M HOW DO WE DO IT IN OUR CLASSROOMS?
- WHERE DO WE GET MORE PROBLEMS?
- ☐ WHAT COMES NEXT?

WHAT COMES NEXT?

Action	Do Now	Start Planning	Don't Do
Try Open Middle problems out with your students			
Find more problems I can use on the Open Middle website.			
Incorporate Open Middle problems on assessments.			
Replace all traditional problems with Open Middle problems.			
Share these resources with colleagues to make them aware.			

Register

Log In





If you've heard of Open Middle problems and maybe used a few of them, but you're not satisfied with how things have gone and want consistently good results, then this mini workshop is for you. I want your students to love using Open Middle problems and have them be your favorite problems to use when getting observed.

We'll begin by discussing how Open Middle problems can help you and your students. Then we'll work through specific examples for grades K-1, 2-5, and 6-12. We'll use them to talk about how to prepare to use a problem as well as how to use them with students. We'll also address how you can use Open Middle problems when teaching students digitally. Then we'll talk about where you can find more Open Middle problems to use and when and where you want to use them in your units. Finally, there's a bonus lesson on



How To Use An Open Middle Problem

by Robert Kaplinsky

\$59.00 \$39.00

Subject: Mathematics

Grade Levels:

- Elementary School
- Middle School
- High School
- College
- Graduate

Registration is open



Register Now











Open Middle

smarturl.it/openmiddle

